

Problem Set 2

ECN 301E - Fall 2024

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Question 1

Define the following terms in your own words.

- a. Experiment and sample space
- b. Random variable
- c. Probability distribution
- d. Cumulative probability distribution
- e. Expected value and variance
- f. Joint probability distribution
- g. Marginal and conditional probability distributions
- h. Covariance and correlation
- i. Skewness and kurtosis

Question 2

Let Y denote the number of **heads** that occur when two coins are tossed. Assume the probability of a heads is 0.4 on either coin.

- a. Derive the probability distribution of Y .
- b. Derive the mean and variance of Y .

Question 3

The following table gives the joint probability distribution between employment status (Y) and college graduation (X) among those either employed or looking for work (unemployed) in the working-age population of Turkey.

	Unemployed $Y = 0$	Employed $Y = 1$	Total
Non-college grads $X = 0$	0.026	0.576	0.602
College grads $X = 1$	0.009	0.389	0.398
Total	0.035	0.965	1.000

- a. Compute $E(Y)$.
- b. Calculate $E(Y|X = 1)$ and $E(Y|X = 0)$.
- c. Calculate the unemployment rate for college graduates and non-college graduates.
- d. A randomly selected member of this population reports being unemployed. What is the probability that this worker is a college graduate? A non-college graduate?
- e. Are educational achievement and employment status independent? Explain.

Question 4

Suppose X is a Bernoulli random variable with $P(X = 1) = p$ and $P(X = 0) = 1 - p$.

- a. Find $E(X^4)$.
- b. Suppose that $p = 0.53$. Compute the mean, variance, skewness, and kurtosis of X .