

1. Single-Point Crossover:

- **Concept:** A single crossover point is randomly chosen on the parent chromosomes. The segments beyond that point are swapped between the parents to create offspring.
- **Example:**
 - Parent 1: 01001 | 10110
 - Parent 2: 10111 | 00001
 - Crossover Point: After the 5th bit
 - Offspring 1: 01001 | 00001 (inherits first 5 bits from parent 1 and last 5 bits from parent 2)
 - Offspring 2: 10111 | 10110 (inherits first 5 bits from parent 2 and last 5 bits from parent 1)

2. Two-Point Crossover:

- **Concept:** Similar to single-point crossover, but two crossover points are chosen, and the segment between those points is swapped.
- **Example:**
 - Parent 1: 01001 | 101 | 10
 - Parent 2: 10111 | 000 | 01
 - Crossover Points: After 5th and 8th bits
 - Offspring 1: 01001 | 000 | 10 (inherits first 5 bits and last 2 bits from parent 1, middle segment from parent 2)
 - Offspring 2: 10111 | 101 | 01 (inherits first 5 bits and last 2 bits from parent 2, middle segment from parent 1)

3. Uniform Crossover:

- **Concept:** Each gene (bit) is chosen independently with a probability (usually 50%) to be inherited from one parent. This creates a more diverse offspring with a mix of genes from both parents.
- **Example:**
 - Parent 1: 0 1 0 0 1
 - Parent 2: 1 0 1 1 0
 - Crossover Probability (coin toss): Heads (inherit from parent 1), Tails (inherit from parent 2)
 - Possible Offspring 1: 1 1 0 0 1 (3 genes from parent 1, 2 genes from parent 2)
 - Possible Offspring 2 (different coin toss outcomes): 0 0 1 1 0 (2 genes from parent 1, 3 genes from parent 2)

4. K-Point Crossover:

- **Concept:** A generalization of two-point crossover. k crossover points are chosen, and the segments between these points are swapped alternately between parents.
- **Example:**

- Similar to two-point crossover, but with additional crossover points. The process follows the same principle of swapping segments based on the chosen points.

5. Ordered Crossover (OX):

- **Concept:** This crossover is particularly useful for problems where the order of elements is important (e.g., scheduling tasks). It ensures that the relative order of elements is preserved in the offspring to a certain extent.
- **Example:**
 - Parent 1: [1, 2, 3, 4, 5]
 - Parent 2: [4, 5, 1, 2, 3]
 - Crossover Points: Randomly chosen (e.g., 2nd and 4th elements)
 - Offspring 1: [**2, 3, 1, **4, 5] (Inherits the order of elements 2, 3 from parent 1, then inserts remaining elements from parent 2 while maintaining their relative order)