

Stat_HW4_Solution

```
In [1]: #載入所需函式庫
from matplotlib import pyplot as plt
import matplotlib inline
# 設定圖形大小; DPI越大圖越大
plt.rcParams["figure.dpi"] = 100
import seaborn as sns
import pandas as pd
import numpy as np
import scipy.stats as stats
import statsmodels.api as sm
import statsmodels.stats.api as sms
import statsmodels.formula.api as smf
import math as math
```

Exercise 4.61 (2% for each quartile)

```
In [2]: # This is a function that computes percentile from input data.
def percetile(data1, p):
    if type(data1) == np.ndarray:
        alldata = data1.copy()
        data1 = data1.copy()
    else:
        alldata = data1.values.copy()
        data1 = data1.values.copy()
    alldata.sort()
    n = alldata.size
    l = (n + 1) * p / 100 - 1
    f_l = math.floor(l)
    c_l = math.ceil(l)
    percentile_v = alldata[f_l] + (alldata[c_l] - alldata[f_l]) * (l - f_l)
    return percentile_v

r1 = np.array([10.5, 14.7, 15.3, 17.7, 15.9, 12.2, 10.0, 14.1, 13.9, 18.5, 13.9, 15.1, 14.7])
p25 = percentile(r1, 25)
p50 = percentile(r1, 50)
p75 = percentile(r1, 75)
print("Q1 = ", p25)
print("Q2 = ", p50)
print("Q3 = ", p75)

Q1 = 13.05
Q2 = 14.7
Q3 = 15.600000000000001
```

Exercise 4.39

(3% for range, 3% for variance, 3% for standard deviation, 3% for interpretation)

```
In [11]: #讀取資料庫
df_xr0439 = pd.read_excel('Xr04-39.xlsx')
print('Head of dataset:')
display(df_xr0439.head())
print('Tail of dataset:')
display(df_xr0439.tail())

print("Range: ",float(df_xr0439.max()-df_xr0439.min()),"dollars(per 100 pills)")
print("Variance: ",float(df_xr0439.var()),"dollars^2(per 100 pills)")
print("Standard deviation: ",float(df_xr0439.std()),"dollars(per 100 pills)")

Head of dataset:
```

	Prozac
0	102.05
1	99.85
2	112.30
3	97.15
4	111.23

Tail of dataset:

	Prozac
95	102.81
96	109.58
97	103.35
98	113.02
99	103.79

Range: 25.850000000000001 dollars(per 100 pills)
Variance: 29.45522322222216 dollars^2(per 100 pills)
Standard deviation: 5.42726664373179 dollars(per 100 pills)

Exercise 4.45

(3% for mean, 3% for standard deviation, 3% for interpretation)

```
In [4]: #讀取資料庫
df_xr0445 = pd.read_excel('Xr04-45.xlsx')
print('Head of dataset:')
display(df_xr0445.head())
print('Tail of dataset:')
display(df_xr0445.tail())

print("Mean: ",float(df_xr0445.mean()),"minutes")
print("Standard deviation: ",float(df_xr0445.std()),"minutes")

Head of dataset:
```

	Flight delay (minutes)
0	37
1	29
2	18
3	45
4	38

Tail of dataset:

	Flight delay (minutes)
120	0
121	30
122	47
123	14
124	32

Mean: 26.024 minutes
Standard deviation: 11.807231245191202 minutes

Exercise 4.63 (3%)

```
In [5]: r1 = np.array([10.5, 14.7, 15.3, 17.7, 15.9, 12.2, 10.0, 14.1, 13.9, 18.5, 13.9, 15.1, 14.7])
p25 = percentile(r1, 25)
p50 = percentile(r1, 50)
p75 = percentile(r1, 75)
print("InterQuartile range: ", p75-p25)

InterQuartile range: 2.5500000000000007
```

Exercise 4.69 (2% for each quartile, 3% for interpretation)

```
In [6]: #讀取資料庫
df_xr0469 = pd.read_excel('Xr04-69.xlsx')
dog=df_xr0469["Dogs"]
cat=df_xr0469["Cats"].dropna()

dog_p25=percentile(dog,25)
dog_p50=percentile(dog,50)
dog_p75=percentile(dog,75)

cat_p25=percentile(cat,25)
cat_p50=percentile(cat,50)
cat_p75=percentile(cat,75)

print("Quartiles of dog\nFirst:",dog_p25,"dollars\nSecond: ",dog_p50,"dollars\nThird: ",dog_p75,"dollars")
print("\nQuartiles of cat\nFirst:",cat_p25,"dollars\nSecond: ",cat_p50,"dollars\nThird: ",cat_p75,"dollars")

Quartiles of dog
First: 1097.5 dollars
Second: 1204.0 dollars
Third: 1337.0 dollars

Quartiles of cat
First: 773.0 dollars
Second: 846.0 dollars
Third: 988.0 dollars
```

Exercise 4.73 (2% for each quartile, 3% for interpretation)

```
In [7]: #讀取資料庫
df_xr0473 = pd.read_excel('Xr04-73.xlsx')
private=df_xr0473["Private"]
public=df_xr0473["Public"].dropna()

private_p25=percentile(private,25)
private_p50=percentile(private,50)
private_p75=percentile(private,75)

public_p25=percentile(public,25)
public_p50=percentile(public,50)
public_p75=percentile(public,75)

print("Quartiles of private\nFirst:",private_p25,"minutes\nSecond: ",private_p50,"minutes\nThird: ",private_p75,"minutes")
print("\nQuartiles of public\nFirst:",public_p25,"minutes\nSecond: ",public_p50,"minutes\nThird: ",public_p75,"minutes")

Quartiles of private
First: 228.0 minutes
Second: 237.0 minutes
Third: 245.75 minutes

Quartiles of public
First: 279.0 minutes
Second: 296.0 minutes
Third: 307.0 minutes
```

Exercise 4.91 (Compute and interpret covariance and r)

(2% for scatter plot, 3% for covariance, 3% for correlation, , 3% for interpretation)

```
In [8]: #讀取資料庫
df_xr0491 = pd.read_excel('Xr04-91.xlsx')

print('Head of dataset:')
display(df_xr0491.head())

print("Tail of dataset:")
display(df_xr0491.tail())

_ = sns.regplot(x='Price of Oil', y= 'Oil Wells', data = df_xr0491, scatter_kws={"color": "black"}, line_kws={"color": "red"}, ci = None)
plt.title('Scatter Plot for Price of Oil and Oil Wells Drilled')
plt.xlabel('Price of Oil (Dollar)')
plt.ylabel('Number of Oil Wells Drilled')
plt.show()

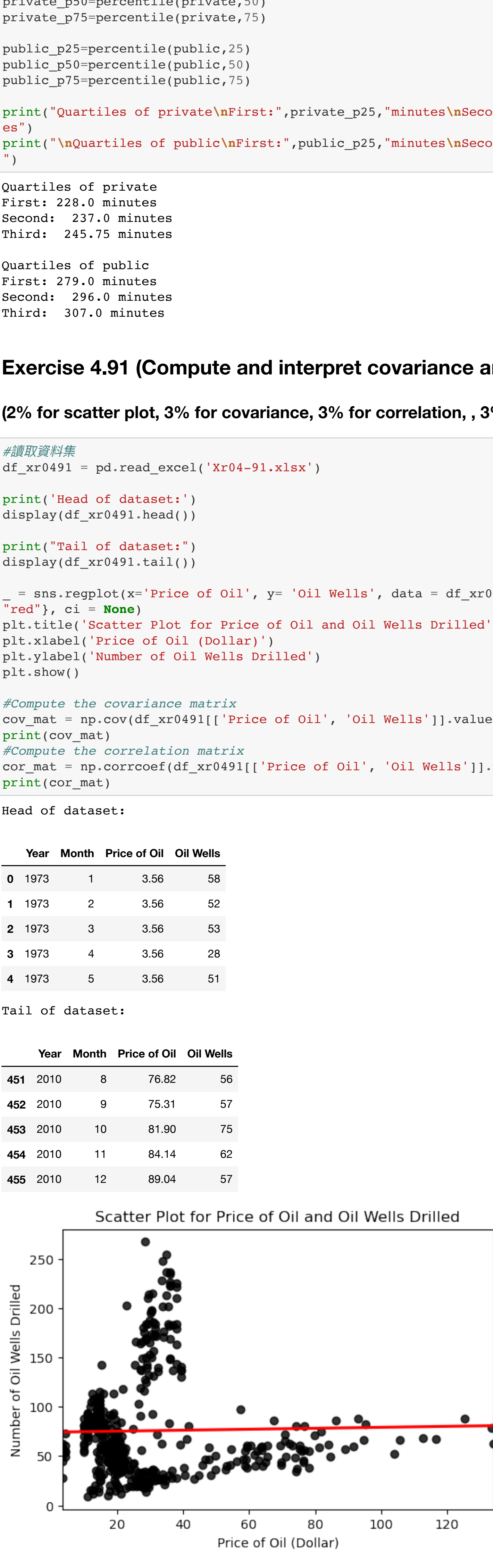
#Compute the covariance matrix
cov_mat = np.cov(df_xr0491[['Price of Oil', 'Oil Wells']].values,rowvar = False)
print(cov_mat)
#Compute the correlation matrix
cor_mat = np.corrcoef(df_xr0491[['Price of Oil', 'Oil Wells']].values,rowvar = False)
print(cor_mat)

Head of dataset:
```

	Year	Month	Price of Oil	Oil Wells
0	1973	1	3.56	58
1	1973	2	3.56	52
2	1973	3	3.56	53
3	1973	4	3.56	28
4	1973	5	3.56	51

Tail of dataset:

	Year	Month	Price of Oil	Oil Wells
461	2010	8	76.82	56
462	2010	9	75.31	57
463	2010	10	81.90	75
464	2010	11	84.14	62
465	2010	12	89.04	57



```
[[ 469.62162871  23.02331203]
 [ 23.02331203 2762.31563042]]
[[1.         0.02021423]
 [0.02021423  1.         ]]
```

Exercise 4.99 (Compute and interpret covariance and r)

(2% for scatter plot, 3% for covariance, 3% for correlation, 3% for interpretation)

```
In [9]: #讀取資料庫
df_xr0499 = pd.read_excel('Xr04-99.xlsx')

print('Head of dataset:')
display(df_xr0499.head())

print("Tail of dataset:")
display(df_xr0499.tail())

_ = sns.regplot(x='Age', y= 'Carbon monoxide', data = df_xr0499, scatter_kws={"color": "black"}, line_kws={"color": "red"}, ci = None)
plt.title('Scatter Plot for Age of Furnace and Carbon Monoxide')
plt.xlabel('Age')
plt.ylabel('Carbon monoxide (ppm)')
plt.show()

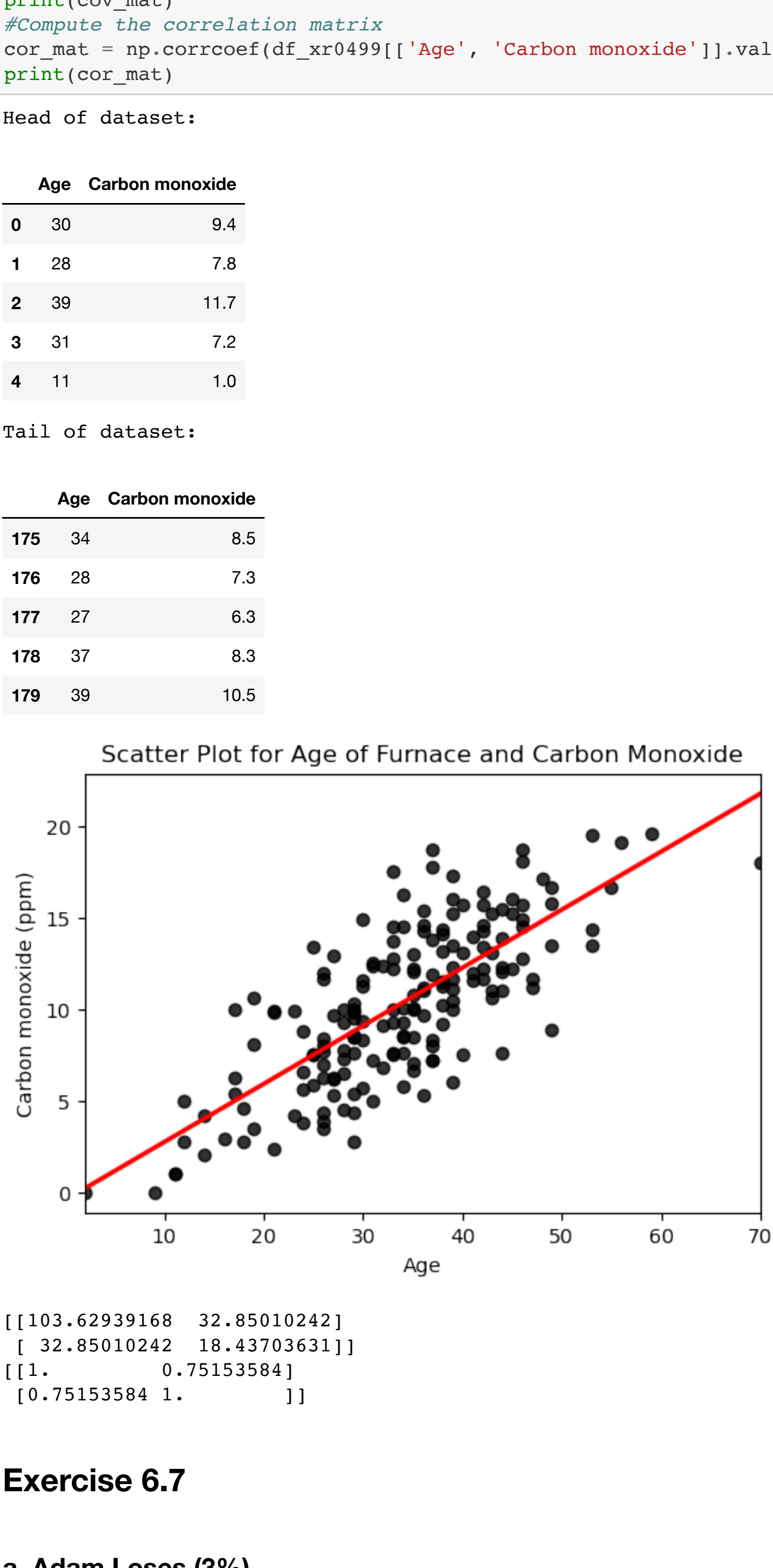
#Compute the covariance matrix
cov_mat = np.cov(df_xr0499[['Age', 'Carbon monoxide']].values,rowvar = False)
print(cov_mat)
#Compute the correlation matrix
cor_mat = np.corrcoef(df_xr0499[['Age', 'Carbon monoxide']].values,rowvar = False)
print(cor_mat)

Head of dataset:
```

	Age	Carbon monoxide
0	30	9.4
1	28	7.8
2	38	11.7
3	31	7.2
4	11	1.0

Tail of dataset:

	Age	Carbon monoxide
175	34	8.5
176	28	7.3
177	27	6.3
178	37	8.3
179	39	10.5



```
[[103.62939168  32.85010242]
 [ 32.85010242  18.43703631]]
[[1.         0.75153584]
 [0.75153584  1.         ]]
```

Exercise 6.7

a. Adam Loses (3%)

$P(\text{Adams loses}) = P(\text{Brown wins}) + P(\text{Collins wins}) + P(\text{Dalton wins}) = 0.09 + 0.27 + 0.22 = 0.58$

b. Either Brown or Dalton wins (3%)

$P(\text{either Brown or Dalton wins}) = P(\text{Brown wins}) + P(\text{Dalton wins}) = 0.09 + 0.22 = 0.31$

c. Adam, Brown, or Collins wins (3%)

$P(\text{Either Adams, Brown, or Collins wins})=P(\text{Dalton loses})=1-0.22=0.78$

Exercise 6.11

a. Determine the sample space for this experiment. (3%)

{ pay with cash, pay with credit card, pay with debit card }

b. Assign probabilities to the simple events (3%)

$P(\text{pay with credit card})=0.6; P(\text{pay with cash})=0.3; P(\text{pay with debit card})=0.1$

c. Which method did you use in part (b) (3%)

Relative Frequency Approach