

✓ **Congratulations! You passed!**

Grade received **80%** To pass 80% or higher

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1. Consider two sets of samples drawn from the same population that are randomly selected. Set X has a sample size = 10, and set Y has a sample size = 100. Which of the following statements is accurate about the confidence interval for the mean of the samples?

1 / 1 point

- ☒ The confidence interval for set X is **larger** than the confidence interval for set Y.
- ☐ The confidence interval for set X is **smaller** than the confidence interval for set Y.
- ☐ The confidence interval for set X **equals** the confidence interval for set Y.
- ☐ There isn't enough information to answer the question.

✓ **Correct**

Confidence interval estimates the range within a population parameter, in this case, the population mean. Since set X has a smaller sample size, the sample distribution gets further away from the normal distribution, and the standard deviation is larger. With a larger standard deviation, this results in a larger confidence interval.

2. Suppose you have a sample of 100 heights of individuals from a specific population. Assume the **population standard deviation** is 1 cm, and the **sample mean** is 175cm from a **random sample** of 100 individuals. What expression describes the margin of error for a confidence level of 99%?

0 / 1 point

- ☐ $\approx 0.01 \cdot \frac{1}{10}$
- ☐ $\approx 0.005 \cdot \frac{1}{100}$
- ☐ $\approx 0.005 \cdot \frac{1}{10}$
- ☒ $\approx 0.1 \cdot \frac{1}{100}$

✗ **Incorrect**

Not quite. The formula for the margin of error is $z_{\alpha/2} \cdot \frac{\sigma}{\sqrt{n}}$.

3. To calculate a confidence interval for the **mean** of a population, what assumptions must be made? **Select all that apply.**

1 / 1 point

☒ The sample is a random sample.

✓ **Correct**

A random sample is crucial for a reliable confidence interval for the population mean as it ensures representativeness. Random sampling provides an equal chance for each population member to be included, reducing bias and enhancing

☐ The population must follow a normal distribution.

☒ The sample size must be big enough (usually over 30).

✓ **Correct**

The Central Limit Theorem says the average sample mean **converges to** a normal distribution. It means that the bigger the sample, the closer it is to a normal, so we must ensure that there are enough points for this approximation to be good enough.

☐ The sample must have a mean = 0 and a standard deviation = 1.

4. You have a sample size of 20 from a population with unknown mean and standard deviation. You measured that the **sample mean** $\bar{X} = 50$ and the **sample standard deviation** is $s = 10$. A confidence interval of 95% of confidence level is given by:

1 / 1 point

Hint: $t_{0.475} = 2.093$

☐ (48.95, 51.05)

☒ (45.32, 54.68)

☐ (45.2, 54.8)

☐ (48.9, 51.1)

✓ **Correct**

5. A manufacturing company takes a sample of 100 items in its product warehouse and determines that 22% of the sample contains a defect. Calculate the **population margin of error** with a 95% confidence interval.

1 / 1 point

Hint: $z_{\alpha/2} = 1.96$

☐ 0.0336

☒ 0.0812

☐ 0.0919

☐ 0.3363

✓ **Correct**

When calculating the confidence interval for proportions, the formula is

$$\text{margin of error} = z_{\alpha/2} \cdot \sqrt{\frac{\hat{p}(1 - \hat{p})}{n}}$$