Beyond Simple Graphs: Knowledge Graph Reasoning

Jiaxuan You
Assistant Professor at UIUC CDS



CS598: Deep Learning with Graphs, 2024 Fall

https://ulab-uiuc.github.io/CS598/

Logistics: Coding Homwork

- Coding Assignment 3 Out
 - Assignment will be released on Canvas today.
 - Implement the GraphSAGE and GAT layers directly.
 - Submit your code and written answers downloaded from Colab to Canvas by Nov 3 (Sun) 11:59 PM, CT.

Recap: KG Completion Task

Given an enormous KG, can we complete the KG?

For a given (head, relation), we predict missing tails.

Alan Poe

• (Note this is slightly different from link prediction task) missing relation: J.R.R Tolkien genre Science Fiction **Example task**: Predict the genre tail "Science Fiction" for genre ("J.K. Rowling", "genre") Influence **Fantasy** genre Stephen King genre J.K. Rowling Influence Influence Influence C.S. Lewis genre Influence

~ S598. Deen Learning with Granhs Liaxuan You

Tragicomedy

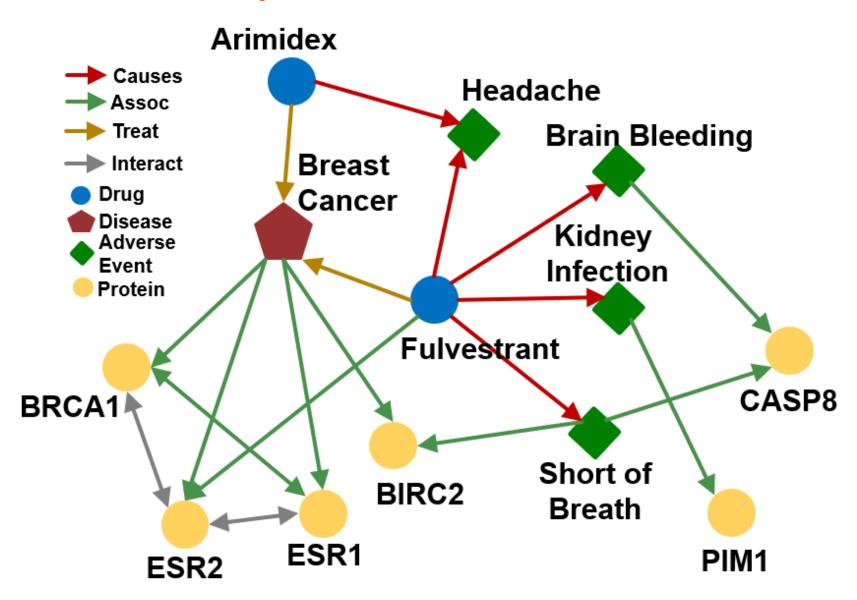
Llovd Alexander

Today: Reasoning over KGs

- Goal:
 - How to perform multi-hop reasoning over KGs?

- Reasoning over Knowledge Graphs
 - Answering multi-hop queries
 - Path Queries
 - Conjunctive Queries
 - Query2Box

Example KG: Biomedicine



Predictive Queries on KG

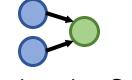
Can we do multi-hop reasoning, i.e., answer complex queries on an incomplete, massive KG?

Query Types	Examples: Natural Language Question, Query
One-hop Queries	What adverse event is caused by Fulvestrant? (e:Fulvestrant, (r:Causes))
Path Queries	What protein is associated with the adverse event caused by Fulvestrant? (e:Fulvestrant, (r:Causes, r:Assoc))
Conjunctive Queries	What is the drug that treats breast cancer and caused headache? ((e:BreastCancer, (r:TreatedBy)), (e:Migraine, (r:CausedBy))

In this lecture, we only focus on answering queries on a KG!







One-hop Queries

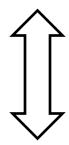
Path Queries

Conjunctive Queries

Predictive One-hop Queries

 We can formulate knowledge graph completion problems as answering one-hop queries.

• KG completion: Is link (h, r, t) in the KG?



- One-hop query: Is t an answer to query (h, r)?
 - For example: What side effects are caused by drug Fulvestrant?

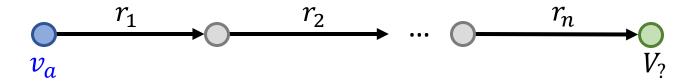
Path Queries

- Generalize one-hop queries to path queries by adding more relations on the path.
- An n-hop path query q can be represented by

$$q = (v_a, (r_1, \dots, r_n))$$

- v_a is an "anchor" entity,
- Let answers to q in graph G be denoted by $[\![q]\!]_G$.

Query Plan of q:

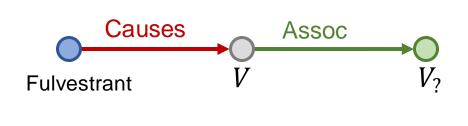


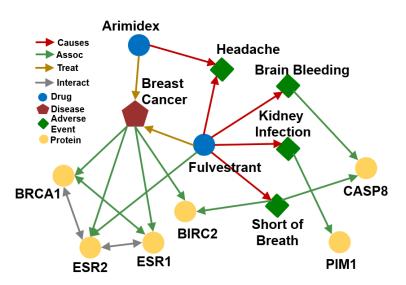
Query plan of path queries is a chain.

Path Queries

Question: "What proteins are **associated** with adverse events **caused** by **Fulvestrant?**"

- v_a is e:Fulvestrant
- (r_1, r_2) is (r:Causes, r:Assoc)
- Query: (e:Fulvestrant, (r:Causes, r:Assoc))



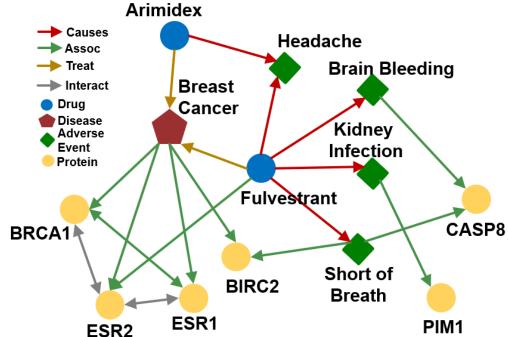


Path Queries

Question: "What proteins are **associated** with adverse events **caused** by **Fulvestrant?**"

Query: (e:Fulvestrant, (r:Causes, r:Assoc))

Given a KG, how to answer a path query?



10/18/2024 CS598: Deen Learning with Granhs Liaxuan You

Traversing Knowledge Graphs

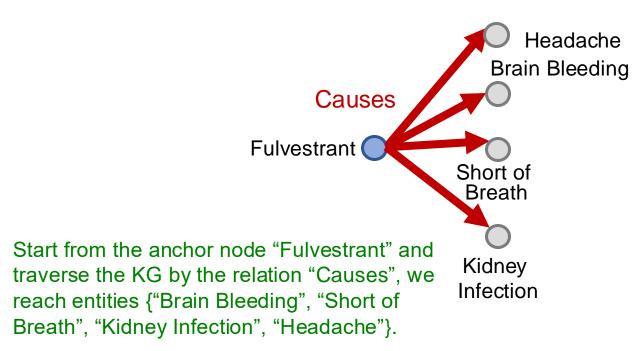
- We answer path queries by traversing the KG: "What proteins are associated with adverse events caused by Fulvestrant?"
- Query: (e:Fulvestrant, (r:Causes, r:Assoc))

Fulvestrant

Start from the **anchor node** (Fulvestrant).

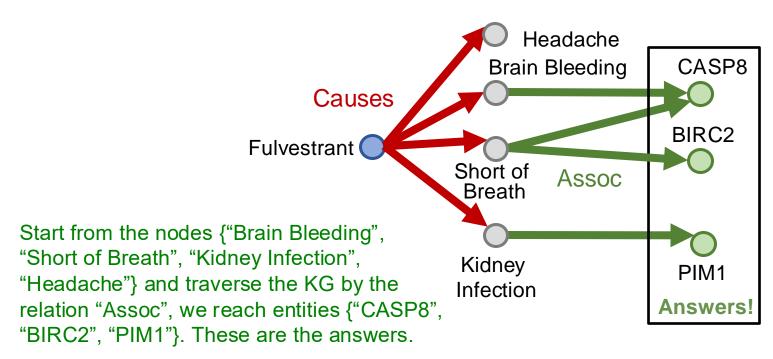
Traversing Knowledge Graphs

- We answer path queries by traversing the KG: "What proteins are associated with adverse events caused by Fulvestrant?"
- Query: (e:Fulvestrant, (r:Causes, r:Assoc))



Traversing Knowledge Graphs

- We answer path queries by traversing the KG: "What proteins are associated with adverse events caused by Fulvestrant?"
- Query: (e:Fulvestrant, (r:Causes, r:Assoc))



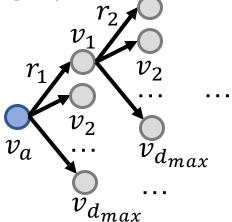
However, KGs are incomplete

- Answering queries seems easy: Just traverse the graph.
- But KGs are incomplete and unknown:
 - Many relations between entities are missing or are incomplete
 - For example, we lack all the biomedical knowledge
 - Enumerating all the facts takes non-trivial time and cost, we cannot hope that KGs will ever be fully complete
- Due to KG incompleteness, one is not able to identify all the answer entities

Can KG Completion Help?

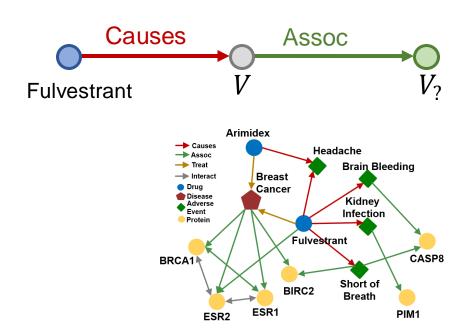
Can we first do KG completion and then traverse the completed (probabilistic) KG?

- Not much! The "completed" KG could be a dense graph!
 - Most (h, r, t) triples (edge on KG) will have some non-zero probability.
 - It's uncertain how to set proper threshold to sparsify the graph v_1
- Time complexity of traversing a dense KG is exponential as a function of the path length L: $O(d_{max}^L)$



Task: Predictive Queries

- We need a way to answer path-based queries over an incomplete knowledge graph.
- We want our approach to implicitly impute and account for the incomplete KG.
- Task: <u>Predictive queries</u>
 - Want to be able to answer arbitrary queries while implicitly imputing for the missing information
 - Generalization of the link prediction task



Outline of the Lecture

1) Given entity embeddings, how do we answer an arbitrary query?

- Path queries: Using a generalization of TransE
- Conjunctive queries: Using Query2Box
- And-Or Queries: Using Query2Box and query rewriting
 (We will assume entity embeddings and relation embeddings are given)

2) How do we train the embeddings?

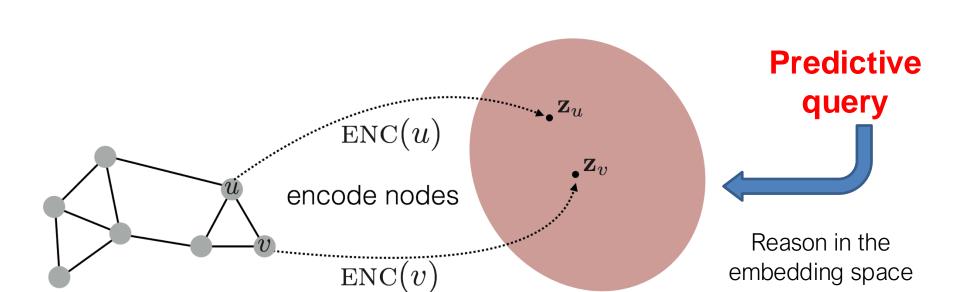
 The process of determining entity and relation embeddings which allow us to embed a query.

Beyond Simple Graphs: Knowledge Graph Reasoning

Answering Predictive Queries on Knowledge Graphs

Embedding space

[Query2box: Reasoning over Knowledge Graphs in Vector Space Using Box Embeddings. Ren, et al., ICLR 2020] General dea



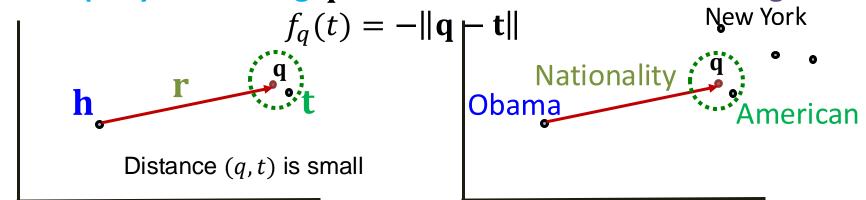
Map queries into embedding space. Learn to reason in that space

- Embed query into a single **point** in the Euclidean space: answer nodes are close to the query.
- Query2Box: Embed query into a hyper-rectangle (box) in the Euclidean space: answer nodes are enclosed in the box.

Knowledge graph

Idea: Traversing KG in Vector Space

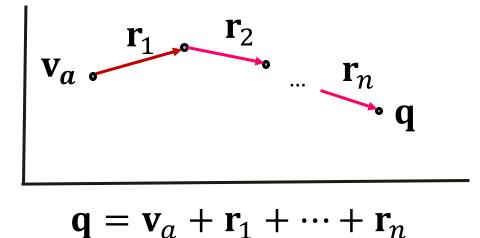
- Key idea: Embed queries!
 - Generalize TransE to multi-hop reasoning.
 - Recap: TransE: Translate \mathbf{h} to \mathbf{t} using \mathbf{r} with score function $f_r(h,t) = -||\mathbf{h} + \mathbf{r} \mathbf{t}||$.
 - Another way to interpret this is that:
 - Query embedding: q = h + r
 - Goal: query embedding q is close to the answer embedding t



Traversing KG in Vector Space

- Key idea: Embed queries!
 - Generalize TransE to multi-hop reasoning.

Given a path query
$$q = (v_a, (r_1, ..., r_n))$$
,



The embedding process only involves vector addition, independent of # entities in the KG!

Traversing KG in Vector Space (1)

Embed path queries in vector space.

- Question: "What proteins are associated with adverse events caused by Fulvestrant?"
- Query: (e:Fulvestrant, (r:Causes, r:Assoc))

Follow the query plan:

Query Plan

Embedding Process

Fulvestrant •



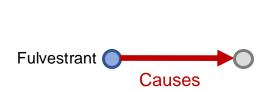
Traversing KG in Vector Space (2)

Embed path queries in vector space.

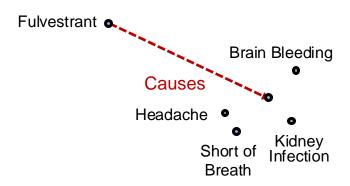
- Question: "What proteins are associated with adverse events caused by Fulvestrant?"
- Query: (e:Fulvestrant, (r:Causes, r:Assoc))

Follow the query plan:

Query Plan



Embedding Process

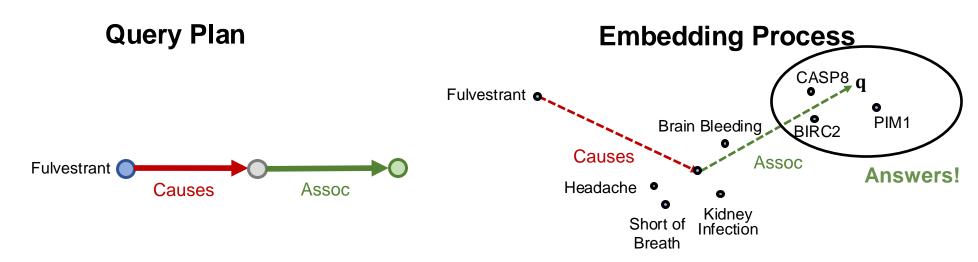


Traversing KG in Vector Space (3)

Embed path queries in vector space.

- Question: "What proteins are associated with adverse events caused by Fulvestrant?"
- Query: (e:Fulvestrant, (r:Causes, r:Assoc))

Follow the query plan:



Traversing KG in Vector Space (4)

Insights:

- We can train TransE to optimize knowledge graph completion objective (Lecture 11)
- Since TransE can naturally handle compositional relations, it can handle path queries by translating in the latent space for multiple hops using addition of relation embeddings.
- For TransR / DistMult / ComplEx, since they cannot easily handle compositional relations, they cannot be easily extended to handle path queries.

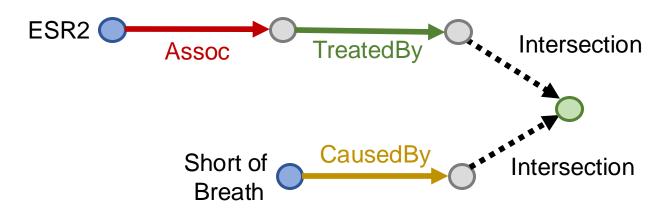
Conjunctive Queries

Can we answer more complex queries with logic conjunction operation?

Conjunctive Queries: "What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?"

((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

Query plan:

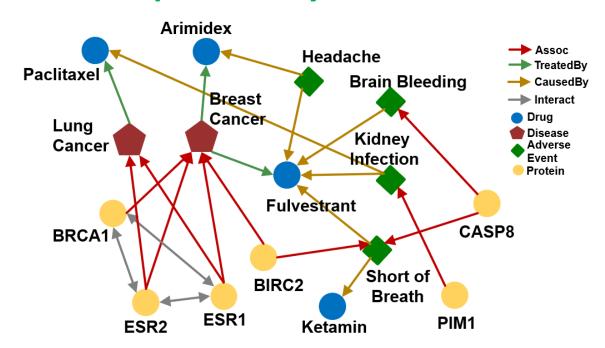


Conjunctive Queries

"What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?"

((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

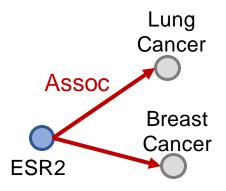
How do we answer the question by KG traversal?



"What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?"

((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

Traverse KG from anchor nodes: ESR2 and Short of Breath:

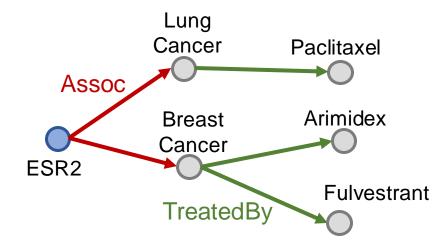


Traverse from the first anchor "ESR2" by relation "Assoc", we reach a set of entities {"Lung Cancer", "Breast Cancer"}

"What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?"

((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

Traverse KG from anchor nodes: ESR2 and Short of Breath:

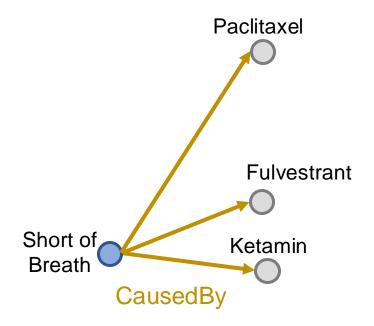


Traverse from the set of entities {"Lung Cancer", "Breast Cancer"} by relation TreatedBy, we reach a set of entities {"Paclitaxel", "Arimidex", "Fulvestrant"}

"What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?"

((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

Traverse KG from anchor nodes: ESR2 and Short of Breath:

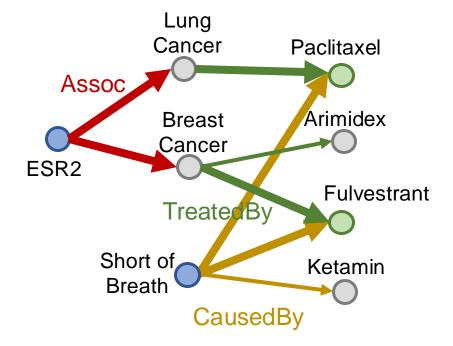


Traverse from the second anchor "Short of Breath" by relation "CausedBy", we reach a set of entities {"Fulvestrant", "Ketamin", "Paclitaxel"}

"What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?"

((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

Traverse KG from anchor nodes: ESR2 and Short of Breath:

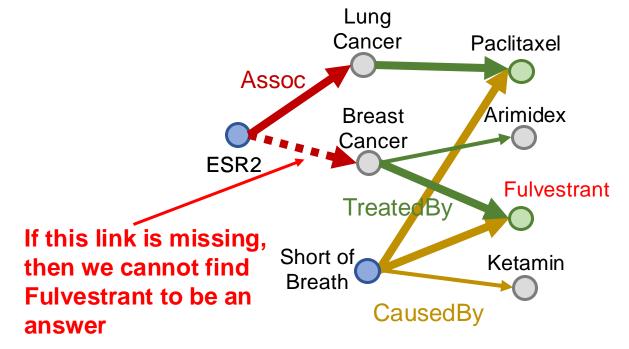


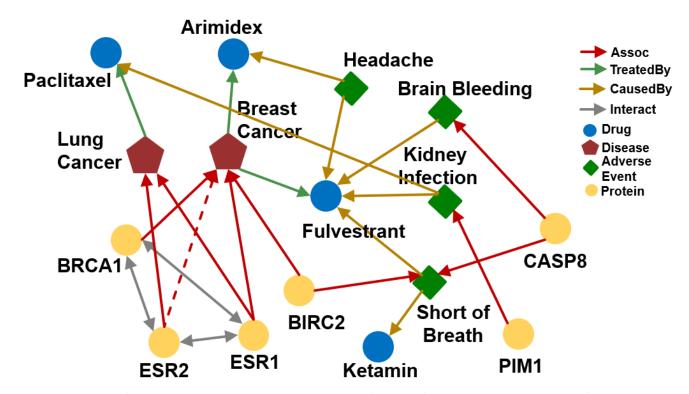
We take intersection between the two sets and get the answers {"Fulvestrant", "Paclitaxel"}

"What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?"

((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

Traverse KG from anchor nodes: ESR2 and Short of Breath:





- How can we use embeddings to implicitly impute the missing (ESR2, Assoc, Breast Cancer)?
- Intuition: ESR2 interacts with both BRCA1 and ESR1. Both proteins are associated with breast cancer.

Traversing KG in Vector Space

"What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?"

((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

Query plan:

ESR2

Assoc

TreatedBy

Intersection

Short of

Rroath

Each intermediate node represents a <u>set of entities</u>, how do we represent it? How do we define the intersection operation in the latent space?

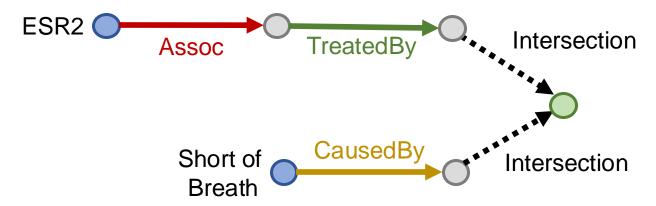
Beyond Simple Graphs: Knowledge Graph Reasoning

Query2Box: Reasoning over KGs Using Box Embeddings

Conjunctive Queries

How can we answer more complex queries with logical conjunction operation?

Query plan:



- (1) Each intermediate node represents a set of entities; how do we represent it?
- (2) How do we define the intersection operation in the latent space?

Box Embeddings

Embed queries with hyper-rectangles (boxes)

$$\mathbf{q} = (Center(q), Offset(q))$$

Short of Breath
 Kidney
 Infection
 Headache

For example, we can embed the adverse events of Fulvestrant with a box that enclose all the answer entities.

Key Insight: Intersection

- Intersection of boxes is well-defined!
- When we traverse the KG to find the answers, each step produces a set of reachable entities.
- How can we better model these sets?
 - Boxes are a powerful abstraction, as we can project the center and control the offset to model the set of entities enclosed in the box

Short of BreathKidneyInfectionHeadache

Things to figure out:

- Entity embeddings (# params: d|V|):
 - Entities are seen as zero-volume boxes
- Relation embeddings (# params 2d|R|)
 - Each relation takes a box and produces a new box
- Intersection operator f:
 - New operator, inputs are boxes and output is a box
 - Intuitively models intersection of boxes

Notation

d: out degree |V|: # entities

|R|: # relations

Embed queries in vector space: "What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?"

```
((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))
```

Traverse KG from anchor nodes: ESR2 and Short of Breath:

Query plan

Embedding Space



?

ESR2 ●

Projection Operator

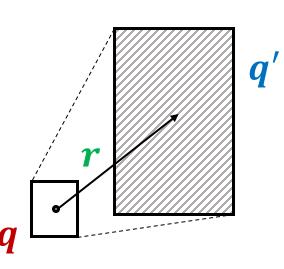
Projection Operator ${\mathcal P}$

- Intuition: Take the current box as input and use the relation embedding to project and expand the box!
- $\mathcal{P}: \mathsf{Box} \times \mathsf{Relation} \to \mathsf{Box}$

$$Cen(q') = Cen(q) + Cen(r)$$

 $Off(q') = Off(q) + Off(r)$

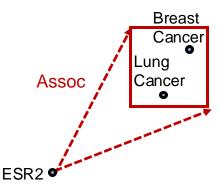
"x" (cross) means the projection operator is a relation from any box and relation to a new box



- **Embed queries in vector space:** "What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?"
- Traverse KG from anchor nodes: ESR2 and Short of Breath:
- Use projection operator again following the query plan.

Query Plan





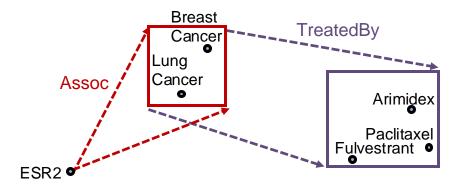
"What is the drug that causes Short of Breath and treats disease associated with protein ESR2?"

((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

Use projection operator again following the query plan.

Query Plan



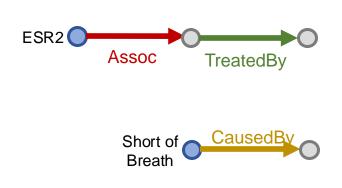


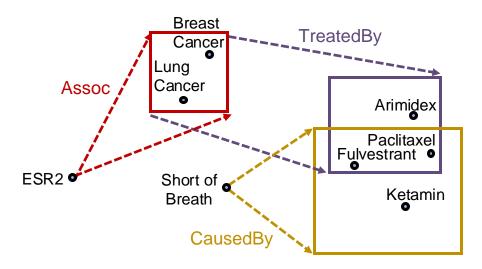
"What is the drug that causes Short of Breath and treats disease associated with protein ESR2?"

((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

Use projection operator again following the query plan.

Query Plan



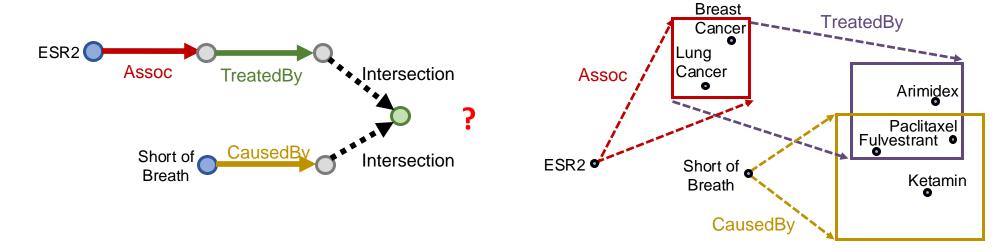


"What is the drug that causes Short of Breath and treats disease associated with protein ESR2?"

((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

How do we take intersection of boxes?

Query Plan



Intersection Operator

Geometric Intersection Operator ${\cal J}$

Take multiple boxes as input and produce the intersection box

Intuition:

- The center of the new box should be "close" to the centers of the input boxes
- The offset (box size) should shrink (since the size of the intersected set is smaller than the size of all the input set)
- $\mathcal{I}: \mathsf{Box} \times \cdots \times \mathsf{Box} \to \mathsf{Box}$

Intersection Operator

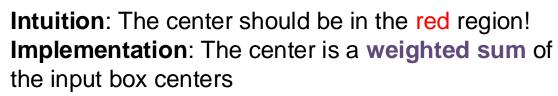
Geometric Intersection Operator \mathcal{J}

• $\mathcal{I}: \mathsf{Box} \times \cdots \times \mathsf{Box} \to \mathsf{Box}$

Hadamard product (element-wise product)

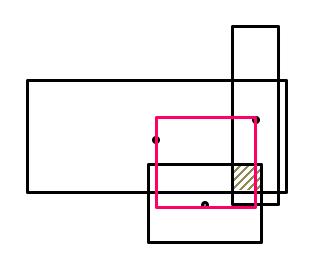
$$Cen(q_{inter}) = \sum_{i} w_{i} \odot Cen(q_{i})$$

$$\mathbf{w}_i = \frac{\exp(f_{cen}(Cen(q_i)))}{\sum_j \exp(f_{cen}(Cen(q_j)))} \qquad Cen(q_i) \in \mathbb{R}^d$$
$$\mathbf{w}_i \in \mathbb{R}^d$$



 $w_i \in \mathbb{R}^d$ is calculated by a neural network f_{cen} (with trainable weights)

 w_i represents a "self-attention" score for the center of each input $Cen(q_i)$.



Intersection Operator

Geometric Intersection Operator \mathcal{J}

• $\mathcal{I}: \mathsf{Box} \times \cdots \times \mathsf{Box} \to \mathsf{Box}$

$$Off(q_{inter}) = \min(Off(q_1), ..., Off(q_n))$$

$$\odot \sigma(f_{off}(Off(q_1), ..., Off(q_n)))$$

Sigmoid function: squashes output in (0,1)

 f_{off} is a neural network (with trainable parameters) that extracts the representation of the input boxes to increase expressiveness

Intuition: The offset should be smaller than the offset of the input box

Implementation: We first **take minimum** of the offset of the input box, and then we make the model more expressive by introducing a new function f_{off} to extract the **representation** of the input boxes with a **sigmoid function** to **guarantee shrinking**.

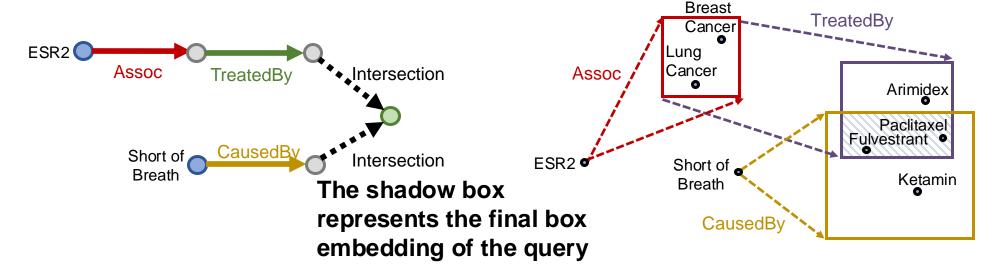
guarantees shrinking

"What is the drug that causes Short of Breath and treats disease associated with protein ESR2?"

((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

Use box intersection operator

Query Plan



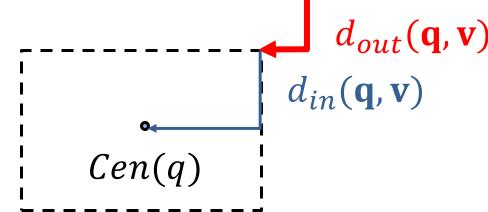
Entity-to-Box Distance

- How do we define the score function $f_q(v)$ (negative distance) for training/eval? $(f_q(v))$ captures inverse distance of a node v as answer to q)
- Given a query box q and entity embedding (box) v,

$$d_{box}(\mathbf{q}, \mathbf{v}) = d_{out}(\mathbf{q}, \mathbf{v}) + \alpha \cdot d_{in}(\mathbf{q}, \mathbf{v})$$

where $0 < \alpha < 1$.

- Intuition: if the point is enclosed in the box, the distance should be downweighted.
- $f_q(v) = -d_{box}(\mathbf{q}, \mathbf{v})$



Extending to Union Operation

• Can we embed complex queries with union?
E.g.: "What drug can treat breast cancer or lung cancer?"

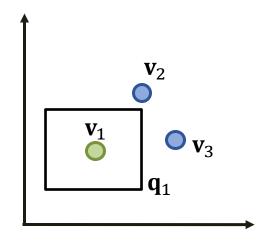
- Conjunctive queries + disjunction is called Existential Positive First-order (EPFO) queries.
 We'll refer to them as AND-OR queries.
- Can we also design a disjunction operator and embed AND-OR queries in low-dimensional vector space?

- Can we embed AND-OR queries in a low-dimensional vector space?
- No! Intuition: Allowing union over arbitrary queries requires highdimensional embeddings!

- Given 3 queries q_1 , q_2 , q_3 , with answer sets:
- If we allow union operation, can we embed them in a two-dimensional plane?

Example:

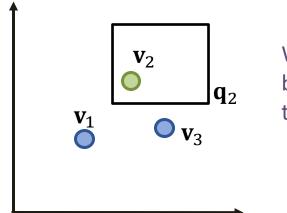
- Given 3 queries q_1 , q_2 , q_3 , with answer sets:
- If we allow union operation, can we embed them in two-dimensional plane?



We want **green dots (answers)** to be in the box while the **blue dots (negative answers)** to be outside the box

Example:

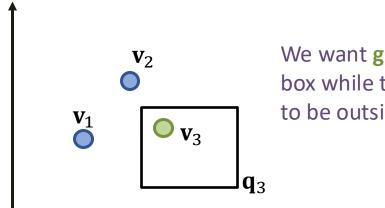
- Given 3 queries q_1 , q_2 , q_3 , with answer sets:
- If we allow union operation, can we embed them in two-dimensional plane?



We want **green dots (answers)** to be in the box while the **blue dots (negative answers)** to be outside the box

Example:

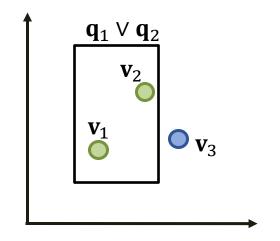
- Given 3 queries q_1 , q_2 , q_3 , with answer sets:
- If we allow union operation, can we embed them in two-dimensional plane?



We want green dots (answers) to be in the box while the blue dots (negative answers) to be outside the box

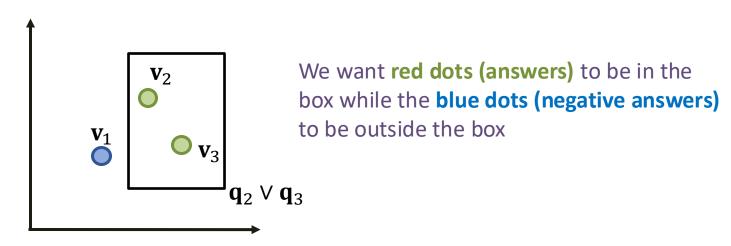
Example:

- Given 3 queries q_1 , q_2 , q_3 , with answer sets:
- If we allow union operation, can we embed them in two-dimensional plane?

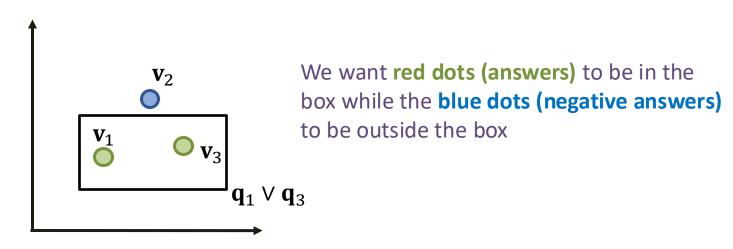


We want **red dots (answers)** to be in the box while the **blue dots (negative answers)** to be outside the box

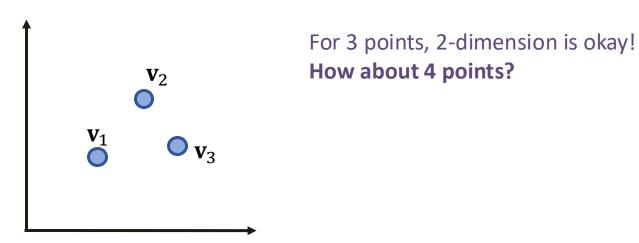
- Given 3 queries q_1 , q_2 , q_3 , with answer sets:
- If we allow union operation, can we embed them in two-dimensional plane?



- Given 3 queries q_1, q_2, q_3 , with answer sets:
- If we allow union operation, can we embed them in two-dimensional plane?

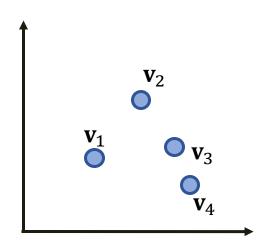


- Given 3 queries q_1, q_2, q_3 , with answer sets:
- If we allow union operation, can we embed them in two-dimensional plane?



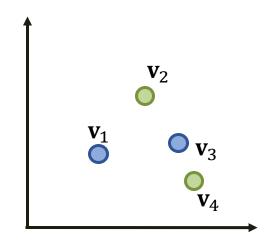
Example 2:

- Given 4 queries q_1 , q_2 , q_3 , q_4 with answers:
- If we allow union operation, can we embed them in two-dimensional plane?



Example 2:

- Given 4 queries q_1 , q_2 , q_3 , q_4 with answers:
- If we allow union operation, can we embed them in two-dimensional plane?



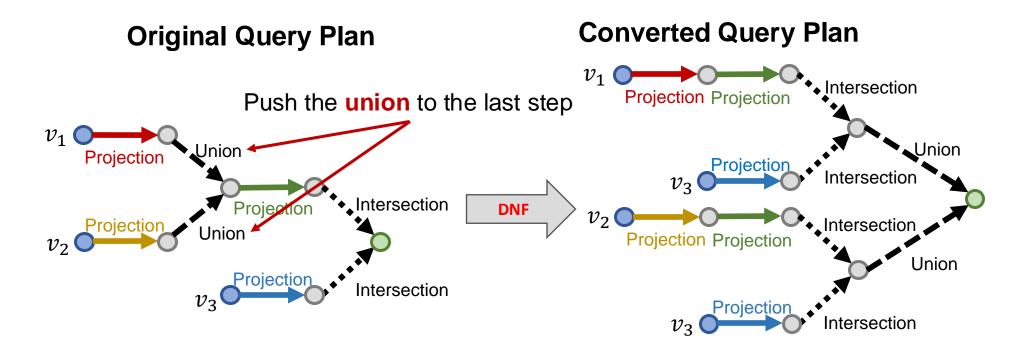
We cannot design a box embedding for $q_2 \lor q_4$, that only v_2 and v_4 are in the box but v_1 and v_3 are outside the box.

Can we embed AND-OR queries in low-dimensional vector space?

- **Conclusion**: Given any M conjunctive queries $q_1, ..., q_M$ with non-overlapping answers, we need dimensionality of $\Theta(M)$ to handle all OR queries.
 - For real-world KG, such as FB15k, we find $M \ge 13,365$, where |V| = 14,951.
 - Remember, this is for arbitrary OR queries.

Since we cannot embed AND-OR queries in low-dimensional space, can we still handle them?

Key idea: take all unions out and only do union at the last step!



Disjunctive Normal Form

 Any AND-OR query can be transformed into equivalent DNF, i.e., disjunction of conjunctive queries.

• Given any AND-OR query q,

$$q = q_1 \vee q_2 \vee \cdots \vee q_m$$

where q_i is a conjunctive query.

• Now we can first embed each q_i and then "aggregate" at the last step!

Distance Between q and an Entity

Distance between entity embedding and a DNF $q=q_1 \vee q_2 \vee \cdots \vee q_m$ is defined as:

$$d_{box}(\mathbf{q}, \mathbf{v}) = min(d_{box}(\mathbf{q}_1, \mathbf{v}), \dots, d_{box}(\mathbf{q}_m, \mathbf{v}))$$

Intuition:

- As long as v is the answer to one conjunctive query q_i , then v should be the answer to q
- As long as \mathbf{v} is close to one conjunctive query \mathbf{q}_i , then \mathbf{v} should be close to \mathbf{q} in the embedding space

Distance Between q and an Entity

Distance between entity embedding and a

DNF
$$q = q_1 \lor q_2 \lor \cdots \lor q_m$$
 is defined as:

$$d_{box}(\mathbf{q}, \mathbf{v}) = min(d_{box}(\mathbf{q}_1, \mathbf{v}), \dots, d_{box}(\mathbf{q}_m, \mathbf{v}))$$

- The process of embedding any AND-OR query q
 - 1. Transform q to equivalent DNF $q_1 \vee \cdots \vee q_m$
 - **2.** Embed q_1 to q_m
 - 3. Calculate the (box) distance $d_{box}(\mathbf{q}_i, \mathbf{v})$
 - 4. Take the minimum of all distance
 - 5. The final score $f_q(v) = -d_{box}(\mathbf{q}, \mathbf{v})$

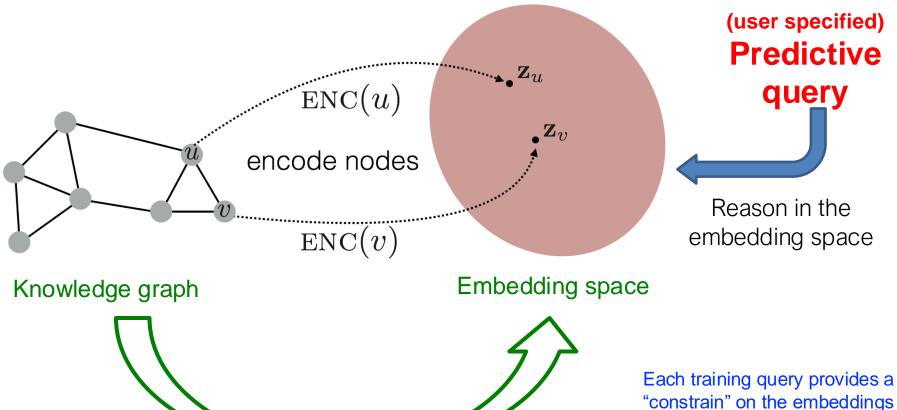
Beyond Simple Graphs: Knowledge Graph Reasoning

How to Train Query2box

Training Overview

- Overview and Intuition (similar to KG completion):
 - Given a query embedding \mathbf{q} , maximize the score $f_q(v)$ for answers $v \in [q]$ and minimize the score $f_q(v')$ for negative answers $v' \notin [q]$
- Trainable parameters:
 - Entity embeddings with d|V| # params
 - Relation embeddings with 2d|R| # params
 - Intersection operator
- How to achieve a query, its answers, its negative answers from the KG to train the parameters?
- How to split the KG for query answering?

Training Overview



Generate a set of training queries (q, v, v').

Train entity embeddings and operators to minimize the loss (i.e., to answer the training queries correctly).

"constrain" on the embeddings of entities.

Training loop:

- Get query (q, v, v')
- Using current operators, embed q.
- Compute the loss to update entity embs. and operators

Training: Details

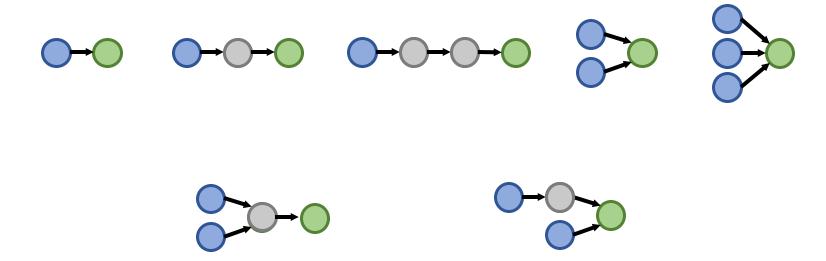
Training:

- 1. Sample a query q from the training graph G_{train} , answer $v \in [q]_{G_{train}}$, and non-answer $v' \notin [q]_{G_{train}}$
- 2. Embed the query **q**.
 - Use current operators, to compute query embedding.
- 3. Calculate the score $f_q(v)$ and $f_q(v')$.
- 4. Optimize embeddings and operators to minimize the loss ℓ (maximize $f_q(v)$ while minimize $f_q(v')$):

$$\ell = -\log\sigma\left(f_q(v)\right) - \log(1 - \sigma\left(f_q(v')\right))$$

Query Generation from Templates

Generate queries from multiple query templates:



Query Generation from Templates

- How can we generate a complex query?
- We start with a query template, which is an abstraction of the query
- We generate a query by instantiating every variable with a concrete entity and relation from the KG:
 - E.g., instantiate Anchor1 with ESR2 (a node on KG),
 - E.g., instantiate Rel1 with Assoc (an edge on KG)
- How to instantiate query template given a KG? Query

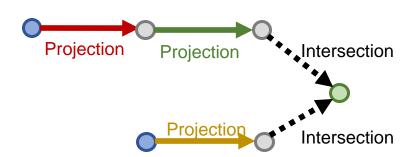
((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

Assoc TreatedBy Intersection

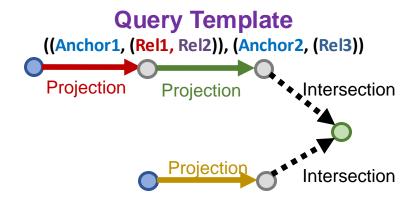
Short of CausedBy Intersection

Short of Breath

Query Template ((Anchor1, (Rel1, Rel2)), (Anchor2, (Rel3))

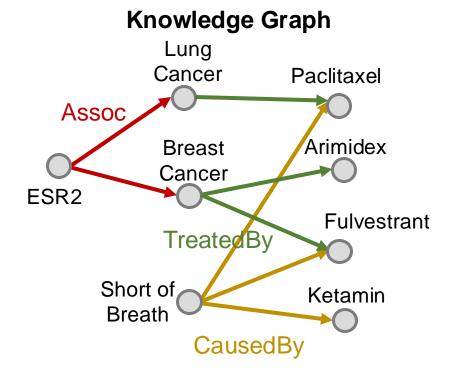


How to instantiate a query template given a KG?

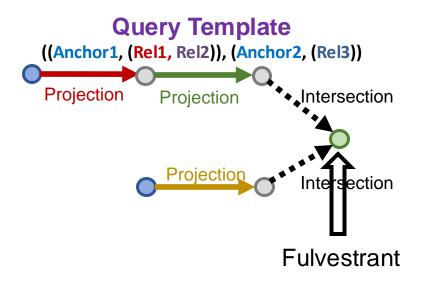


Overview:

Start from instantiating the **answer node** of the query template and then iteratively instantiate the other edges and nodes until we ground all the anchor nodes

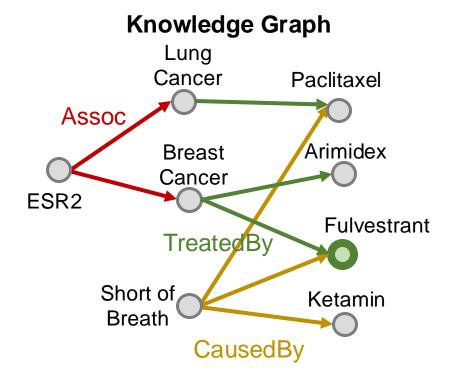


How to instantiate a query template given a KG?

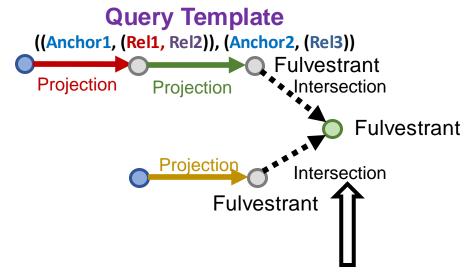


Start from instantiating the **root node** of the query template.

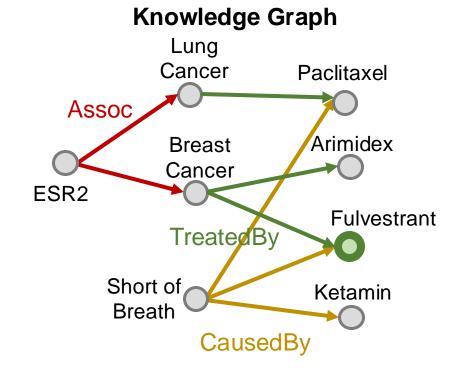
Randomly pick one entity from KG as the root node, e.g., we pick **Fulvestrant**.



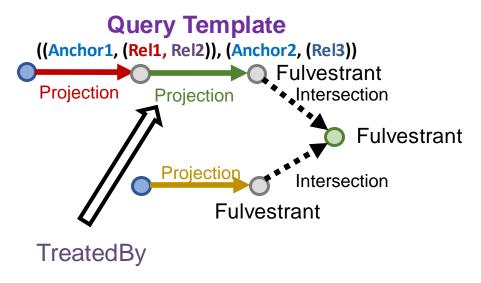
How to instantiate a query template given a KG?



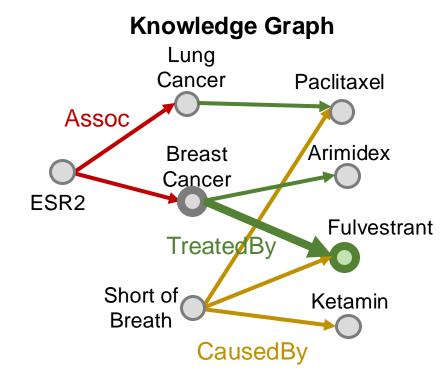
Now we look at intersection.
What we have is that the intersection of the sets of entities is **Fulvestrant**, then naturally the two sets should also contain **Fulvestrant**.



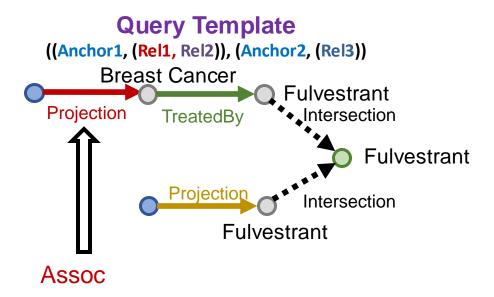
How to instantiate a query template given a KG?



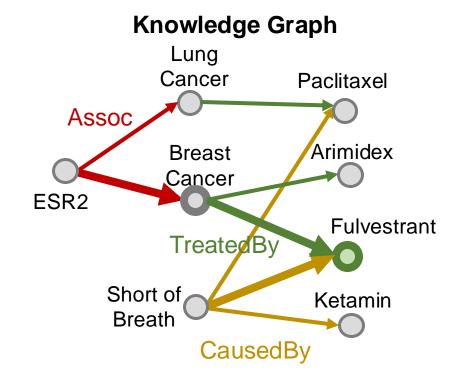
We instantiate the **Projection edge** in the template by randomly sample one relation associated with the current entity **Fulvestrant**. For example, we may select relation **TreatedBy**, and check what entities are connected to **Fulvestrant** with **TreatedBy**: {**Breast Cancer**}.



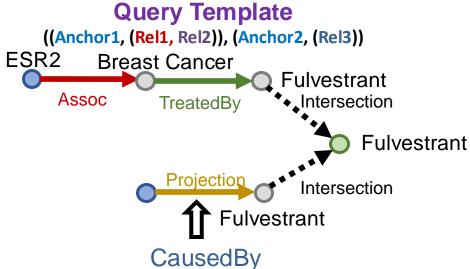
How to instantiate a query template given a KG?



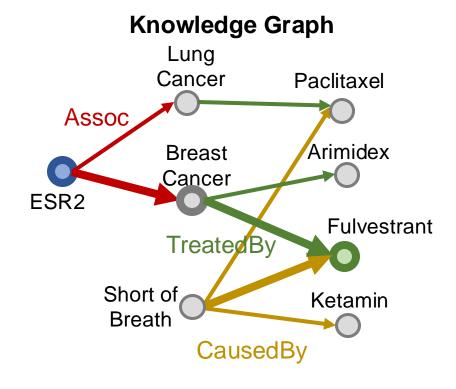
We first look at one branch and ground the **Projection edge** with the relation associated with **Breast Cancer**, e.g., **Assoc**. Then we check what entities are connected to **Breast Cancer** with **Assoc**: {**ESR2**}.



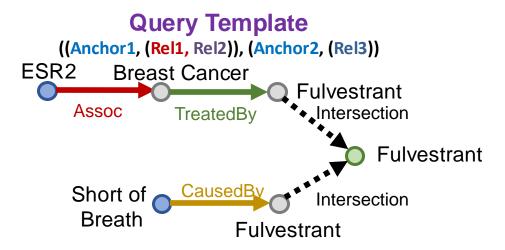
How to instantiate a query template given a KG?



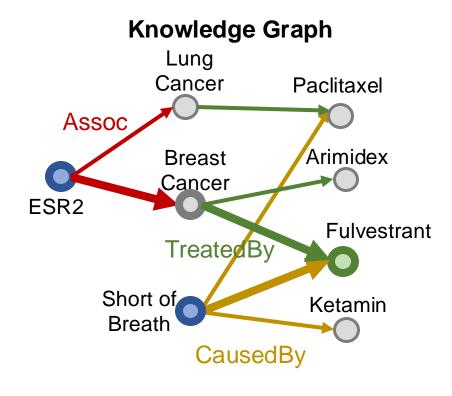
Then we look at the second branch and ground the **Projection edge** with the relation associated with **Fulvestrant**, e.g., **CausedBy**. Then we check what entities are connected to **Fulvestrant** with **CausedBy**: {**Short of Breath**}.



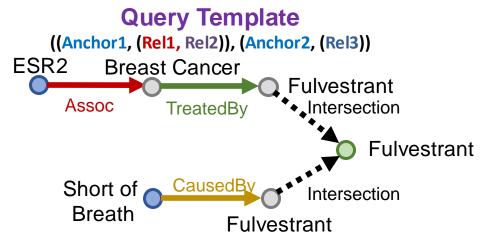
How to instantiate a query template given a KG?



We select entity from {Short of Breath}, set it as the anchor node.



How to instantiate a query template given a KG?



Now, we instantiated a query q!

q: ((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

- The query q must have answers on the KG and one of the answers is the instantiated answer node: Fulvestrant.
- We may obtain the full set of answers $[\![q]\!]_G$ by KG traversal.
- We can sample negative answers $v' \notin \llbracket q \rrbracket_G$

Beyond Simple Graphs: Knowledge Graph Reasoning

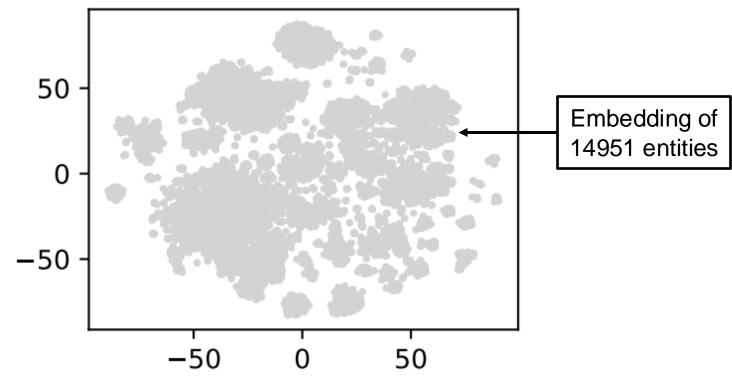
Example of Query2box

Visualization

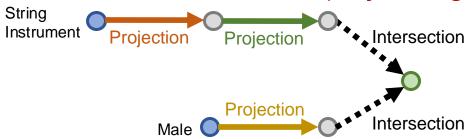
What do box embeddings actually learn?

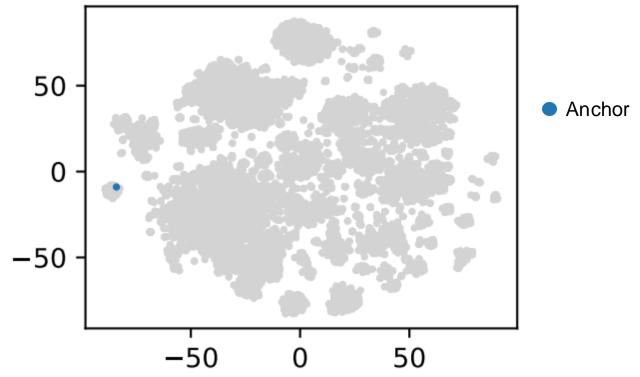
Example: "List male instrumentalists who play string instruments"

 We use t-SNE to reduce the embedding space to a 2-dimensional space, in order to visualize the query results



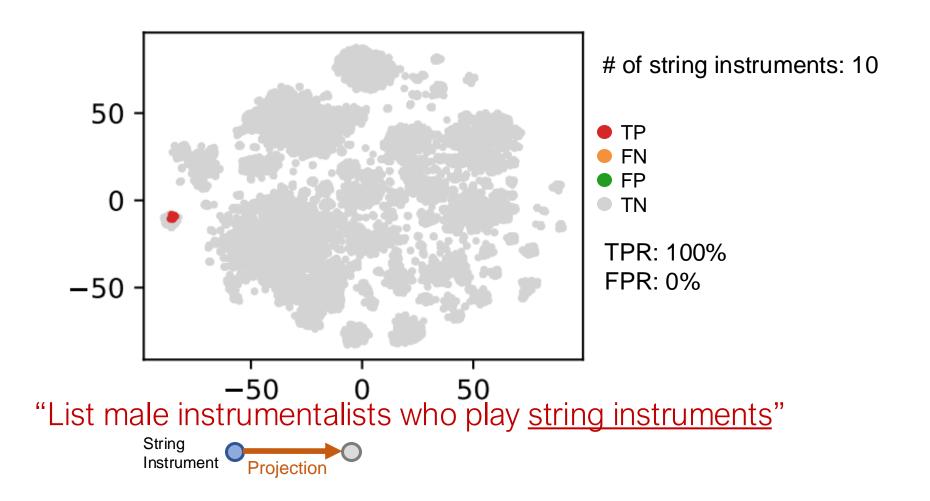
"List male instrumentalists who play string instruments"

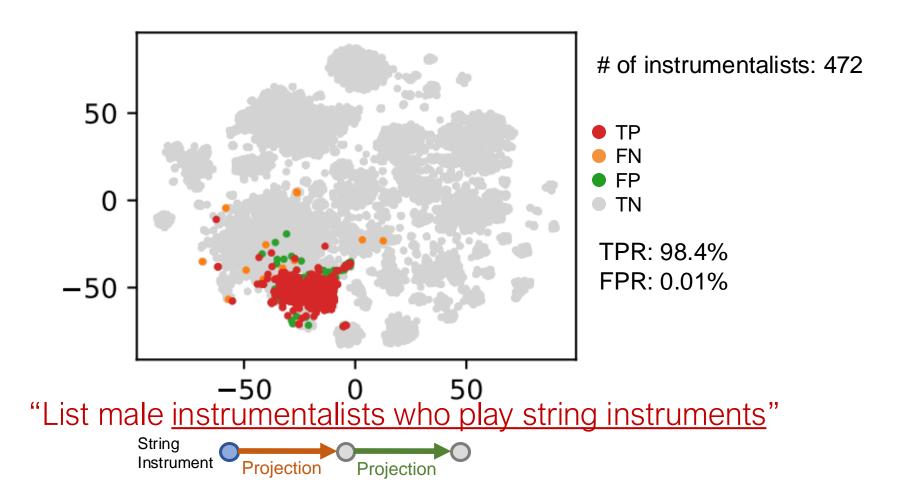


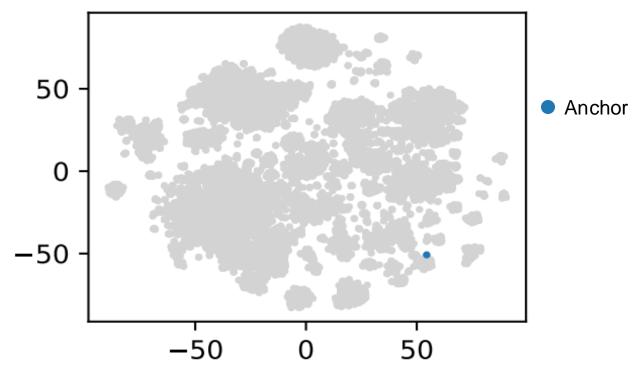


"List male instrumentalists who play string instruments"

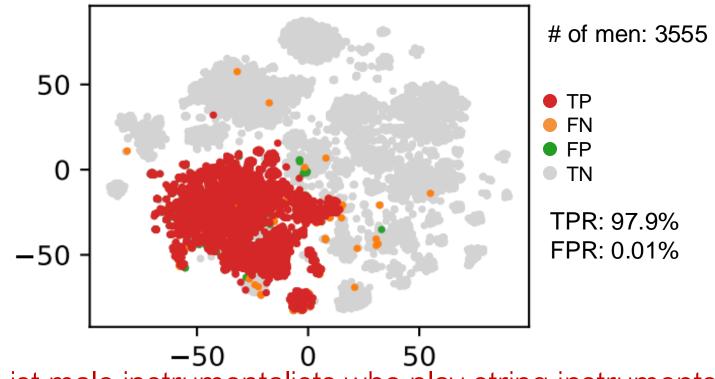




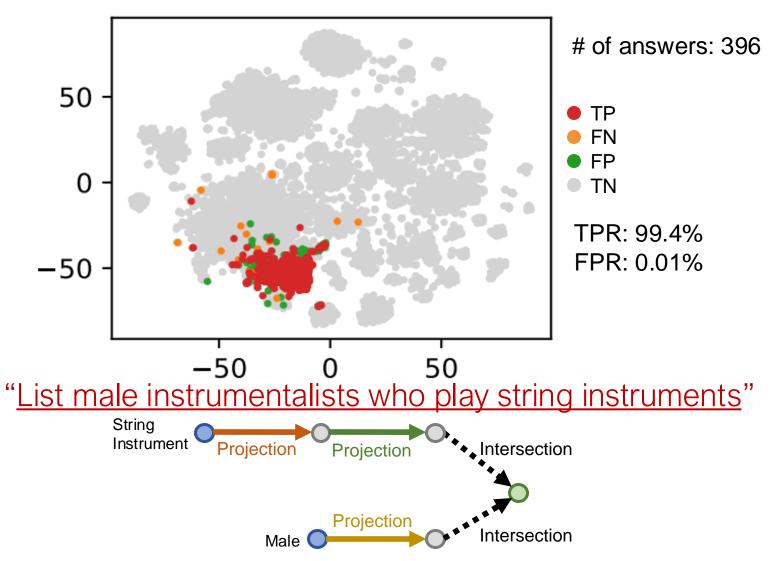




"List male instrumentalists who play string instruments"



"List male instrumentalists who play string instruments"



Summary

- We introduce answering predictive queries on large knowledge graphs.
- The key idea is to embed queries by navigating the embedding space!
 - We embed the query by composing learned operators
 - Embedding of the query is close to its answers in the embedding space