

Tutorial problems for Lectures 1, 2, and beginning of 3. Due April 27, 2017.

**Problem 1:** Make a new text file with your name, email address, what you're working on for your honours project, plus a few things you'd like to learn in the course. Initialize a git repository and commit this file. (5)

**Problem 2:** Put your answers to the other tutorial questions into another text file. Add this to the repository also. (5)

**Problem 3:** Make a github account and push the repository onto github. Email Hazmatally (hazmatally@gmail.com) and me (jonathan.sievers@gmail.com) your github name so we can have a look at your file/answers. (10)

**Problem 3:** Write a python script to make a vector of  $n$  evenly spaced numbers between 0 and  $\pi/2$ . i.e.  $x[0]=0$ ,  $x[-1]=\pi/2$  (5)

Use this vector to integrate  $\cos(x)$  from 0 to  $\pi/2$  for a range of number of points using the simple method. Include 10,30,100,300,1000 points between 0 and  $\pi/2$ . How does error scale with number of points? Your answer should look like  $err \propto n^\alpha$ , say what  $\alpha$  is (5)

**Problem 4:** Python supports array slicing -  $x[5:10:2]$  will take points 5,7,9 from  $x$ .  $x[5::2]$  will take points 5,7,9 from  $x$ . How can I take all odd points from an array? How can I take all even points from an array, but skipping the first and last points? (5)

**Problem 5:** Write a python function to integrate this vector using Simpsons rule. How does error scale with number of points? How many points did we need to use in part 2 to get same accuracy as 11 points with Simpsons rule? (10)

**Problem 6:** Plot the errors as a function of number of points using Simpsons rule and standard sum. You will want to use a log scale here - look at logplot.py in the github distribution (5)

**Bonus:** The scipy module has built in integration functions in `scipy.integrate`. The `quad` routine will do numerical integrals. `quad` will try to put its effort where the function changes quickly, which can save huge amounts of computation for some problems.

**B1:** Look at `scipy_quad_example.py`, which uses `scipy` to integrate our Gaussian function over two different ranges. The integrals should be (almost) identical - yet they are not. Can you figure out why? (5)

**B2:** Can you write another function that will always give the correct answer to this integral? (5) Hint - you may want to do two integrals instead of one.