

Introduction to Recursion

Any function which calls itself is called recursion. **A recursive method solves a problem by calling a copy of itself to work on a smaller problem.** Each time a function calls itself with a slightly simpler version of the original problem. This sequence of smaller problems must eventually converge on a base case.

Working of recursion

We can define the steps of the recursive approach by summarizing the above three steps:

- **Base case:** A recursive function must have a terminating condition at which the process will stop calling itself. Such a case is known as the base case. In the absence of a base case, it will keep calling itself and get stuck in an infinite loop. Soon, the recursion depth* will be exceeded and it will throw an error.
- **Recursive call (Smaller problem):** The recursive function will invoke itself on a smaller version of the main problem. We need to be careful while writing this step as it is crucial to correctly figure out what your smaller problem is.
- **Self-work :** Generally, we perform a calculation step in each recursive call. We can achieve this calculation step before or after the recursive call depending upon the nature of the problem.

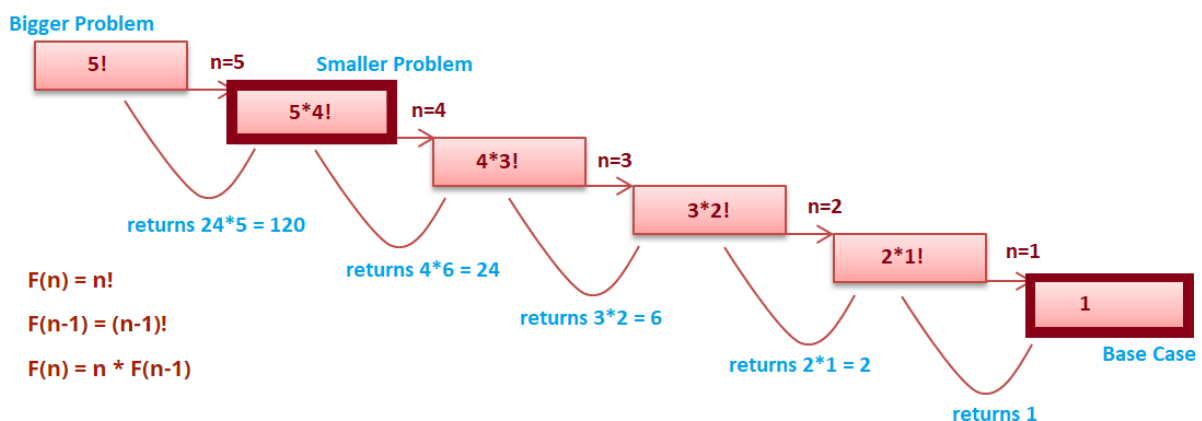
Note*: Recursion uses an in-built stack that stores recursive calls. Hence, the number of recursive calls must be as small as possible to avoid memory-overflow. If the number of recursion calls exceeded the maximum permissible amount, the **recursion depth*** will be exceeded. This condition is called **stack overflow**.

Now, let us see how to solve a few common problems using Recursion.

Problem Statement - Find Factorial of a number n.

Factorial of any number n is defined as $n! = n * (n-1) * (n-2) * \dots * 1$. Ex: $5! = 5 * 4 * 3 * 2 * 1 = 120$;

Let $n = 5$;



In recursion, the idea is that we represent a problem in terms of smaller problems. We know that $5! = 5 * 4!$. Let's assume that recursion will give us an answer of $4!$. Now to get the solution to our problem will become $5 * (\text{the answer of the recursive call})$.

Similarly, when we give a recursive call for $4!$; recursion will give us an answer of $3!$. Since the same work is done in all these steps we write only one function and give it a call recursively. Now, what if there is no base case? Let's say $1!$ Will give a call to $0!$; $0!$ will give a call to $-1!$ (doesn't exist) and so on. Soon the function call stack will be full of method calls and give an error **Stack Overflow**. To avoid this we need a base case. So in the base case, we put our own solution to one of the smaller problems.

```
function factorial(n)
    // base case
    if n equals 0
        return 1
    // getting answer of the smaller problem
    recursionResult = factorial(n-1)
    // self work
    ans = n * recursionResult
    return ans
```

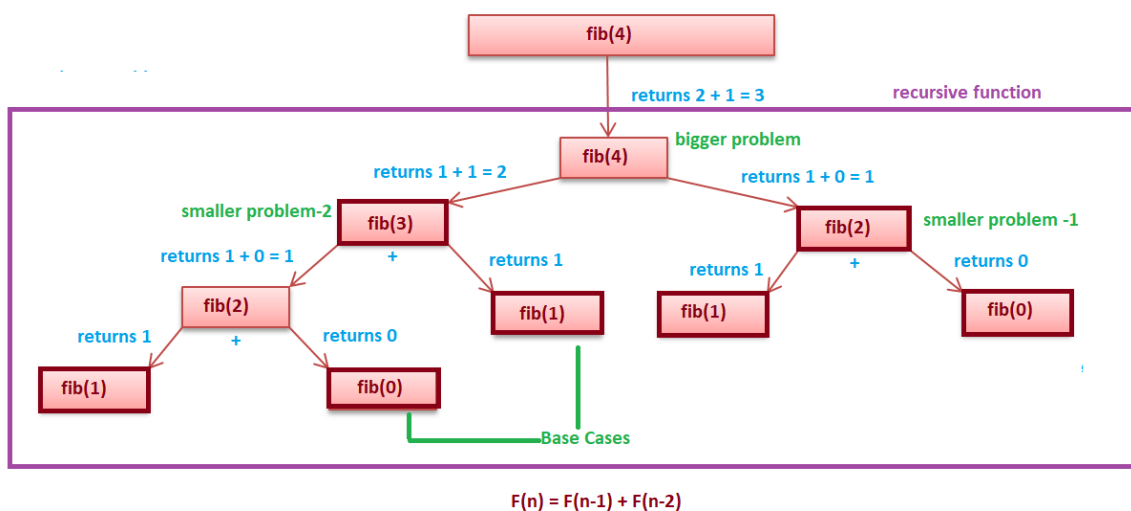
Problem Statement - Find nth fibonacci.

We know that Fibonacci numbers are defined as follows

fib(n) = n for $n \leq 1$

fib(n) = fib(n - 1) + fib(n - 2) otherwise

Let $n = 4$



As you can see from the above fig and recursive equation that the bigger problem is dependent on 2 smaller problems.

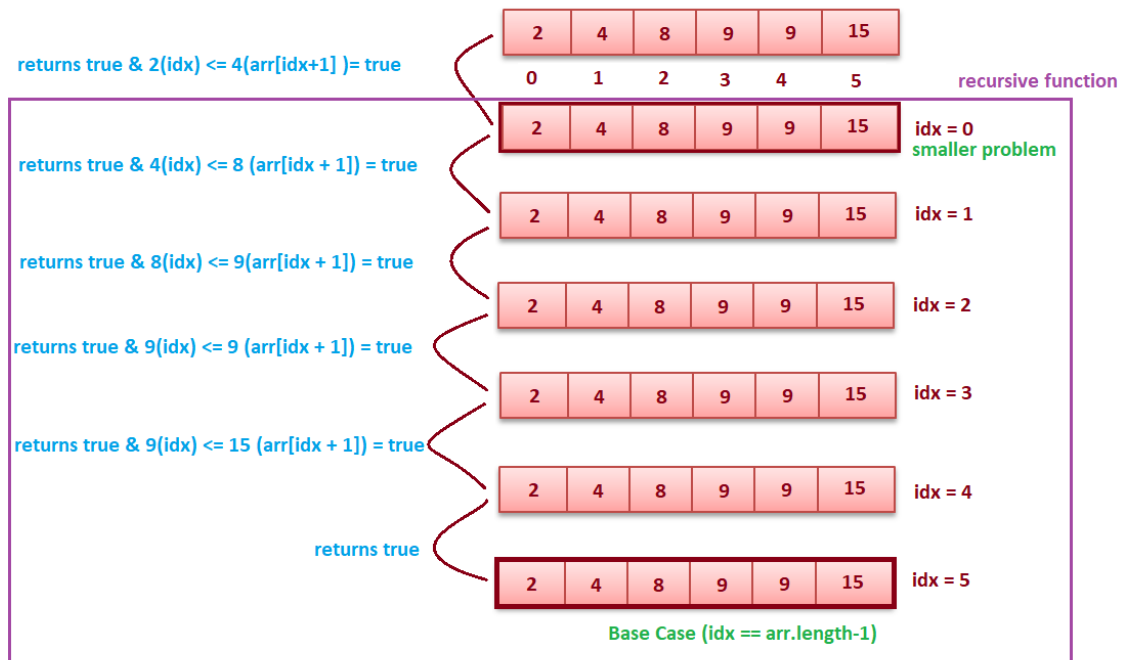
Depending upon the question, the bigger problem can depend on N number of smaller problems.

```
function fibonacci(n)
    // base case
    if n equals 1 OR 0
        return n
    // getting answer of the smaller problem
    recursionResult1 = fibonacci(n - 1)
    recursionResult2 = fibonacci(n - 2)
    // self work
    ans = recursionResult1 + recursionResult2
    return ans
```

Problem Statement - Check if an array is sorted

For example:

- If the array is {2, 4, 8, 9, 9, 15}, then the output should be **true**.
- If the array is {5, 8, 2, 9, 3}, then the output should be **false**.



```
function isArraySorted(arr, idx) // 0 is passed in idx
// base case
if idx equals arr.length - 1
    return true
// getting answer of the smaller problem
recursionResult = isArraySorted(arr, idx+1)

// self work
ans = recursionResult & arr[idx] <= arr[idx+1]
return ans
```