## Programming Languages: Functional Programming Practicals 0: Functions and Definitions

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You should have installed GHC, with its commandline interface GHCi. Open your favourite text editor, create a new plain text file. The filename extension must end in .hs. This will be your working file for this practical. Type ghci <filename>.hs in the command line to load the working file into GHCi.

1. Define a function myeven:: Int  $\rightarrow$  Bool that determines whether the input is an even number. You may use the following functions:

```
mod :: Int \rightarrow Int \rightarrow Int , (==) :: Int \rightarrow Int \rightarrow Bool .
```

(Types of the functions written above are not in their most general form.)

- 2. Define a function that computes the area of a circle with given radius r (using 22/7 as an approximation to  $\pi$ ). The return type of the function might be Float.
- 3. Part-time students in Institute of Information Science are paid NTD 130 per hour. Define a function *payment* :: Int → Int that, when applied to the numbers of weeks a student work, compute the amount of money the Institute has to pay the student.
  - (a) Assume that there are five working days in a week, eight working hours per day. Define *payment*. For clarity, use **let** to define local variables recording number of days worked, number of hours worked, etc.
  - (b) Define *payment* again, but declare the local variables using **where**. Which style do you prefer?
  - (c) The regulation states that students are considered workers, and if a worker works for more than 19 weeks, the Institute has to pay, in addition to the salary, health insurance and pension reserves for the worker. The amount is 6% of the worker's salary.

Update definition of *payment* in the form:

```
payment :: Int \rightarrow Int payment weeks | weeks > 19 = ... | otherwise = ...
```

You may need a function *fromIntegral* to convert Int to Float, and a function *round* that rounds a floating point number to the nearest integer.

In this case, should you use **let** or **where**?

## 4. More on let.

(a) Guess what the value of *nested* would be. Type it into your working file and evaluated in in GHCi to see whether you guessed right. Note that indentation matters.

```
nested:: Int

nested = let x = 3

in (let x = 5

in x + x + x + x + x = 5
```

(b) Guess what the value of *recursive* would be. Try it in GHCi.

```
recursive :: Int

recursive = let x = 3

in let x = x + 1

in x
```

5. Type in the definition of *smaller* into your working file.

```
smaller :: Int \rightarrow Int \rightarrow Int

smaller x y = \mathbf{if} x \leq y \mathbf{then} x \mathbf{else} y.
```

Then try the following:

- (a) In GHCi, type:t smaller to see the type of smaller.
- (b) Try applying it to some arguments, e.g. smaller 3 4, smaller 3 1.
- (c) Use :t to see the type of *smaller* 3 4.
- (d) Use :t to see the type of *smaller* 3.
- (e) In your working file, define a new function st3 = smaller 3.
- (f) Find out the type of st3 in GHCi. Try st3 4, st3 1. Explain the results you see.
- 6. More practice on curried functions.
  - (a) Define a function *poly* such that *poly* a b c  $x = a \times x^2 + b \times x + c$ . All the inputs and the result are of type *Float*.
  - (b) Reuse *poly* to define a function *poly1* such that *poly1*  $x = x^2 + 2 \times x + 1$ .
  - (c) Reuse *poly* to define a function *poly*2 such that *poly*2 a b  $c = a \times 2^2 + b \times 2 + c$ .
- 7. Type in the definition of *square* in your working file.
  - (a) Define a function  $quad :: Int \rightarrow Int$  such that quad x computes  $x^4$ .

(b) Type in this definition into your working file. Describe, in words, what this function does.

twice 
$$:: (a \rightarrow a) \rightarrow (a \rightarrow a)$$
  
twice  $f x = f (f x)$ .

- (c) Define quad using twice.
- 8. Replace the previous *twice* with this definition:

twice 
$$:: (a \rightarrow a) \rightarrow (a \rightarrow a)$$
  
twice  $f = f \cdot f$ .

- (a) Does *quad* still behave the same?
- (b) Explain in words what this operator  $(\cdot)$  does.
- 9. Functions as arguments, and a quick practice on sectioning.
  - (a) Type in the following definition to your working file, without giving the type.

forktimes 
$$f g x = f x \times g x$$
.

Use : t in GHCi to find out the type of *forktimes*. You will end up getting a complex type which, for now, can be seen as equivalent to

$$(t \to Int) \to (t \to Int) \to t \to Int$$
.

Can you explain this type?

- (b) Define a function that, given input x, use *forktimes* to compute  $x^2 + 3 \times x + 2$ . **Hint**:  $x^2 + 3 \times x + 2 = (x+1) \times (x+2)$ .
- (c) Type in the following definition into your working file:  $lift2 \ hf \ g \ x = h \ (f \ x) \ (g \ x)$ . Find out the type of lift2. Can you explain its type?
- (d) Use *lift2* to compute  $x^2 + 3 \times x + 2$ .
- 10. Let the following identifiers have type:

$$f :: Int \rightarrow Char$$
  
 $g :: Int \rightarrow Char \rightarrow Int$   
 $h :: (Char \rightarrow Int) \rightarrow Int \rightarrow Int$   
 $x :: Int$   
 $y :: Int$   
 $c :: Char$ 

Which of the following expressions are type correct?

1. 
$$(g \cdot f) \times c$$

2. 
$$(g x \cdot f) y$$

3. 
$$(h \cdot g) x y$$

4. 
$$(h \cdot g x) c$$

5. 
$$h \cdot g \times c$$

You may type the expressions into Haskell and see whether they type check. To define f, for example, include the following in your working file:

$$f :: Int \rightarrow Char$$
  
 $f = undefined$ 

However, it is better if you can explain why the answers are as they are.