

ASSIGNMENT -13

18K41A0482

Let us consider a sample dataset have one input (x_i^a) and output (y_i^a) and number of samples 4. Develop a Simple linear regression model using ADAGRAD Optimizer

Sample (i)	x_i^a	y_i^a
1	0.2	3.9
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

Do manual calculations for 2 iterations with first 2 samples.

Step 1: $[x, y]$, epochs = 2, $m=1$, $c=-1$, $\epsilon_m = G_{ic} = 0$,
 $\eta = 0.1 \cdot \epsilon = 10^{-8}$

Step 2: iter = 1

Step 3: Sample = 1

Step 4: $g_m = (3.9 - (1)(0.2) + 1) \cdot 0.2$
 $= -0.84$

$g_c = -(3.9 - (1)(0.2) + 1)$
 $= -4.2$

Step 5: $G_m = 0 + (-0.84)^2 = 0.7056$
 $G_c = 0 + (-4.2)^2 = 17.64$

$$\text{Step 6: } \Delta m = \frac{-\eta}{\sqrt{61m + \epsilon}} g_m = \frac{-0.1}{\sqrt{0.7056 + 10^8}} \times 0.8 = 0.09$$

$$\Delta c = \frac{-(0.1)}{\sqrt{17.64 + 10^8}} \times 4.2 = 0.09$$

$$\text{Step 7: } m = m + \Delta m = 1 + 0.09 = 1.09$$

$$c = c + \Delta c = -1 + 0.09 = -0.91$$

$$\text{Step 8: } \text{Sample} = \text{Sample} + 1 = 1 + 1 = 2$$

$$\text{Step 9: } \text{if (sample} > \text{ns) go to step 10}$$

$$2 > 2$$

else : step 4

$$\text{Step 4: } g_m = -(3.5 - (1.09)(0.4) + 0.91)0.4 = -1.7$$

$$g_c = -(3.84 - (1.08)(0.4) + 0.91) = -4.27$$

$$\text{Step 5: } \epsilon_m = 0.7056 + (-1.7)^2 = 3.54$$

$$\epsilon_c = 17.64 + (-4.27)^2 = 35.57$$

$$\text{Step 6: } \Delta m = \frac{-0.1}{\sqrt{3.59 + 10^8}} \times -1.7 = 0.08$$

$$\Delta c = \frac{-0.1}{\sqrt{35.87 + 10^8}} \times -4.27 = 0.07$$

$$\text{Step 7: } m = m + \Delta m = 1.09 + 0.08 = 1.17$$

$$c = c + \Delta c = -0.91 + 0.07 = -0.84$$

Step 8: sample + 1 $\Rightarrow 2 + 1 = 3$

Step 9: if (sample > ns) goto ⑩

else: goto ④

Step 10: iter = iter + 1 $\Rightarrow 1 + 1 = 2$

Step 11: if (iter > epochs) goto ⑫

2 > 2

else goto step ②

Step 3: sample = 1

Step 4: $g_m = (-2.4 - (1.17)(0.2) + 0.84) 0.2$

$$= -0.80$$

$$g_c = -((-2.4 - (1.17)(0.2) + 0.84)$$

$$= -4.0$$

$$\text{Step 5: } \epsilon_m = 3.59 + (-0.80)^2 = 4.23$$

$$\epsilon_c = 35.89 + (-4.0)^2 = 51.89$$

$$\text{Step 6: } \Delta m = \frac{-0.1}{\sqrt{4.23 + 10^{-2}}} \times 0.80 = 0.038$$

$$\Delta c = \frac{-0.1}{\sqrt{51.89 + 10^{-8}}} \times -4.0 = 0.05$$

$$\text{Step 7: } m = m + \Delta m = 0.038 + 1.17 = 1.208$$

$$c = c + \Delta c = -0.84 + 0.05 = -0.79$$

Step 8: if (sample > ns) goto step ⑩

else

goto step ④

Step 4: $g_m = -(3.8 - (1.20)(0.4) + 0.79) \times 0.4 = -1.64$

$g_c = -(3.8 - (-1.20)(0.4) + 0.79) = -4.11$

Step 5: $\epsilon_m = 4.23 + (-1.64)^2 = 6.9$

$\epsilon_c = 51.89 + (-4.11)^2 = 68.7$

Step 6: $\Delta m = \frac{-0.1}{\sqrt{6.9 + 10^{-8}}} \times -1.64 = 0.06$

$\Delta c = \frac{-0.1}{\sqrt{68.7 + 10^{-8}}} \times -4.11 = 0.04$

Step 7: $m = m + \Delta m = 1.208 + 0.06$
 $= 1.26$

$c = c + \Delta c = -0.79 + 0.04$
 $= -0.75$

Step 8: $\text{sample} = \text{sample} + 1 = 3$

Step 9: if (sample > ns) go to step ⑩

$3 > 2$

else: go to ④

Step 10: $\text{iter} + 1 = 1 \Rightarrow 2 + 1 = 3$

Step 11: if (iter > epochs) goto ⑫

else
goto ③

Step 12: $m = 1.76$

$c = -0.75$