$$\overline{\overline{\overline{A}A}AAA} = \overline{\overline{\overline{0}A}AA} = \overline{\overline{\overline{A}A}A} = \overline{\overline{\overline{0}A}} = \overline{\overline{A}}$$
(1)

$$(A + \overline{B}).(\overline{A.C}).(\overline{A.\overline{C}}) = (A + \overline{B}).\overline{A.C + A.\overline{C}} = (A + \overline{B}).\overline{A.(C + \overline{C})} = \overline{A}.(A + \overline{B}) = 0 + \overline{A}.\overline{B} = \overline{A + B}$$
(2)

$$(A \to W).(B \to S) + (\overline{A} \to S).(\overline{B} \to W) =$$
  
 $(\overline{A} + W).(\overline{B} + S) + (A + S).(B + W) =$ 

$$W.(\overline{B} + S + A + S) + \overline{A}.(\overline{B} + S) + B.(A + S) =$$

$$W.S + W.(A + \overline{B}) + S.(\overline{A} + B) + A.B + \overline{A}.\overline{B} =$$

$$= (***)(A \equiv B) + W.S + W.(A.\overline{B}) + S.(\overline{A}.B)$$
(3)

$$A \to B \to A \to B \to A =$$

$$\overline{A} + B \to A \to B \to A =$$

$$\overline{\overline{A} + B} + A \to B \to A =$$

$$A\overline{B} + A \to B \to A =$$

$$A \to B \to A =$$

$$\overline{A} + B \to A =$$

$$\overline{A} + B \to A =$$

$$\overline{\overline{A} + B} + A =$$

$$(4)$$

$$\overline{AB \to C} \to B + \overline{AC} = AB\overline{C} \to B + \overline{A} + \overline{C} = \overline{AB\overline{C}} + B + \overline{A} + \overline{C} = \overline{A} + \overline{B} + C + B + \overline{A} + \overline{C} = 1$$

$$(5)$$

 $A\overline{B} + A = A$ 

$$(***)\overline{AC} \leftarrow B \to \overline{A} + \overline{C} =$$

$$\overline{(B \to AC).(B \to \overline{A} + \overline{C})} =$$

$$\overline{(B \to AC).(B \to \overline{AC})} =$$

$$\overline{(\overline{B} + AC).(\overline{B} + \overline{AC})} =$$

$$\overline{(\overline{B} + AC.\overline{AC})} = B$$

$$(6)$$