

Comprehensive Guidelines and Templates for Thesis Writing

Master's Thesis

of
Author

Date of issue:
Date of submission:
Examiner:
Supervisor:

Statutory Declaration

I, Author, hereby affirm that the following Master's thesis has been elaborated solely by myself. No other means and sources except those stated, referenced and acknowledged have been used.

(Author)

Abstract

Contents

Statutory Declaration	iii
Abstract	v
1 List of Notes	1
2 Notes	3
2.1 Base ODE-System	3
2.2 Computational Saving	3
2.3 Implementation Differences	4
2.4 Metrics	4
2.4.1 Kuramoto Parameter	4
2.5 Data	4
2.6 Model	4
3 Introduction	7
4 Preliminaries	9
4.1 Sepsis	9
4.1.1 Sepsis-3 definition	9
4.2 Biology and Cytokine Storms	11
4.3 The need for sepsis prediction	11
4.4 Maybe Treatment	11
5 The Data and Task problems	13
6 Problem definition	15
7 State of the Art	17
7.1 Model Based Methods	17
7.2 Data Based Methods	17
7.2.1 Selected Works	17
8 Dynamic Network Model (DNM)	19
8.1 Description	19
8.1.1 Functional Models	19
8.1.2 Parenchymal	19
8.1.3 Immune System	19
8.1.4 Kuramoto	19
8.2 Implementation	19
8.2.1 Standard	19
8.2.2 Lie	19
9 Latent Dynamics Model	21
9.1 Task - Definition of Ins and Outs	21
9.2 Data	21

9.2.1	MIMIC-III/IV	21
9.2.2	YAIB + (Further) Preprocessing	21
9.2.2.1	ricu-Concepts	21
9.3	Latent Dynamics Model (LDM)	21
9.3.1	The high level ideas	21
9.3.1.1	Representation Learning and Latent Spaces	21
9.3.1.2	Semantics	21
9.3.1.3	Autoregressive Prediction	21
9.3.2	The Lookup (FSQ)	21
9.3.3	Encoder	21
9.3.4	Decoder	21
9.3.5	Introducing time	21
9.3.6	Combining the building blocks	21
9.4	Metrics (How to validate performance?)	21
10	Experimental Results	23
10.1	Metrics	23
10.2	Further Experiments	23
10.2.1	Custom Latent Space	23
10.2.2	SOFA vs Infection	23
11	Conclusion	25
	Bibliography	26

Acronyms Index

TUHH:	Hamburg University of Technology
SOFA:	Sequential Organ Failure Assessment
qSOFA:	Quick Sequential Organ Failure Assessment
ICU:	Intensive Care Unit
EHR:	Electronic Health Record
YAIB:	Yet Another ICU Benchmark
FSQ:	Finite Scalar Quantization
RL:	Reinforcement Learning

1 List of Notes

<input type="checkbox"/>	table for parameters	13
◦		
<input type="checkbox"/>	cite	14
◦		
<input type="checkbox"/>	Entropy, Splay Ratio, MPV Std, Cluster Ratio	14
◦		
<input type="checkbox"/>	table	14
◦		
<input type="checkbox"/>	How to structure the latent space? Binary classification (sepsis, no sepsis) may not provide enough information to accurately structure the latent space. The options : Add more classes like resilient/vulnerable... maybe even the full spectrum? need to be modeled by RIntroduce the time/action component as additional information (like the environment?)	15
◦		
<input type="checkbox"/>	mapping not really clear, which metrics correspond to sofa/infection	15
◦		
<input type="checkbox"/>	YAIB and other resources care about the onset of infection and sepsis . For sepsis this isn't really problematic since we could use the state transitions as indicators. But for the suspected infection it is problematic, maybe use si__upr and si__lwr provided by (https://eth-mds.github.io/ricu/reference/label_si.html). These would be 48h - SI - 24h adapted from , maybe a bit too much.	15
◦		
<input type="checkbox"/>	label	20
◦		
<input type="checkbox"/>	risk increase by classification	20
◦		
<input type="checkbox"/>	dynamic	20
◦		

2 Notes

2.1 Base ODE-System

$$\dot{\varphi}_i^1 = \omega^1 - \frac{1}{N} \sum_{j=1}^N \{ (a_{ij}^1 + \kappa_{ij}^1) \sin(\varphi_i^1 - \varphi_j^1 + \alpha^{11}) \} - \sigma \sin(\varphi_i^1 - \varphi_i^2 + \alpha^{12}) \quad (1.1)$$

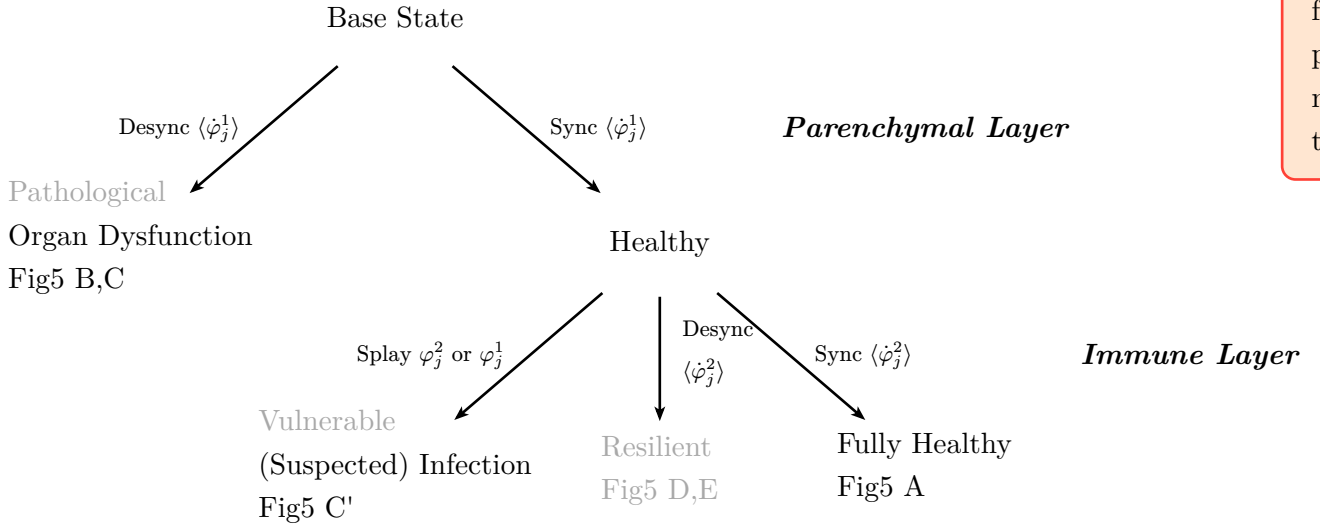
$$\dot{\kappa}_{ij}^1 = -\varepsilon^1 (\kappa_{ij}^1 + \sin(\varphi_i^1 - \varphi_j^1 - \beta)) \quad (1.2)$$

$$\dot{\varphi}_i^2 = \omega^2 - \frac{1}{N} \sum_{j=1}^N \kappa_{ij}^2 \sin(\varphi_i^2 - \varphi_j^2 + \alpha^{22}) - \sigma \sin(\varphi_i^2 - \varphi_i^1 + \alpha^{21}) \quad (1.3)$$

$$\dot{\kappa}_{ij}^2 = -\varepsilon^2 (\kappa_{ij}^2 + \sin(\varphi_i^2 - \varphi_j^2 - \beta)) \quad (1.4)$$

Introduced in [1] and slightly adapted in [2].

table
for
para-
me-
ters



2.2 Computational Saving

For parts in the form of $\sin(\theta_l - \theta_m)$ following [3] one can calculate and cache the terms $\sin(\theta_l), \sin(\theta_m), \cos(\theta_l), \cos(\theta_m)$ in advance:

$$\sin(\theta_l - \theta_m) = \sin(\theta_l) \cos(\theta_m) - \cos(\theta_l) \sin(\theta_m) \quad \forall l, m \in \{1, \dots, N\} \quad (2)$$

so the computational cost for the left-hand side for N oscillators can be reduced from $N(N - 1)$ to $4N$ trigonometric function evaluations, positively impacting the computational efficiency of the whole ODE-system significantly.

2.3 Implementation Differences

- Actual Mean Phase Velocity instead of averaged difference over time.
- +They Calculate the difference wrong since the phase difference should be mod[2π]
- Different solver accuracy, but very similar
- They are not batching the computation

2.4 Metrics

2.4.1 Kuramoto Parameter

Kuramoto Order Parameter

$$R_2^\mu = \frac{1}{N} \left| \sum_j^N e^{i \cdot \varphi_j(t)} \right| \quad \text{with } 0 \leq R_2^\mu \leq 1 \quad (3)$$

cite

$R_2^\mu = 0$ splay-state and $R_2^\mu = 1$ is fully synchronized.

Mean Phase Velocities

$$\langle \varphi^\mu \rangle = \frac{1}{N} \sum_j^N \varphi_j^\mu \quad (4)$$

2.5 Data

MIMIC-3

<https://github.com/alistairewj/sepsis3-mimic/tree/v1.0.0>

2.6 Model

For a general model setup, the latent space $z = (a^1, \sigma, \alpha, \beta, \omega^1, \omega^2, \frac{C}{N}, \varepsilon^1, \varepsilon^2)$ represents the parameter of the dynamic network model, so we have

$$z \in \mathbb{R}^d \quad \text{with } d = 9 \quad (5)$$

As shown in the supplemental material of [2], for example, the parameter α exhibits a π -periodicity, allowing to reduce the effective parameter space by constraining certain parameters with upper and lower bounds. These bounds are omitted here for simplicity but are included in [1]. To further reduce the latent space z , we keep $a^1, \omega^1, \omega^2, \frac{C}{N}, \varepsilon^1$ and ε^2 fixed. The reduced latent space $z' = (\sigma, \alpha, \beta)$:

$$z' \in \mathbb{R}^{d'} \quad \text{with } d' = 3 \quad (6)$$

where both alpha and beta exhibit a periodic behavior Each point in the latent space z_j can be categorized as either of *healthy*, *vulnerable* or *pathological*.

We relate high-dimensional physiological observations (e.g. samples from the MIMIC-III database) to the latent space via:

$$x_j = f(z_j) + \varepsilon \quad (7)$$

En-
tropy,
Splay
Ratio,
MPV
Std,
Clus-
ter
Ratio

table

where f is unknown an unknown function and ε the measurement noise. Note that different observations x_j can be mapped to the same classification, as for the latent space. We define two the two class mappings Q and R :

$$Q(x_j) = c_j = R(z_j) \quad \text{where } x_j = f(z_j) + \varepsilon \quad (8)$$

mapping observations and the latent representation to a shared class label c . To make things more complicated, R does not directly act on z , but rather the metrics derived from the solution to a dynamical system (initial value problem) (Equation 1) parameterized by z . The metrics are detailed in Section 2.4.

In the setting of structured latent variational learning we want to approximate an encoder $q(z|x)$ to infer the latent variables from observed data X and the class.

How to structure the latent space? Binary classification (sepsis, no sepsis) may not provide enough information to accurately structure the latent space. The options:

- Add more classes like resilient/vulnerable... maybe even the full spectrum?
 - need to be modeled by R
- Introduce the time/action component as additional information (like the Reinforcement Learning (RL) environment?)

For the cohort extraction and SOFA calculation I use [4] and [5]. The nice thing is we could interpret larger SOFA scores (> 3) as the vulnerable state introduced by [2]. Increases in SOFA score ≥ 2 could then be used as definition for sepsis.

mapping not really clear, which metrics correspond to sofa/infection

YAIB [5] and other resources care about the “onset” of infection and sepsis [6]. For sepsis this isn’t really problematic since we could use the “state transitions” as indicators. But for the suspected infection it is problematic, maybe use si_upr and si_lwr provided by [4] (https://eth-mds.github.io/ricu/reference/label_si.html^o). These would be 48h - SI - 24h adapted from [7], maybe a bit too much.

3 Introduction

4 Preliminaries

4.1 Sepsis

As the most extreme course of an infectious disease, sepsis poses a serious health threat, with a high mortality rate and frequent long-term consequences for survivors. In 2017, an estimated 48.9 million people worldwide suffered from sepsis and the same year, 11.0 million deaths were associated with sepsis [8]. Untreated, the disease is always fatal and even with successful treatment, around 75% of those affected suffer long-term consequences. Highlighting the importance of early recognition and treatment of infections in patients with pre-existing health conditions. Overall, untreated septic diseases in particular represent an enormous burden on the global healthcare system.

The triggers for sepsis are varied, but almost half of all sepsis-related deaths occur as a secondary complication of an underlying injury or non-communicable, also known as chronic disease [9]. Faster recognition of a septic condition significantly increases the chance of survival [10], it urges to develop accurate and robust detection and prediction methods, i.e. reducing the time to receive the appropriate medical attention.

A most broad definition describes sepsis a host overreaction to an infection causing life-threatening organ dysfunction. There are multiple (now historic) more specific definitions available and sometimes blurry terminology used when dealing with the sepsis and septic shocks. The following chapter Section 4.1.1 gives a more detailed introduction to the most commonly used sepsis definition, which is referred to as Sepsis-3, additionally the chapter provides a short explanation of both the pathology and biology of sepsis

4.1.1 Sepsis-3 definition

Out of the need for an update of an outdated and partly misleading sepsis model a task force led by the “Society of Critical Care Medicine and the European Society of Intensive Care Medicine”, was formed. Their “Third International Consensus Definitions for Sepsis and Septic Shock” [11] from 2016 provides until today the most up to date and most widely used sepsis definition and guidance for sepsis identification.

In general sepsis does not classify as a specific illness, rather a condition of “physiologic, pathologic, and biochemical abnormalities” [11], where the original causes are still uncertain. The Sepsis-3 defines a condition as septic when a patient exhibits an abnormal host reaction against a documented or suspected infection, i.e. an immune system overreaction to some kind of infection or inflammation harmful to the body and organ system.

In clinical practice any patient prescribed with antibiotics or has body fluids sampled for cultivation is characterized with a suspected infection. A responses dysregulation is measured by the change of organ functionality over time. Capturing the Sequential Organ Failure Assessment (SOFA) score [12] is regularly used to evaluate the severity of an illness and helps to guide treatment decisions and predict the risk of mortality outside of a sepsis context. The SOFA score is calculated at least every 24 hours and assess six different organ systems and assigns a score from 0 (normal function) to 4 (high degree of dysfunction) each, as stated in Table 1. While the magnitude or baseline of a patients initials SOFA score captures preexisting organ dysfunction, an increase in SOFA score ≥ 2 between measurements indicates an acute organ dysfunction and a drastic worsening in the patients condition.

CATEGORY	INDICATOR	1	2	3	4
Respiration	PaO ₂ /FiO ₂ [mmHg]	< 400	< 300	< 200	< 100
	Mechanical Ventilation			yes	yes
Coagulation	Platelets [$\times \frac{10^3}{\text{mm}^3}$]	< 150	< 100	< 50	< 20
Liver	Bilirubin [$\frac{\text{mg}}{\text{dl}}$]	1.2-1.9	2.0-5.9	6.0-11.9	> 12.0
Cardiovascular ¹	MAP [mmHg]	< 70			
	or Dopamine		≤ 5	> 5	> 15
	or Dobutamine		any dose		
	or Epinephrine			≤ 0.1	> 0.1
	or Noepinephrine			≤ 0.1	> 0.1
Central Nervous System	Glasgow Coma Score	13-14	10-12	6-9	< 6
Renal	Creatinine [$\frac{\text{mg}}{\text{dl}}$]	1.2-1.9	2.0-3.4	3.5-4.9	> 5.0
	or Urine Output [$\frac{\text{ml}}{\text{day}}$]			< 500	< 200

Also newly introduced in [12] a bedside clinical score termed Quick Sequential Organ Failure Assessment (qSOFA):

- Respiratory rate $\geq 22/\text{min}$
- Altered mentation
- Systolic blood pressure $\leq 100 \text{ mm Hg}$

If a patient fulfills at least two of these criteria have an increased risk of organ failure, but it is not as accurate as the SOFA score and is designed as a fast patient screening tool.

¹Adrenergica agents administered for at least 1h (doses given are in [$\mu\text{g}/\text{kg} \cdot \text{min}$])

4.2 Biology and Cytokine Storms

4.3 The need for sepsis prediction

4.4 Maybe Treatment

The Parenchymal (Equation 1.1[◦] and Equation 1.2[◦]) and Immune (Equation 1.3[◦] and Equation 1.4[◦]) layer and their respective states of the dynamical system naturally are consistent with the two cornerstones of the Sepsis-3 definition [11], i.e. SOFA score and suspicion of an infection.

Healthy \rightarrow sync $\langle \dot{\varphi}_j^1 \rangle$ and $\langle \dot{\varphi}_j^1 \rangle$

SOFA \rightarrow desync $\langle \dot{\varphi}_j^1 \rangle$

Suspected infection \rightarrow splay/desync $\langle \dot{\varphi}_j^2 \rangle$

septic \rightarrow desync $\langle \dot{\varphi}_j^1 \rangle$ and $\langle \dot{\varphi}_j^1 \rangle$

5 The Data and Task problems

6 Problem definition In [13], a survey among clinicians regarding AI-assistance in healthcare, one participant emphasizes that specific vitals signs might not be to be of less importance, rather the change/trend of a patients trajectory. Another piece of finding of the same study was the preference of trajectories over plain event predictions.

7 State of the Art

7.1 Model Based Methods

7.2 Data Based Methods

7.2.1 Selected Works

8 Dynamic Network Model (DNM)

8.1 Description

8.1.1 Functional Models

8.1.2 Parenchymal

8.1.3 Immune System

8.1.4 Kuramoto

8.2 Implementation

8.2.1 Standard

8.2.2 Lie

9 Latent Dynamics Model

9.1 Task - Definition of Ins and Outs

9.2 Data

9.2.1 MIMIC-III/IV

9.2.2 YAIB + (Further) Preprocessing

9.2.2.1 ricu-Concepts

9.3 Latent Dynamics Model (LDM)

9.3.1 The high level ideas

9.3.1.1 Representation Learning and Latent Spaces

9.3.1.2 Semantics

9.3.1.3 Autoregressive Prediction

9.3.2 The Lookup (FSQ)

9.3.3 Encoder

9.3.4 Decoder

9.3.5 Introducing time

9.3.6 Combining the building blocks

9.4 Metrics (How to validate performance?)

10 Experimental Results

10.1 Metrics

10.2 Further Experiments

10.2.1 Custom Latent Space

10.2.2 SOFA vs Infection

11 Conclusion

Bibliography

- [1] J. Sawicki, R. Berner, T. Löser, and E. Schöll, “Modeling Tumor Disease and Sepsis by Networks of Adaptively Coupled Phase Oscillators,” *Frontiers in Network Physiology*, vol. 1, 2022, doi: 10.3389/fnetp.2021.730385[◦].
- [2] R. Berner, J. Sawicki, M. Thiele, T. Löser, and E. Schöll, “Critical Parameters in Dynamic Network Modeling of Sepsis,” *Frontiers in Network Physiology*, vol. 2, 2022, doi: 10.3389/fnetp.2022.904480[◦].
- [3] T. Böhle, C. Kuehn, and M. Thalhaammer, “On the reliable and efficient numerical integration of the Kuramoto model and related dynamical systems on graphs,” *International Journal of Computer Mathematics*, vol. 99, no. 1, pp. 31–57, 2022, doi: 10.1080/00207160.2021.1952997[◦].
- [4] N. Bennett, D. Plečko, I.-F. Ukor, N. Meinshausen, and P. Bühlmann, “ricu: R’s interface to intensive care data,” *GigaScience*, vol. 12, p. giad41, 2023.
- [5] R. van de Water, H. N. A. Schmidt, P. Elbers, P. Thorat, B. Arnrich, and P. Rockenschaub, “Yet Another ICU Benchmark: A Flexible Multi-Center Framework for Clinical ML,” in *The Twelfth International Conference on Learning Representations*, Oct. 2024.
- [6] M. Moor, B. Rieck, M. Horn, C. R. Jutzeler, and K. Borgwardt, “Early Prediction of Sepsis in the ICU Using Machine Learning: A Systematic Review,” *Frontiers in Medicine*, 2021, doi: 10.3389/fmed.2021.607952[◦].
- [7] C. W. Seymour *et al.*, “Assessment of Clinical Criteria for Sepsis: For the Third International Consensus Definitions for Sepsis and Septic Shock (Sepsis-3),” *JAMA*, vol. 315, no. 8, pp. 762–774, 2016, doi: 10.1001/jama.2016.0288[◦].
- [8] K. E. Rudd and et al., “Global, regional, and national sepsis incidence and mortality, 1990–2017: analysis for the Global Burden of Disease Study,” *The Lancet*, vol. 395, no. 10219, pp. 200–211, 2020, doi: 10.1016/S0140-6736(19)32989-7[◦].
- [9] C. Fleischmann-Struzek, D. Schwarzkopf, and K. Reinhart, “Inzidenz der Sepsis in Deutschland und weltweit: Aktueller Wissensstand und Limitationen der Erhebung in Abrechnungsdaten,” *Medizinische Klinik - Intensivmedizin und Notfallmedizin*, vol. 117, no. 4, pp. 264–268, May 2022, doi: 10.1007/s00063-021-00777-5[◦].
- [10] C. W. Seymour *et al.*, “Time to Treatment and Mortality during Mandated Emergency Care for Sepsis,” *The New England Journal of Medicine*, vol. 376, pp. 2235–2244, Jun. 2017, doi: 10.1056/NEJMoa1703058[◦].
- [11] M. Singer *et al.*, “The Third International Consensus Definitions for Sepsis and Septic Shock (Sepsis-3),” *JAMA*, vol. 315, no. 8, pp. 801–810, Feb. 2016, doi: 10.1001/jama.2016.0287[◦].
- [12] J. L. Vincent *et al.*, “The SOFA (Sepsis-related Organ Failure Assessment) score to describe organ dysfunction/failure. On behalf of the Working Group on Sepsis-Related Problems of the European Society of Intensive Care Medicine,” *Intensive care medicine*, vol. 22, no. 7, pp. 707–710, 1996.
- [13] B. Eini-Porat, O. Amir, D. Eytan, and U. Shalit, “Tell me something interesting: Clinical utility of machine learning prediction models in the ICU,” *Journal of Biomedical Informatics*, vol. 132, p. 104107, 2022, doi: 10.1016/j.jbi.2022.104107[◦].