

**Introduction to Data Science****Assignment#5****Sentences:**

- sunshine state enjoy sunshine
- brown fox jump high, brown fox run
- sunshine state fox run fast

**Bag Of Words:**

	Sunshine	State	Enjoy	Brown	Fox	Jump	High	,	Run	fast	Total length
S1	2	1	1	0	0	0	0	0	0	0	4
S2	0	0	0	2	2	1	1	1	1	0	8
S3	1	1	0	0	1	0	0	0	1	1	5

**Term Frequencies:**

	Sunshine	State	Enjoy	Brown	Fox	Jump	High	,	Run	fast
S1	1/2	1/4	1/4	0	0	0	0	0	0	0
S2	0	0	0	1/4	1/4	1/8	1/8	1/8	1/8	0
S3	1/5	1/5	0	0	1/5	0	0	0	1/5	1/5

**Inverse Document Frequencies:**

$$\text{Idf}(\text{'sunshine'}) = \log(3/2) = 0.1760$$

$$\text{Idf}(\text{'state'}) = \log(3/2) = 0.1760$$

$$\text{Idf}(\text{'enjoy'}) = \log(3/1) = 0.4771$$

$$\text{Idf}(\text{'brown'}) = \log(3/1) = 0.4771$$

$$\text{Idf}(\text{'fox'}) = \log(3/2) = 0.1760$$

$$\text{Idf}(\text{'jump'}) = \log(3/1) = 0.4771$$

$$\text{Idf}(\text{'high'}) = \log(3/1) = 0.4771$$

$$\text{Idf}(\text{','}) = \log(3/1) = 0.4771$$

$$\text{Idf}(\text{'run'}) = \log(3/2) = 0.1760$$

$$\text{Idf}(\text{'fast'}) = \log(3/1) = 0.4771$$

	Sunshine	State	Enjoy	Brown	Fox	Jump	High	,	Run	fast
IDF	0.1760	0.1760	0.4771	0.4771	0.1760	0.4771	0.4771	0.4771	0.1760	0.4771

## TF-IDF:

### S1:

$\text{Idf}(\text{'sunshine'}) = 0.1760 \times 1/2 = 0.088$

$\text{Idf}(\text{'state'}) = 0.1760 \times 1/4 = 0.044$

$\text{Idf}(\text{'enjoy'}) = 0.4771 \times 1/4 = 0.044$

$\text{Idf}(\text{'brown'}) = 0.4771 \times 0 = 0$

$\text{Idf}(\text{'fox'}) = 0.1760 \times 0 = 0$

$\text{Idf}(\text{'jump'}) = 0.4771 \times 0 = 0$

$\text{Idf}(\text{'high'}) = 0.4771 \times 0 = 0$

$\text{Idf}(\text{' ,'}) = 0.4771 \times 0 = 0$

$\text{Idf}(\text{'run'}) = 0.1760 \times 0 = 0$

$\text{Idf}(\text{'fast'}) = 0.4771 \times 0 = 0$

### S2:

$\text{Idf}(\text{'sunshine'}) = 0.1760 \times 0 = 0$

$\text{Idf}(\text{'state'}) = 0.1760 \times 0 = 0$

$\text{Idf}(\text{'enjoy'}) = 0.4771 \times 0 = 0$

$\text{Idf}(\text{'brown'}) = 0.4771 \times 1/4 = 0.1192$

$\text{Idf}(\text{'fox'}) = 0.1760 \times 1/4 = 0.044$

$\text{Idf}(\text{'jump'}) = 0.4771 \times 1/8 = 0.0596$

$\text{Idf}(\text{'high'}) = 0.4771 \times 1/8 = 0.0596$

$\text{Idf}(\text{' ,'}) = 0.4771 \times 1/8 = 0.0596$

$\text{Idf}(\text{'run'}) = 0.1760 \times 1/8 = 0.022$

$\text{Idf}(\text{'fast'}) = 0.4771 \times 0 = 0$

### S3:

$\text{Idf}(\text{'sunshine'}) = 0.1760 \times 1/5 = 0.0352$

$\text{Idf}(\text{'state'}) = 0.1760 \times 1/5 = 0.0352$

$\text{Idf}(\text{'enjoy'}) = 0.4771 \times 0 = 0$

$\text{Idf}(\text{'brown'}) = 0.4771 \times 0 = 0$

$\text{Idf}(\text{'fox'}) = 0.1760 \times 1/5 = 0.0352$

$\text{Idf('jump')} = 0.4771 \times 0 = 0$

$\text{Idf('high')} = 0.4771 \times 0 = 0$

$\text{Idf(',')} = 0.4771 \times 0 = 0$

$\text{Idf('run')} = 0.1760 \times 1/5 = 0.0352$

$\text{Idf('fast')} = 0.4771 \times 1/5 = 0.0954$

	Sunshine	State	Enjoy	Brown	Fox	Jump	High	,	Run	fast
Idf(S1)	0.088	0.044	0.044	0	0	0	0	0	0	0
Idf(S2)	0	0	0	0.1192	0.044	0.0596	0.0596	0.0596	0.022	0
Idf(S3)	0.0352	0.0352	0	0	0.0352	0	0	0	0.0352	0.0954

## Cosine Similarity Between S1 and S3:

$\text{Cos}(S1, S3) = S1 \cdot S3 / |S1| |S3|$

**Taking Bag of Words Vector:**

$S1 = [2, 1, 1, 0, 0, 0, 0, 0, 0]$

$S3 = [1, 1, 0, 0, 1, 0, 0, 0, 1, 1]$

$S1 \cdot S3 = 2 \times 1 + 1 \times 1 + 1 \times 0 + 0 \times 0 + 0 \times 1 + 0 \times 0 + 0 \times 0 + 0 \times 0 + 0 \times 1 + 0 \times 1 = 3$

$|S1| = (2^2 + 1^2 + 1^2 + 0^2 + 0^2 + 0^2 + 0^2 + 0^2 + 0^2 + 0^2)^{0.5} = 2.4494$

$|S2| = (1^2 + 1^2 + 0^2 + 0^2 + 1^2 + 0^2 + 0^2 + 0^2 + 1^2 + 1^2)^{0.5} = 2.2360$

$\text{Cos}(S1, S3) = 3 / (2.4494 \times 2.2360)$

$\text{Cos}(S1, S3) = 3 / 5.4768$

$\text{Cos}(S1, S3) = 0.5477$