

Embedded Domain Specific Languages in Idris

Lecture 3: State, Side Effects and Resources

Edwin Brady (ecb10@st-andrews.ac.uk)
University of St Andrews, Scotland, UK
[@edwinbrady](https://twitter.com/edwinbrady)

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An Effectful Problem (Haskell)

Evaluator

```
data Expr = Val Int | Add Expr Expr
```

An Effective Problem (Haskell)

Evaluator

```
data Expr = Val Int | Add Expr Expr
```

```
eval :: Expr -> Int
```

```
eval (Val x) = x
```

```
eval (Add x y) = eval x + eval y
```

An Effectful Problem (Haskell)

Evaluator with variables

```
data Expr = Val Int | Add Expr Expr  
          | Var String
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type Env = [(String, Int)]
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eval :: Expr -> ReaderT Env Maybe Int
```

Evaluator with variables

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data Expr = Val Int | Add Expr Expr  
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```
type Env = [(String, Int)]
```

```
eval :: Expr -> ReaderT Env Maybe Int
```

```
eval (Val n)    = return n
```

```
eval (Add x y) = liftM2 (+) (eval x) (eval y)
```

```
eval (Var x)    = do env <- ask  
                  val <- lift (lookup x env)  
                  return val
```

An Effectful Problem (Haskell)

Evaluator with variables and random numbers

```
data Expr = Val Int | Add Expr Expr  
         | Var String  
         | Random Int
```


An Effective Problem (Haskell)

Evaluator with variables and random numbers

```
data Expr = Val Int | Add Expr Expr  
          | Var String  
          | Random Int
```

```
eval :: RandomGen g =>  
      Expr -> RandT g (ReaderT Env Maybe) Int
```

An Effectful Problem (Haskell)

Evaluator with variables and random numbers

```
data Expr = Val Int | Add Expr Expr
          | Var String
          | Random Int

eval :: RandomGen g =>
      Expr -> RandT g (ReaderT Env Maybe) Int
...
eval (Var x) = do env <- lift ask
                  val <- lift (lift (lookup x env))
                  return val
eval (Random x) = do val <- getRandomR (0, x)
                     return val
```

Challenge — write the following:

```
dropReader :: RandomGen g =>  
    RandT g Maybe a ->  
    RandT g (ReaderT Env Maybe) a
```

```
commute :: RandomGen g =>  
    ReaderT (RandT g Maybe) a ->  
    RandT g (ReaderT Env Maybe) a
```

An Effectful Problem (Idris)

Instead, we could capture everything in one evaluation monad:

Eval monad

```
EvalState : Type
```

```
EvalState = (Int, List (String, Int))
```

```
data Eval a
```

```
  = MkEval (EvalState -> Maybe (a, EvalState))
```

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We make `Eval` an instance of `Monad` (for `do` notation) and `Applicative` (for idiom brackets)

Eval operations

```
rndInt : Int -> Int -> Eval Int  
get    : Eval EvalState  
put    : EvalState -> Eval ()
```

An Effectful Problem (Idris)

Evaluator

```
eval : Expr -> Eval Int
eval (Val i) = return i
eval (Var x) = do (seed, env) <- get
                  lift (lookup x env)
eval (Add x y) = [| eval x + eval y |]
eval (Random upper) = do val <- rndInt 0 upper
                        return val
```

Neither solution is satisfying!

- Composing monads with transformers becomes hard to manage
 - Order matters, but our effects are largely independent
- Building one special purpose monad limits reuse

Instead:

- We will build an *extensible* embedded domain specific language (EDSL) to capture *algebraic effects*.

The rest of this lecture is about an EDSL, `Effect`. It is in three parts:

- How to *use* effects
- How to *implement* new effects
- How `Effect` works

Effectful programs

```
data EffM : (m : Type -> Type) -> (res : Type) ->  
    (in_effects : List EFFECT) ->  
    (out_effects : res -> List EFFECT) ->  
    Type
```

Effectful programs

```
data EffM : (m : Type -> Type) -> (res : Type) ->  
    (in_effects : List EFFECT) ->  
    (out_effects : res -> List EFFECT) ->  
    Type
```

Composing programs

```
(>>=) : EffM m res es es' ->  
    ((x : res) -> EffM m b (es' x) es'') ->  
    EffM m b es es''
```

```
get   :      EffM m t  [STATE t] (\x : t => [STATE t])
put   : t -> EffM m ()  [STATE t] (\x : () => [STATE t])

putM  : t' -> EffM m ()  [STATE t]
                                   (\x : () => [STATE t'])
```

```
get   :      Eff t [STATE t]
put   : t -> Eff () [STATE t]

putM  : t' -> Eff () [STATE t] [STATE t']
```

Combining effects

```
inc : Eff () [STDIO, STATE Nat]
inc = do x <- get
        putStrLn ("Old value " ++ show x)
        put (x + 1)
```

Labelling effects

```
sumStates : Eff Nat ['xval :: STATE Nat,  
                    'yval :: STATE Nat]  
sumStates = do x <- 'xval :- get  
              y <- 'yval :- get  
              return (x + y)
```

Running Effectful Programs

```
run : Applicative m => {auto env : Env m xs} ->
    (prog : EffM m a xs xs') -> m a
runPure : {auto env : Env id xs} ->
    (prog : Eff id a xs xs') -> a
```




Demonstration: An Effectful Evaluator

Effect Signatures

```
Effect : Type
Effect = (t : Type) -> (res : Type) ->
          (res' : t -> Type) -> Type
```

```
data State : Effect where
  Get :      State a a (const a)
  Put : b -> State () a (const b)
```

```
STATE : Type -> EFFECT
STATE t = MkEff t State
```

```
Effect : Type
Effect = (t : Type) -> (res : Type) ->
          (res' : t -> Type) -> Type
```

```
data State : Effect where
  Get :      sig State a  a
  Put : b -> sig State () a b
```

```
STATE : Type -> EFFECT
STATE t = MkEff t State
```

```
data StdIO : Effect where
  PutStr  : String -> sig StdIO ()
  GetStr  :          sig StdIO String
  PutCh   : Char ->   sig StdIO ()
  GetCh   :          sig StdIO Char
```

```
STDIO : EFFECT
STDIO = MkEff () StdIO
```

Handlers

```
class Handler (e : Effect) (m : Type -> Type) where
  covering
  handle : (r : res) -> (eff : e t res resk) ->
    (k : ((x : t) -> resk x -> m a)) -> m a
```

Example Instances

```
instance Handler State m
instance Handler StdIO IO
instance Handler StdIO (List String ->
  (a, List String))
```

State

```
instance Handler State m where  
  handle st Get      k = k st st  
  handle st (Put n) k = k () n
```

State

```
instance Handler State m where
  handle st Get      k = k st st
  handle st (Put n) k = k () n
```

StdIO

```
instance Handler StdIO IO where
  handle () (PutStr s) k = do putStr s; k () ()
  handle () GetStr      k = do x <- getLine; k x ()
  handle () (PutCh c)   k = do putChar c; k () ()
  handle () GetCh       k = do x <- getChar; k x ()
```



Demonstration: Dependent Effects

Why are we interested in dependent types?

- *Safety*
 - Programs checked against precise specifications

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- *Genericity*
 - e.g. program generation

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 - Type system should be *helping*, not telling you off!
- *Genericity*
 - e.g. program generation
- *Efficiency*
 - More precise type information should help the compiler
 - *Partial evaluation*, *erasure*.

Dependent types are an active research topic, and we're having lots of fun. Some things we've been working on:

- Concurrency (e.g. verify absence of deadlock)
- Network transport protocols
- Packet formats
- Type-safe web applications
- Scientific programming
- ...