### Tensors Introduction

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### 1 Introduction to Tensor Notes:

A tensor is a container which can house data in N dimensions, along with its linear operations, though there is nuance in what tensors technically are and what we refer to as tensors in practice.

Scalar	Vector	Matrix	Tensor
1	1 2	1       2         3       4	1     2     3     2       1     7     5     4

```
[1]: #Import Tensorflow
import tensorflow as tf
print(tf.__version__)
import numpy
```

2.3.0

vector

# 2 Create tesnors with tf.constant()

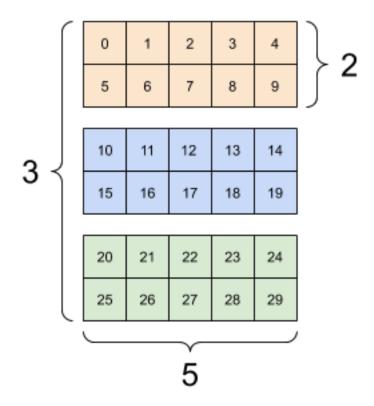
vector = tf.constant([10,10])

```
[2]: scalar = tf.constant(7)
    scalar

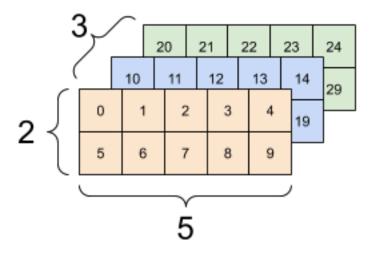
[2]: <tf.Tensor: shape=(), dtype=int32, numpy=7>
[3]: #Check the number of dimensions of tensor using ndim
    scalar.ndim
[3]: 0
[4]: #Create a vector
```

```
[4]: <tf.Tensor: shape=(2,), dtype=int32, numpy=array([10, 10])>
 [5]: vector.ndim
 [5]: 1
 [6]: #Create a matrix
      matrix = tf.constant([[10,7],
                           [7,10]]
                           )
      matrix
 [6]: <tf.Tensor: shape=(2, 2), dtype=int32, numpy=
      array([[10, 7],
             [ 7, 10]])>
 [7]: matrix.ndim
 [7]: 2
     At this point, we can relate that ndim represents the number of elements in the shape tuple
 [8]: #Create another matric
      matrix_2 = tf.constant([[10.,7.],
                              [3.,2.],
                               [1.,2.]],dtype=tf.float16) #Here we use float16 since
      →our numbers are small
      matrix_2
 [8]: <tf.Tensor: shape=(3, 2), dtype=float16, numpy=
      array([[10., 7.],
             [3., 2.],
             [ 1., 2.]], dtype=float16)>
 [9]: matrix_2.ndim
 [9]: 2
[10]: #Create a tensor
      tensor = tf.constant([[[1,2,3],
                            [4,5,6]],
                             [[7,8,9],
                              [10,11,12]],
                             [[13,14,15],
                              [16,17,18]])
      tensor
```

```
[10]: <tf.Tensor: shape=(3, 2, 3), dtype=int32, numpy=
     array([[[ 1, 2, 3],
             [4, 5,
                      6]],
            [[7, 8, 9],
             [10, 11, 12]],
            [[13, 14, 15],
             [16, 17, 18]]])>
[11]: rank_3_tensor = tf.constant([
        [[0, 1, 2, 3, 4],
        [5, 6, 7, 8, 9]],
        [[10, 11, 12, 13, 14],
        [15, 16, 17, 18, 19]],
       [[20, 21, 22, 23, 24],
        [25, 26, 27, 28, 29]],])
     print(rank_3_tensor)
     tf.Tensor(
     [[[0 1 2 3 4]
       [5 6 7 8 9]]
      [[10 11 12 13 14]
       [15 16 17 18 19]]
      [[20 21 22 23 24]
       [25 26 27 28 29]]], shape=(3, 2, 5), dtype=int32)
```



The above example for a 3 dimensional tensor represents: Number of matrices, Number of rows in a matrices and Number of columns in a matrices i.e. Shape = (3,2,5). You can also visualise this as matrices stacked on top of each other to produce a 3D structure as shown below



## 2.1 Summary so far:

- 1. Scalar : Single number
- 2. Vector: A number with both direction and magnitude
- 3. Matrix: A 2 dimensional array of numbers
- 4. Tensor: A n-dimensional array of numbers which can constitude all of the above as well.

## 3 Create tesnors with tf.Variable()

```
[12]: #Create a tensor with tf. Variable and see the difference between tf. constant
      changeable_tensor = tf.Variable([10,10])
      unchageable_tensor = tf.constant([10,10])
[13]: changeable_tensor , unchageable_tensor
[13]: (<tf.Variable 'Variable:0' shape=(2,) dtype=int32, numpy=array([10, 10])>,
       <tf.Tensor: shape=(2,), dtype=int32, numpy=array([10, 10])>)
[14]: # Changing element in the changeable tensor
      changeable_tensor[0]
[14]: <tf.Tensor: shape=(), dtype=int32, numpy=10>
     This gives a values of numpy 10
[16]: #Now lets try channging using assignment method
      changeable_tensor[0] = 7
             TypeError
                                                        Traceback (most recent call_
      →last)
             <ipython-input-16-204a6df08bff> in <module>
               1 #Now lets try channging using assignment method
         ----> 2 changeable_tensor[0] = 7
             TypeError: 'ResourceVariable' object does not support item assignment
```

We see that the changeable tensor doesnt allow item assignment. This is where we refer to tensorflow documentation to see how to assign values to change the tensor.

```
[]: #using the assign method to change the value of changeable tensor changeable_tensor[0].assign(7) changeable_tensor
```

```
[]: #Trying the same as above for unchangeable tensor unchangeable_tensor[0].assign(7) unchangeable_tensor
```

Thus, the above examples conclude the difference between variable and constant tensors. > **Note**1: If you declare a tf. Variable, you can change it's value later on if you want to. On the other

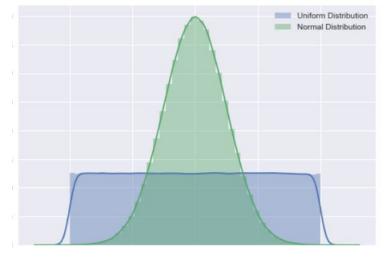
hand, tf.constant is immutable, meaning that once you define it you can't change its value.

**Note 2:** Most of the time in practice you will need to decide between using tf.constant or tf.variable depending on the use case. However, most of the time, Tensorflwo will automatically decide or choose for you when loading or modelling the data

### 4 Create random tensors

Random tensors are tensors of some abitrary size which contain random numbers. Why would you want to create random tensors? This is what neural networks use to intialize their weights (patterns) that they're trying to learn in the data.

**Note 3:** Normal Distribution Vs Uniform Distribution Normal Distribution is a probability distribution where probability of x is highest at centre and lowest in the ends whereas in Uniform Distribution probability of x is constant.



### 5 Shuffling order of elements in a Tensor

Why do we want to shuffle the elements in a Tensor? Let's say you working with 15,000 images of cats and dogs and the first 10,000 images of were of cats and the next 5,000 were of dogs. This order could effect how a neural network learns (it may overfit by learning the order of the data), instead, it might be a good idea to move your data around.

```
[]: #Shuffling the above tensor tf.random.shuffle(not_shuffled)
```

The above tf.random.shuffle is shuffled around based on the first dimension

### 6 Other methods to creating Tensors

```
[]: #1. Tensorflow operation similar to numpy ones tf.ones([5,5],dtype='int32')
```

```
[]: #2. Tensorflow operation similar to numpy zeroes tf.zeros(shape=(5,5),dtype='int32')
```

### 6.1 Turn numpy arrays into Tensors

**Note 4:** Why Tensors over Numpy arrays? This because TensorFlow tesnors can be run on a GPU much faster for numerical computing than numpy

```
[17]: #Numpy into Tensors

import numpy as np
numpy_A = np.arange(1,25,dtype=np.int32)
numpy_A , numpy_A.shape
```

```
[17]: (array([ 1,  2,  3,  4,  5,  6,  7,  8,  9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24]),
(24,))
```

```
[18]: #converting above numpy_A to tensor
A = tf.constant(numpy_A, shape=(2,3,4))
A
```

```
[19]: B = tf.constant(numpy_A,shape=(6,4))
B
```

```
[19]: <tf.Tensor: shape=(6, 4), dtype=int32, numpy=
     array([[ 1, 2, 3, 4],
            [5, 6, 7, 8],
            [ 9, 10, 11, 12],
            [13, 14, 15, 16],
            [17, 18, 19, 20],
            [21, 22, 23, 24]])>
[22]: #Now trying to make a tensor with different shape which doesn't multiplies to 24
     C = tf.constant(numpy_A,shape=(10,2))
     С
            TypeError
                                                    Traceback (most recent call,
      →last)
            <ipython-input-22-9703eb7c673f> in <module>
              →multiplies to 24
         ---> 2 C = tf.constant(numpy A,shape=(10,2))
      →\Anaconda\envs\fyp\lib\site-packages\tensorflow\python\framework\constant_op.
      →py in constant(value, dtype, shape, name)
            262
                  return _constant_impl(value, dtype, shape, name, __
      →verify_shape=False,
        --> 264
                                       allow_broadcast=True)
            265
            266
            D:
      →\Anaconda\envs\fyp\lib\site-packages\tensorflow\python\framework\constant_op.
      →py in _constant_impl(value, dtype, shape, name, verify_shape, allow_broadcast)
            273
                      with trace.Trace("tf.constant"):
            274
                        return _constant_eager_impl(ctx, value, dtype, shape, __
      →verify_shape)
         --> 275
                    return _constant_eager_impl(ctx, value, dtype, shape, __
      →verify_shape)
            276
            277
                  g = ops.get_default_graph()
```

TypeError: Eager execution of tf.constant with unsupported shape (value $_{\sqcup}$   $\rightarrow$ has 24 elements, shape is (10, 2) with 20 elements).

Thus, we have to take note of the shape and ensure the dimensions tally with the original dimensions.

## 7 Getting more Information from Tensors

Attribute	Meaning	Code
Shape	The length (number of elements) of each of the dimensions of a tensor.	tensor.shape
Rank	The number of tensor dimensions. A scalar has rank 0, a vector has rank 1, a matrix is rank 2, a tensor has rank n.	tensor.ndim
Axis or dimension	A particular dimension of a tensor.	tensor[0], tensor[:, 1]
Size	The total number of items in the tensor.	tf.size(tensor)

```
[0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]
              [[0., 0., 0., 0., 0.],
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]]
             [[[0., 0., 0., 0., 0.],
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]
              [[0., 0., 0., 0., 0.],
               [0., 0., 0., 0., 0.],
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]
              [[0., 0., 0., 0., 0.],
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]]]], dtype=float32)>
[25]: #Verifying the rank of the above tensor
      rank_4_tensor.ndim
[25]: 4
[26]: rank_4_tensor[0] #oth axis
[26]: <tf.Tensor: shape=(3, 4, 5), dtype=float32, numpy=
      array([[[0., 0., 0., 0., 0.],
              [0., 0., 0., 0., 0.]
              [0., 0., 0., 0., 0.]
              [0., 0., 0., 0., 0.]
             [[0., 0., 0., 0., 0.],
              [0., 0., 0., 0., 0.],
              [0., 0., 0., 0., 0.]
              [0., 0., 0., 0., 0.]
             [[0., 0., 0., 0., 0.],
              [0., 0., 0., 0., 0.]
```

[[0., 0., 0., 0., 0.],

```
[0., 0., 0., 0., 0.],
[0., 0., 0., 0., 0.]]], dtype=float32)>

[27]: tf.size(rank_4_tensor) #120 elements present i.e. 2x3x4x5
```

```
[27]: <tf.Tensor: shape=(), dtype=int32, numpy=120>
```

```
[28]: # Get various attributes of tensor

print("Datatype of every element:", rank_4_tensor.dtype)

print("Number of dimensions (rank):", rank_4_tensor.ndim)

print("Shape of tensor:", rank_4_tensor.shape)

print("Elements along axis 0 of tensor:", rank_4_tensor.shape[0])

print("Elements along last axis of tensor:", rank_4_tensor.shape[-1])

print("Total number of elements (2*3*4*5):", tf.size(rank_4_tensor).numpy()) # .

→numpy() converts to NumPy array
```

```
Datatype of every element: <dtype: 'float32'>
Number of dimensions (rank): 4
Shape of tensor: (2, 3, 4, 5)
Elements along axis 0 of tensor: 2
Elements along last axis of tensor: 5
Total number of elements (2*3*4*5): 120
```

#### 7.1 Summary of attributes from Tensors:

- 1. Data type
- 2. Number of dimension or Rank
- 3. Shape
- 4. Number of elements

### 8 Indexing Tensors

Tensors can be indexed like Python lists

```
[29]: #Get the first two elements of each dimension of the rank 4 tensor above rank_4_tensor

[29]: <tf.Tensor: shape=(2, 3, 4, 5), dtype=float32, numpy=
```

```
[[0., 0., 0., 0., 0.],
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]]
             [[[0., 0., 0., 0., 0.],
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]
              [[0., 0., 0., 0., 0.],
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]
              [[0., 0., 0., 0., 0.],
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]]]], dtype=float32)>
[30]: rank_4_tensor[:2,:2,:2,:2]
[30]: <tf.Tensor: shape=(2, 2, 2, 2), dtype=float32, numpy=
      array([[[[0., 0.],
               [0., 0.]],
              [[0., 0.],
               [0., 0.]]],
             [[[0., 0.],
               [0., 0.]],
              [[0., 0.],
               [0., 0.]]]], dtype=float32)>
[31]: #create a Rank2 tensor
      rank_2_tensor = tf.constant([[10,1],
                                  [7,2]])
      rank_2_tensor
[31]: <tf.Tensor: shape=(2, 2), dtype=int32, numpy=
      array([[10, 1],
             [7, 2])>
```

```
[32]: #Get last item of each of our row of rank2 tensor
      rank_2_tensor[:,-1].numpy()
[32]: array([1, 2])
[33]: #Add in extra dimension to our rank2 tensor
      rank_3_tensor = rank_2_tensor[...,tf.newaxis]
      rank_3_tensor
[33]: <tf.Tensor: shape=(2, 2, 1), dtype=int32, numpy=
      array([[[10],
              [1]],
             [[7],
              [ 2]]])>
           Note 5: rank_2_tensor[...,tf.newaxis] is same as rank_2_tensor[:,:,tf.newaxis]
[34]: #Alternatice to tf.newaxis
      tf.expand_dims(rank_2_tensor,axis=-1) #"-1" means expand final axis
[34]: <tf.Tensor: shape=(2, 2, 1), dtype=int32, numpy=
      array([[[10],
              [ 1]],
             [[7],
              [ 2]]])>
[35]: tf.expand_dims(rank_2_tensor,axis=0) #Extra dimension in the front
[35]: <tf.Tensor: shape=(1, 2, 2), dtype=int32, numpy=
      array([[[10, 1],
              [7, 2]])>
         Tensor operations
[36]: # Addition operator
      tensor=tf.constant([[10,7],
                          [3,4]])
      tensor+10
[36]: <tf.Tensor: shape=(2, 2), dtype=int32, numpy=
      array([[20, 17],
             [13, 14]])>
[37]: #Multiplication
      tensor*10
```

```
[37]: <tf.Tensor: shape=(2, 2), dtype=int32, numpy=
      array([[100, 70],
                   40]])>
             [ 30,
[38]: #subtraction
      tensor-10
[38]: <tf.Tensor: shape=(2, 2), dtype=int32, numpy=
      array([[ 0, -3],
             [-7, -6]])>
[39]: #Division
      tensor/10
[39]: <tf.Tensor: shape=(2, 2), dtype=float64, numpy=
      array([[1., 0.7],
             [0.3, 0.4]])>
[40]: #Using the tensorflow builtin functions
      tf.multiply(tensor,10)
[40]: <tf.Tensor: shape=(2, 2), dtype=int32, numpy=
      array([[100, 70],
             [ 30, 40]])>
[41]: tf.add(tensor,10)
[41]: <tf.Tensor: shape=(2, 2), dtype=int32, numpy=
      array([[20, 17],
             [13, 14]])>
```

The above will take advatage of the gpu to speed up the computation

# 10 Matrix Multiplication using tf.linalg.matmul

$$\begin{bmatrix} a_1 & a_2 & a_3 \\ a_4 & a_5 & a_6 \\ a_7 & a_8 & a_9 \end{bmatrix} \begin{bmatrix} b_1 & b_2 & b_3 \\ b_4 & b_5 & b_6 \\ b_7 & b_8 & b_9 \end{bmatrix} = \begin{bmatrix} c_1 & c_2 & c_3 \\ c_4 & c_5 & c_6 \\ c_7 & c_8 & c_9 \end{bmatrix}$$

**Note 5:** The main two rules for matrix multiplication to remember are: 1. The inner dimensions must match: 2. The resulting matrix has the shape of the outer dimensions

Visualization of matrix : http://matrixmultiplication.xyz/

```
[42]: #Matrix multiplication in tensorflow
      print(tensor)
      #In tensorflow we can drop the intermediate areas i.e. instead of using tf.
       \hookrightarrow linalg.matmul we can use tf.matmul
      tf.matmul(tensor,tensor)
     tf.Tensor(
     [[10 7]
      [ 3 4]], shape=(2, 2), dtype=int32)
[42]: <tf.Tensor: shape=(2, 2), dtype=int32, numpy=
      array([[121, 98],
             [ 42, 37]])>
     The above shows multiplication between two tensors
[43]: tensor*tensor
[43]: <tf.Tensor: shape=(2, 2), dtype=int32, numpy=
      array([[100, 49],
             [ 9, 16]])>
     The above does element wise multiplication between the corresponding elements
[44]: #To do matrix multiplication with python operator use @
      tensor@tensor
[44]: <tf.Tensor: shape=(2, 2), dtype=int32, numpy=
      array([[121, 98],
             [ 42, 37]])>
[45]: X = tf.constant([[1,2],
                       [3,4],
                        [5,6]])
      Y = tf.constant([[7,8],
                       [9,10],
                        [11, 12])
[46]: tf.matmul(X,Y)
              InvalidArgumentError
                                                         Traceback (most recent call
      →last)
```

```
<ipython-input-46-cc348e6d8216> in <module>
  ----> 1 tf.matmul(X,Y)
       D:\Anaconda\envs\fyp\lib\site-packages\tensorflow\python\util\dispatch.
→py in wrapper(*args, **kwargs)
       199
               """Call target, and fall back on dispatchers if there is a_{\sqcup}
→TypeError."""
       200
   --> 201
                 return target(*args, **kwargs)
               except (TypeError, ValueError):
       202
       203
                 # Note: convert_to_eager_tensor currently raises a ValueError, __
→not a
       D:\Anaconda\envs\fyp\lib\site-packages\tensorflow\python\ops\math_ops.py_
→in matmul(a, b, transpose_a, transpose_b, adjoint_a, adjoint_b, a_is_sparse,
→b is sparse, name)
      3253
               else:
      3254
                 return gen_math_ops.mat_mul(
  -> 3255
                     a, b, transpose_a=transpose_a, transpose_b=transpose_b,_
→name=name)
      3256
      3257
      D:
→\Anaconda\envs\fyp\lib\site-packages\tensorflow\python\ops\gen_math_ops.py in_
→mat_mul(a, b, transpose_a, transpose_b, name)
      5622
                 return _result
      5623
               except _core._NotOkStatusException as e:
   -> 5624
                 _ops.raise_from_not_ok_status(e, name)
      5625
               except _core._FallbackException:
      5626
                 pass
       D:\Anaconda\envs\fyp\lib\site-packages\tensorflow\python\framework\ops.
→py in raise_from_not_ok_status(e, name)
             message = e.message + (" name: " + name if name is not None else_{\sqcup}
      6841
→"")
             # pylint: disable=protected-access
      6842
             six.raise_from(core._status_to_exception(e.code, message), None)
  -> 6843
      6844
             # pylint: enable=protected-access
      6845
```

```
→from_value)
             InvalidArgumentError: Matrix size-incompatible: In[0]: [3,2], In[1]:
      \hookrightarrow [3,2] [Op:MatMul]
     Thus, we need to reshape one of the matrix to perform the multiplication
[47]: #reshaping matrix Y
      Y = tf.reshape(Y, shape=(2,3))
      Y
[47]: <tf.Tensor: shape=(2, 3), dtype=int32, numpy=
      array([[ 7, 8, 9],
             [10, 11, 12]])>
[48]: tf.matmul(X,Y)
[48]: <tf.Tensor: shape=(3, 3), dtype=int32, numpy=
      array([[ 27, 30, 33],
             [61, 68, 75],
             [ 95, 106, 117]])>
     Transpose is when the cols become rows and the rows become cols
[49]: X = tf.constant([[1,2],
                       [3,4],
                        [5,6]])
      Y = tf.constant([[7,8],
                       [9,10],
                        [11,12]])
[50]: tf.matmul(X,tf.transpose(Y))
[50]: <tf.Tensor: shape=(3, 3), dtype=int32, numpy=
      array([[ 23, 29, 35],
             [53, 67, 81],
             [ 83, 105, 127]])>
[52]: #Seeing difference between transpose and reshape
      Y,tf.reshape(Y,shape=(2,3)), tf.transpose(Y)
[52]: (<tf.Tensor: shape=(3, 2), dtype=int32, numpy=
       array([[ 7, 8],
              [9, 10],
              [11, 12]])>,
       <tf.Tensor: shape=(2, 3), dtype=int32, numpy=
```

D:\Anaconda\envs\fyp\lib\site-packages\six.py in raise\_from(value,\_

Thus, transposing is shifting the axises while reshaping reshuffles the elements in the matrix

#### 10.1 The dot product

Multiplying matrices by eachother is also referred to as the dot product.

You can perform the tf.matmul() operation using tf.tensordot()

### 11 Changing datatype of a tensor

```
[59]: #Create a new tensor with default datatype (float32)
    B = tf.constant([1.7,2])
    B

[59]: <tf.Tensor: shape=(2,), dtype=float32, numpy=array([1.7, 2. ], dtype=float32)>

[61]: #Change float 32 to float 16
    B = tf.cast(B,dtype=tf.float16)
    B

[61]: <tf.Tensor: shape=(2,), dtype=float16, numpy=array([1.7, 2. ], dtype=float16)>

[ ]:
```