Syntaks og semantik

Lektion 12

10 april 2007

Blokke

- Abstrakt syntaks for Bip
- 2 Environment-store-modellen
- Aritmetiske og boolske udtryk
- Variabel-erklæringer
- 5 Kommandoer minus procedurekald
- Scoperegler
- Statisk binding

Bip = Bims + blokke og parameterløse procedurer:

Kom:
$$S ::= x := a \mid \text{skip} \mid S_1; S_2 \mid \text{if } b \text{ then } S_1 \text{ else } S_2 \mid \text{while } b \text{ do } S \mid \text{begin } D_V \mid D_P \mid S \text{ end} \mid \text{call } p$$
ErkV: $D_V ::= \text{var } x := a; D_V \mid \varepsilon$

ErkP:
$$D_P ::= \operatorname{proc} p \text{ is } S; D_P \mid \varepsilon$$

- lokale erklæringer af variable (ErkV) og procedurer (ErkP) i en blok
- variable initialiseres ved erklæring
- semantikken af procedurekald afhænger af scope-regler
- bogen beskæftiger sig både med dynamisk og statisk scope
- vi lægger mest vægt på statisk scope her

- brug for ny tilstandsmodel for at kunne erklære variable
- før: Tilstande = $Var \rightarrow \mathbb{Z}$
- nu: $Var \rightarrow Loc \rightarrow \mathbb{Z}$

Abstrakt syntaks

- Loc: lokationer; lager-adresser
- \Rightarrow en tilstand (*env_V*, *sto*) beskrives ved:

env_V variabel-environment

- hvilken adresse er en given variabel bundet til?
- $\mathbf{Env}_V = \mathbf{Var} \cup \{\mathbf{next}\} \rightharpoonup \mathbf{Loc}$
- next peger til næste frie lokation
- ullet for os: Loc $=\mathbb{Z}$

sto store

- hvilken værdi indeholder en given adresse?
- Store = Loc $\rightharpoonup \mathbb{Z}$ • opdatering: $sto[\ell \mapsto v](\ell') = \begin{cases} sto(\ell') & \text{hvis } \ell' \neq \ell \\ v & \text{hvis } \ell' = \ell_{4/18} \end{cases}$

Udtryk

ErkV:
$$D_V ::= \text{var } x := a; D_V \mid \varepsilon$$

- erklæringer modificerer env_V (pga. nye variable) og sto (pga. nye værdier til nye variable)
- ⇒ transitionssystem:
 - konfigurationer

$$\Gamma_{DV} = \text{ErkV} \times \text{Env}_V \times \text{Store} \cup \text{Env}_V \times \text{Store}$$

- slutkonfigurationer $T_{DV} = \mathbf{Env}_V \times \mathbf{Store}$
 - dvs. konfigurationer (D_V , env_V , sto) og (env_V , sto)

[var-erkl_{bss}]

$$\frac{\langle \mathcal{D}_V, \textit{env}_V[x \mapsto \ell][\mathsf{next} \mapsto \mathsf{new}(\ell)], \textit{sto}[\ell \mapsto v] \rangle \rightarrow_{\mathit{DV}} \langle \textit{env}_V, \textit{sto}' \rangle}{\langle \mathsf{var} \ \textit{x} := \textit{a}; \mathcal{D}_V, \textit{env}_V, \textit{sto} \rangle \rightarrow_{\mathit{DV}} \langle \textit{env}_V, \textit{sto}' \rangle} \\ \mathsf{hvor} \ \textit{env}_V, \textit{sto} \vdash \textit{a} \rightarrow_{\textit{a}} \textit{v} \ \mathsf{og} \ \ell = \textit{env}_V(\mathsf{next})$$

[tom-var-erkl_{bss}] $\langle \varepsilon, env_V, sto \rangle \rightarrow_{DV} \langle env_V, sto \rangle$

- big-step: variabelerklæringer sker i ét hug
- new : Loc \rightarrow Loc giver næste lokation; new $(\ell) = \ell + 1$

- også procedure-environment $env_P \in \mathbf{Env}_P$, til at holde styr på procedurer
- med tilhørende big-step-semantik for procedure-erklæringer $(\Gamma_{DP}, \rightarrow_{DP}, T_{DP})$
- men det snakker vi om senere
- dvs. procedure-environment env_P, variabel-environment env_V og store sto
- men kommandoer kan ikke ændre env_V og env_P!
- \Rightarrow transitioner på formen env_V , $env_P \vdash \langle S, sto \rangle \rightarrow sto'$
- dvs. konfigurationer Kom x Store ∪ Store
- og slutkonfigurationer Store

Abstrakt syntaks

$$[ass_{bss}] \qquad env_{V}, env_{P} \vdash \langle x := a, sto \rangle \rightarrow sto[\ell \mapsto v] \\ \qquad \qquad hvor \ env_{V}, sto \vdash a \rightarrow_{a} v \ og \ env_{V}(x) = \ell$$

$$[skip_{bss}] \qquad env_{V}, env_{P} \vdash \langle skip, sto \rangle \rightarrow sto$$

$$env_{V}, env_{P} \vdash \langle S_{1}, sto \rangle \rightarrow sto''$$

$$env_{V}, env_{P} \vdash \langle S_{2}, sto'' \rangle \rightarrow sto'$$

$$env_{V}, env_{P} \vdash \langle S_{1}, S_{2}, sto \rangle \rightarrow sto'$$

$$env_{V}, env_{P} \vdash \langle S_{1}, sto \rangle \rightarrow sto'$$

$$env_{V}, env_{P} \vdash \langle if \ b \ then \ S_{1} \ else \ S_{2}, sto \rangle \rightarrow sto'$$

$$hvis \ env_{V}, sto \vdash b \rightarrow_{b} tt$$

$$[if-falsk_{bss}] \qquad env_{V}, env_{P} \vdash \langle if \ b \ then \ S_{1} \ else \ S_{2}, sto \rangle \rightarrow sto'$$

$$env_{V}, env_{P} \vdash \langle if \ b \ then \ S_{1} \ else \ S_{2}, sto \rangle \rightarrow sto'$$

$$env_{V}, env_{P} \vdash \langle if \ b \ then \ S_{1} \ else \ S_{2}, sto \rangle \rightarrow sto'$$

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Abstrakt syntaks

 $env_V, env_P \vdash \langle S, sto \rangle \rightarrow sto''$ $env_V, env_P \vdash \langle while b do S, sto'' \rangle \rightarrow sto'$ [while-sand_{hss}] $env_V, env_P \vdash \langle while b do S, sto \rangle \rightarrow sto'$ hvis env_V , $sto \vdash b \rightarrow_b tt$ [while-falskbss] $env_V, env_P \vdash \langle while b do S, sto \rangle \rightarrow sto$ hvis env_V , $sto \vdash b \rightarrow_b ff$ $\langle D_V, env_V, sto \rangle \rightarrow_{DV} \langle env_V, sto'' \rangle$ $enV_V \vdash \langle D_P, env_P \rangle \rightarrow_{DP} enV_P$ $enV_{V}, enV_{D} \vdash \langle S, sto'' \rangle \rightarrow sto'$ [blok_{bss}] $env_V, env_P \vdash \langle begin D_V D_P S end, sto \rangle \rightarrow sto'$

- dynamisk binding af variable og procedurer: y = 10
- statisk binding af variable og procedurer: y = 9
- også muligt: statisk binding af variable og dynamisk binding af procedurer, og omvendt

- statisk binding af variable og procedurer: ved procedurekald skal anvendes det variabel- og procedure-environment der fandtes ved erklæringen
- ⇒ procedurer skal huske env_V og env_P
- \Rightarrow Env_P = Pnavne \rightarrow Kom \times Env_V \times Env_P
 - (**Pnavne**: procedurenavne)
 - dvs. **Env**_P består af partielle afbildninger $p \mapsto \langle S, env_V, env_P \rangle$
 - S: procedure "kroppen"
 - env_V, env_P: variabel- og procedure-environment da p blev erklæret
 - en rekursiv definition!
 - big-step-semantik:
 - tilstande ErkP × Env_P ∪ Env_P
 - sluttilstande Env_P
 - transitioner \rightarrow_{DP}

$$\begin{array}{ll} [\mathsf{proc}_{\mathsf{bss}}] & \frac{\mathsf{env}_V \vdash \langle D_P, \mathsf{env}_P[p \mapsto (S, \mathsf{env}_V, \mathsf{env}_P)] \rangle \to_{\mathsf{DP}} \mathsf{env}_P}{\mathsf{env}_V \vdash \langle \mathsf{proc} \ \mathsf{p} \ \mathsf{is} \ S \ ; D_P, \mathsf{env}_P \rangle \to_{\mathsf{DP}} \mathsf{env}_P} \\ [\mathsf{proc}\text{-}\mathsf{tom}_{\mathsf{bss}}] & \frac{\mathsf{env}_V \vdash \langle \varepsilon, \mathsf{env}_P \rangle \to_{\mathsf{DP}} \mathsf{env}_P}{\mathsf{env}_P \vdash \langle \varepsilon, \mathsf{env}_P \rangle \to_{\mathsf{DP}} \mathsf{env}_P} \\ [\mathsf{call}_{\mathsf{bss}}] & \frac{\mathsf{env}_V[\mathsf{next} \mapsto \ell], \mathsf{env}_P \vdash \langle S, \mathsf{sto} \rangle \to \mathsf{sto}'}{\mathsf{env}_V, \mathsf{env}_P \vdash \langle \mathsf{call} \ \mathsf{p}, \mathsf{sto} \rangle \to \mathsf{sto}'} \\ & \mathsf{hvor} \ \mathsf{env}_P(p) = (S, \mathsf{env}_V, \mathsf{env}_P) \\ & \mathsf{og} \ \ell = \mathsf{env}_V(\mathsf{next}) \end{array}$$

Procedurer med parametre

- 8 Referenceparametre
- Rekursion
 - Værdiparametre

At udvide **Bip** med procedurer med én referenceparameter:

```
Kom: S ::= x := a \mid \text{skip} \mid S_1; S_2 \mid \text{if } b \text{ then } S_1 \text{ else } S_2 \mid \text{while } b \text{ do } S \mid \text{begin } D_V \mid D_P \mid S \text{ end} \mid \text{call } p(y)

ErkV: D_V ::= \text{var } x := a; D_V \mid \varepsilon

ErkP: D_P ::= \text{proc } p(\text{var } x) \text{ is } S; D_P \mid \varepsilon
```

- referenceparametre: den formelle parameter x er en reference til adressen på den aktuelle parameter y

• procedure-environment:

$$\mathsf{Env}_P = \mathsf{Pnavne} \rightharpoonup \mathsf{Kom} \times \mathsf{Var} \times \mathsf{Env}_V \times \mathsf{Env}_P$$

- skal huske navnet på den formelle parameter
- at erklære procedurer:

$$[\operatorname{proc}_{\operatorname{bss}}] \quad \frac{\operatorname{env}_V \vdash \langle D_P, \operatorname{env}_P[p \mapsto (S, x, \operatorname{env}_V, \operatorname{env}_P)] \rangle \rightarrow_{DP} \operatorname{env}_P}{\operatorname{env}_V \vdash \langle \operatorname{proc} p (\operatorname{var} x) \text{ is } S; D_P, \operatorname{env}_P \rangle \rightarrow_{DP} \operatorname{env}_P}$$

$$[\operatorname{proc-tom}_{\operatorname{bss}}] \quad \operatorname{env}_V \vdash \langle \varepsilon, \operatorname{env}_P \rangle \rightarrow_{DP} \operatorname{env}_P$$

at kalde procedurer:

Problem: dén regel tillader ikke rekursive procedurekald

fordi enV_P er procedure-environmentet fra før p blev erklæret

Løsning: ny regel:

At udvide **Bip** med procedurer med én værdiparameter:

```
Kom: S ::= x := a \mid \text{skip} \mid S_1; S_2 \mid \text{if } b \text{ then } S_1 \text{ else } S_2 \mid \text{while } b \text{ do } S \mid \text{begin } D_V \mid D_P \mid S \text{ end} \mid \text{call } p(a)

ErkV: D_V ::= \text{var } x := a; D_V \mid \varepsilon

ErkP: D_P ::= \text{proc } p(\text{var } x) \text{ is } S; D_P \mid \varepsilon
```

- værdiparametre: den formelle parameter x bliver til en lokal variabel i proceduren, med startværdi = værdien af den aktuelle parameter

• procedure-erklæringer (uændret):

$$[\operatorname{proc}_{\operatorname{bss}}] \quad \frac{\operatorname{\textit{env}}_V \vdash \langle D_P, \operatorname{\textit{env}}_P[p \mapsto (S, x, \operatorname{\textit{env}}_V, \operatorname{\textit{env}}_P)] \rangle \rightarrow_{\mathit{DP}} \operatorname{\textit{env}}_P}{\operatorname{\textit{env}}_V \vdash \langle \operatorname{proc} p (\operatorname{var} x) \text{ is } S; D_P, \operatorname{\textit{env}}_P \rangle \rightarrow_{\mathit{DP}} \operatorname{\textit{env}}_P}$$

[proc-tom_{bss}] $env_V \vdash \langle \varepsilon, env_P \rangle \rightarrow_{DP} env_P$

procedurekald:

$$[\text{call-val}_{\text{bss}}] \qquad \frac{\textit{env}_{V}[x \mapsto \ell][\mathsf{next} \mapsto \mathsf{new}(\ell)], \textit{env}_{P}}{\frac{\vdash \langle S, \textit{sto}[\ell \mapsto v] \rangle \rightarrow \textit{sto}'}{\textit{env}_{V}, \textit{env}_{P} \vdash \langle \texttt{call} \ \textit{p}(\textit{a}), \textit{sto} \rangle \rightarrow \textit{sto}'}}{\mathsf{hvor} \ \textit{env}_{P}(\textit{p}) = (S, x, \textit{env}_{V}, \textit{env}_{P}),}}$$

 env_V , $sto \vdash a \rightarrow_a v \text{ og } \ell = env_V(\text{next})$

 env_V , $sto \vdash a \rightarrow_a v \text{ og } \ell = env_V(\text{next})$

$$\begin{array}{c} \textit{env}_V[x \mapsto \ell][\mathsf{next} \mapsto \mathsf{new}(\ell)], \\ \textit{env}_P[p \mapsto (S, x, \textit{env}_V, \textit{env}_P)] \\ \hline [\mathsf{call-val-rec}_\mathsf{bss}] & \frac{\vdash \langle S, \textit{sto}[\ell \mapsto v] \rangle \to \textit{sto}'}{\textit{env}_V, \textit{env}_P \vdash \langle \mathsf{call} \ p(a), \textit{sto} \rangle \to \textit{sto}'} \\ & \mathsf{hvor} \ \textit{env}_P(p) = (S, x, \textit{env}_V, \textit{env}_P), \end{array}$$