

## Section B (36 marks)

10 (i)

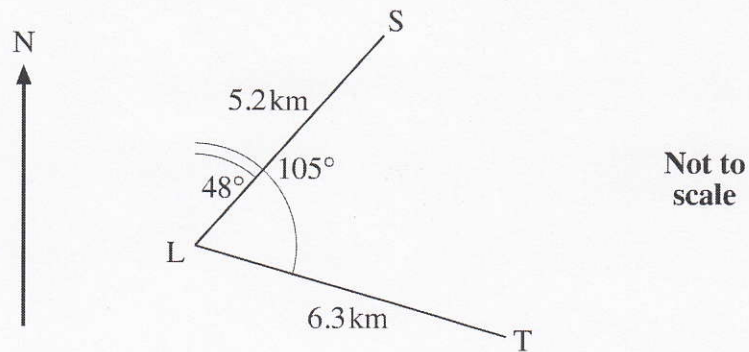


Fig. 10.1

At a certain time, ship S is 5.2 km from lighthouse L on a bearing of  $048^\circ$ . At the same time, ship T is 6.3 km from L on a bearing of  $105^\circ$ , as shown in Fig. 10.1.

For these positions, calculate

(A) the distance between ships S and T, [3]

(B) the bearing of S from T. [3]

(ii)

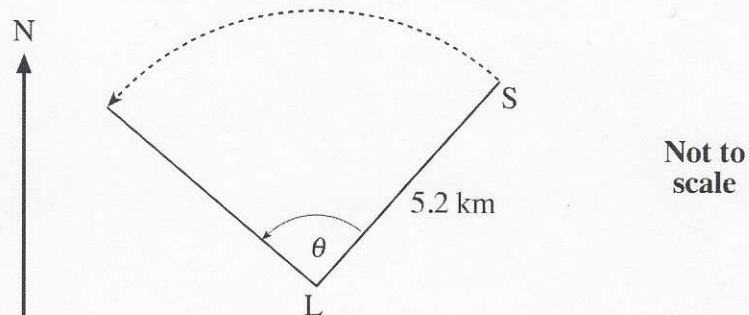


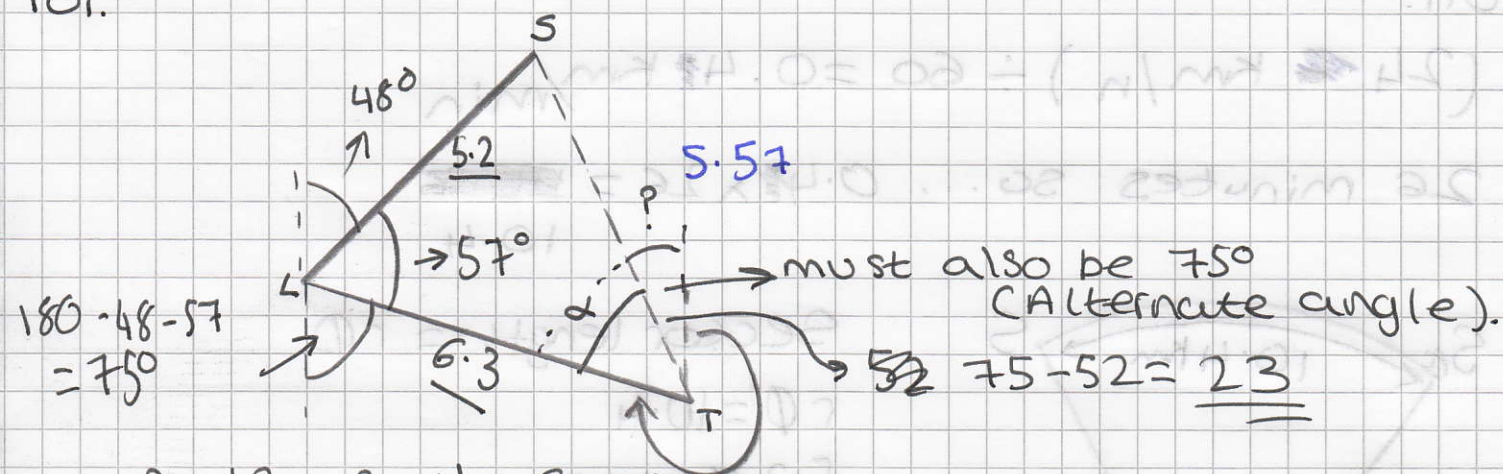
Fig. 10.2

Ship S then travels at  $24 \text{ km h}^{-1}$  anticlockwise along the arc of a circle, keeping 5.2 km from the lighthouse L, as shown in Fig. 10.2.

Find, in radians, the angle  $\theta$  that the line LS has turned through in 26 minutes.

Hence find, in degrees, the bearing of ship S from the lighthouse at this time. [5]

101.



A.  $a^2 = b^2 + c^2 - 2bc \cos A$

$$a^2 = 6.3^2 + 5.2^2 - (2 \times 6.3 \times 5.2) \times \cos(57)$$

$$a^2 = 31.045$$

$$a = \sqrt{31.045} \approx 5.57 \text{ km}$$

B.

$$a^2 = b^2 + c^2 - 2bc \cos A$$

find angle  $\alpha$ 

$$\frac{a^2 - b^2 - c^2}{-2bc} = \cos A = \frac{(5.2^2) - (5.57^2) - (6.3^2)}{(-2 \times 5.57 \times 6.63)}$$

$$\cos A = 0.622309 \dots$$

$$A = \cos^{-1}(0.623 \dots) \approx 51.515^\circ \approx \underline{51.5^\circ}$$

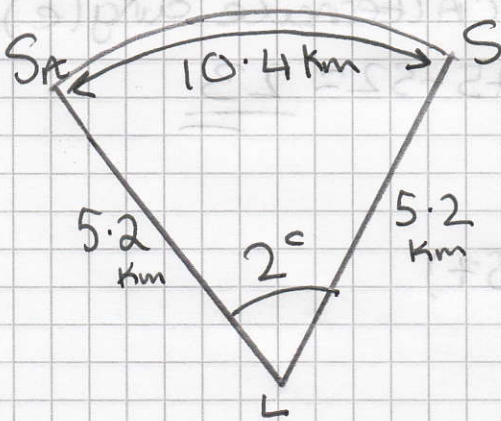
$$\text{Bearing} = 360 - 23^\circ = \underline{337^\circ}$$



10ii.

$$(24 \text{ km/h}) \div 60 = 0.4 \text{ km/min}$$

$$26 \text{ minutes so } \dots 0.4 \times 26 = 10.4$$



$$\text{Sector length} = r\theta$$

$$r\theta = 10.4$$

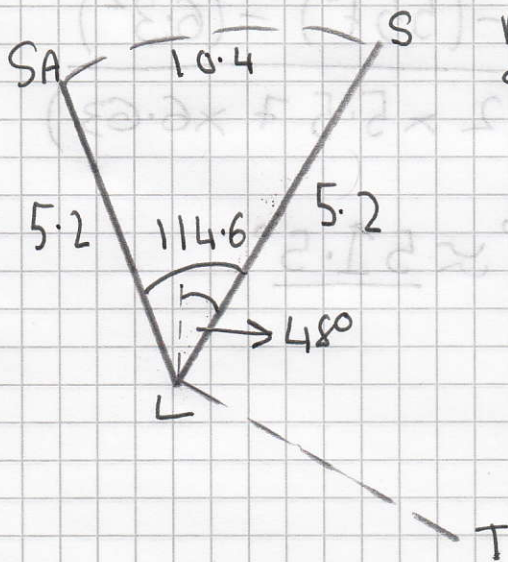
$$5.2\theta = 10.4$$

$$\theta = \frac{10.4}{5.2}$$

$$\theta = 2^\circ$$

Then Convert to degrees for bearing

$$\frac{180}{\pi} \times 2 = 114.6^\circ$$



At this time so ship is at SA

$$114.6 - 48 = 66.6$$

$$360 - 66.6 = 293.4^\circ$$