# SVM Handwriting Classification Final Exam

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## 1 Digit 3 Versus 6

The results obtained by the Nonlinear Rescaling-Augmented Lagrangian Matlab code were identical (to within the sigma specified) to the results obtained for the midterm exam using AMPL. This was the case for both the radial and polynomial kernels. Table 1 summarizes the misclassification error rate achieved.

Table 1: Misclassification Error: Digits 3 vs 6

Data Set	Error	95% Confide	ence Interval
		Lower Bound	Upper Bound
Polynomial Training	0.000	0.000	0.000
Radial Training	0.000	0.000	0.000
Polynomial Testing	0.037	-0.004	0.077
Radial Testing	0.024	-0.010	0.058

### 1.1 Polynomial Kernel Output

1.1 Polynomial Kernel Output	
Iteration: 1  * Newton Step: 1 Norm Gradient Phi: 7.017994e+03  * Newton Step: 2 Norm Gradient Phi: 2.110626e+03  * Newton Step: 3 Norm Gradient Phi: 1.583672e+02  * Newton Step: 4 Norm Gradient Phi: 2.820811e+00  * Newton Step: 5 Norm Gradient Phi: 1.207266e+00  * Newton Step: 6 Norm Gradient Phi: 4.798095e-01  * Newton Step: 7 Norm Gradient Phi: 1.613325e-01  Newton Steps: 7  Objective Value: -5.956487e+01  Equality Constraints Infeasibility: 1.026272e-04  Inequality Constraints Infeasibility: 1.461072e-03  Complementarity: 9.999000e-03  Norm of Gradient of Lagrangian: 1.613325e-01  Max Stop Criteria: 1.837724e+00	Iteration: 6  * Newton Step: 1 Norm Gradient Phi: 1.617247e-05  * Newton Step: 2 Norm Gradient Phi: 1.649713e-08 Newton Steps: 2 Objective Value: -6.001664e+01 Equality Constraints Infeasibility: 7.590450e-08 Inequality Constraints Infeasibility: 1.619316e-06 Complementarity: 1.403848e-06 Norm of Gradient of Lagrangian: 1.649713e-08 Max Stop Criteria: 2.743425e-04
Iteration: 2  * Newton Step: 1 Norm Gradient Phi: 3.095329e+01  * Newton Step: 2 Norm Gradient Phi: 9.970849e-01  * Newton Step: 3 Norm Gradient Phi: 2.440984e-01  * Newton Step: 4 Norm Gradient Phi: 3.200653e-02  * Newton Step: 5 Norm Gradient Phi: 2.926546e-03  Newton Steps: 5  Objective Value: -5.997201e+01  Equality Constraints Infeasibility: 2.554650e-05  Inequality Constraints Infeasibility: -2.915931e-04  Complementarity: 1.067875e-03  Norm of Gradient of Lagrangian: 2.926546e-03  Max Stop Criteria: 3.760220e-01	Equality Constraints Infeasibility: 2.186758e-08 Inequality Constraints Infeasibility: 2.134740e-06 Complementarity: 3.670600e-07 Norm of Gradient of Lagrangian: 1.990369e-10 Max Stop Criteria: 6.836852e-05 Iteration: 8 * Newton Step: 1 Norm Gradient Phi: 7.788941e-08 Newton Steps: 1 Objective Value: -6.001665e+01 Equality Constraints Infeasibility: 5.995201e-09 Inequality Constraints Infeasibility: 8.251807e-07 Complementarity: 9.578625e-08
Iteration: 3  * Newton Step: 1 Norm Gradient Phi: 5.925091e-01  * Newton Step: 2 Norm Gradient Phi: 8.074392e-02  * Newton Step: 3 Norm Gradient Phi: 1.736469e-02  * Newton Step: 4 Norm Gradient Phi: 1.350338e-03  * Newton Step: 5 Norm Gradient Phi: 1.591475e-05  Newton Steps: 5  Objective Value: -6.001292e+01  Equality Constraints Infeasibility: 3.850654e-07  Inequality Constraints Infeasibility: -9.212220e-06  Complementarity: 9.993395e-05  Norm of Gradient of Lagrangian: 1.591475e-05	Norm of Gradient of Lagrangian: 7.788941e-08 Max Stop Criteria: 1.732893e-05
Max Stop Criteria: 4.011331e-02	Iteration: 10  * Newton Step: 1 Norm Gradient Phi: 3.376285e-10 Newton Steps: 1 Objective Value: -6.001665e+01 Equality Constraints Infeasibility: 4.293496e-10 Inequality Constraints Infeasibility: 7.194552e-08 Complementarity: 6.787791e-09 Norm of Gradient of Lagrangian: 3.376285e-10 Max Stop Criteria: 1.167655e-06  Iteration: 11  * Newton Step: 1 Norm Gradient Phi: 8.656509e-11 Newton Steps: 1
* Newton Step: 1 Norm Gradient Phi: 2.343069e-04  * Newton Step: 2 Norm Gradient Phi: 2.512844e-06  Newton Steps: 2  Objective Value: -6.001659e+01  Equality Constraints Infeasibility: 2.448429e-07  Inequality Constraints Infeasibility: 4.805526e-06  Complementarity: 5.361956e-06  Norm of Gradient of Lagrangian: 2.512844e-06  Max Stop Criteria: 1.166411e-03	Objective Value: -6.001665e+01 Equality Constraints Infeasibility: 1.133764e-10 Inequality Constraints Infeasibility: 1.955965e-08 Complementarity: 1.782874e-09 Norm of Gradient of Lagrangian: 8.656509e-11 Max Stop Criteria: 3.032099e-07

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Radial Kernel Output
Iteration: 1
                                                      Iteration: 6
* Newton Step: 1 Norm Gradient Phi: 6.931331e+03
                                                      * Newton Step: 1 Norm Gradient Phi: 7.022949e-05
                                                      * Newton Step: 2 Norm Gradient Phi: 1.932518e-07
* Newton Step: 2 Norm Gradient Phi: 2.484910e+03
* Newton Step: 3 Norm Gradient Phi: 1.432481e+03
                                                      Newton Steps: 2
* Newton Step: 4 Norm Gradient Phi: 4.175104e+02
                                                      Objective Value: -5.383860e+01
* Newton Step: 5 Norm Gradient Phi: 1.604049e+02
                                                      Equality Constraints Infeasibility: 2.779462e-07
* Newton Step: 6 Norm Gradient Phi: 1.159400e+02
                                                      Inequality Constraints Infeasibility: 2.328036e-05
* Newton Step: 7 Norm Gradient Phi: 1.808279e+00
                                                      Complementarity: 6.320571e-06
                                                      Norm of Gradient of Lagrangian: 1.932518e-07
* Newton Step: 8 Norm Gradient Phi: 7.984806e-01
* Newton Step: 9 Norm Gradient Phi: 3.144736e-01
                                                      Max Stop Criteria: 1.109351e-03
* Newton Step: 10 Norm Gradient Phi: 9.388754e-02
Newton Steps: 10
                                                      Iteration: 7
Objective Value: -5.325819e+01
                                                      * Newton Step: 1 Norm Gradient Phi: 1.243716e-05
Equality Constraints Infeasibility: 8.085655e-05
                                                      * Newton Step: 2 Norm Gradient Phi: 7.041632e-09
Inequality Constraints Infeasibility: 5.797742e-04
                                                      Newton Steps: 2
Complementarity: 9.950263e-03
                                                      Objective Value: -5.383864e+01
Norm of Gradient of Lagrangian: 9.388754e-02
                                                      Equality Constraints Infeasibility: 1.233954e-07
Max Stop Criteria: 1.911769e+00
                                                      Inequality Constraints Infeasibility: 9.859381e-06
                                                      Complementarity: 3.600585e-06
                                                      Norm of Gradient of Lagrangian: 7.041632e-09
* Newton Step: 1 Norm Gradient Phi: 4.161087e+01
                                                      Max Stop Criteria: 5.393950e-04
* Newton Step: 2 Norm Gradient Phi: 1.028650e+00
* Newton Step: 3 Norm Gradient Phi: 2.475090e-01
* Newton Step: 4 Norm Gradient Phi: 3.003328e-02
                                                      * Newton Step: 1 Norm Gradient Phi: 2.843813e-06
* Newton Step: 5 Norm Gradient Phi: 1.824418e-03
                                                      Newton Steps: 1
Newton Steps: 5
                                                      Objective Value: -5.383865e+01
Objective Value: -5.379403e+01
                                                      Equality Constraints Infeasibility: 6.282017e-08
Equality Constraints Infeasibility: 3.654177e-05
                                                      Inequality Constraints Infeasibility: 5.381736e-06
Inequality Constraints Infeasibility: 1.475506e-03
                                                      Complementarity: 2.257747e-06
Complementarity: 9.879219e-04
                                                      Norm of Gradient of Lagrangian: 2.843813e-06
Norm of Gradient of Lagrangian: 1.824418e-03
                                                      Max Stop Criteria: 3.081614e-04
Max Stop Criteria: 3.905918e-01
Iteration: 3
                                                      * Newton Step: 1 Norm Gradient Phi: 9.428880e-07
* Newton Step: 1 Norm Gradient Phi: 2.292880e-01
                                                      Newton Steps: 1
* Newton Step: 2 Norm Gradient Phi: 5.735189e-02
                                                      Objective Value: -5.383866e+01
* Newton Step: 3 Norm Gradient Phi: 1.169970e-02
                                                      Equality Constraints Infeasibility: 3.547164e-08
* Newton Step: 4 Norm Gradient Phi: 9.913998e-04
                                                      Inequality Constraints Infeasibility: 3.339605e-06
* Newton Step: 5 Norm Gradient Phi: 1.363580e-05
                                                      Complementarity: 1.525655e-06
                                                      Norm of Gradient of Lagrangian: 9.428880e-07
Newton Steps: 5
Objective Value: -5.383408e+01
                                                      Max Stop Criteria: 1.984124e-04
Equality Constraints Infeasibility: 2.965729e-06
Inequality Constraints Infeasibility: 6.034579e-04
                                                      Iteration: 10
Complementarity: 1.478299e-04
                                                      * Newton Step: 1 Norm Gradient Phi: 4.186526e-07
Norm of Gradient of Lagrangian: 1.363580e-05
                                                      Newton Steps: 1
Max Stop Criteria: 5.126194e-02
                                                      Objective Value: -5.383866e+01
                                                      Equality Constraints Infeasibility: 2.303498e-08
                                                      Inequality Constraints Infeasibility: 2.297566e-06
Iteration: 4
                                                      Complementarity: 1.087752e-06
* Newton Step: 1 Norm Gradient Phi: 4.412096e-03
* Newton Step: 2 Norm Gradient Phi: 2.943626e-04
                                                      Norm of Gradient of Lagrangian: 4.186526e-07
* Newton Step: 3 Norm Gradient Phi: 2.736765e-06
                                                      Max Stop Criteria: 1.395656e-04
Newton Steps: 3
Objective Value: -5.383792e+01
                                                      Iteration: 11
Equality Constraints Infeasibility: 1.896586e-06
                                                      * Newton Step: 1 Norm Gradient Phi: 2.045800e-07
Inequality Constraints Infeasibility: 2.682708e-04
                                                      Newton Steps: 1
                                                      Objective Value: -5.383866e+01
Complementarity: 3.806888e-05
Norm of Gradient of Lagrangian: 2.736765e-06
                                                      Equality Constraints Infeasibility: 1.612770e-08
Max Stop Criteria: 9.680553e-03
                                                      Inequality Constraints Infeasibility: 1.674627e-06
                                                      Complementarity: 8.088111e-07
Iteration: 5
                                                      Norm of Gradient of Lagrangian: 2.045800e-07
* Newton Step: 1 Norm Gradient Phi: 4.640537e-04
                                                      Max Stop Criteria: 1.033786e-04
* Newton Step: 2 Norm Gradient Phi: 6.560533e-06
Newton Steps: 2
                                                      Iteration: 12
Objective Value: -5.383848e+01
                                                      * Newton Step: 1 Norm Gradient Phi: 1.060876e-07
Equality Constraints Infeasibility: 7.127341e-07
                                                      Newton Steps: 1
Inequality Constraints Infeasibility: 7.397461e-05
                                                      Objective Value: -5.383866e+01
Complementarity: 1.335408e-05
                                                      Equality Constraints Infeasibility: 1.196548e-08
Norm of Gradient of Lagrangian: 6.560533e-06
                                                      Inequality Constraints Infeasibility: 1.271092e-06
Max Stop Criteria: 2.818255e-03
                                                      Complementarity: 6.218835e-07
                                                      Norm of Gradient of Lagrangian: 1.060876e-07
                                                      Max Stop Criteria: 7.953896e-05
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Iteration: 20 \* Newton Step: 1 Norm Gradient Phi: 5.734159e-08 \* Newton Step: 1 Norm Gradient Phi: 3.067153e-09 Newton Steps: 1 Newton Steps: 1 Objective Value: -5.383866e+01 Objective Value: -5.383866e+01 Equality Constraints Infeasibility: 9.255843e-09 Equality Constraints Infeasibility: 2.721469e-09 Inequality Constraints Infeasibility: 9.952126e-07 Inequality Constraints Infeasibility: 2.966841e-07 Complementarity: 4.913232e-07 Complementarity: 1.504992e-07 Norm of Gradient of Lagrangian: 5.734159e-08 Norm of Gradient of Lagrangian: 3.067153e-09 Max Stop Criteria: 6.299114e-05 Max Stop Criteria: 1.962085e-05 \* Newton Step: 1 Norm Gradient Phi: 3.194075e-08 \* Newton Step: 1 Norm Gradient Phi: 2.883678e-09 Newton Steps: 1 Newton Steps: 1 Objective Value: -5.383866e+01 Objective Value: -5.383866e+01 Equality Constraints Infeasibility: 7.381562e-09 Equality Constraints Infeasibility: 2.393165e-09 Inequality Constraints Infeasibility: 7.987023e-07 Inequality Constraints Infeasibility: 2.609539e-07 Complementarity: 3.969559e-07 Complementarity: 1.326255e-07 Norm of Gradient of Lagrangian: 3.194075e-08 Norm of Gradient of Lagrangian: 2.883678e-09 Max Stop Criteria: 5.104040e-05 Max Stop Criteria: 1.731761e-05 Iteration: 15 Iteration: 22 \* Newton Step: 1 Norm Gradient Phi: 1.822726e-08 \* Newton Step: 1 Norm Gradient Phi: 2.764939e-09 Newton Steps: 1 Newton Steps: 1 Objective Value: -5.383866e+01 Objective Value: -5.383866e+01 Equality Constraints Infeasibility: 6.024922e-09 Equality Constraints Infeasibility: 2.120128e-09 Inequality Constraints Infeasibility: 6.540616e-07 Inequality Constraints Infeasibility: 2.312101e-07 Complementarity: 3.267641e-07 Complementarity: 1.177052e-07 Norm of Gradient of Lagrangian: 2.764939e-09 Norm of Gradient of Lagrangian: 1.822726e-08 Max Stop Criteria: 4.213668e-05 Max Stop Criteria: 1.539103e-05 Iteration: 16 Iteration: 23 \* Newton Step: 1 Norm Gradient Phi: 2.645183e-09 \* Newton Step: 1 Norm Gradient Phi: 1.066175e-08 Newton Steps: 1 Newton Steps: 1 Objective Value: -5.383866e+01 Objective Value: -5.383866e+01 Equality Constraints Infeasibility: 5.008411e-09 Equality Constraints Infeasibility: 1.890505e-09 Inequality Constraints Infeasibility: 2.062003e-07 Inequality Constraints Infeasibility: 5.447012e-07 Complementarity: 1.051290e-07 Complementarity: 2.732712e-07 Norm of Gradient of Lagrangian: 1.066175e-08 Norm of Gradient of Lagrangian: 2.645183e-09 Max Stop Criteria: 3.533335e-05 Max Stop Criteria: 1.376410e-05 Iteration: 17 Iteration: 24 \* Newton Step: 1 Norm Gradient Phi: 6.539583e-09 \* Newton Step: 1 Norm Gradient Phi: 2.523492e-09 Newton Steps: 1 Newton Steps: 1 Objective Value: -5.383866e+01 Objective Value: -5.383866e+01 Equality Constraints Infeasibility: 4.226518e-09 Equality Constraints Infeasibility: 1.695872e-09 Inequality Constraints Infeasibility: 4.601386e-07Inequality Constraints Infeasibility: 1.849808e-07 Complementarity: 2.316487e-07 Complementarity: 9.443553e-08 Norm of Gradient of Lagrangian: 6.539583e-09 Norm of Gradient of Lagrangian: 2.523492e-09 Max Stop Criteria: 3.002438e-05 Max Stop Criteria: 1.237838e-05 Iteration: 18 Iteration: 25 \* Newton Step: 1 Norm Gradient Phi: 4.412573e-09 \* Newton Step: 1 Norm Gradient Phi: 2.396222e-09 Newton Steps: 1 Newton Steps: 1 Objective Value: -5.383866e+01 Objective Value: -5.383866e+01 Equality Constraints Infeasibility: 3.611950e-09 Equality Constraints Infeasibility: 1.529369e-09 Inequality Constraints Infeasibility: 3.934905e-07 Inequality Constraints Infeasibility: 1.668300e-07 Complementarity: 1.986761e-07 Complementarity: 8.527081e-08 Norm of Gradient of Lagrangian: 4.412573e-09 Norm of Gradient of Lagrangian: 2.396222e-09 Max Stop Criteria: 2.580669e-05 Max Stop Criteria: 1.118891e-05 Iteration: 19 Iteration: 26 \* Newton Step: 1 Norm Gradient Phi: 3.456332e-09 \* Newton Step: 1 Norm Gradient Phi: 2.263485e-09 Newton Steps: 1 Newton Steps: 1 Objective Value: -5.383866e+01 Objective Value: -5.383866e+01 Equality Constraints Infeasibility: 3.120528e-09 Equality Constraints Infeasibility: 1.385853e-09 Inequality Constraints Infeasibility: 3.400896e-07 Inequality Constraints Infeasibility: 1.511892e-07 Complementarity: 1.721440e-07 Complementarity: 7.735961e-08 Norm of Gradient of Lagrangian: 3.456332e-09 Norm of Gradient of Lagrangian: 2.263485e-09 Max Stop Criteria: 2.240378e-05 Max Stop Criteria: 1.016067e-05 Iteration: 27 \* Newton Step: 1 Norm Gradient Phi: 2.133584e-09 Newton Steps: 1 Objective Value: -5.383866e+01 Equality Constraints Infeasibility: 1.261428e-09 Inequality Constraints Infeasibility: 1.376203e-07 Complementarity: 7.048552e-08 Norm of Gradient of Lagrangian: 2.133584e-09 Max Stop Criteria: 9.266044e-06

Table 2: Misclassification Error: All Digits

Data Set	Error	95% Confide	ence Interval
		Lower Bound	Upper Bound
Radial Training C=2 Radial Training C=100 Radial Testing C=2	0.0526 0.001 0.222	0.038 -0.001 0.182	0.067 0.003 0.262
Radial Testing C=100	0.197	0.159	0.236

## 2 All Digits

The radial kernel produced the best results for the 3 versus 6 case, so it was used for the full problem. However, while C=2 produced the best results for the 3 versus 6 case, C=100 was used for the full problem. The Nonlinear Rescaling-Augmented Lagrangian method results for C=2 match the AMPL results from the midterm exactly (to within the sigma specified). However, the Nonlinear Rescaling-Augmented Lagrangian code was also run with C=100, which produced a slightly better error rate.

For the full run, epsilon was set to 1e-4 because the calculation ran too slowly using 1e-5, which was used for the two digit case. This did not appear to affect the overall classifier performance (as compared to the AMPL results from the midterm).

As indicated in Table 2, the overall testing misclassification error achieved by the radial SVM classifier was 0.197 for C=100 and 0.222 for C=2. The C=2 misclassification error matches the AMPL results from the midterm.

## -1 D:-:4 0

2.1 Radial Kernel Digit 0	
Tteration: 1   Norm Gradient Phi: 1.851569e+04	Iteration: 5 * Newton Step: 1 Norm Gradient Phi: 1.072228e-03 * Newton Step: 2 Norm Gradient Phi: 3.652208e-05 Newton Steps: 2 Objective Value: -1.611900e+02 Equality Constraints Infeasibility: 1.316042e-06 Inequality Constraints Infeasibility: 1.857148e-05 Complementarity: 1.394434e-05 Norm of Gradient of Lagrangian: 3.652208e-05 Max Stop Criteria: 8.983516e-03
Equality Constraints Infeasibility: 7.534581e-03 Inequality Constraints Infeasibility: 4.155711e-03 Complementarity: 9.999000e-03 Norm of Gradient of Lagrangian: 3.392874e-01 Max Stop Criteria: 2.541708e+01	Iteration: 6 * Newton Step: 1 Norm Gradient Phi: 9.206424e-05 Newton Steps: 1 Objective Value: -1.611919e+02 Equality Constraints Infeasibility: 3.908648e-07 Incomplete Constraints Infeasibility: 4 E45218e-06
**Newton Step: 1 Norm Gradient Phi: 5.387824e+01  **Newton Step: 2 Norm Gradient Phi: 2.102655e+00  **Newton Step: 3 Norm Gradient Phi: 5.155774e-01  **Newton Step: 4 Norm Gradient Phi: 5.155774e-02  **Newton Step: 5 Norm Gradient Phi: 3.150267e-03  Newton Steps: 5  Objective Value: -1.607204e+02  Equality Constraints Infeasibility: 2.141693e-04  Inequality Constraints Infeasibility: -1.388436e-04  Complementarity: 2.393791e-03  Norm of Gradient of Lagrangian: 3.150267e-03  Max Stop Criteria: 1.126405e+00	Inequality Constraints Infeasibility: 4.545218e-0 Complementarity: 5.099275e-06 Norm of Gradient of Lagrangian: 9.206424e-05 Max Stop Criteria: 1.944635e-03
Iteration: 3  * Newton Step: 1 Norm Gradient Phi: 1.214817e+00  * Newton Step: 2 Norm Gradient Phi: 1.103515e-01  * Newton Step: 3 Norm Gradient Phi: 2.526265e-02  * Newton Step: 4 Norm Gradient Phi: 3.087718e-03  Newton Steps: 4  Objective Value: -1.611146e+02  Equality Constraints Infeasibility: 3.238919e-05  Inequality Constraints Infeasibility: 1.187301e-04  Complementarity: 3.133910e-04	Iteration: 8  * Newton Step: 1 Norm Gradient Phi: 3.833684e-06 Newton Steps: 1 Objective Value: -1.611924e+02 Equality Constraints Infeasibility: 5.230957e-08 Inequality Constraints Infeasibility: 8.735660e-07 Complementarity: 1.196187e-06 Norm of Gradient of Lagrangian: 3.833684e-06 Max Stop Criteria: 2.158108e-04
Norm of Gradient of Lagrangian: 3.087718e-03 Max Stop Criteria: 2.468780e-01	Iteration: 9 * Newton Step: 1 Norm Gradient Phi: 9.377549e-07 Newton Steps: 1
<pre>Iteration: 4 * Newton Step: 1 Norm Gradient Phi: 9.183538e-03 * Newton Step: 2 Norm Gradient Phi: 3.237340e-04 Newton Steps: 2 Objective Value: -1.611794e+02 Equality Constraints Infeasibility: 5.834581e-06 Inequality Constraints Infeasibility: 3.154672e-05 Complementarity: 6.370340e-05</pre>	Objective Value: -1.611924e+02 Equality Constraints Infeasibility: 2.316347e-08 Inequality Constraints Infeasibility: 3.830583e-07 Complementarity: 5.718307e-07 Norm of Gradient of Lagrangian: 9.377549e-07 Max Stop Criteria: 9.939667e-05

Complementarity: 6.370340e-05
Norm of Gradient of Lagrangian: 3.237340e-04
Max Stop Criteria: 4.451503e-02

2.2 Radial Kernel Digit 1	
* Newton Step: 1 Norm Gradient Phi: 3.732292e+04  * Newton Step: 2 Norm Gradient Phi: 1.484191e+04  * Newton Step: 3 Norm Gradient Phi: 7.327838e+03  * Newton Step: 4 Norm Gradient Phi: 9.600119e+02  * Newton Step: 5 Norm Gradient Phi: 9.600119e+02  * Newton Step: 6 Norm Gradient Phi: 9.586526e+00  * Newton Step: 7 Norm Gradient Phi: 1.501459e+00  * Newton Step: 8 Norm Gradient Phi: 6.155011e-01  * Newton Step: 9 Norm Gradient Phi: 2.316943e-01  Newton Step: 9 Norm Gradient Phi: 2.316943e-01  Newton Step: 9 Norm Gradient Phi: 2.387041e-02  Equality Constraints Infeasibility: 2.387041e-02  Inequality Constraints Infeasibility: 8.619943e-03  Complementarity: 9.999000e-03  Norm of Gradient of Lagrangian: 2.316943e-01  Max Stop Criteria: 6.526028e+01	* Newton Step: 1 Norm Gradient Phi: 1.204973e-05 Newton Steps: 1 Objective Value: -2.470886e+02 Equality Constraints Infeasibility: 4.067702e-07 Inequality Constraints Infeasibility: 9.838724e-06 Complementarity: 2.493687e-06 Norm of Gradient of Lagrangian: 1.204973e-05 Max Stop Criteria: 1.063668e-03
Objective Value: -2.470693e+02 Equality Constraints Infeasibility: 4.133046e-05 Inequality Constraints Infeasibility: 5.956936e-05 Complementarity: 8.504435e-05 Norm of Gradient of Lagrangian: 9.019341e-06 Max Stop Criteria: 8.204599e-02	Iteration: 10  * Newton Step: 1 Norm Gradient Phi: 3.687721e-07 Newton Steps: 1 Objective Value: -2.470888e+02 Equality Constraints Infeasibility: 7.680799e-09 Inequality Constraints Infeasibility: 5.412760e-06 Complementarity: 4.241321e-07 Norm of Gradient of Lagrangian: 3.687721e-07 Max Stop Criteria: 1.315988e-04
Inequality Constraints Infeasibility: 4.748422e-05 Complementarity: 2.124098e-05 Norm of Gradient of Lagrangian: 1.627775e-04 Max Stop Criteria: 1.671530e-02	Newton Steps: 1 Objective Value: -2.470888e+02 Equality Constraints Infeasibility: 7.423726e-09 Inequality Constraints Infeasibility: 5.709365e-06 Complementarity: 3.084846e-07 Norm of Gradient of Lagrangian: 1.846258e-07 Max Stop Criteria: 9.712937e-05

### 2.3 Radial Kernel Digit 2

2.3 Radial Kernel Digit 2	
Iteration: 1  * Newton Step: 1 Norm Gradient Phi: 5.209840e+06  * Newton Step: 2 Norm Gradient Phi: 5.209840e+04  * Newton Step: 3 Norm Gradient Phi: 5.533639e+03  * Newton Step: 4 Norm Gradient Phi: 5.533639e+03  * Newton Step: 4 Norm Gradient Phi: 2.285356e+03  * Newton Step: 5 Norm Gradient Phi: 3.695606e+02  * Newton Step: 6 Norm Gradient Phi: 2.952644e+00  * Newton Step: 7 Norm Gradient Phi: 1.318872e+00  * Newton Step: 8 Norm Gradient Phi: 6.239989e-01  * Newton Step: 9 Norm Gradient Phi: 3.215332e-01  Newton Steps: 9  Objective Value: -6.347290e+02  Equality Constraints Infeasibility: 5.836365e-03  Complementarity: 9.999000e-03	Iteration: 5 * Newton Step: 1 Norm Gradient Phi: 1.432980e-04 * Newton Step: 2 Norm Gradient Phi: 8.789280e-07 Newton Steps: 2 Objective Value: -6.356986e+02 Equality Constraints Infeasibility: 9.058686e-07 Inequality Constraints Infeasibility: 9.058686e-07 Inequality Constraints Infeasibility: 2.027835e-05 Complementarity: 1.591626e-05 Norm of Gradient of Lagrangian: 8.789280e-07 Max Stop Criteria: 3.140923e-03
Norm of Gradient of Lagrangian: 3.215332e-01 Max Stop Criteria: 3.748640e+01	Equality Constraints Infeasibility: 2.576446e-07 Inequality Constraints Infeasibility: 9.686387e-06 Complementarity: 6.821732e-06 Norm of Gradient of Lagrangian: 8.727036e-06
* Newton Step: 1 Norm Gradient Phi: 6.885732e+01  * Newton Step: 2 Norm Gradient Phi: 2.035773e+00  * Newton Step: 3 Norm Gradient Phi: 4.174253e-01  * Newton Step: 4 Norm Gradient Phi: 4.110007e-02  * Newton Step: 5 Norm Gradient Phi: 1.663760e-03  Newton Steps: 5  Objective Value: -6.354974e+02  Equality Constraints Infeasibility: 3.402519e-04  Inequality Constraints Infeasibility: 4.872119e-03  Complementarity: 1.794207e-03  Norm of Gradient of Lagrangian: 1.663760e-03  Max Stop Criteria: 7.595423e-01	Max Stop Criteria: 1.199273e-03  Iteration: 7  * Newton Step: 1 Norm Gradient Phi: 1.280149e-06 Newton Steps: 1 Objective Value: -6.356989e+02 Equality Constraints Infeasibility: 9.926605e-08 Inequality Constraints Infeasibility: 5.081421e-06 Complementarity: 3.323358e-06 Norm of Gradient of Lagrangian: 1.280149e-06 Max Stop Criteria: 5.623771e-04
Iteration: 3  * Newton Step: 1 Norm Gradient Phi: 1.002789e+00  * Newton Step: 2 Norm Gradient Phi: 6.237712e-02  * Newton Step: 3 Norm Gradient Phi: 1.257798e-02  * Newton Step: 4 Norm Gradient Phi: 1.027925e-03  * Newton Step: 5 Norm Gradient Phi: 1.021925e-05  Newton Steps: 5  Objective Value: -6.356773e+02  Equality Constraints Infeasibility: 3.900675e-05  Inequality Constraints Infeasibility: 1.268359e-04  Complementarity: 1.509164e-04  Norm of Gradient of Lagrangian: 1.021925e-05  Max Stop Criteria: 8.336291e-02	Iteration: 8  * Newton Step: 1 Norm Gradient Phi: 2.968621e-07 Newton Steps: 1 Objective Value: -6.356989e+02 Equality Constraints Infeasibility: 4.513808e-08 Inequality Constraints Infeasibility: 2.625121e-06 Complementarity: 1.968064e-06 Norm of Gradient of Lagrangian: 2.968621e-07 Max Stop Criteria: 2.935791e-04
Iteration: 4  * Newton Step: 1 Norm Gradient Phi: 4.259643e-03  * Newton Step: 2 Norm Gradient Phi: 1.940024e-04  * Newton Step: 3 Norm Gradient Phi: 2.796757e-06  Newton Steps: 3  Objective Value: -6.356966e+02  Equality Constraints Infeasibility: 4.948742e-06  Inequality Constraints Infeasibility: 5.642939e-05  Complementarity: 4.289966e-05  Norm of Gradient of Lagrangian: 2.796757e-06  Max Stop Criteria: 1.265257e-02	Equality Constraints Infeasibility: 2.144513e-08 Inequality Constraints Infeasibility: 1.385736e-06 Complementarity: 1.222695e-06 Norm of Gradient of Lagrangian: 6.806404e-08 Max Stop Criteria: 1.630774e-04 Iteration: 10 * Newton Step: 1 Norm Gradient Phi: 1.680559e-08 Newton Steps: 1 Objective Value: -6.356989e+02 Equality Constraints Infeasibility: 1.034971e-08 Inequality Constraints Infeasibility: 7.513223e-07 Complementarity: 7.841448e-07 Norm of Gradient of Lagrangian: 1.680559e-08 Max Stop Criteria: 9.549244e-05

### 2.4 Radial Kernel Digit 3

2.4 Radial Kernel Digit 3	
Iteration: 1  * Newton Step: 1 Norm Gradient Phi: 4.297456e+04  * Newton Step: 2 Norm Gradient Phi: 1.289545e+04  * Newton Step: 3 Norm Gradient Phi: 5.231594e+03  * Newton Step: 4 Norm Gradient Phi: 1.582732e+03  * Newton Step: 5 Norm Gradient Phi: 2.264873e+01  * Newton Step: 6 Norm Gradient Phi: 2.264873e+01  * Newton Step: 7 Norm Gradient Phi: 1.120879e+00  * Newton Step: 7 Norm Gradient Phi: 1.120879e+00  * Newton Step: 8 Norm Gradient Phi: 2.013696e-01  Newton Step: 9 Norm Gradient Phi: 2.013696e-01  Newton Step: 9  Objective Value: -5.949923e+02  Equality Constraints Infeasibility: 1.590373e-02  Inequality Constraints Infeasibility: 7.059411e-03  Complementarity: 9.999000e-03  Norm of Gradient of Lagrangian: 2.013696e-01  Max Stop Criteria: 4.698938e+01	Iteration: 5 * Newton Step: 1 Norm Gradient Phi: 3.644832e-04 * Newton Step: 2 Norm Gradient Phi: 3.414080e-06 Newton Steps: 2 Objective Value: -5.953499e+02 Equality Constraints Infeasibility: 1.137056e-06 Inequality Constraints Infeasibility: 8.407905e-06 Complementarity: 8.052752e-06 Norm of Gradient of Lagrangian: 3.414080e-06 Max Stop Criteria: 3.329665e-03
* Newton Step: 1 Norm Gradient Phi: 6.921989e+01  * Newton Step: 2 Norm Gradient Phi: 2.261957e+00  * Newton Step: 3 Norm Gradient Phi: 4.174322e-01  * Newton Step: 4 Norm Gradient Phi: 3.877653e-02  * Newton Step: 5 Norm Gradient Phi: 4.797372e-03  Newton Steps: 5  Objective Value: -5.951737e+02  Equality Constraints Infeasibility: 3.625927e-04  Inequality Constraints Infeasibility: 4.732402e-04  Complementarity: 7.832286e-04  Norm of Gradient of Lagrangian: 4.797372e-03  Max Stop Criteria: 7.769935e-01	Max Stop Criteria: 9.089859e-04  Iteration: 7  * Newton Step: 1 Norm Gradient Phi: 3.901473e-06 Newton Steps: 1 Objective Value: -5.953502e+02 Equality Constraints Infeasibility: 8.091747e-08 Inequality Constraints Infeasibility: 3.748121e-06 Complementarity: 2.197046e-06 Norm of Gradient of Lagrangian: 3.901473e-06 Max Stop Criteria: 3.240841e-04
Iteration: 3  * Newton Step: 1 Norm Gradient Phi: 2.461743e-01  * Newton Step: 2 Norm Gradient Phi: 4.218244e-02  * Newton Step: 3 Norm Gradient Phi: 8.646029e-03  * Newton Step: 4 Norm Gradient Phi: 9.386652e-04  * Newton Step: 5 Norm Gradient Phi: 2.583588e-05  Newton Steps: 5  Objective Value: -5.953357e+02  Equality Constraints Infeasibility: 4.498559e-05  Inequality Constraints Infeasibility: 2.702953e-05  Complementarity: 1.224544e-04  Norm of Gradient of Lagrangian: 2.583588e-05  Max Stop Criteria: 1.086829e-01	Iteration: 8  * Newton Step: 1 Norm Gradient Phi: 1.427375e-06 Newton Steps: 1 Objective Value: -5.953502e+02 Equality Constraints Infeasibility: 3.588929e-08 Inequality Constraints Infeasibility: 2.606425e-06 Complementarity: 1.407688e-06 Norm of Gradient of Lagrangian: 1.427375e-06 Max Stop Criteria: 1.809314e-04
Iteration: 4  * Newton Step: 1 Norm Gradient Phi: 5.908811e-03  * Newton Step: 2 Norm Gradient Phi: 7.880056e-04  * Newton Step: 3 Norm Gradient Phi: 4.758147e-05  Newton Steps: 3  Objective Value: -5.953485e+02  Equality Constraints Infeasibility: 6.059668e-06  Inequality Constraints Infeasibility: 2.419104e-05  Complementarity: 2.917893e-05  Norm of Gradient of Lagrangian: 4.758147e-05  Max Stop Criteria: 1.627899e-02	Inequality Constraints Infeasibility: 4.586650e-06 Complementarity: 9.657749e-07 Norm of Gradient of Lagrangian: 6.077789e-07 Max Stop Criteria: 1.175712e-04

2.5 Radial Kernel Digit 4	
Iteration: 1  * Newton Step: 1 Norm Gradient Phi: 4.705215e+04  * Newton Step: 2 Norm Gradient Phi: 1.571905e+04  * Newton Step: 3 Norm Gradient Phi: 6.460616e+03  * Newton Step: 4 Norm Gradient Phi: 2.345630e+03  * Newton Step: 5 Norm Gradient Phi: 2.345630e+03  * Newton Step: 6 Norm Gradient Phi: 2.141179e+02  * Newton Step: 7 Norm Gradient Phi: 1.909383e+02  * Newton Step: 7 Norm Gradient Phi: 2.013132e+00  * Newton Step: 8 Norm Gradient Phi: 9.269356e-01  * Newton Step: 9 Norm Gradient Phi: 1.190911e-01  Newton Steps: 10  Objective Value: -6.520045e+02  Equality Constraints Infeasibility: 8.912807e-03  Inequality Constraints Infeasibility: 6.385065e-03  Complementarity: 9.999000e-03  Norm of Gradient of Lagrangian: 1.190911e-01  Max Stop Criteria: 2.755928e+01	Iteration: 6  * Newton Step: 1 Norm Gradient Phi: 2.554797e-05 Newton Steps: 1 Objective Value: -6.519242e+02 Equality Constraints Infeasibility: 1.488310e-07 Inequality Constraints Infeasibility: 6.479363e-06 Complementarity: 4.650661e-06 Norm of Gradient of Lagrangian: 2.554797e-05 Max Stop Criteria: 1.276733e-03
Iteration: 2  * Newton Step: 1 Norm Gradient Phi: 6.857702e+01  * Newton Step: 2 Norm Gradient Phi: 2.000148e+00  * Newton Step: 3 Norm Gradient Phi: 3.734989e-01  * Newton Step: 4 Norm Gradient Phi: 3.556324e-02  * Newton Step: 5 Norm Gradient Phi: 2.583244e-03  Newton Steps: 5  Objective Value: -6.517194e+02  Equality Constraints Infeasibility: 2.334661e-04  Inequality Constraints Infeasibility: 1.581451e-03  Complementarity: 1.062306e-03	Iteration: 8  * Newton Step: 1 Norm Gradient Phi: 1.957067e-06 Newton Steps: 1 Objective Value: -6.519244e+02 Equality Constraints Infeasibility: 2.124574e-08 Inequality Constraints Infeasibility: 1.707053e-06 Complementarity: 1.325332e-06 Norm of Gradient of Lagrangian: 1.957067e-06 Max Stop Criteria: 3.290717e-04
Norm of Gradient of Lagrangian: 2.583244e-03  Max Stop Criteria: 5.284254e-01	Iteration: 9 * Newton Step: 1 Norm Gradient Phi: 7.183747e-07 Newton Steps: 1 Objective Value: -6.519244e+02 Equality Constraints Infeasibility: 1.153805e-08 Inequality Constraints Infeasibility: 9.893613e-07 Complementarity: 7.659304e-07 Norm of Gradient of Lagrangian: 7.183747e-07 Max Stop Criteria: 1.908430e-04
Objective Value: -6.518977e+02  Equality Constraints Infeasibility: 3.418451e-05 Inequality Constraints Infeasibility: 8.995204e-05 Complementarity: 1.270415e-04 Norm of Gradient of Lagrangian: 6.881584e-04 Max Stop Criteria: 8.334295e-02	Iteration: 10  * Newton Step: 1 Norm Gradient Phi: 2.730915e-07 Newton Steps: 1 Objective Value: -6.519244e+02 Equality Constraints Infeasibility: 6.734104e-09 Inequality Constraints Infeasibility: 5.929204e-07 Complementarity: 4.575402e-07 Norm of Gradient of Lagrangian: 2.730915e-07 Max Stop Criteria: 1.142069e-04
* Newton Step: 3 Norm Gradient Phi: 2.029240e-06 Newton Steps: 3 Objective Value: -6.519206e+02 Equality Constraints Infeasibility: 4.558850e-06 Inequality Constraints Infeasibility: 2.712002e-05 Complementarity: 2.722803e-05 Norm of Gradient of Lagrangian: 2.029240e-06 Max Stop Criteria: 1.374056e-02	Tteration: 11  * Newton Step: 1 Norm Gradient Phi: 1.045520e-07 Newton Steps: 1 Objective Value: -6.519244e+02 Equality Constraints Infeasibility: 4.068361e-09 Inequality Constraints Infeasibility: 3.611900e-07 Complementarity: 2.773786e-07 Norm of Gradient of Lagrangian: 1.045520e-07
Iteration: 5 * Newton Step: 1 Norm Gradient Phi: 2.679267e-04 * Newton Step: 2 Norm Gradient Phi: 2.079151e-06 Newton Steps: 2 Objective Value: -6.519237e+02 Equality Constraints Infeasibility: 7.075670e-07 Inequality Constraints Infeasibility: 1.282519e-05 Complementarity: 1.017659e-05 Norm of Gradient of Lagrangian: 2.079151e-06 Max Stop Criteria: 3.373550e-03	Max Stop Criteria: 6.951168e-05

### 2.6 Radial Kernel Digit 5

2.6 Radiai Kernei Digit 5	
Iteration: 1  * Newton Step: 1 Norm Gradient Phi: 3.177861e+04  * Newton Step: 2 Norm Gradient Phi: 9.974503e+03  * Newton Step: 3 Norm Gradient Phi: 2.872137e+03  * Newton Step: 4 Norm Gradient Phi: 3.968737e+02  * Newton Step: 5 Norm Gradient Phi: 4.469698e+00  * Newton Step: 6 Norm Gradient Phi: 1.886190e+00  * Newton Step: 7 Norm Gradient Phi: 7.291223e-01  * Newton Step: 8 Norm Gradient Phi: 2.454204e-01  Newton Steps: 8  Objective Value: -3.914340e+02	Iteration: 5 * Newton Step: 1 Norm Gradient Phi: 4.059047e-04 * Newton Step: 2 Norm Gradient Phi: 6.810572e-06 Newton Steps: 2 Objective Value: -3.938422e+02 Equality Constraints Infeasibility: 3.699642e-07 Inequality Constraints Infeasibility: 2.562605e-05 Complementarity: 4.872429e-06 Norm of Gradient of Lagrangian: 6.810572e-06 Max Stop Criteria: 2.020850e-03
Equality Constraints Infeasibility: 1.200865e-02 Inequality Constraints Infeasibility: 4.498182e-03 Complementarity: 9.999000e-03 Norm of Gradient of Lagrangian: 2.454204e-01 Max Stop Criteria: 3.937285e+01	Iteration: 6 * Newton Step: 1 Norm Gradient Phi: 3.196839e-05 Newton Steps: 1 Objective Value: -3.938425e+02 Equality Constraints Infeasibility: 1.529236e-08 Inequality Constraints Infeasibility: 7.933976e-06 Complementarity: 1.972671e-06
* Newton Step: 1 Norm Gradient Phi: 8.820601e+01  * Newton Step: 2 Norm Gradient Phi: 2.356458e+00  * Newton Step: 3 Norm Gradient Phi: 5.390633e-01  * Newton Step: 4 Norm Gradient Phi: 6.434345e-02  * Newton Step: 5 Norm Gradient Phi: 1.069343e-02	Norm of Gradient of Lagrangian: 3.196839e-05 Max Stop Criteria: 5.824617e-04
Newton Steps: 5 Objective Value: -3.935885e+02 Equality Constraints Infeasibility: 2.945021e-04 Inequality Constraints Infeasibility: 2.206061e-04 Complementarity: 1.258278e-03 Norm of Gradient of Lagrangian: 1.069343e-02 Max Stop Criteria: 6.298825e-01	Newton Steps: 1 Objective Value: -3.938425e+02 Equality Constraints Infeasibility: 1.728958e-08 Inequality Constraints Infeasibility: 2.710300e-06 Complementarity: 1.122546e-06 Norm of Gradient of Lagrangian: 2.713099e-06 Max Stop Criteria: 2.422907e-04
Iteration: 3 * Newton Step: 1 Norm Gradient Phi: 1.312494e+00 * Newton Step: 2 Norm Gradient Phi: 1.119279e-01 * Newton Step: 3 Norm Gradient Phi: 2.243456e-02 * Newton Step: 4 Norm Gradient Phi: 1.565652e-03 * Newton Step: 5 Norm Gradient Phi: 1.353173e-05 Newton Steps: 5 Objective Value: -3.938212e+02 Equality Constraints Infeasibility: 2.991688e-05 Inequality Constraints Infeasibility: 1.042958e-04	Iteration: 8 * Newton Step: 1 Norm Gradient Phi: 9.628024e-07 Newton Steps: 1 Objective Value: -3.938425e+02 Equality Constraints Infeasibility: 1.576384e-08 Inequality Constraints Infeasibility: 2.115381e-06 Complementarity: 7.008054e-07 Norm of Gradient of Lagrangian: 9.628024e-07 Max Stop Criteria: 1.433209e-04
Complementarity: 1.083993e-04  Norm of Gradient of Lagrangian: 1.353173e-05  Max Stop Criteria: 7.339688e-02	Iteration: 9 * Newton Step: 1 Norm Gradient Phi: 3.739023e-07 Newton Steps: 1 Objective Value: -3.938425e+02
Iteration: 4  * Newton Step: 1 Norm Gradient Phi: 9.900454e-03  * Newton Step: 2 Norm Gradient Phi: 1.627480e-03  * Newton Step: 3 Norm Gradient Phi: 9.738931e-05  Newton Steps: 3  Objective Value: -3.938403e+02  Equality Constraints Infeasibility: 3.323246e-06  Inequality Constraints Infeasibility: 7.780799e-05  Complementarity: 1.962797e-05  Norm of Gradient of Lagrangian: 9.738931e-05  Max Stop Criteria: 1.034544e-02	Equality Constraints Infeasibility: 1.106462e-08 Inequality Constraints Infeasibility: 1.425552e-06 Complementarity: 4.698021e-07 Norm of Gradient of Lagrangian: 3.739023e-07 Max Stop Criteria: 9.228617e-05

### 2.7 Radial Kernel Digit 6

2.7 Radial Kernel Digit 6	
Iteration: 1  * Newton Step: 1 Norm Gradient Phi: 3.250235e+04  * Newton Step: 2 Norm Gradient Phi: 1.195457e+04  * Newton Step: 3 Norm Gradient Phi: 5.298462e+03  * Newton Step: 4 Norm Gradient Phi: 3.151725e+03  * Newton Step: 5 Norm Gradient Phi: 2.817518e+02  * Newton Step: 6 Norm Gradient Phi: 3.813862e+00  * Newton Step: 7 Norm Gradient Phi: 1.474092e+00  * Newton Step: 8 Norm Gradient Phi: 5.498910e-01  * Newton Step: 9 Norm Gradient Phi: 1.766787e-01  Newton Steps: 9	Iteration: 5 * Newton Step: 1 Norm Gradient Phi: 5.312925e-04 * Newton Step: 2 Norm Gradient Phi: 9.711987e-06 Newton Steps: 2 Objective Value: -3.655729e+02 Equality Constraints Infeasibility: 4.082783e-06 Inequality Constraints Infeasibility: 1.744522e-05 Complementarity: 2.023606e-05 Norm of Gradient of Lagrangian: 9.711987e-06 Max Stop Criteria: 9.729003e-03
Objective Value: -3.663020e+02 Equality Constraints Infeasibility: 1.280051e-02 Inequality Constraints Infeasibility: 8.290002e-03 Complementarity: 9.999000e-03 Norm of Gradient of Lagrangian: 1.766787e-01 Max Stop Criteria: 4.330545e+01	Iteration: 6 * Newton Step: 1 Norm Gradient Phi: 6.098738e-05 Newton Steps: 1 Objective Value: -3.655740e+02 Equality Constraints Infeasibility: 1.323126e-06 Inequality Constraints Infeasibility: 1.745828e-05 Complementarity: 9.797352e-06 Norm of Gradient of Lagrangian: 6.098738e-05 Max Stop Criteria: 3.445685e-03
* Newton Step: 2 Norm Gradient Phi: 2.333306e+00  * Newton Step: 3 Norm Gradient Phi: 3.921453e-01  * Newton Step: 4 Norm Gradient Phi: 4.265869e-02  * Newton Step: 5 Norm Gradient Phi: 2.301060e-03  Newton Steps: 5  Objective Value: -3.653497e+02  Equality Constraints Infeasibility: 5.318937e-04  Inequality Constraints Infeasibility: 3.518503e-06  Complementarity: 1.378997e-03  Norm of Gradient of Lagrangian: 2.301060e-03  Max Stop Criteria: 1.136557e+00	Iteration: 7 * Newton Step: 1 Norm Gradient Phi: 1.096106e-05 Newton Steps: 1 Objective Value: -3.655742e+02 Equality Constraints Infeasibility: 5.157215e-07 Inequality Constraints Infeasibility: 8.806262e-06 Complementarity: 5.558462e-06 Norm of Gradient of Lagrangian: 1.096106e-05 Max Stop Criteria: 1.504169e-03
**Newton Step: 1 Norm Gradient Phi: 3.661755e-01  * Newton Step: 2 Norm Gradient Phi: 6.183224e-02  * Newton Step: 3 Norm Gradient Phi: 1.148524e-02  * Newton Step: 4 Norm Gradient Phi: 8.541579e-04  Newton Steps: 4  Objective Value: -3.655355e+02  Equality Constraints Infeasibility: 8.782728e-05  Inequality Constraints Infeasibility: 9.474220e-05  Complementarity: 2.180017e-04  Norm of Gradient of Lagrangian: 8.541579e-04  Max Step Criteria: 1.842478e-01	Iteration: 8  * Newton Step: 1 Norm Gradient Phi: 4.128358e-06 Newton Steps: 1 Objective Value: -3.655743e+02 Equality Constraints Infeasibility: 2.458999e-07 Inequality Constraints Infeasibility: 5.153806e-06 Complementarity: 3.470900e-06 Norm of Gradient of Lagrangian: 4.128358e-06 Max Stop Criteria: 8.078809e-04
Iteration: 4  * Newton Step: 1 Norm Gradient Phi: 5.790418e-03  * Newton Step: 2 Norm Gradient Phi: 3.629340e-04  * Newton Step: 3 Norm Gradient Phi: 5.745380e-06  Newton Steps: 3  Objective Value: -3.655676e+02  Equality Constraints Infeasibility: 1.655450e-05  Inequality Constraints Infeasibility: 4.863241e-05  Complementarity: 5.610863e-05  Norm of Gradient of Lagrangian: 5.745380e-06  Max Stop Criteria: 3.663367e-02	Objective Value: -3.655744e+02 Equality Constraints Infeasibility: 1.338055e-07 Inequality Constraints Infeasibility: 2.966042e-06 Complementarity: 2.331087e-06 Norm of Gradient of Lagrangian: 1.680598e-06 Max Stop Criteria: 4.955162e-04

Iteration: 11 \* Newton Step: 1 Norm Gradient Phi: 3.756609e-07Newton Steps: 1 Objective Value: -3.655744e+02 Equality Constraints Infeasibility: 5.444058e-08 Inequality Constraints Infeasibility: 1.158868e-06 Complementarity: 1.225644e-06 Norm of Gradient of Lagrangian: 3.756609e-07 Max Stop Criteria: 2.417176e-04 \* Newton Step: 1 Norm Gradient Phi: 1.946534e-07 Newton Steps: 1 Objective Value: -3.655744e+02 Equality Constraints Infeasibility: 3.897795e-08 Inequality Constraints Infeasibility: 7.951791e-07 Complementarity: 9.393080e-07 Norm of Gradient of Lagrangian: 1.946534e-07 Max Stop Criteria: 1.829736e-04 Iteration: 13 \* Newton Step: 1 Norm Gradient Phi: 1.054299e-07 Newton Steps: 1 Objective Value: -3.655744e+02 Equality Constraints Infeasibility: 2.939826e-08 Inequality Constraints Infeasibility: 5.775864e-07 Complementarity: 7.398535e-07 Norm of Gradient of Lagrangian: 1.054299e-07 Max Stop Criteria: 1.433401e-04 Iteration: 14 \* Newton Step: 1 Norm Gradient Phi: 5.896601e-08 Newton Steps: 1 Objective Value: -3.655744e+02 Equality Constraints Infeasibility: 2.304192e-08 Inequality Constraints Infeasibility: 4.399576e-07 Complementarity: 5.959974e-07 Norm of Gradient of Lagrangian: 5.896601e-08 Max Stop Criteria: 1.152576e-04 Iteration: 15 \* Newton Step: 1 Norm Gradient Phi: 3.387059e-08 Newton Steps: 1 Objective Value: -3.655744e+02 Equality Constraints Infeasibility: 1.859029e-08 Inequality Constraints Infeasibility: 3.480063e-07 Complementarity: 4.891837e-07 Norm of Gradient of Lagrangian: 3.387059e-08 Max Stop Criteria: 9.460906e-05

2.9 Radial Kernel Digit 8	
2.9 Radial Kernel Digit 8  Iteration: 1  * Newton Step: 1 Norm Gradient Phi: 5.209830e+06  * Newton Step: 2 Norm Gradient Phi: 1.304886e+04  * Newton Step: 3 Norm Gradient Phi: 5.906741e+03  * Newton Step: 5 Norm Gradient Phi: 2.152047e+02  * Newton Step: 6 Norm Gradient Phi: 1.252047e+02  * Newton Step: 7 Norm Gradient Phi: 1.308916e+02  * Newton Step: 8 Norm Gradient Phi: 1.404523e+00  * Newton Step: 8 Norm Gradient Phi: 1.404523e+00  * Newton Step: 9 Norm Gradient Phi: 1.989465e-01  * Newton Step: 9 Norm Gradient Phi: 1.989465e-01  Newton Steps: 9  * Objective Value: -7.22127e+02  Equality Constraints Infeasibility: 1.031602e-02  Inequality Constraints Infeasibility: 6.160873e-03  Complementarity: 9.999000e-03  Norm of Gradient of Lagrangian: 1.989465e-01  Max Stop Criteria: 3.257213e+01	Iteration: 6 * Newton Steps: 1 Norm Gradient Phi: 4.028132e-05 Newton Steps: 1 Dbjective Value: -7.231882e+02 Equality Constraints Infeasibility: 1.035744e-09 Inequality Constraints Infeasibility: 3.550212e-05 Complementarity: 3.916026e-06 Norm of Gradient of Lagrangian: 4.028132e-05 Max Stop Criteria: 8.581893e-04
Equality Constraints Infeasibility: 4.413471e-06 Inequality Constraints Infeasibility: 2.038065e-04	Newton Steps: 1 Objective Value: -7.231883e+02 Equality Constraints Infeasibility: 6.743528e-09 Inequality Constraints Infeasibility: 1.459445e-06 Complementarity: 3.581086e-07 Norm of Gradient of Lagrangian: 2.198802e-07
Iteration: 5  * Newton Step: 1 Norm Gradient Phi: 2.542586e-04  * Newton Step: 2 Norm Gradient Phi: 2.811193e-06  Newton Steps: 2  Objective Value: -7.231880e+02  Equality Constraints Infeasibility: 4.471567e-07  Inequality Constraints Infeasibility: 9.088977e-05  Complementarity: 8.348665e-06  Norm of Gradient of Lagrangian: 2.811193e-06  Max Stop Criteria: 2.098549e-03	Max Stop Criteria: 6.883592e-05

### 2.10 Radial Kernel Digit 9

```
Iteration: 1
                                                      Iteration: 4
* Newton Step: 1 Norm Gradient Phi: 5.006381e+04
                                                      * Newton Step: 1 Norm Gradient Phi: 6.024430e-04
* Newton Step: 2 Norm Gradient Phi: 1.876691e+04
                                                      * Newton Step: 2 Norm Gradient Phi: 2.009011e-05
* Newton Step: 3 Norm Gradient Phi: 1.088150e+04
                                                      Newton Steps: 2
* Newton Step: 4 Norm Gradient Phi: 3.274279e+03
                                                      Objective Value: -9.214343e+02
                                                      Equality Constraints Infeasibility: 3.994033e-06
* Newton Step: 5 Norm Gradient Phi: 4.473892e+02
* Newton Step: 6 Norm Gradient Phi: 5.360784e+02
                                                      Inequality Constraints Infeasibility: 4.854216e-06
* Newton Step: 7 Norm Gradient Phi: 2.058079e+00
                                                      Complementarity: 1.047910e-05
* Newton Step: 8 Norm Gradient Phi: 8.749511e-01
                                                      Norm of Gradient of Lagrangian: 2.009011e-05
* Newton Step: 9 Norm Gradient Phi: 4.095136e-01
                                                      Max Stop Criteria: 9.478215e-03
* Newton Step: 10 Norm Gradient Phi: 1.731676e-01
Newton Steps: 10
                                                      Iteration: 5
Objective Value: -9.237480e+02
                                                      * Newton Step: 1 Norm Gradient Phi: 7.022253e-05
Equality Constraints Infeasibility: 2.464143e-02
                                                      Newton Steps: 1
Inequality Constraints Infeasibility: 9.554396e-03
                                                      Objective Value: -9.214353e+02
Complementarity: 9.999000e-03
                                                      Equality Constraints Infeasibility: 5.072431e-07
                                                      Inequality Constraints Infeasibility: 1.298983e-06
Norm of Gradient of Lagrangian: 1.731676e-01
Max Stop Criteria: 7.051693e+01
                                                      Complementarity: 3.041750e-06
                                                      Norm of Gradient of Lagrangian: 7.022253e-05
                                                      Max Stop Criteria: 1.271033e-03
* Newton Step: 1 Norm Gradient Phi: 6.487336e+01
* Newton Step: 2 Norm Gradient Phi: 2.576436e+00
* Newton Step: 3 Norm Gradient Phi: 3.227255e-01
                                                       * Newton Step: 1 Norm Gradient Phi: 6.526771e-06
* Newton Step: 4 Norm Gradient Phi: 2.311970e-02
* Newton Step: 5 Norm Gradient Phi: 7.301489e-04
                                                      Objective Value: -9.214355e+02
Newton Steps: 5
                                                      Equality Constraints Infeasibility: 6.735584e-08
Objective \overline{\text{Value:}} -9.213781e+02
                                                      Inequality Constraints Infeasibility: 2.997654e-07
Equality Constraints Infeasibility: 1.292835e-04
                                                       Complementarity: 1.545691e-06
Inequality Constraints Infeasibility: 1.693638e-03
                                                      Norm of Gradient of Lagrangian: 6.526771e-06
Complementarity: 7.561376e-04
                                                      Max Stop Criteria: 2.451241e-04
Norm of Gradient of Lagrangian: 7.301489e-04
Max Stop Criteria: 4.626902e-01
                                                      Iteration: 7
                                                       * Newton Step: 1 Norm Gradient Phi: 3.388013e-06
                                                      Newton Steps: 1
Iteration: 3
* Newton Step: 1 Norm Gradient Phi: 1.213999e-01
                                                      Objective Value: -9.214355e+02
* Newton Step: 2 Norm Gradient Phi: 3.090568e-02
                                                      Equality Constraints Infeasibility: 1.160526e-08
* Newton Step: 3 Norm Gradient Phi: 5.256942e-03
                                                      Inequality Constraints Infeasibility: 2.123180e-07
* Newton Step: 4 Norm Gradient Phi: 3.003113e-04
                                                      Complementarity: 6.557002e-07
Newton Steps: 4
                                                      Norm of Gradient of Lagrangian: 3.388013e-06
Objective Value: -9.214256e+02
                                                      Max Stop Criteria: 1.244068e-04
Equality Constraints Infeasibility: 3.131447e-05
Inequality Constraints Infeasibility: 2.458840e-05
                                                      Iteration: 8
Complementarity: 6.416766e-05
                                                      * Newton Step: 1 Norm Gradient Phi: 6.559602e-07
Norm of Gradient of Lagrangian: 3.003113e-04
                                                      Newton Steps: 1
                                                      Objective Value: -9.214355e+02
Max Stop Criteria: 7.329791e-02
                                                      Equality Constraints Infeasibility: 2.799243e-09
                                                      Inequality Constraints Infeasibility: 1.316630e-07
                                                      Complementarity: 2.944887e-07
                                                      Norm of Gradient of Lagrangian: 6.559602e-07
                                                      Max Stop Criteria: 5.512888e-05
```

#### 2.11 Radial Kernel Alphas Digit 9

Optimal alpha values for one of the ten cases in the full problem (digit 9) with C=2 are provided below. Results for C=2 were chosen because they can be compared with the AMPL results in the midterm report (which also included optimal alpha values for digit 9, C=2). The results match to within the 1e-4 prevision used by the NRAL code.

1	-1.4537e-08	101	1.0438e-08	201	9.2658e-09	301	2 0110- 08	401	2.7270e-09
2	1.9897e-08	102	-4.0290e-09	201	2.0524e-08	302	3.2110e-08 1.4024e-09	402	1.1490e+00
3	1.2926e-08	103	3.6985e-08	203	1.7176e-08	303	4.5505e-08	403	2.0000e+00
4	1.0958e-01	104	-4.7998e-07	204	3.4917e-08	304	1.0913e-08	404	4.7079e-01
5	-1.3697e-08	105	-6.6537e-09	205	1.5871e-08	305	9.0716e-09	405	4.7079e-01
6	2.5008e-01	106	-8.5294e-07	206	-4.9151e-09	306	-4.1537e-07	406	2.0000e+00
7	1.6348e-08	107	-6.8158e-09	207	1.2809e-07	307	3.8604e-08	407	2.0000e+00
8	1.4777e-09	108	-8.6290e-09	208	7.0755e-09	308	-7.3719e-09	408	4.6392e-07
9	-1.0397e-08	109	-6.0811e-09	209	2.5731e-08	309	1.1851e-08	409	2.9402e-01
10	-5.0000e-08	110	-6.6537e-09	210	1.0593e-08	310	1.4308e-08	410	1.7725e+00
11	-8.2480e-08	111	-1.3676e-08	211	6.4152e-08	311	2.4242e-08	411	2.0000e+00
12	9.1618e-09	112	-1.4777e-07	212	1.4721e-08	312	-3.4228e-08	412	-1.1616e-07
13	1.4533e-08	113	-1.2641e-07	213	7.7678e-08	313	5.8346e-01	413	2.6726e-09
14	6.1841e-09	114	-1.2641e-07	214	2.8009e-08	314	-5.5440e-09	414	2.0000e+00
15	4.7366e-08	115	-5.0443e-08	215	2.7270e-08	315	2.9188e-01	415	1.3485e+00
16	6.8323e-01	116	2.3669e-08	216	2.5698e-08	316	6.9442e-09	416	2.0000e+00
17	-2.5362e-08	117	-1.1066e-07	217	8.4243e-08	317	1.5572e+00	417	2.0000e+00
18	9.9011e-08	118	-1.7403e-08	218	-1.1871e-09	318	6.0714e-09	418	2.0000e+00
19	-3.4207e-08	119	-1.7403e-08	219	3.3551e-09	319	-7.2794e-09	419	2.0000e+00
20	2.3519e-08	120	-1.1505e-09	220	2.0360e-08	320	-7.3004e-09	420	8.3866e-01
21	5.0526e-08	121	-1.3676e-08	221	1.2888e-09	321	8.3031e-09	421	2.0000e+00
22	-1.1937e-08	122	-1.3676e-08	222	3.1066e-08	322	1.7658e-08	422	1.4466e-08
23	1.7064e-08	123	-1.1505e-09	223	3.2706e-08	323	1.2487e-08	423	3.2751e-08
24	4.5492e-09	124	-6.6537e-09	224	2.4315e-08	324	3.0624e-01	424	-1.4101e-08
25	3.8127e-01	125	-3.7797e-08	225	1.7061e-08	325	-1.2221e-08	425	8.0350e-01
26	1.0280e+00	126	-1.7308e-08	226	-1.8188e-11	326	1.2479e-06	426	2.0000e+00
27	-1.0365e-08	127	-1.7458e-07	227	9.3004e-09	327	8.2227e-09	427	7.2236e-01
28	2.5000e-08	128	-1.3489e-07	228	1.0647e-08	328	-3.4263e-09	428	1.4075e-09
29	2.9072e-08	129	2.2510e-08	229	2.9104e-09	329	7.1002e-09	429	4.9850e-09
30	2.9072e-08	130	-2.6066e-09	230	2.5591e-08	330	1.4958e-01	430	-1.4303e-07
31	-1.5435e-08	131	3.3118e-07	231	1.2415e-08	331	-9.9232e-08	431	-6.7821e-07
32	2.0460e-08	132	-1.5933e-08	232	1.3324e-08	332	1.8794e-06	432	1.1097e-07
33	4.4651e-08	133	-6.6537e-09	233	2.8310e-08	333	-1.7880e-09	433	2.5341e-08
34	2.1262e-11	134	-8.2719e-08	234	1.0700e-10	334	4.3017e-01	434	-9.0735e-09
35	1.0769e-08	135	-7.3560e-09	235	-2.6931e-08	335	-5.1801e-09	435	1.6608e-08
36	1.5094e-08	136	-1.8148e-09	236	2.8099e-08	336	5.9742e-09	436	7.2247e-09
37	8.0243e-09	137	1.8392e+00	237	-1.1849e-07	337	-6.0326e-09	437	1.4536e-08
38	1.4693e-08	138	-3.6997e-08	238	5.2822e-09	338	1.5392e+00	438	2.9475e-07
39	-1.8816e-08	139	-4.4575e-08	239	1.8679e-08	339	1.6407e-08	439	5.0409e-01
40	-1.6452e-08	140	-1.5614e-08	240	3.3678e-08	340	7.3612e-09	440	-1.4523e-08
41	-3.0812e-08	141	9.4619e-01	241	2.4066e-08	341	2.0000e+00	441	2.7909e-08
42	-4.1648e-08	142	-3.0208e-09	242	6.7097e-09	342	4.0293e-08	442	2.0000e+00
43	-1.1616e-08	143	-6.6537e-09	243	1.0692e-08	343	-6.1807e-10	443	5.3105e-08
44	-1.9012e-08	144	-2.6724e-08	244	2.1693e-08	344	3.2671e-09	444	2.0000e+00
45	-1.0823e-08	145	-5.6542e-08	245	4.3869e-02	345	4.9912e-09	445	2.0000e+00
46	-3.9909e-08	146	-5.6542e-08	246	-1.5865e-08	346	-2.3640e-08	446	2.0000e+00
47	-2.2879e-08	147	1.7705e-01	247	1.9067e-08	347	2.0000e+00	447	2.0000e+00
48	-1.0344e-08	148	9.7331e-09	248	3.0530e-08	348	-1.6783e-08	448	1.8435e+00
49	-1.4416e-08	149	5.1656e-01	249	8.5985e-09	349	1.5692e-08	449	-5.8675e-08
50		150		250		350		450	
	1.6888e-08	151	5.9630e-08	251	-2.7577e-08	351	-7.5273e-09	451	6.4350e-09
51	-3.8618e-09		1.4236e-07		-2.6963e-08		6.3897e-09		2.0774e-08
52	4.8273e-08	152	1.5734e-07	252	1.0124e-08	352	7.8601e-09	452	2.0000e+00
53	1.9124e+00	153	-1.7403e-08	253	9.0701e-09	353	-3.7991e-09	453	-3.8227e-08
54	-4.8402e-08	154	-2.8817e-08	254	2.2988e-08	354	3.1469e-08	454	2.6624e-08
55	-1.1302e-09	155	2.5730e-08	255	1.6583e-08	355	-1.7650e-08	455	3.0279e-08
56	-1.1661e-08	156	-2.1439e-08	256	3.0064e-09	356	-8.2904e-08	456	7.0255e-08
57	1.3145e-09	157	-1.1505e-09	257	-3.5012e-09	357	1.9907e-09	457	2.0000e+00
58	1.9954e-08	158	-1.1505e-09	258	8.5368e-09	358	-5.8304e-09	458	-1.8603e-08
59	-1.8770e-09	159	-9.0993e-08	259	1.5453e=08	359	-1.1567e-08	459	1.0890e-08
60	8.1970e-09	160	-8.8153e-08	260	-1.5177e-08	360	8.1643e-08	460	1.6457e+00
61	4.6336e-07	161	1.2839e+00	261	-3.7597e-09	361	1.0629e-01	461	2.0000e+00
62	-1.1028e-08	162	5.0578e-08	262	1.9472e-01	362	2.6973e-02	462	4.2341e-08
63	-1.7032e-08	163	2.0000e+00	263	-1.2559e-07	363	2.0000e+00	463	2.1624e-07
64	2.2741e-08	164	-2.1439e-08	264	1.7976e-08	364	1.6003e-08	464	3.8928e-09
65	2.3233e-08	165	3.4149e-08	265	8.9977e-09	365	1.0932e-07	465	4.2973e-09
66	1.2249e-09	166	3.6068e-09	266	-2.5699e-08	366	2.0000e+00	466	-6.6627e-09
67	1.7890e-08	167	-7.7678e-10	267	1.4513e-08	367	2.7364e-08	467	2.8477e-08
68	2.9277e-08	168	1.3272e-08	268	3.3434e=08	368	2.2819e-01	468	5.5718e-08
69	1.6212e-08	169	1.4835e+00	269	1.5349e-08	369	-2.1287e-09	469	2.9434e-08
70	-1.2587e-08	170	-2.7239e-08	270	2.0642e-08	370	3.8888e-09	470	6.3213e-08
70	-3.2567e-09	171	3.5861e-08	271	1.5378e-07	371	-7.4088e-09	471	-4.1329e-08
72	4.1232e-02	172	-2.8672e-08	272	1.8429e-08	372	-1.6927e-08	471	1.0077e-08
73	1.8409e-08	173	-6.6537e-09	273	1.0429e=00 6.1578e=09	373	1.3825e+00	473	-1.0077e=08
74	-7.0110e-09	174	-6.6537e-09	274	-3.9041e-08	374	1.7398e-07	474	-3.2552e-08
75	1.6337e=08	175	-0.0537e-09 -2.1439e-08	275	-9.1389e-08	375	3.7036e-09	474	2.3952e=00
75 76	1.4252e-08		-2.1439e-08 -1.7366e-08					476	
		176		276	2.0110e-09	376	8.3987e-09	476	7.9065e-09
77	-6.3864e-09	177	1.2923e-08	277	9.0739e-01	377	1.6497e-08		3.1596e-09
78	2.9822e-08	178	1.3700e-08	278	-3.2980e-09	378	2.0000e+00	478	3.2315e-01
79	1.0688e-08	179	-9.9879e-09	279	4.4978e-09	379	1.1370e-08	479	-6.9053e-09
80	-5.8399e-08	180	-2.0820e-08	280	1.9324e-01	380	1.5584e-01	480	-9.0668e-07
81	-4.9076e-08	181	-2.1439e-08	281	-1.3047e-09	381	-4.2430e-08	481	-9.5059e-09
82	-7.9131e-09	182	-1.3676e-08	282	2.6803e-08	382	7.6520e-09	482	-1.2359e-09
83	9.3370e-09	183	8.5468e-08	283	1.1540e+00	383	7.4573e-01	483	4.4584e-09
84	9.7819e-09	184	-1.3676e-08	284	8.9554e-09	384	4.8229e-09	484	-5.4035e-08
85	1.9221e-08	185	-6.6537e-09	285	-3.0884e-11	385	3.2705e-08	485	3.7950e-01
86	2.4396e-08	186	-4.7998e-07	286	-5.1291e-08	386	2.0000e+00	486	2.0684e-08
87	-1.5381e-08	187	8.9692e-09	287	1.3474e-08	387	1.7429e+00	487	-2.4548e-09
88	-1.0879e-08	188	3.4347e-09	288	-1.3547e-08	388	2.0000e+00	488	-1.8749e-08
89	-2.0736e-09	189	9.7305e-09	289	3.5100e-01	389	2.0000e+00	489	7.7232e-01
90	4.8506e-09	190	6.4259e-09	290	-1.5875e-08	390	2.0000e+00	490	-2.9347e-08
91	-4.5377e-11	191	3.1555e-08	291	-6.3616e-09	391	2.0000e+00	491	6.3213e-08
92	-3.0184e-08	192	3.1977e-09	292	7.8260e-09	392	1.7723e+00	492	-1.8749e-08
93		193	2.3108e-08	293	2.5456e-08	393	2.0000e+00	493	1.1690e-08
	-4.6582e=08	100		294	2.5732e-08	394	2.0000e+00 2.0000e+00	494	5.9392e-09
9.4	-4.6582e-08 -1.3676e-08	194				007			
94 95	-1.3676e-08	194	1.4357e-08 1.0752e-08			305	-1 5599e-08		
95	-1.3676e-08 -3.2413e-07	195	1.0752e-08	295	-6.0104e-09	395	-1.5599e-08	495	7.3842e-09
95 96	-1.3676e-08 -3.2413e-07 1.2663e-07	195 196	1.0752e-08 -5.5654e-08	295 296	-6.0104e-09 -1.1842e-08	396	-1.0644e-08	495 496	7.3842e-09 -1.6758e-08
95 96 97	-1.3676e-08 -3.2413e-07 1.2663e-07 2.0000e+00	195 196 197	1.0752e-08 -5.5654e-08 9.4224e-09	295 296 297	-6.0104e-09 -1.1842e-08 -2.9908e-09	396 397	-1.0644e-08 3.7226e-08	495 496 497	7.3842e-09 -1.6758e-08 4.9524e-08
95 96 97 98	-1.3676e-08 -3.2413e-07 1.2663e-07 2.0000e+00 2.0000e+00	195 196 197 198	1.0752e-08 -5.5654e-08 9.4224e-09 9.0359e-08	295 296 297 298	-6.0104e-09 -1.1842e-08 -2.9908e-09 2.1752e-08	396 397 398	-1.0644e-08 3.7226e-08 1.5854e-08	495 496 497 498	7.3842e-09 -1.6758e-08 4.9524e-08 -1.8378e-08
95 96 97 98 99	-1.3676e-08 -3.2413e-07 1.2663e-07 2.0000e+00 2.0000e+00 2.7254e-08	195 196 197 198 199	1.0752e-08 -5.5654e-08 9.4224e-09 9.0359e-08 4.1381e-08	295 296 297 298 299	-6.0104e-09 -1.1842e-08 -2.9908e-09 2.1752e-08 -3.4003e-08	396 397 398 399	-1.0644e-08 3.7226e-08 1.5854e-08 2.5854e-08	495 496 497 498 499	7.3842e-09 -1.6758e-08 4.9524e-08 -1.8378e-08 9.0953e-09
95 96 97 98	-1.3676e-08 -3.2413e-07 1.2663e-07 2.0000e+00 2.0000e+00	195 196 197 198	1.0752e-08 -5.5654e-08 9.4224e-09 9.0359e-08	295 296 297 298	-6.0104e-09 -1.1842e-08 -2.9908e-09 2.1752e-08	396 397 398	-1.0644e-08 3.7226e-08 1.5854e-08	495 496 497 498	7.3842e-09 -1.6758e-08 4.9524e-08 -1.8378e-08

501	7.5171e-09	601	-5.5818e-08	701	1.2646e-08	801	-6.7521e-09
502	-3.2976e-08	602	1.0172e-10	702	-1.8673e-08	802	1.0650e+00
503	8.5339e-09	603	3.3393e-09	703	-2.9196e-08	803	-5.0981e-08
504	-1.0650e-08	604	-8.4243e-09	704	8.2491e-01	804	-1.2359e-08
505	7.6605e-10	605	-1.2867e-08	705	-5.3853e-09	805	6.1969e-01
506	-1.2534e-08	606	1.3378e-08	706	-7.6631e-08	806	6.4553e-08
507	-1.2236e-08	607	-1.0201e-08	707	6.9367e-10	807	-1.5153e-09
508	-4.5254e-08	608	4.3234e-08	708	-9.8698e-09	808	4.3972e-09
509	1.9710e-01	609	4.4295e-08	709	2.6351e-08	809	2.8440e-08
510	3.1517e-08	610	8.4844e-09	710	1.5736e+00	810	-4.9460e-09
511	-1.8107e-10	611	1.5625e-09	711	2.3381e-01	811	9.2956e-09
512	-1.1722e-09	612	-3.1961e-09	712	2.0000e+00	812	1.2506e-08
513	-6.3267e-09	613	-1.7876e-09	713	1.0207e-08	813	7.8702e-01
514	-9.5597e-10	614	1.0005e-08	714	3.2755e-08	814	6.4179e-01
515 516	-6.7951e-08 -1.2107e-07	615 616	1.7284e-08 2.4716e-08	715 716	3.7742e-01 7.8935e-01	815 816	9.1706e-01 2.0000e+00
517	6.9154e-09	617	3.6602e-08	717	-1.2845e-08	817	1.0085e+00
518	-1.3869e-08	618	-2.6328e-09	718	5.0445e-08	818	-5.5896e-08
519	2.0900e-01	619	-2.0103e-09	719	1.3250e-08	819	-3.1722e-08
520	-5.9411e-08	620	-7.5523e-09	720	1.1811e-08	820	1.2533e-08
521	3.6947e-01	621	5.8939e-09	721	1.0270e-01	821	2.1218e-08
522	-1.7311e-08	622	3.0466e-09	722	-6.6860e-09	822	8.1671e-09
523	2.4670e-08	623	5.8216e-09	723	-1.1474e-07	823	-3.2444e-07
524	-1.5513e-08	624	3.1925e-09	724	-2.0823e-08	824	-1.1198e-07
525	4.1329e-08	625	-1.2332e-10	725	2.0000e+00	825	-1.7342e-08
526	1.6564e-08	626	1.4277e-08	726	1.2291e+00	826	-6.2397e-09
527	2.7081e-09	627	-5.6169e-09	727	6.1857e-08	827	1.9674e-05
528	7.4206e-01	628	3.3152e-08	728	-1.0827e-07	828	-7.4050e-08
529	1.4996e-08	629	3.2271e-08	729	3.0408e-08	829	2.8163e-09
530	8.6366e-02	630	-1.6587e-08	730	1.3929e+00	830	-5.9060e-09
531	-1.6207e-08	631	-8.8916e-08	731	-1.3484e-08	831	8.2799e-08
532	-1.5090e-08	632	3.6765e-09 -2.1608e-09	732	-1.8970e-10	832	-1.2064e-08
533 534	1.7329e-08 1.2889e+00	633 634	-2.1608e-09 -4.8805e-08	733 734	-1.3697e-08 3.4283e-09	833 834	7.2117e-08 -2.9830e-09
535	-1.0373e-08	635	7.6773e-09	734	9.4475e-01	835	1.3595e=09
536	-8.1385e-09	636	4.9756e-09	736	4.2407e-09	836	2.0000e+00
537	9.6399e-02	637	1.4949e-08	737	1.5409e=08	837	-1.3105e-07
538	4.0435e-01	638	4.7394e-08	738	4.8003e-09	838	2.0000e+00
539	1.3237e+00	639	1.2483e-08	739	2.8921e-08	839	2.0000e+00
540	1.2720e-08	640	6.0184e-08	740	4.7729e-08	840	2.0000e+00
541	-2.6507e-08	641	1.9185e-08	741	-9.2828e-10	841	2.0000e+00
542	8.9458e-02	642	7.2629e-09	742	-5.2358e-09	842	2.0000e+00
543	5.9747e-09	643	-2.8040e-09	743	4.3677e-08	843	2.0000e+00
544	2.2002e-10	644	1.2768e-08	744	-2.4666e-07	844	2.0000e+00
545	-4.2650e-09	645	1.4127e-08	745	-1.0823e-07	845	2.0000e+00
546	-2.3918e-06	646	1.2638e-08	746	2.2401e-08	846	2.0000e+00
547	-1.7326e-08	647	-3.4386e-09	747	6.5883e-08	847	2.0000e+00
548	2.7367e-08	648	-2.3193e-09	748	2.1398e-08	848	2.0000e+00
549	3.3263e-08	649	7.6918e-09	749	1.2000e-08	849	2.0000e+00
550	-6.3200e-09	650	-1.1027e-08	750	3.5843e-08	850	2.0000e+00
551	-1.5245e-08	651	-2.4790e-11	751	-2.0405e-08	851	2.0000e+00
552	2.0000e+00	652	6.5299e-08	752	2.4468e-09	852	2.0000e+00
553	1.4040e-06	653	8.9931e-09	753	1.8808e+00	853	2.0000e+00
554 555	1.4390e-08	654	5.9411e-01	754	-1.0680e-08	854	2.0000e+00
556	-1.6238e-08 1.0118e+00	655 656	-3.5177e-08 8.8234e-11	755 756	-1.1367e-08 4.6448e-09	855 856	2.0000e+00 1.8501e+00
557	8.8705e-09	657	-3.7521e-08	757	-1.3718e-09	857	7.4988e-08
558	-3.5617e-08	658	-1.1206e-08	758	5.1337e-09	858	2.0000e+00
559	1.5491e-08	659	-2.8024e-08	759	-9.0241e-09	859	2.0000e+00
560	1.8795e-09	660	-5.1798e-08	760	1.4667e-07	860	2.0000e+00
561	5.3583e-09	661	-2.6968e-08	761	6.6520e-08	861	2.0000e+00
562	-1.6169e-08	662	9.3018e-01	762	2.7618e-08	862	2.0000e+00
563	-3.4239e-10	663	4.0574e-09	763	2.0000e+00	863	2.0000e+00
564	4.3911e-01	664	1.8340e+00	764	1.1823e-08	864	2.0000e+00
565	8.3256e-09	665	7.1697e-01	765	-1.3428e-08	865	2.0000e+00
566	8.3570e-09	666	1.5769e+00	766	-1.1132e-08	866	2.0000e+00
567	-2.4120e-08	667	2.0000e+00	767	2.2147e-08	867	2.0000e+00
568	2.1121e-10	668	7.6981e-08	768	2.0000e+00	868	2.0000e+00
569	1.6798e-08	669	-7.4072e-08	769	1.1688e-09	869	1.1883e+00
570 571	5.4366e-09 1.5811e-08	670 671	2.1119e-08 1.5994e+00	770 771	6.5129e-02 -1.0680e-08	870 871	-3.9755e-08 2.0000e+00
572	5.9137e-09	672	-5.3362e-08	771	-1.0680e-08	871	2.0000e+00 2.0000e+00
573	3.1098e-08	673	-1.5712e-08	773	4.2453e-09	873	2.0000e+00 2.0000e+00
574	8.8379e-05	674	-2.3235e-08	774	1.4487e-08	874	2.0000e+00
575	2.0000e+00	675	-1.4972e-08	775	8.8493e-01	875	4.8307e-08
576	2.5293e-07	676	6.1648e-09	776	2.0000e+00	876	2.0000e+00
577	6.0512e-09	677	3.1381e-09	777	1.3936e-08	877	1.8328e+00
578	-2.1449e-08	678	8.4286e-09	778	-2.4671e-08	878	-3.7027e-08
579	-1.1439e-09	679	4.9126e-07	779	2.0000e+00	879	2.0000e+00
580	-1.0516e-08	680	-3.1371e-08	780	-2.0573e-09	880	2.0000e+00
581	8.0448e-08	681	4.2041e-06	781	-9.8951e-09	881	2.0000e+00
582	-3.5702e-09	682	2.7463e-08	782	4.5057e-08	882	2.0000e+00
583	-1.2295e-09	683	4.7693e-09	783	5.6287e-08	883	9.7797e-01
584 585	-9.1182e-09	684	-1.5554e-08	784 785	1.8473e-07	884	1.4113e+00
585 586	5.3565e-09 1.9577e-08	685 686	1.6468e+00 8.3906e-01	785 786	1.6499e+00 -2.4946e-08	885 886	2.0000e+00 2.0000e+00
587	1.4647e-08	687	-2.3799e-07	786 787	1.7741e-08	887	2.0000e+00 2.0000e+00
588	2.4149e-08	688	-2.0930e-08	788	-3.6156e-09	888	2.0000e+00 2.0000e+00
589	3.6603e-08	689	8.9189e-09	789	6.4721e-09	889	2.0000e+00
590	3.1528e-08	690	2.0000e+00	790	9.5633e-01	890	2.0000e+00
591	7.2390e-09	691	3.7373e-09	791	1.0649e-07	891	2.0000e+00
592	-1.4648e-11	692	-2.6834e-08	792	-1.0860e-09	892	2.0000e+00
593	1.9767e-08	693	-2.7665e-08	793	-2.5642e-09	893	2.0000e+00
594	1.0835e-08	694	-2.4705e-08	794	-1.1849e-07	894	2.0000e+00
595	4.8011e-09	695	-2.4936e-08	795	-1.9213e-08	895	2.0000e+00
596	-3.4235e-10	696	-3.7477e-09	796	-6.7617e-08	896	1.4001e+00
597	2.7939e-09	697	1.5122e+00	797	5.0133e-08	897	2.0000e+00
598	1.0781e-08	698	2.9929e-01	798	2.7862e-01	898	2.0000e+00
599	4.9568e-09	699	-3.1799e-08	799	4.2428e-08	899	2.0000e+00
600	2.4951e-08	700	3.5963e-01	800	-2.5193e-08	900	2.0000e+00

2.0000e+00 1.6426e+00 2.0000e+00 2.0000e+00