

# 1<sup>st</sup>North African Olympiad in Informatics 2025

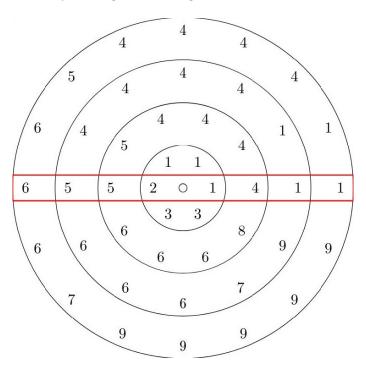
## **Target Rotation**

Time limit: 1.5 seconds Memory limit: 256 MB

In the city of **Djelfa**, players **Ahmad Karawita** and **Hamoud Habibi Hamoud** love playing with a unique puzzle consisting of **concentric circular discs**. There are n discs, named  $d_1, d_2, \ldots, d_n$ , where  $d_i$  represents the disc of radius i. Each disc  $d_i$  contains digits  $0, 1, \ldots, 9$  sorted and written in **counterclockwise order**, starting from the rightmost point of the disc. The number of occurrences of each digit j on disc  $d_i$  is given by  $a_{j,i}$ , and the total number of digits on any disc is guaranteed to be even.

The discs are stacked concentrically, with  $d_1$  on top and  $d_n$  on the bottom. Players can rotate each disc independently by one position in either the **clockwise** or **counterclockwise** direction any number of times.

The **goal** is to align the digits on the middle horizontal line, as shown in the figure. The middle horizontal line consists of exactly 2n digits: one digit from each disc on the left and right side.



#### Task

Given q target strings  $x_1, x_2, \ldots, x_q$ , each of length 2n, determine the **minimum number of rotations** required to align the middle horizontal line to exactly match each target string. If aligning a target string is **impossible**, output -1. The queries are independent from each other, in other words, for each query we start from the same initial configuration described in the first paragraph.

### Input

- 1. An integer n  $(1 \le n \le 10^5)$ : the number of discs.
- 2. A  $10 \times n$  grid of integers, where the entry  $a_{j,i} \leq 10^9$  ( $0 \leq j \leq 9$ ,  $1 \leq i \leq n$ ) specifies the number of times digit j appears on disc  $d_i$ . it is guaranteed that each disc has an even number of digits.
- 3. An integer q ( $1 \le q \le 2 \times 10^6$ ): the number of target strings.
- 4. q strings  $x_1, x_2, \ldots, x_q$ , each of length 2n: the target strings.
- It is guaranteed that  $nq \le 7 \times 10^6$

### Output

For each target string  $x_k$   $(1 \le k \le q)$ , output:

- On the first line, output POSSIBLE if one can align the middle line to  $x_k$ .
- On the second line, the **minimum number of rotations** required to align the middle line to  $x_k$ , or -1 if it is impossible.

If the first line of output is correct while the second is not, half of the mark is given

#### Constraints

- $1 \le n \le 10^5$
- $0 \le a_{j,i} \le 10^9$
- $1 \le q \le 2 \times 10^6$
- $nq < 7 \times 10^6$

#### **Subtasks**

Subtask	Score	Constraints
1	6	n = q = 1
2	6	Each disk has only one number on it
3	10	For all $i, \sum_{j=0}^{9} a_{j,i} \le 2$
4	8	n = 1
5	20	For all $i, j, x, y : a_{i,j} = a_{x,y}$
6	30	$nq \le 10^5$
7	20	No further conditions

#### Examples

#### Input

```
4
0 3 1 2 0 0 0 0 0 0
0 0 0 4 2 3 0 1 0
0 2 0 0 4 1 3 1 0 1
0 2 0 0 4 1 3 1 0 5
4
65521411
65521419
75521410
```

**Note**: This is the example shown in the figure of the 1st page.

# Output

```
POSSIBLE
0
POSSIBLE
1
POSSIBLE
2
IMPOSSIBLE
-1
```

# Input

```
1
4 3 2 3 1 1 4 3 9 2
1
71
```

## Output

```
POSSIBLE 4
```