

Final Exam

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1 Implementation

The support vector machine constrained optimization problem was modeled and solved using AMPL (www.ampl.com/). Computations were performed using the LOQO solver (www.princeton.edu/~rvdb/loqo/LOQO.html) on the NEOS server (www.neos-server.org/neos/solvers/). Once the solution to the dual problem was obtained, the α values were imported into Java.

Java (version 1.6.0_27) was used to make the final classification. The code is available as a Subversion repository on Google Code at <http://code.google.com/p/csi873/>. Compiling and running the code requires the Java build tool Maven (<http://maven.apache.org/>).

2 Model

The following AMPL model was used to solve the dual SVM problem in Equation 1 with a polynomial kernel.

$$\begin{aligned} \max_{\alpha} \quad & \sum_{i=1}^l \alpha_i - 0.5 \sum_{i,j} \alpha_i \alpha_j y_i y_j K(x_i, x_j) \\ & s.t. \\ & \sum_{i=1}^l \alpha_i y_i = 0 \\ & 0 \geq \alpha_i \geq C, i = 1, 2, \dots, l \end{aligned} \tag{1}$$

```
model;
```

```
# number of training examples  
param l;
```

```
# number of input parameters (pixels in digit image)
```

```

param n;

# weight on xi penalty coefficient in primal problem
param C;

# parameters for polynomial machine kernel
param alpha;
param beta;
param delta;

# output vector (1 or -1)
param y { 1..1 };

# input data
param x { 1..1, 1..n };

# dual problem variables and simple constraints
var a {1..1} >= 0, <= C;

maximize obj: sum { i in 1..1 } a[i] - 0.5 *
    sum { i in 1..1, j in 1..1 } a[i] * a[j] * y[i] * y[j] *
    ( alpha * ( sum { k in 1..n } x[i,k] * x[j,k] ) + beta ) ^ delta;

s.t. const: sum { i in 1..1 } a[i] * y[i] = 0;

option solver loqo;

```

The model used for the radial basis kernel was almost identical except for the objective (and some different parameters):

```

# parameters for radial basis function kernel
param gamma;

maximize obj: sum { i in 1..1 } a[i] - 0.5 *
    sum { i in 1..1, j in 1..1 } a[i] * a[j] * y[i] * y[j] *
    exp( -gamma * ( sum { k in 1..n } ( x[i,k] - x[j,k] )^2 ) );

```

3 Two Digit Results

When the model was trained with the digit "2" and digit "5" training data, a misclassification error (on the testing data set) of 0.098 was achieved with the polynomial kernel and 0.110 with the radial kernel. The full results are summarized in Table 1.

Table 1: Digit 2 vs 5 Error

Data Set	Error	95% Confidence Interval	
		Lower Bound	Upper Bound
Polynomial Training	0.000	0.000	0.000
Polynomial Testing	0.098	0.033	0.162
Radial Training	0.027	0.004	0.050
Radial Testing	0.110	0.042	0.177

		Classifier									
		0	1	2	3	4	5	6	7	8	9
Truth	0	0	0	0	0	0	0	0	0	0	0
	1	0	0	0	0	0	0	0	0	0	0
	2	0	0	38	0	0	3	0	0	0	0
	3	0	0	0	0	0	0	0	0	0	0
	4	0	0	0	0	0	0	0	0	0	0
	5	0	0	5	0	0	36	0	0	0	0
	6	0	0	0	0	0	0	0	0	0	0
	7	0	0	0	0	0	0	0	0	0	0
	8	0	0	0	0	0	0	0	0	0	0
	9	0	0	0	0	0	0	0	0	0	0

Figure 1: Polynomial Kernel 2 Digit Test Error Confusion Matrix

Figures 1 and 2 show the confusion matrices for the polynomial and radial kernels respectively. Figures 3, 4, 5, and 6 display images for the correctly classified training data samples for the polynomial and radial kernels applied to the "2" versus "5" classification problem. Figures 7 and 8 display the incorrectly classified "2" digits for the polynomial and radial kernels. Figures 9 and 10 display the incorrectly classified "5" digits for the polynomial and radial kernels.

Based on these experiments, the polynomial kernel was chosen to be used for the full problem. However, both methods performed quite well and their 95% confidence intervals have significant overlap. So it is unclear which method is actually superior for this handwriting problem.

		Classifier									
		0	1	2	3	4	5	6	7	8	9
Truth	0	0	0	0	0	0	0	0	0	0	0
	1	0	0	0	0	0	0	0	0	0	0
	2	0	0	38	0	0	3	0	0	0	0
	3	0	0	0	0	0	0	0	0	0	0
	4	0	0	0	0	0	0	0	0	0	0
	5	0	0	6	0	0	35	0	0	0	0
	6	0	0	0	0	0	0	0	0	0	0
	7	0	0	0	0	0	0	0	0	0	0
	8	0	0	0	0	0	0	0	0	0	0
	9	0	0	0	0	0	0	0	0	0	0

Figure 2: Radial Kernel 2 Digit Test Error Confusion Matrix

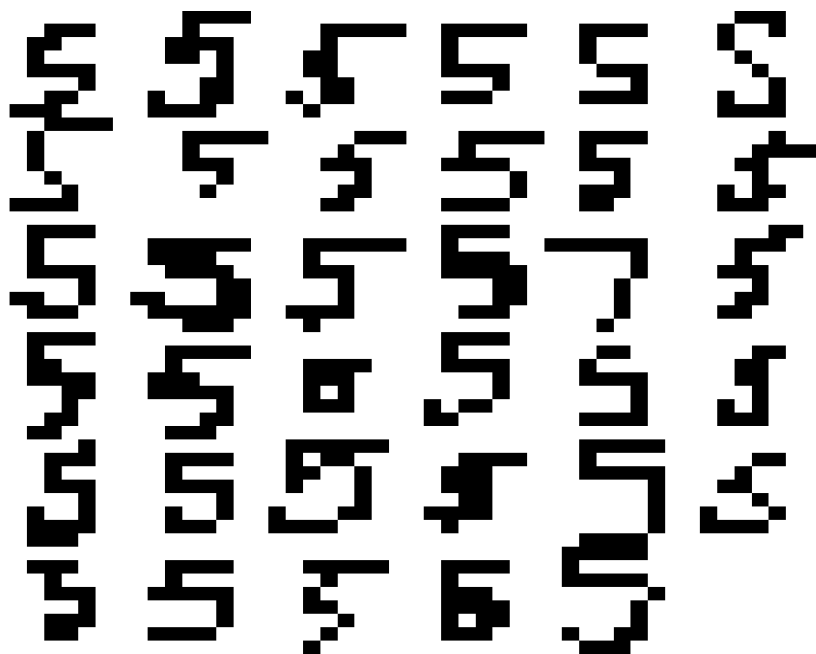


Figure 3: Radial Kernel Correctly Classified 5 Digits

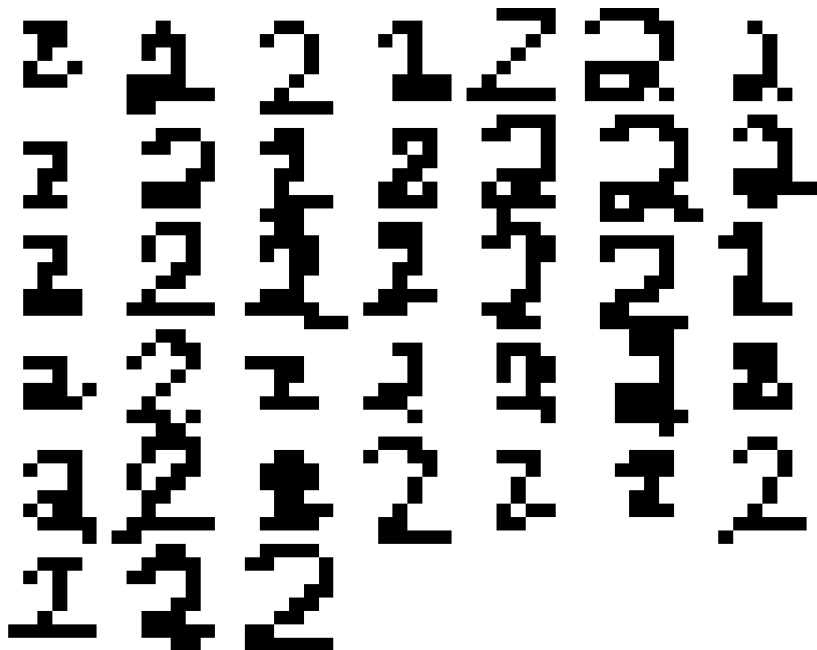


Figure 4: Radial Kernel Correctly Classified 2 Digits

4 All Digit Results

A misclassification error (on the full ten digit testing data set) of 0.200 was achieved with the polynomial kernel. The full results are summarized in Table 2. Figures 11 and 12 provide confusion matrices for the testing and training data sets.

5 Parameterization

The α_i upper bound parameter C was initially set at 100. Table 3 gives the number of support vectors (with non-zero and non- C α_i value) for each of the

Table 2: All Digits Error

Data Set	Error	95% Confidence Interval	
		Lower Bound	Upper Bound
Polynomial Training	0.029	0.018	0.040
Polynomial Testing	0.200	0.161	0.239

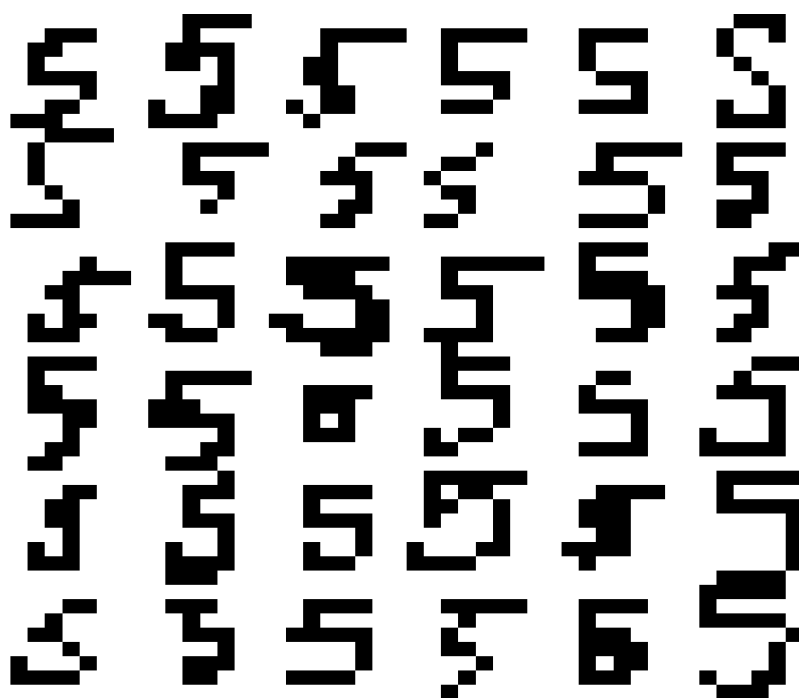


Figure 5: Polynomial Kernel Correctly Classified 5 Digits

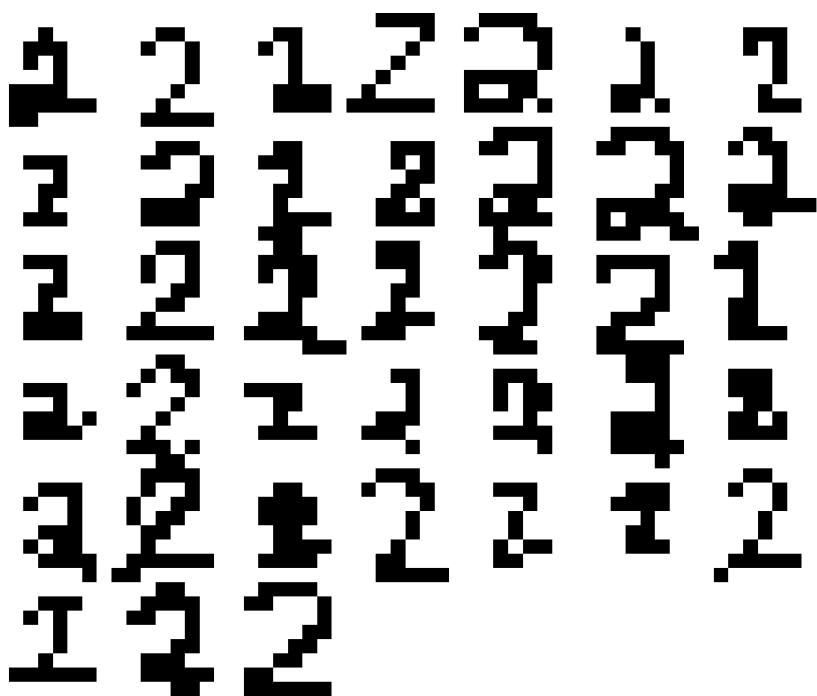


Figure 6: Polynomial Kernel Correctly Classified 2 Digits

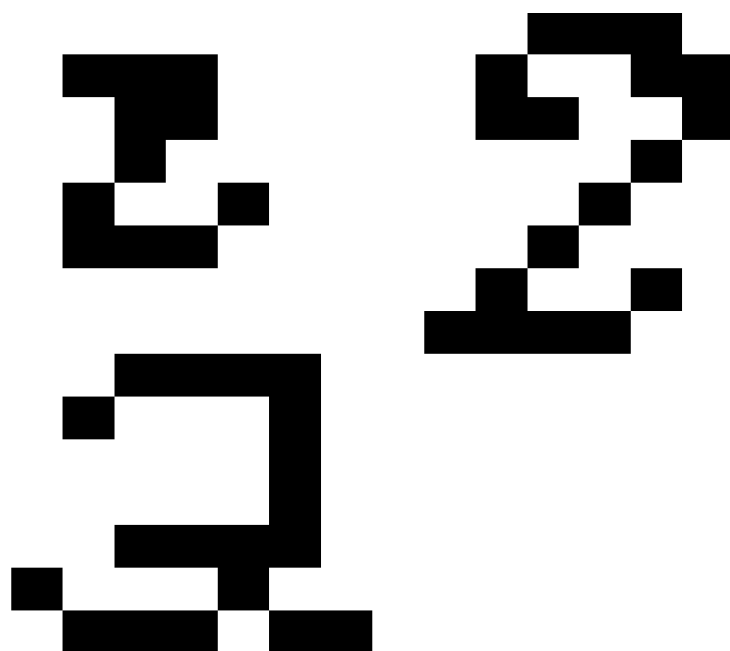


Figure 7: Polynomial Kernel 2 Misclassified as 5

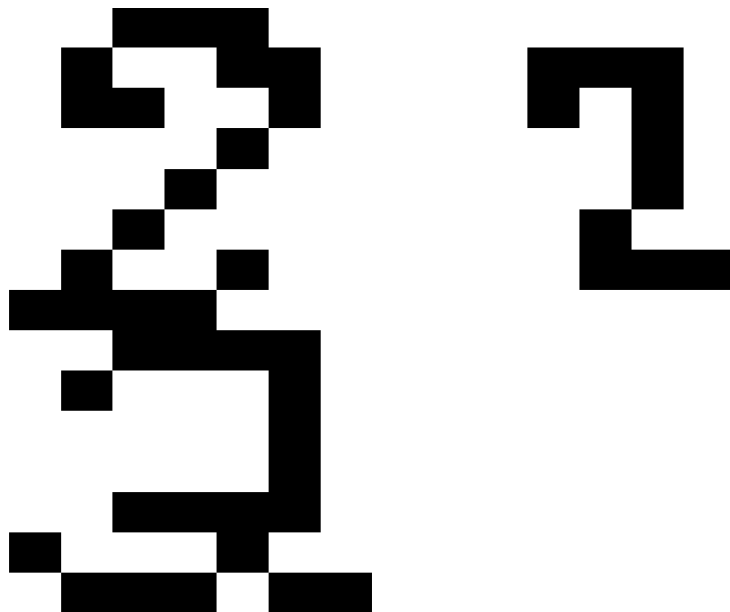


Figure 8: Radial Kernel 2 Misclassified as 5

10 SVM optimization problems solved for the 10 digit case. Out of 930 input vectors, only about 10% to 20% are chosen as support vectors by the solver. This relatively low number of support vectors indicates that the choice of C as 100 was reasonable.

6 Comparison

Figure 4 provides an error rate comparison between the four major classification methods which were applied to the handwriting data set. Weighted K-Nearest Neighbors with $k = 7$ came close to the performance achieved by the polynomial kernel support vector machine (with 0.217 error versus 0.200 for the support vector machine). Naive Bayes and Neural Networks trailed with 0.388 and 0.463 misclassification error respectively.

7 Appendix

The appendix to this report contains a number of supporting documents. The Java source code used to read the AMPL results, perform the classification, and compute statistics is included first. The code is also available at <http://code.google.com/p/csi873/source/browse/trunk/src/main/java/edu/gmu/classifier/svm/ampl/DataFileGenerator.java>.

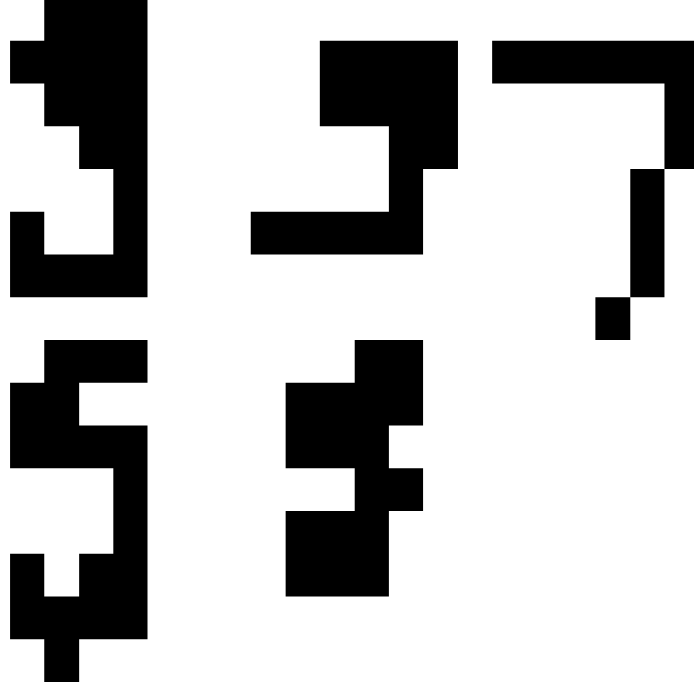


Figure 9: Polynomial Kernel 5 Misclassified as 2

Table 3: Number of Support Vectors Out Of 930

Digit	Support Vector Count
0	150
1	121
2	174
3	189
4	145
5	216
6	170
7	147
8	187
9	155

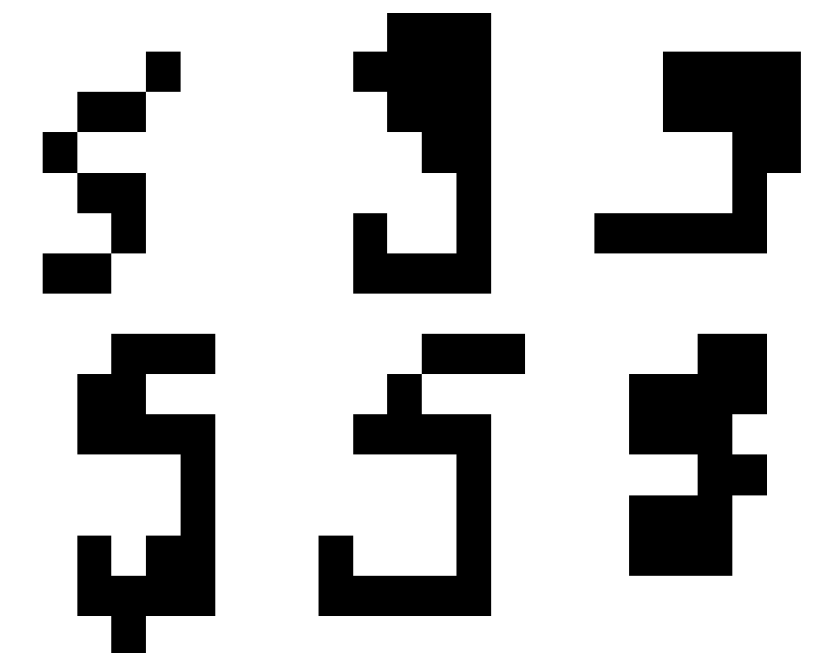


Figure 10: Radial Kernel 5 Misclassified as 2

	Classifier									
	0	1	2	3	4	5	6	7	8	9
0	37	0	0	0	2	1	1	0	0	0
1	0	36	1	2	0	0	1	1	0	0
2	0	2	31	2	0	0	0	3	3	0
3	0	2	2	33	0	1	1	1	1	0
4	0	1	0	0	32	0	2	2	1	3
5	1	1	1	1	1	31	1	3	1	0
6	0	1	1	0	3	0	35	0	0	1
7	0	2	0	0	2	0	0	36	1	0
8	0	0	0	0	1	4	0	1	30	5
9	0	1	0	1	4	1	0	7	0	27

Figure 11: Polynomial Kernel 10 Digit Test Error Confusion Matrix

	Classifier									
	0	1	2	3	4	5	6	7	8	9
Truth	0	93	0	0	0	0	0	0	0	0
	1	0	93	0	0	0	0	0	0	0
	2	0	0	91	1	1	0	0	0	0
	3	0	0	2	89	0	1	0	1	0
	4	0	0	0	0	89	0	1	0	3
	5	0	0	0	0	0	91	2	0	0
	6	0	1	0	0	0	1	91	0	0
	7	0	0	0	0	0	0	0	93	0
	8	0	0	2	0	0	0	2	0	88
	9	0	2	0	0	4	0	0	2	85

Figure 12: Polynomial Kernel 10 Digit Training Error Confusion Matrix

Table 4: Missclassification Error Overview

Algorithm	Error	95% Confidence Interval	
		Lower Bound	Upper Bound
Support Vector Machine	0.200	0.161	0.239
K-Nearest Neighbors	0.217	0.177	0.257
Naive Bayes	0.388	0.341	0.435
Neural Network	0.463	0.415	0.512

Following the Java code are the AMPL model files (both with the polynomial and radial kernels) and the AMPL data file for the "2" versus "5" classification problem (the data file for the full problem is omitted due to length). However, all AMPL model, data, and NEOS output files are also available at <http://code.google.com/p/csi873/source/browse/#svn%2Ftrunk%2Ffinal%2Fampl>.

References

- [1] Tom M. Mitchell, *Machine Learning*, WCB McGraw-Hill, Boston, 1997.

```

package edu.gmu.classifier.svm.ampl;

import java.io.BufferedReader;
import java.io.BufferedWriter;
import java.io.File;
import java.io.FileInputStream;
import java.io.FileOutputStream;
import java.io.IOException;
import java.io.InputStream;
import java.io.InputStreamReader;
import java.io.OutputStream;
import java.io.OutputStreamWriter;
import java.util.ArrayList;
import java.util.HashMap;
import java.util.List;
import java.util.Map;
import java.util.Map.Entry;

import edu.gmu.classifier.database.ResultsUploader;
import edu.gmu.classifier.database.UploadResultQuery;
import edu.gmu.classifier.database.UploadRunQuery;
import edu.gmu.classifier.io.DataLoader;
import edu.gmu.classifier.io.TrainingExample;

public class DataFileGenerator
{
    // a functor interface which defines a function for calculating the
    // y (output) value for a given training example
    // this function should always return either 1 or -1
    public interface OutputGenerator
    {
        public double getOutput( TrainingExample data );
    }

    // a functor interface which defines a function that takes
    // two input vectors (two 64 length vectors containing 0 or 1
    // in each element representing a handwriting sample) and outputs
    // a scalar value.
    public interface Kernel
    {
        public double getValue( double[] x1, double[] x2 );
    }

    // the polynomial kernel
    public static class Polynomial implements Kernel
    {
        double alpha, beta, delta;

        public Polynomial( double alpha, double beta, double delta )
        {
            this.alpha = alpha;
            this.beta = beta;
            this.delta = delta;
        }

        @Override
        public double getValue( double[] x1, double[] x2 )
        {
            double dot = 0.0;
            for ( int i = 0; i < x1.length; i++ )
            {
                dot += x1[i] * x2[i];
            }

            return Math.pow( alpha * dot + beta, delta );
        }
    }

    // the radial basis kernel
    public static class Radial implements Kernel
    {
        double gamma;

        public Radial( double gamma )
        {
            this.gamma = gamma;
        }

        @Override
        public double getValue( double[] x1, double[] x2 )
        {
            double norm = 0.0;
            for ( int i = 0; i < x1.length; i++ )
            {
                norm += Math.pow( x1[i] - x2[i], 2.0 );
            }

            return Math.exp( -gamma * norm );
        }
    }
}

```

```

// The output generator for one digit versus all others.
// If the TrainingExample is an instance of the digit
// the result is 1.0 otherwise it is -1.0.
public static class OneVersusAll implements OutputGenerator
{
    protected int digit;

    public OneVersusAll( int digit )
    {
        this.digit = digit;
    }

    @Override
    public double getOutput( TrainingExample data )
    {
        return data.getDigit( ) == digit ? 1 : -1;
    }
};

// The output generator for the two class (one digit versus
// one other digit) problem.
// If the TrainingExample is an instance of digit1 the
// result is a 1.0 otherwise it is -1.0.
public static class TwoClass implements OutputGenerator
{
    protected int digit1;
    protected int digit2;

    public TwoClass( int digit1, int digit2 )
    {
        this.digit1 = digit1;
        this.digit2 = digit2;
    }

    @Override
    public double getOutput( TrainingExample data )
    {
        int digit = data.getDigit( );

        if ( digit == digit1 )
            return 1;
        else if ( digit == digit2 )
            return -1;
        else
            return 0;
    }
};

// a routine for generating AMPL data files from the provided training example data files
// this generates 11 data files (ten for the 10 digit classification problem and one for
// the 2 versus 5 classification problem).
public static void generateAllDataFiles( String inDirectoryString, String outDirectoryString ) throws IOException
{
    generateDataFile( inDirectoryString, outDirectoryString, "classify_2-5", 2, 5 );

    for ( int i = 0; i < 10; i++ )
    {
        generateDataFile( inDirectoryString, outDirectoryString, String.format( "classify_%d", i ), i );
    }
}

// a helper routine which generates a single AMPL data file using
// data from all the digits and classifying the given digit against all others
public static void generateDataFile( String inFileName, String outDirectoryName, String outFilePrefix, int digit ) throws
IOException
{
    List<TrainingExample> dataList = DataLoader.loadDirectoryTrain( inFileName );

    File outDirectory = new File( outDirectoryName );
    File outFile = new File( outDirectory, outFilePrefix + ".dat" );
    outputDataFile( new FileOutputStream( outFile ), dataList, new OneVersusAll( digit ) );
}

// a helper routine which generates a single AMPL data file using
// data from only the two provided digits
public static void generateDataFile( String inFileName, String outDirectoryName, String outFilePrefix, int digit1, int digit2 )
throws IOException
{
    List<TrainingExample> dataList = loadData( inFileName, false, digit1, digit2 );

    File outDirectory = new File( outDirectoryName );
    File outFile = new File( outDirectory, outFilePrefix + ".dat" );
    outputDataFile( new FileOutputStream( outFile ), dataList, new TwoClass( digit1, digit2 ) );
}

// loads the training examples corresponding to the two given digits from either the test or training data set
public static List<TrainingExample> loadData( String inFileName, boolean test, int digit1, int digit2 ) throws IOException
{
    List<TrainingExample> dataList = test ? DataLoader.loadDirectoryTest( inFileName ) : DataLoader.loadDirectoryTrain

```

```

( inFileName );

List<TrainingExample> filteredList = new ArrayList<TrainingExample>( dataList.size( ) );
for ( TrainingExample data : dataList )
{
    if ( data.getDigit( ) == digit1 || data.getDigit( ) == digit2 )
    {
        filteredList.add( data );
    }
}

return filteredList;
}

// generates an AMLP data file for the given dataList and output generator
public static void outputDataFile( OutputStream stream, List<TrainingExample> dataList, OutputGenerator gen ) throws IOException
{
    BufferedWriter out = new BufferedWriter( new OutputStreamWriter( stream ) );

    out.write( "data;" );
    out.newLine( );

    int l = dataList.size( );
    out.write( String.format( "param l := %d;%n", l ) );

    int n = dataList.get( 0 ).getInputs( ).length;
    out.write( String.format( "param n := %d;%n", n ) );

    out.write( String.format( "param C := %f;%n", 100.0 ) );

    // Radial Kernel Parameters
    //out.write( String.format( "param gamma := %f;%n", 0.0521 ) );

    // Polynomial Kernel Parameters
    out.write( String.format( "param alpha := %f;%n", 0.0156 ) );

    out.write( String.format( "param beta := %f;%n", 0.0 ) );

    out.write( String.format( "param delta := %f;%n", 3.0 ) );

    out.write( String.format( "param y :=%n" ) );
    for ( int i = 0; i < l; i++ )
    {
        TrainingExample data = dataList.get( i );
        out.write( String.format( " %d %.1f%n", i + 1, gen.getOutput( data ) ) );
    }
    out.write( ";" );
    out.newLine( );

    out.write( String.format( "param x:" ) );
    for ( int i = 0; i < n; i++ )
    {
        out.write( String.format( " %d", i + 1 ) );
    }
    out.write( String.format( " :=%n" ) );
    for ( int i = 0; i < l; i++ )
    {
        TrainingExample data = dataList.get( i );
        double[] input = data.getInputs( );

        out.write( String.format( " %d", i + 1 ) );

        for ( int j = 0; j < n; j++ )
        {
            out.write( String.format( " %.1f", input[j] ) );
        }

        out.newLine( );
    }
    out.write( ";" );
    out.newLine( );

    out.close( );
}

// reads a NEOS AMPL output file and returns the calculated alpha values
public static double[] read_a( String file ) throws IOException
{
    FileInputStream stream = new FileInputStream( file );
    try
    {
        return read_a( stream );
    }
    finally
    {
        stream.close( );
    }
}

// reads a NEOS AMPL output file and returns the calculated alpha values

```



```

public static double[] read_a( InputStream stream ) throws IOException
{
    List<Double> list = new ArrayList<Double>( );

    BufferedReader in = new BufferedReader( new InputStreamReader( stream ) );
    String line = null;
    boolean parseMode = false;

    while ( ( line = in.readLine( ) ) != null )
    {
        if ( parseMode )
        {
            String[] tokens = line.trim( ).split( "[\\s]+" );

            try
            {
                for ( int i = 0; i < tokens.length / 2; i++ )
                {
                    int index = Integer.parseInt( tokens[i * 2] ) - 1;
                    double value = Double.parseDouble( tokens[i * 2 + 1] );

                    ensureLength( index, list );

                    list.set( index, value );
                }
            }
            catch ( NumberFormatException e )
            {
                parseMode = false;
            }
        }
        else if ( line.startsWith( "a [*] :=" ) )
        {
            parseMode = true;
        }
    }

    double[] array = new double[list.size( )];
    for ( int i = 0; i < list.size( ); i++ )
        array[i] = list.get( i );

    return array;
}

// calculate b's for each a
// only one is needed for an i s.t. 0 < a[i] < C, but this is a good check
public static double[] calculate_b( List<TrainingExample> dataList, OutputGenerator out, Kernel kernel, double C, double[] a )
throws IOException
{
    double[] b = new double[a.length];

    for ( int i = 0; i < b.length; i++ )
    {
        double[] x_i = dataList.get( i ).getInputs( );
        double y_i = out.getOutput( dataList.get( i ) );

        double sum = 0.0;
        for ( int j = 0; j < b.length; j++ )
        {
            TrainingExample x = dataList.get( j );
            double[] x_j = x.getInputs( );
            double y_j = out.getOutput( x );

            sum += y_j * a[j] * kernel.getValue( x_j, x_i );
        }

        b[i] = sum - y_i;
    }

    return b;
}

/**
 * Makes a classification decision for the 2 versus 5 case based on the AMPL solution.
 */
* @param dataListTest a list of data samples of classify
* @param dataListTrain the training data list used to train the svm classifier
* @param out a generator for calculating expected output values from the training data
* @param kernel the kernel used in the AMPL model to calculate the alpha vector
* @param a the alpha vector generated via AMPL
* @param b the beta value calculated from the AMPL solution
* @return a vector containing the predicted y values for each testing example
*/
public static double[] calculate_y_predicted( List<TrainingExample> dataListTest, List<TrainingExample> dataListTrain,
OutputGenerator out, Kernel kernel, double[] a, double b )
{
    double[] y_predicted = new double[ dataListTest.size( ) ];

```

```

// iterate over the training examples
for ( int i = 0; i < dataListTest.size( ); i++ )
{
    TrainingExample x_i = dataListTest.get( i );

    // apply the formula from the svm slides to compute a y_predicted value
    // based on the alpha vector (solution to the dual problem)
    double sum = 0.0;
    for ( int j = 0; j < a.length; j++ )
    {
        TrainingExample x_j = dataListTrain.get( j );
        double y_j = out.getOutput( x_j );
        double a_j = a[j];

        sum += y_j * a_j * kernel.getValue( x_j.getInputs( ), x_i.getInputs( ) );
    }

    y_predicted[i] = sum - b;
}

return y_predicted;
}

// ensures that the length of the provided list is at least large enough to contain index
private static void ensureLength( int index, List<Double> list )
{
    if ( list.size( ) > index ) return;

    for ( int i = list.size( ); i <= index; i++ )
    {
        list.add( i, 0.0 );
    }
}

// uses calculate_y_predicted( ) to classify each testing example and compute an error rate
public static int[] calculateErrorRate( List<TrainingExample> dataListTest, List<TrainingExample> dataListTrain,
OutputGenerator out, Kernel kernel, double[] a, double b )
{
    int[] digit = new int[ dataListTest.size( ) ];

    double[] y = calculate_y_predicted( dataListTest, dataListTrain, out, kernel, a, b );

    double count = 0.0;
    for ( int i = 0; i < dataListTest.size( ); i++ )
    {
        double value = y[i];
        double predicted = y[i] > 0 ? 1.0 : -1.0;
        double actual = out.getOutput( dataListTest.get( i ) );

        digit[i] = predicted > 0 ? 2 : 5;

        if ( predicted == actual )
        {
            count += 1.0;
        }

        System.out.printf( "Value %.4f Predicted %.1f Actual %.1f\n", value, predicted, actual );
    }

    double errorRate = 1.0 - ( count / dataListTest.size( ) );
    double errorInterval = 1.96 * Math.sqrt( errorRate * ( 1 - errorRate ) / dataListTest.size( ) );

    System.out.printf( "Error Rate: %.3f Train Interval: (%.3f, %.3f)\n", errorRate, errorRate - errorInterval, errorRate +
errorInterval );

    return digit;
}

// a database helper method for uploading results in the SQL data format
// required by the CSI710 handwriting sample viewer (used for generating
// confusion matrices and handwriting sample visualizations)
public static void uploadResultsTest2_5( String description, List<TrainingExample> list, int[] predicted )
{
    int first2id = 171257;
    int first5id = 171380;

    UploadRunQuery uploadRunQuery = new UploadRunQuery( description, System.currentTimeMillis( ) );
    uploadRunQuery.runQuery( );
    int ixRunId = uploadRunQuery.getRunId( );

    int count2 = 0;
    int count5 = 0;

    for ( int i = 0 ; i < list.size( ); i++ )
    {
        TrainingExample data = list.get( i );
        String sClassification = String.valueOf( predicted[i] );

        int index;
        if ( data.getDigit( ) == 2 )

```

```

        {
            index = first2id + count2;
            count2 += 1;
        }
        else
        {
            index = first5id + count5;
            count5 += 1;
        }

        UploadResultQuery uploadResultQuery = new UploadResultQuery( index, ixRunId, sClassification );
        uploadResultQuery.runQuery( );
    }
}

// helper method for generating AMPL model and data files
public static void generateAmplDataFiles( ) throws IOException
{
    String inputDirectory = "/home/ulman/CSI873/midterm/data";
    String outputDirectory = "/home/ulman/CSI873/midterm/repository/final/ampl";
    generateAllDataFiles( inputDirectory, outputDirectory );
}

public static void generateTestingResultsPolynomial_25( ) throws IOException
{
    generateTestingResults( new Polynomial( 0.0156, 0.0, 3.0 ), "SVM 2vs5 run  $\alpha = 0.0156$ ,  $\beta = 0$ ,  $d = 3$ " );
}

public static void generateTestingResultsRadial_25( ) throws IOException
{
    generateTestingResults( new Radial( 0.0521 ), "SVM 2vs5 radial" );
}

// runs two digit 2-5 classification problem and calculates and displays results
public static void generateTestingResults( Kernel kernel, String name ) throws IOException
{
    List<TrainingExample> dataListTrain = loadData( "/home/ulman/CSI873/midterm/data", false, 2, 5 );
    List<TrainingExample> dataListTest = loadData( "/home/ulman/CSI873/midterm/data", true, 2, 5 );
    String outputDirectory = "/home/ulman/CSI873/midterm/repository/final/ampl";
    String temporaryOutput = String.format( "%s/%s", outputDirectory, "out.tmp" );

    double C = 100.0;
    OutputGenerator out = new TwoClass( 2, 5 );

    double[] a = read_a( temporaryOutput );
    double[] b = calculate_b( dataListTrain, out, kernel, C, a );

    double count = 0.0;
    double b_sum = 0.0;

    for ( int i = 0 ; i < a.length ; i++ )
    {
        if ( a[i] < C && a[i] > 0.001 )
        {
            System.out.printf( "%.4f %.12f\n", a[i], b[i] );
            b_sum += b[i];
            count += 1.0;
        }
    }

    double b_avg = b_sum / count;

    System.out.println( "Error rate on Training Data." );
    calculateErrorRate( dataListTrain, dataListTrain, out, kernel, a, b_avg );

    System.out.println( "Error rate on Testing Data." );
    int[] testPredictions = calculateErrorRate( dataListTest, dataListTrain, out, kernel, a, b_avg );

    uploadResultsTest2_5( name, dataListTest, testPredictions );
}

////////////////////////////////////
/// Full 10 Digit Problem ///
////////////////////////////////////

// a helper data structure for storing the alpha output values from AMPL
// along with the calculated b value and an OutputGenerator
public static class Model
{
    double[] a;
    double b;
    OutputGenerator out;

    public Model( double[] a, double b, OutputGenerator out )
    {
        this.a = a;
        this.b = b;
        this.out = out;
    }
}

```

```

// runs ten digit classification problem and calculates and displays results
public static void generateTestingResultsAll( ) throws IOException
{
    List<TrainingExample> dataListTrain = DataLoader.loadDirectoryTrain( "/home/ulman/CSI873/midterm/data" );
    List<TrainingExample> dataListTest = DataLoader.loadDirectoryTest( "/home/ulman/CSI873/midterm/data" );

    Kernel kernel = new Polynomial( 0.0156, 0.0, 3.0 );

    Map<Integer,Model> map = new HashMap<Integer,Model>( );
    for ( int i = 0 ; i < 10 ; i++ )
    {
        String outputDirectory = "/home/ulman/CSI873/midterm/repository/final/ampl";
        String temporaryOutput = String.format( "%s/%s", outputDirectory, String.format( "out_%d.txt", i ) );

        double C = 100.0;
        OutputGenerator out = new OneVersusAll( i );

        double[] a = read_a( temporaryOutput );
        double[] b = calculate_b( dataListTrain, out, kernel, C, a );

        double count = 0.0;
        double b_sum = 0.0;

        for ( int j = 0 ; j < a.length ; j++ )
        {
            if ( a[j] < C && a[j] > 0.001 )
            {
                System.out.printf( "%.4f %.12f\n", a[j], b[j] );
                b_sum += b[j];
                count += 1.0;
            }
        }

        double b_avg = b_sum / count;

        map.put( i, new Model( a, b_avg, out ) );
    }

    System.out.println( "Error rate on Training Data." );
    int[] trainPredictions = calculateErrorRate( dataListTrain, dataListTrain, kernel, map );

    System.out.println( "Error rate on Testing Data." );
    int[] testPredictions = calculateErrorRate( dataListTest, dataListTrain, kernel, map );

    uploadResultsAllTrain( trainPredictions );
    uploadResultsAllTest( testPredictions );
}

// uses calculate_y_predicted( ) to classify each testing example and compute an error rate
public static int[] calculateErrorRate( List<TrainingExample> dataListTest, List<TrainingExample> dataListTrain, Kernel kernel,
Map<Integer,Model> map )
{
    int[] predicted_digit = calculate_y_predicted( dataListTest, dataListTrain, kernel, map );

    double count = 0.0;
    for ( int i = 0; i < dataListTest.size( ); i++ )
    {
        TrainingExample data = dataListTest.get( i );

        if ( data.getDigit( ) == predicted_digit[i] )
        {
            count += 1.0;
        }
    }

    double errorRate = 1.0 - ( count / dataListTest.size( ) );
    double errorInterval = 1.96 * Math.sqrt( errorRate * ( 1 - errorRate ) / dataListTest.size( ) );

    System.out.printf( "Error Rate: %.3f Train Interval: (%.3f, %.3f)\n", errorRate, errorRate - errorInterval, errorRate +
errorInterval );

    return predicted_digit;
}

/**
 * Makes a classification decision for the 10 digit classification problem based on the solutions
 * to the ten individual AMPL problems.
 *
 * @param dataListTest a list of data samples of classify
 * @param dataListTrain the training data list used to train the svm classifier
 * @param out a generator for calculating expected output values from the training data
 * @param kernel the kernel used in the AMPL model to calculate the alpha vector
 * @param map the alpha and beta values generated via AMPL for each of the ten separate SVMs constructed (one for each digit)
 * @return a vector containing the predicted y values for each testing example
 */
public static int[] calculate_y_predicted( List<TrainingExample> dataListTest, List<TrainingExample> dataListTrain, Kernel
kernel, Map<Integer,Model> map )
{
    int[] predicted_digit = new int[ dataListTest.size( ) ];

```

```

for ( int i = 0; i < dataListTest.size( ); i++ )
{
    TrainingExample x_i = dataListTest.get( i );

    int best_digit = -1;
    double best_value = Double.NEGATIVE_INFINITY;

    for ( Entry<Integer,Model> entry : map.entrySet( ) )
    {
        int digit = entry.getKey( );
        Model model = entry.getValue( );
        double[] a = model.a;
        double b = model.b;
        OutputGenerator out = model.out;

        double sum = 0.0;
        for ( int j = 0; j < a.length; j++ )
        {
            TrainingExample x_j = dataListTrain.get( j );
            double y_j = out.getOutput( x_j );
            double a_j = a[j];

            sum += y_j * a_j * kernel.getValue( x_j.getInputs( ), x_i.getInputs( ) );
        }

        double value = sum - b;

        if ( value > best_value )
        {
            best_value = value;
            best_digit = digit;
        }
    }

    predicted_digit[i] = best_digit;
}

return predicted_digit;
}

public static void uploadResultsAllTest( int[] predicted_digit )
{
    uploadResultsAll( "svm_testing_polynomial_all", ResultsUploader.IX_TEST_FIRST_INDEX, predicted_digit );
}

public static void uploadResultsAllTrain( int[] predicted_digit )
{
    uploadResultsAll( "svm_training_polynomial_all", ResultsUploader.IX_TRAIN_FIRST_INDEX, predicted_digit );
}

public static void uploadResultsAll( String description, int firstDataId, int[] predicted_digit )
{
    UploadRunQuery uploadRunQuery = new UploadRunQuery( description, System.currentTimeMillis( ) );
    uploadRunQuery.runQuery( );
    int ixRunId = uploadRunQuery.getRunId( );

    for ( int i = 0 ; i < predicted_digit.length; i++ )
    {
        String sClassification = String.valueOf( predicted_digit[i] );

        UploadResultQuery uploadResultQuery = new UploadResultQuery( firstDataId + i, ixRunId, sClassification );
        uploadResultQuery.runQuery( );
    }
}

public static void main( String[] args ) throws IOException
{
    generateTestingResultsAll( );
}
}

```

```

model;

# number of training examples
param l;

# number of input parameters (number of pixels in the handwriting digit images)
param n;

# weight on xi penalty coefficient in primal problem
param C;

# parameters for radial basis function kernel
param gamma;

# output vector (1 or -1)
param y { 1..l };

# input data
param x { 1..l, 1..n };

# dual problem variables and simple constraints
var a {1..l} >= 0, <= C;

maximize obj: sum { i in 1..l } a[i] - 0.5 * sum { i in 1..l, j in 1..l } a[i] * a[j] * y[i] * y[j] * exp( -gamma * ( sum { k in 1..n }
( x[i,k] - x[j,k] )^2 ) );

s.t. const: sum { i in 1..l } a[i] * y[i] = 0;

option solver loqo;

```

```

model;

# number of training examples
param l;

# number of input parameters (number of pixels in the handwriting digit images)
param n;

# weight on xi penalty coefficient in primal problem
param C;

# parameters for polynomial machine kernel
param alpha;
param beta;
param delta;

# output vector (1 or -1)
param y { 1..l };

# input data
param x { 1..l, 1..n };

# dual problem variables and simple constraints
var a {1..l} >= 0, <= C;

maximize obj: sum { i in 1..l } a[i] - 0.5 * sum { i in 1..l, j in 1..l } a[i] * a[j] * y[i] * y[j] * ( alpha * ( sum { k in 1..n } x
[i,k] * x[j,k] ) + beta ) ^ delta;

s.t. const: sum { i in 1..l } a[i] * y[i] = 0;

option solver loqo;

```

```
data;  
  
param l := 186;  
param n := 64;  
param C := 100.000000;  
param alpha := 0.015600;  
param beta := 0.000000;  
param delta := 3.000000;
```

```
param y :=
```

```
1 1.0  
2 1.0  
3 1.0  
4 1.0  
5 1.0  
6 1.0  
7 1.0  
8 1.0  
9 1.0  
10 1.0  
11 1.0  
12 1.0  
13 1.0  
14 1.0  
15 1.0  
16 1.0  
17 1.0  
18 1.0  
19 1.0  
20 1.0  
21 1.0  
22 1.0  
23 1.0  
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26 1.0  
27 1.0  
28 1.0  
29 1.0  
30 1.0  
31 1.0  
32 1.0  
33 1.0  
34 1.0  
35 1.0  
36 1.0  
37 1.0  
38 1.0  
39 1.0  
40 1.0  
41 1.0  
42 1.0  
43 1.0  
44 1.0  
45 1.0  
46 1.0  
47 1.0  
48 1.0  
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63 1.0  
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67 1.0  
68 1.0  
69 1.0  
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71 1.0  
72 1.0  
73 1.0  
74 1.0  
75 1.0  
76 1.0  
77 1.0  
78 1.0  
79 1.0  
80 1.0
```


81 1.0
82 1.0
83 1.0
84 1.0
85 1.0
86 1.0
87 1.0
88 1.0
89 1.0
90 1.0
91 1.0
92 1.0
93 1.0
94 -1.0
95 -1.0
96 -1.0
97 -1.0
98 -1.0
99 -1.0
100 -1.0
101 -1.0
102 -1.0
103 -1.0
104 -1.0
105 -1.0
106 -1.0
107 -1.0
108 -1.0
109 -1.0
110 -1.0
111 -1.0
112 -1.0
113 -1.0
114 -1.0
115 -1.0
116 -1.0
117 -1.0
118 -1.0
119 -1.0
120 -1.0
121 -1.0
122 -1.0
123 -1.0
124 -1.0
125 -1.0
126 -1.0
127 -1.0
128 -1.0
129 -1.0
130 -1.0
131 -1.0
132 -1.0
133 -1.0
134 -1.0
135 -1.0
136 -1.0
137 -1.0
138 -1.0
139 -1.0
140 -1.0
141 -1.0
142 -1.0
143 -1.0
144 -1.0
145 -1.0
146 -1.0
147 -1.0
148 -1.0
149 -1.0
150 -1.0
151 -1.0
152 -1.0
153 -1.0
154 -1.0
155 -1.0
156 -1.0
157 -1.0
158 -1.0
159 -1.0
160 -1.0
161 -1.0
162 -1.0
163 -1.0
164 -1.0
165 -1.0
166 -1.0
167 -1.0
168 -1.0
169 -1.0
170 -1.0

[illegible]

[illegible]

[illegible]

[illegible]

Output sample from NEOS Server for full SVM problem: digit 0 versus digit 1-9

NEOS Server Version 5.0
Job# : 48781
Password : eyVHLKkZ
Solver : nco:LOQO:AMPL
Start : 2011-12-03 20:17:45
End : 2011-12-03 20:18:53
Host : neos-1.chtc.wisc.edu

Disclaimer:

This information is provided without any express or implied warranty. In particular, there is no warranty of any kind concerning the fitness of this information for any particular purpose.

Job 48781 sent to neos-1.chtc.wisc.edu

password: eyVHLKkZ

----- Begin Solver Output -----

Executing /opt/neos/Drivers/loqo-ampl/loqo-driver.py at time: 2011-12-03 20:17:45.496927

File exists

You are using the solver loqo.

Executing AMPL.

processing data.

processing commands.

930 variables, all nonlinear

1 constraint, all linear; 930 nonzeros

1 equality constraint

1 nonlinear objective; 930 nonzeros.

LOQO 6.07: optimal solution (41 QP iterations, 121 evaluations)

primal objective 4720.34696

dual objective 4720.346974

a [*] :=

1	2.54104e-07	234	17.4712	467	4.87526e-08	700	5.87498e-08
2	1.19626e-07	235	30.5848	468	2.03188e-08	701	2.21626e-08
3	1.34122e-08	236	1.22409e-07	469	8.16445e-09	702	6.0253e-08
4	3.98039	237	8.33865e-09	470	8.14434e-09	703	1.55225e-08
5	9.71702e-09	238	1.57041e-08	471	19.2816	704	1.61523e-08
6	2.58456e-06	239	9.67456e-09	472	3.90321e-08	705	2.06737e-08
7	9.93516e-09	240	6.95511e-08	473	8.43092e-09	706	1.83124e-08
8	1.18059e-08	241	4.81713e-09	474	2.68542e-08	707	8.23788e-09
9	79.0103	242	4.52188e-09	475	5.75013e-08	708	2.76888e-08
10	66.8627	243	3.97575e-09	476	1.47491e-08	709	3.30243e-08
11	29.4992	244	1.39611e-08	477	1.46324e-08	710	3.63636
12	95.701	245	6.16609e-09	478	1.74349e-08	711	3.36838e-07
13	50.4826	246	2.20327e-08	479	1.30328e-08	712	0.883297
14	29.1869	247	2.18117e-08	480	7.13772e-09	713	1.33965e-07
15	63.0077	248	1.58383e-08	481	2.80275e-08	714	4.01726e-08
16	100	249	2.39507e-08	482	2.74134e-08	715	2.59658e-08
17	19.0734	250	2.65994e-08	483	2.2169e-08	716	4.67839e-08
18	57.3959	251	2.51157e-08	484	4.15796e-08	717	2.95377e-08
19	54.6249	252	5.32651e-08	485	8.23745	718	89.2605
20	53.6528	253	3.17409e-08	486	2.73684e-08	719	2.52053e-08
21	100	254	6.59136e-08	487	1.32297e-08	720	1.77329e-08
22	41.421	255	1.9533e-08	488	2.45174e-08	721	1.20815e-08
23	91.599	256	6.35262e-09	489	1.48766e-08	722	6.50441e-09
24	100	257	9.72672e-09	490	1.52682e-08	723	1.35738e-08
25	100	258	4.07421e-09	491	8.14434e-09	724	2.76213e-08
26	100	259	6.37795e-09	492	2.45174e-08	725	18.7365
27	100	260	7.83337e-09	493	5.57514e-08	726	2.92533e-08
28	100	261	9.37859e-09	494	6.42128e-08	727	1.05137e-08
29	100	262	4.4875	495	5.48359e-08	728	2.13431e-08
30	100	263	7.23894e-09	496	1.20387e-08	729	2.49374e-08
31	55.3495	264	8.59847e-09	497	2.6448e-07	730	1.44496e-08
32	23.8046	265	7.93346e-09	498	1.0586e-08	731	4.62007
33	100	266	1.42034e-08	499	1.70863e-08	732	8.96058
34	0.468614	267	3.82261e-08	500	8.20964e-09	733	2.0332e-08
35	100	268	4.15888e-08	501	2.13967e-08	734	1.562e-07
36	32.8671	269	1.48333e-07	502	8.33854e-08	735	1.02088e-08
37	4.89027e-09	270	1.01998e-08	503	6.4014e-09	736	1.93147e-08
38	100	271	1.81366e-08	504	2.18686e-08	737	1.94745e-08
39	100	272	2.72315e-08	505	5.35617e-09	738	1.74742e-08
40	8.59328e-09	273	1.674e-08	506	2.96089e-09	739	3.31582e-08
41	1.45215e-08	274	4.64615e-08	507	8.86299e-09	740	29.6416
42	6.23803e-08	275	1.35814e-07	508	1.9907e-08	741	4.5877e-08
43	6.94796e-09	276	2.64469e-08	509	1.14618e-08	742	1.91541e-08
44	2.29794e-08	277	1.82098e-08	510	8.52856e-09	743	2.2468e-08
45	1.69539e-08	278	4.9414e-08	511	9.37591e-09	744	2.08865e-08
46	13.4704	279	4.79054e-08	512	1.26803e-08	745	1.83089e-08
47	6.9851e-08	280	2.55699e-08	513	7.76705e-09	746	2.96616e-08
48	1.1076e-08	281	1.20888e-08	514	12.306	747	1.48627e-08
49	40.5431	282	5.12537e-09	515	1.61456e-07	748	11.4963
50	3.54224e-08	283	1.26779e-08	516	1.9956e-08	749	2.18718e-08
51	59.5613	284	23.3861	517	3.70136e-08	750	3.91503e-08

52	29.3258	285	1.29012e-08
53	9.82969e-09	286	1.13853e-08
54	17.9755	287	1.16266e-08
55	3.54791e-08	288	2.05013e-08
56	1.95069e-08	289	1.55203e-08
57	6.87856e-09	290	2.7949e-08
58	100	291	1.33001e-08
59	1.91574	292	64.6035
60	100	293	1.00033e-08
61	100	294	7.72382e-09
62	1.68637e-06	295	1.9299e-08
63	3.22921e-08	296	2.73438e-08
64	100	297	2.76609e-08
65	100	298	1.45769e-08
66	4.84071e-07	299	3.46291e-08
67	100	300	8.41646e-09
68	75.5297	301	7.85982e-08
69	100	302	83.4905
70	6.32841e-09	303	2.57202e-08
71	4.0333e-09	304	1.64889e-08
72	2.22391e-08	305	2.29576e-08
73	100	306	1.87963e-08
74	1.55623e-08	307	1.94092e-08
75	100	308	1.25786e-07
76	1.41779e-07	309	2.40743e-08
77	2.94677e-08	310	1.3949e-08
78	100	311	9.40763e-09
79	100	312	1.30028e-08
80	2.51005e-08	313	7.94895e-09
81	53.0538	314	7.03787e-09
82	100	315	3.02551e-08
83	100	316	8.11268e-09
84	2.0639e-08	317	7.96406e-09
85	8.55713e-09	318	6.09149e-09
86	75.1753	319	7.30344e-09
87	72.3981	320	3.22578
88	4.50408e-08	321	1.32705e-08
89	88.6124	322	9.33881e-09
90	2.68238e-08	323	7.04953e-09
91	1.74891e-08	324	8.13147e-09
92	29.4659	325	8.9976e-09
93	6.40354	326	6.25153e-09
94	5.70093e-07	327	4.44801e-09
95	1.18143e-07	328	7.13239e-09
96	95.4334	329	1.86176e-08
97	2.16e-08	330	8.88263e-09
98	2.65149e-08	331	2.98174e-08
99	1.94551e-08	332	1.26561e-08
100	4.96008e-08	333	7.81472e-09
101	4.92112e-08	334	6.62479e-09
102	4.93881e-08	335	1.21847e-08
103	1.39675e-07	336	1.23951e-08
104	4.9432e-08	337	0.818902
105	1.02334e-07	338	5.11663
106	9.91209e-08	339	0.526704
107	1.21861e-07	340	6.35364e-08
108	3.37421e-06	341	1.34441e-08
109	1.43245e-07	342	1.76907e-08
110	1.02334e-07	343	2.80312e-08
111	5.70093e-07	344	3.10516e-08
112	1.45749e-07	345	2.0243e-08
113	1.04659e-07	346	1.40558e-08
114	1.04659e-07	347	2.06604e-08
115	6.14558e-08	348	8.71565e-08
116	2.48369e-08	349	1.70372e-08
117	5.9402e-08	350	5.93449e-09
118	100	351	1.58516e-08
119	100	352	4.11252e-08
120	5.20151e-07	353	1.51187e-08
121	5.70093e-07	354	2.16536e-08
122	5.70093e-07	355	1.57554e-08
123	5.20151e-07	356	8.50927e-09
124	1.02334e-07	357	9.71347e-09
125	21.5335	358	1.1988e-08
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128	5.77438e-08	361	1.13474e-08
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135	5.35017e-08	368	4.58223
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137	2.20649e-08	370	1.00832e-08
138	1.60545e-08	371	2.94072e-08
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556	6.3892e-08
557	36.2011
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578	49.9234
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838	2.52157e-08
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142	9.66486e-09	375	20.1633	608	2.48364e-08	841	7.95741e-06
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145	5.53809e-08	378	2.03594e-08	611	2.56254e-08	844	22.1924
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147	1.99422e-08	380	1.27199e-08	613	7.72954e-09	846	21.2986
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149	1.2861e-08	382	1.23401e-08	615	3.11913e-08	848	1.28492e-08
150	1.09542e-08	383	7.62784e-08	616	3.11907e-08	849	2.73101e-07
151	2.13299e-08	384	27.2171	617	9.25047e-09	850	4.7705e-08
152	1.92667e-07	385	1.37407e-08	618	2.36977e-08	851	38.0972
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156	1.87558e-07	389	2.47875e-08	622	2.3416e-08	855	2.49449e-08
157	5.20151e-07	390	8.86408e-08	623	1.13234e-08	856	2.51318e-08
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161	6.64538e-08	394	2.99264e-08	627	1.29527e-08	860	2.14264e-08
162	100	395	4.06366e-08	628	6.15296e-09	861	2.53905e-08
163	1.06591e-08	396	4.0852e-08	629	17.7125	862	2.78768e-08
164	1.87558e-07	397	100	630	2.27535e-08	863	20.2213
165	2.9957e-08	398	38.3001	631	2.02758e-08	864	1.10992e-07
166	1.35284e-08	399	65.4451	632	15.1093	865	6.31223e-08
167	1.19697e-07	400	3.54449e-08	633	3.24086e-08	866	2.53534e-08
168	1.76641e-07	401	3.8498e-08	634	15.9598	867	1.7201e-08
169	4.19078e-08	402	2.36009e-08	635	36.2095	868	3.09273e-08
170	4.40335e-08	403	1.66105e-08	636	3.31771	869	3.77642e-08
171	2.33274e-08	404	3.01124e-08	637	1.62809e-08	870	1.16611e-08
172	3.43441e-08	405	3.01124e-08	638	1.16284e-05	871	1.89849e-08
173	1.02334e-07	406	1.52561e-08	639	24.9877	872	1.53376e-08
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176	3.52827e-07	409	2.49312e-08	642	1.75216e-08	875	9.95763e-09
177	1.87999e-08	410	1.39885e-08	643	1.35339e-08	876	7.19758e-09
178	1.28175e-08	411	1.88709e-08	644	5.54892e-08	877	1.11478e-08
179	2.56711e-08	412	1.53606e-08	645	24.2709	878	1.18418e-08
180	4.64274e-08	413	9.64378e-09	646	3.40897e-08	879	1.02442e-08
181	1.87558e-07	414	1.07262e-08	647	2.31233e-08	880	9.12941e-09
182	5.70093e-07	415	3.05385e-08	648	13.371	881	1.7495e-08
183	100	416	1.73858e-08	649	2.00226e-08	882	2.53534e-08
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185	1.02334e-07	418	2.8581e-08	651	2.38337	884	5.54365
186	4.9432e-08	419	2.8581e-08	652	0.495867	885	1.68253e-08
187	1.25038e-08	420	7.31885e-09	653	5.51548e-08	886	7.66081e-09
188	7.68674e-09	421	1.60356e-08	654	4.77801e-08	887	2.13601e-08
189	2.08558e-08	422	1.20679e-08	655	3.50108e-08	888	1.43996e-08
190	1.63374e-08	423	2.14087e-08	656	2.51646e-08	889	3.57152e-08
191	1.09468e-08	424	7.37835e-09	657	2.51499e-08	890	6.01533e-08
192	3.04858	425	1.87619e-08	658	12.582	891	8.7674e-09
193	35.4882	426	8.53409e-09	659	33.3076	892	8.32414e-09
194	7.4284e-08	427	1.33366e-08	660	4.70003e-08	893	1.60036e-08
195	1.14531e-08	428	2.79618e-08	661	5.1817e-08	894	9.38604e-09
196	1.57079e-08	429	34.6565	662	19.6549	895	1.26229e-08
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198	2.65985e-08	431	5.57306e-09	664	3.34334e-08	897	2.64163e-08
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203	5.27549e-08	436	2.64663e-08	669	8.09602e-08	902	2.93149e-08
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205	2.32679e-08	438	1.30377e-08	671	1.06244e-08	904	3.19172e-08
206	4.40799	439	1.66787e-08	672	1.87626e-08	905	1.93123e-08
207	12.5803	440	1.35817e-08	673	3.06638e-08	906	7.62597e-08
208	2.36189e-08	441	2.33235e-08	674	3.19671e-08	907	7.22766e-09
209	1.72547e-08	442	1.1371e-08	675	2.76627e-08	908	9.02114e-09
210	100	443	1.05029e-08	676	2.39489e-08	909	4.02114e-08
211	2.07402e-08	444	2.37505e-08	677	8.30498e-08	910	1.7339e-08
212	1.44934e-08	445	6.64982e-08	678	1.85878e-08	911	1.89005e-08
213	62.9367	446	1.11484e-08	679	1.92596e-08	912	1.63775e-08
214	2.67088e-08	447	1.66349e-08	680	4.38342e-08	913	6.99876e-09
215	2.09632e-08	448	1.7268e-07	681	4.37393e-08	914	2.82903e-08
216	1.92502e-08	449	2.94979	682	4.52816e-08	915	5.02608e-08
217	18.466	450	1.055e-08	683	9.63688e-08	916	1.28352e-08
218	85.3915	451	1.92705e-08	684	6.1303e-08	917	1.55777e-08
219	48.0768	452	1.0629e-08	685	3.76734e-08	918	1.64948e-08
220	9.20391e-09	453	1.43087e-08	686	4.72628e-08	919	5.05662e-08
221	6.67695e-09	454	2.81716	687	3.27956	920	5.05662e-08
222	1.60233e-08	455	1.46738e-06	688	5.28699e-08	921	1.58743e-08
223	8.08041e-09	456	1.21587e-08	689	4.98319e-08	922	1.36395e-08
224	1.30634e-07	457	3.52278e-08	690	1.89477e-08	923	3.94626e-08
225	1.69851e-08	458	2.73913e-08	691	5.39992e-09	924	1.3901e-07
226	13.4811	459	5.78015e-08	692	6.6157e-09	925	2.36461e-08
227	21.847	460	6.97589e-08	693	2.23245e-08	926	32.7848
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229	5.71778e-09	462	1.85802e-08	695	1.54787e-08	928	9.78166e-09
230	6.08565e-09	463	3.24946e-08	696	1.2899e-08	929	1.61469e-08
231	9.02116e-09	464	3.06425e-08	697	4.29067e-08	930	10.4218

232	6.01545e-09	465	14.7284	698	4.65553
233	1.36818e-07	466	4.40484e-08	699	25.3571

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