



# Uncertainty in NLP

*quantification, interpretation & evaluation*

Priberam Machine Learning Lunch Seminars

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Instituto Superior Técnico  
Instituto de Telecomunicações



Models don't always know  
what they don't know



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  - ➔ Active learning
  - ➔ Curriculum learning
- ✓ Compare models with respect to their overall confidence

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The more uncertain the model the harder it is to choose among ***valid*** candidate outputs

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- ✓ Refine the input: Provide more information
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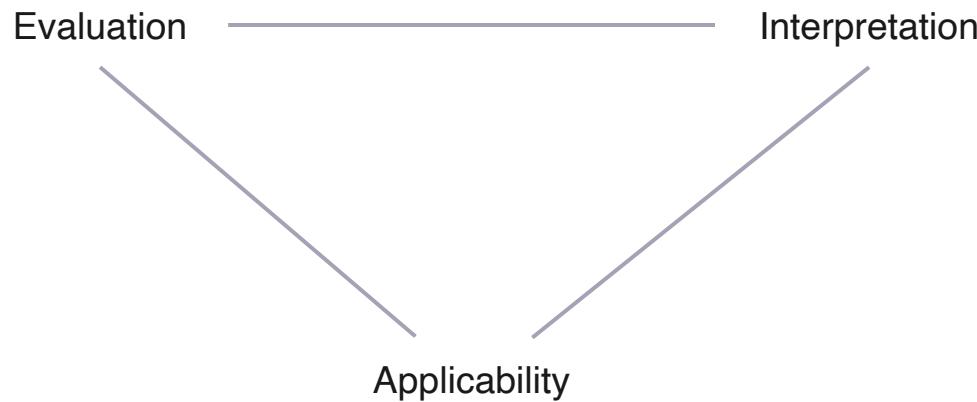
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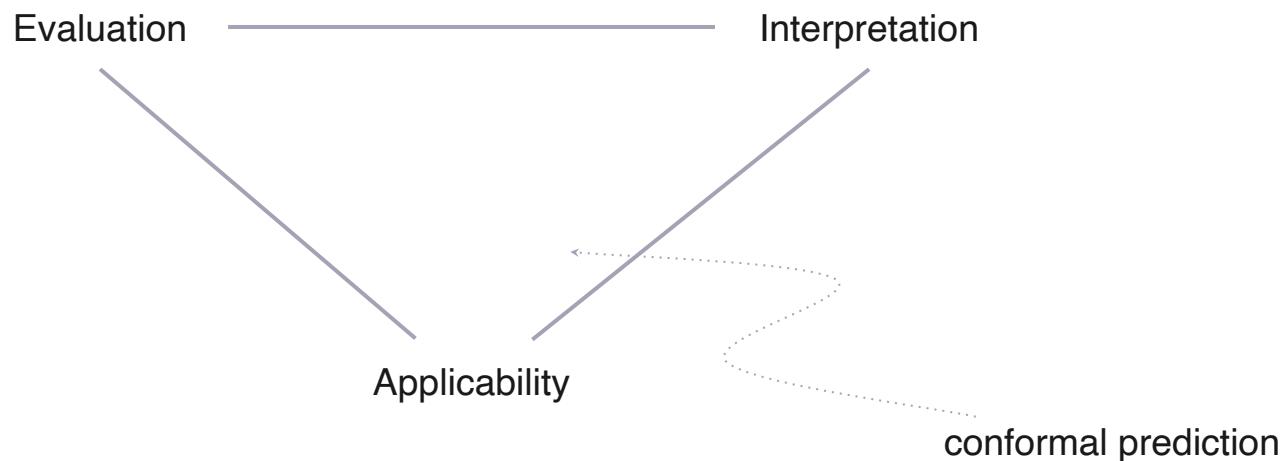
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- ✓ Refine the output: Provide more information
  - ➡ To the user

# What is a good uncertainty quantifier

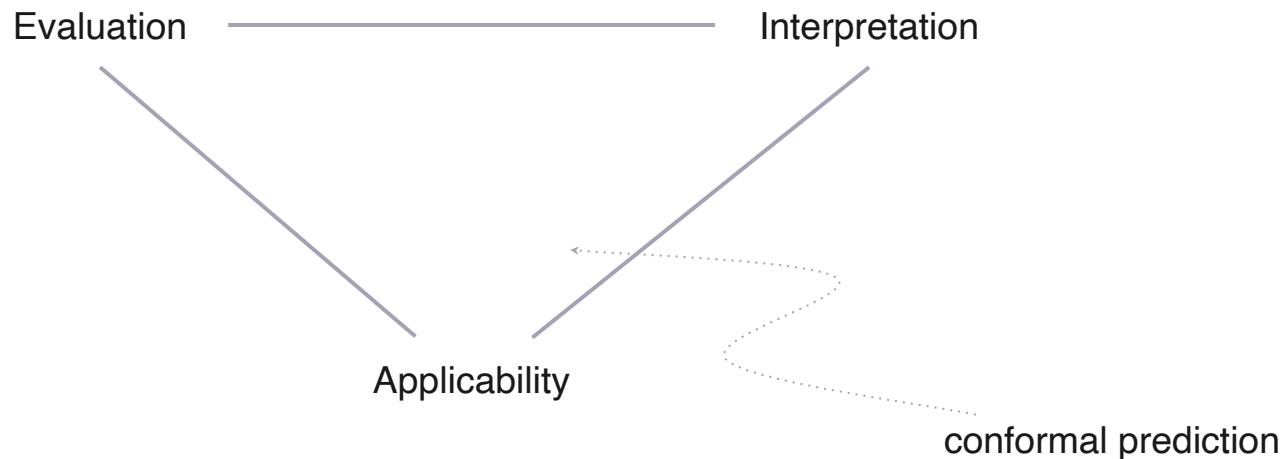
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★Machine Translation  
tasks

# Uncertainty in MT related tasks

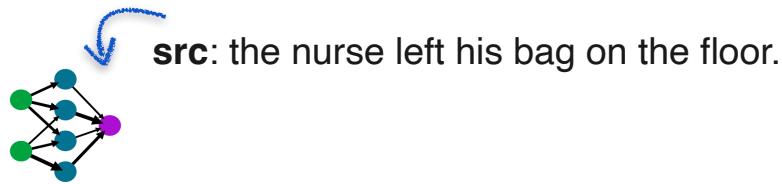
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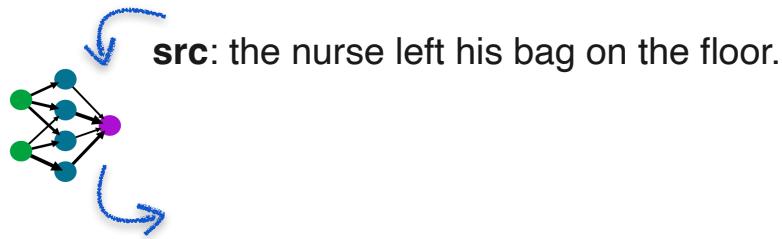


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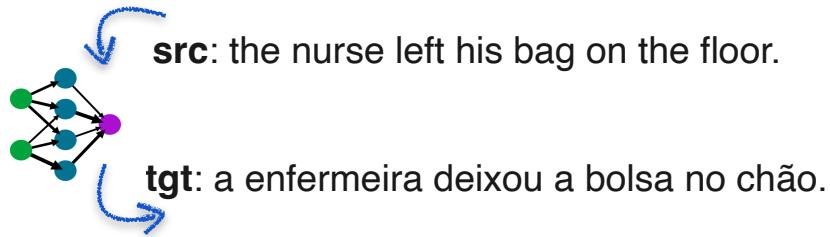
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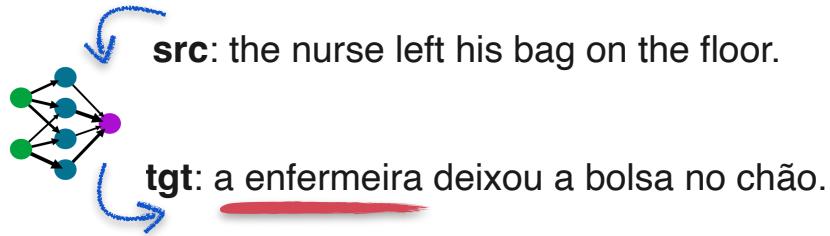
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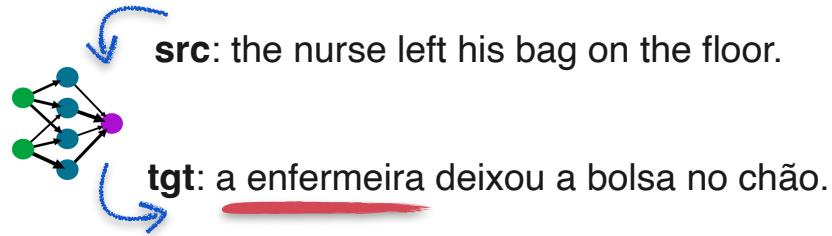
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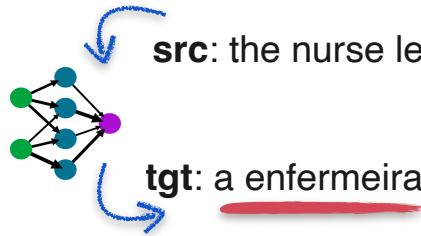
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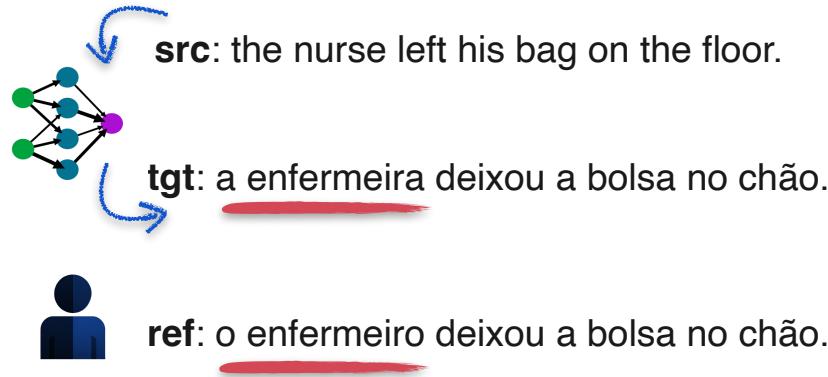
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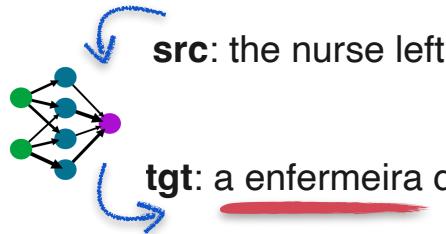


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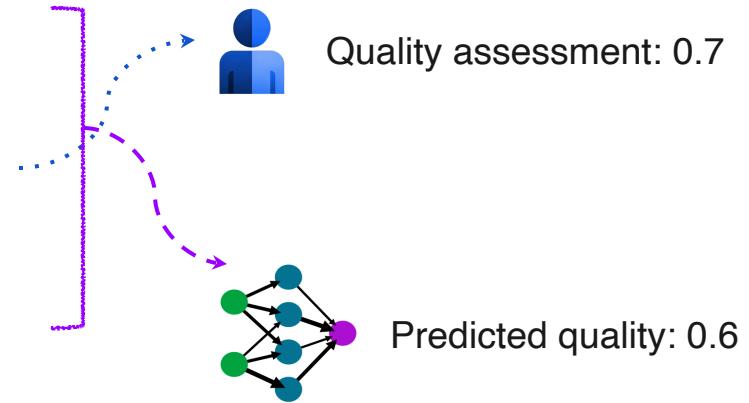
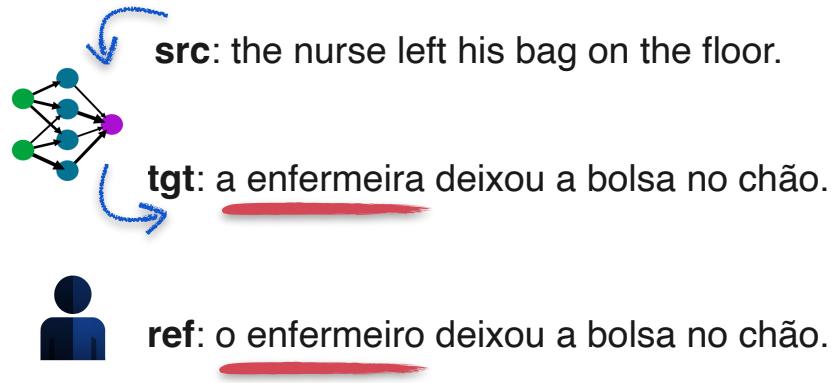


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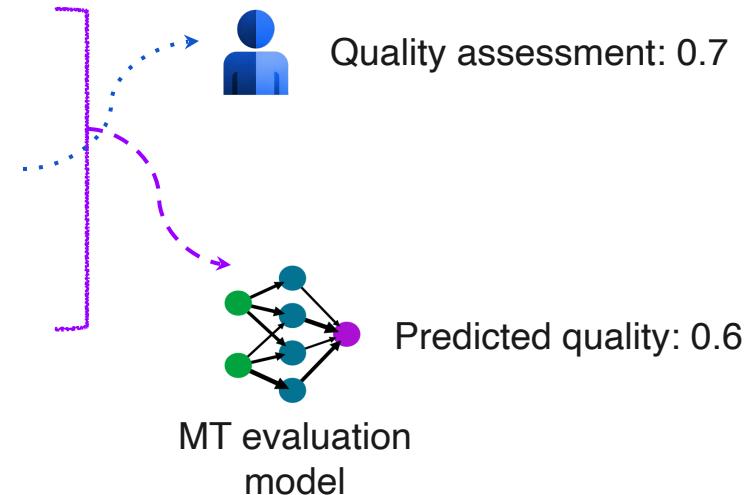
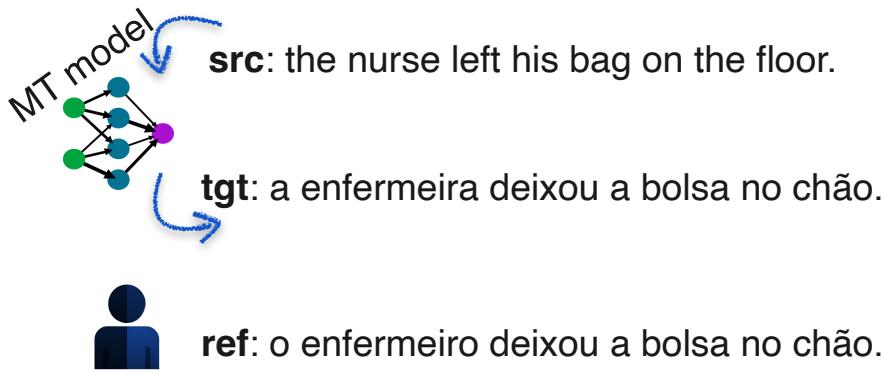


Quality assessment: 0.7

# Uncertainty in MT related tasks



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# Applicability

and underlying assumptions

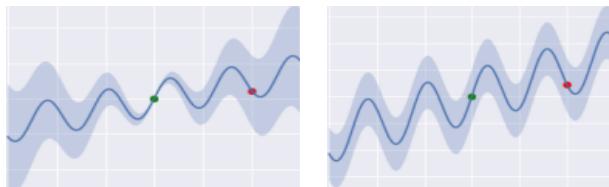
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What are our assumptions on distribution?

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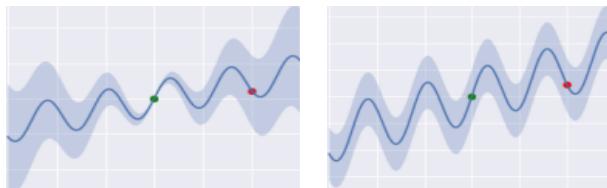
Heteroscedastic vs homoscedastic  
noise



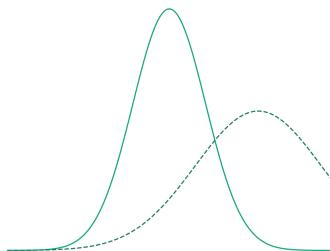
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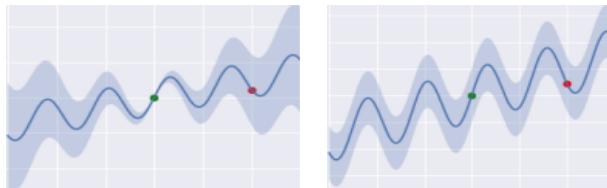
Modeling annotator disagreement



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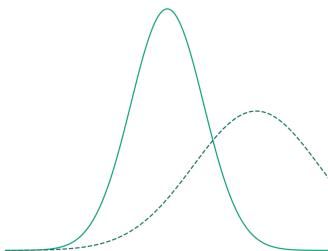
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Bayesian Neural Networks

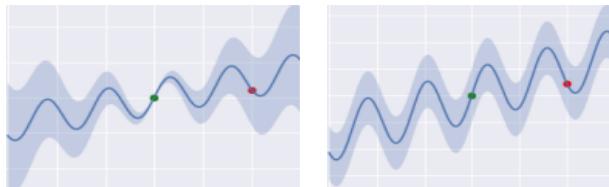
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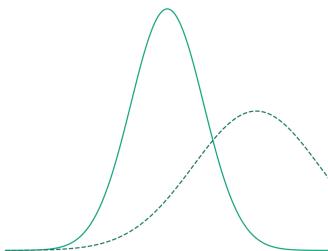
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Bayesian Neural Networks

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MC dropout

Deep ensembles

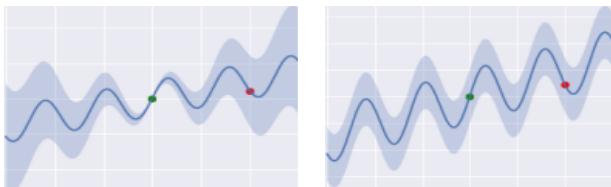
Test-time augmentation

Stochastic variational inference

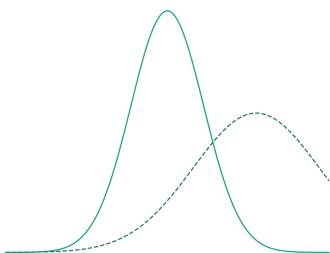
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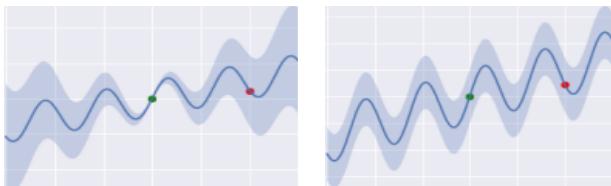
Dirichlet-based uncertainty models

PriorNet (Malinin and Gales 2018)

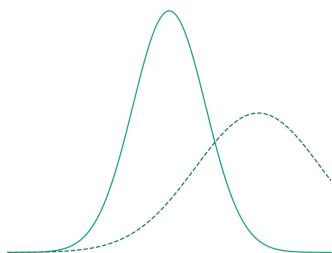
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⋮ ⋮ ⋮

Deterministic uncertainty models

- assumptions on modelling feature density
- access to OOD data

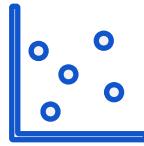
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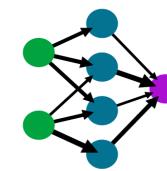
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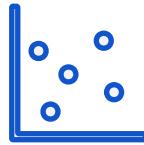
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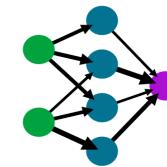
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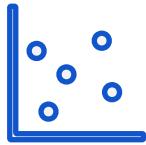
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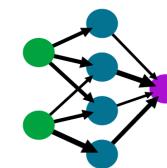
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epistemic



- Data filtering
- Ambiguity detection
- ✓ Better for detecting low quality MT references

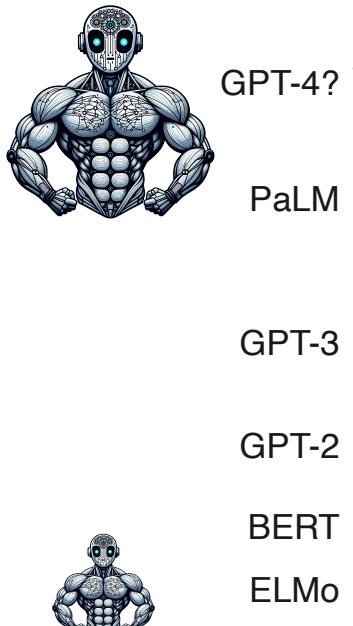
- Active learning setups
- Better detection of OOD instances
- ✓ Better detector of hallucinations  
(Xiao & Wang, 2021)
- ✓ Better for detecting domain shifts in MT evaluation

\*(Zerva et al., 2022)

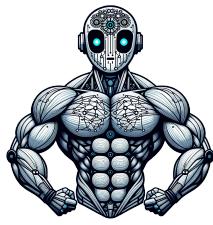
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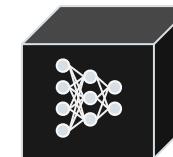
PaLM

GPT-3

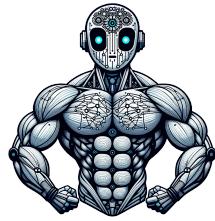
GPT-2

BERT

ELMo



# what can we use?



GPT-4?

PaLM

GPT-3

GPT-2

BERT

ELMo



● Access output probabilities?

● Extend and tune with a different loss?

● Use several checkpoints?

● Retrain with different objectives?

● Prompt to output uncertainty?

● Test-time augmentation

● Sample several times?

# Evaluation - Interpretation

and underlying assumptions

# Evaluation

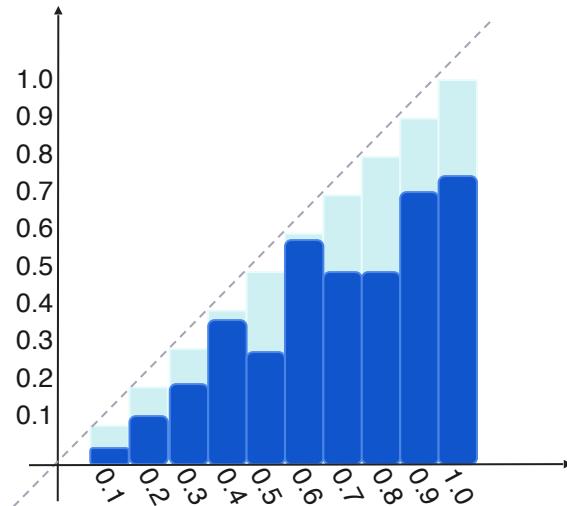
**Well calibrated**

# Evaluation

**Well calibrated**

Estimated Calibration error (ECE)

$$ECE = \frac{1}{M} \sum_{b=1}^M |acc(B_m) - conf(B_m)|$$

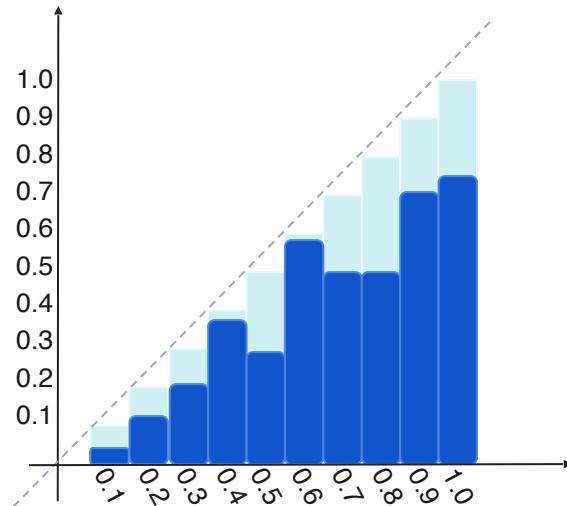


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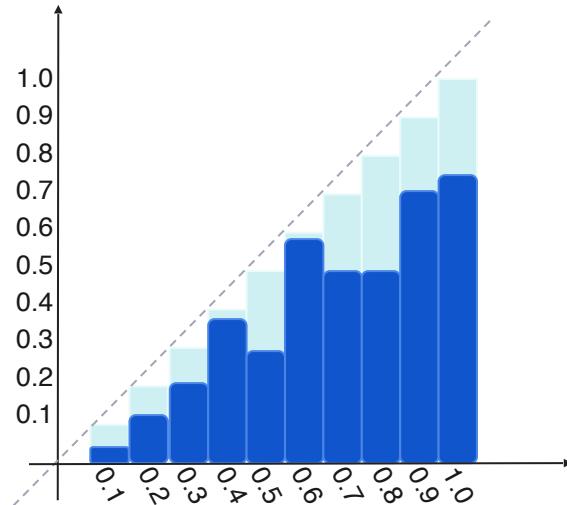
- ✗ Sensitive to the choice of bin width
- ✗ small changes to model predictions can cause large jumps in the ECE
- ✗ Not suitable in tasks with high label variability

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- ✗ small changes to model predictions can cause large jumps in the ECE
- ✗ Not suitable in tasks with high label variability
  
- Max calibration error
- Logit-smoothed ECE
- Human Entropy Calibration Score
- Human Distribution Calibration Error

# Evaluation

**Focussing on errors**

# Evaluation

## Focussing on errors

- Correlation with error

$$\rho(u(X_{\text{test}}), |\hat{Y}_{\text{test}} - Y_{\text{test}}|)$$

$$r(u(X_{\text{test}}), |\hat{Y}_{\text{test}} - Y_{\text{test}}|)$$

# Evaluation

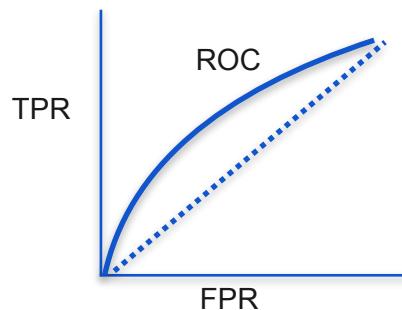
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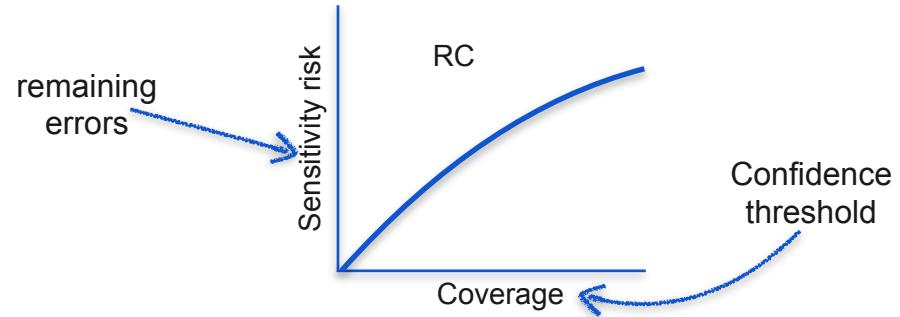
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- AUROC



- AUC-RC



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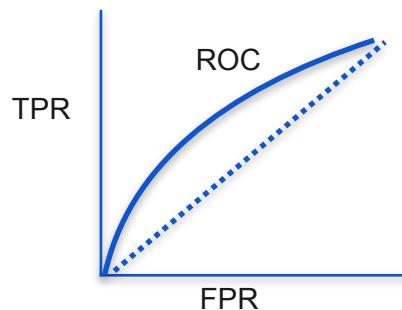
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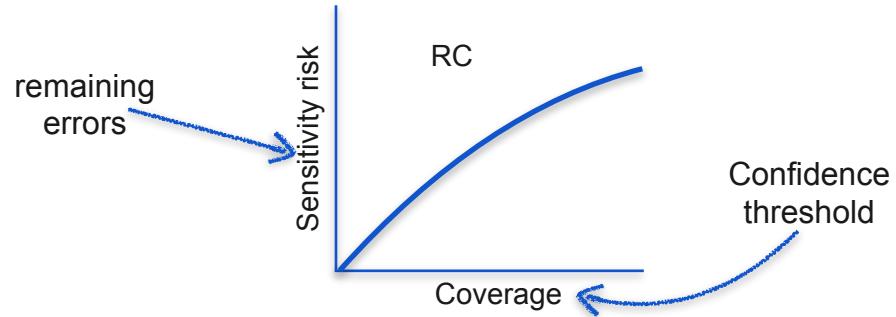
$$r(u(X_{\text{test}}), |\hat{Y}_{\text{test}} - Y_{\text{test}}|)$$

- ✗ Sensitive to outliers
- ✗ Not informative in terms of scale

- AUROC



- AUC-RC

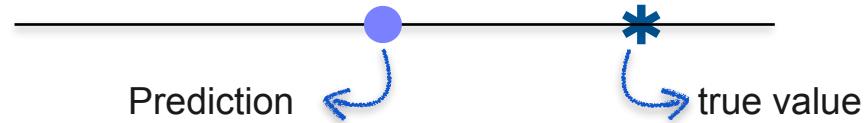
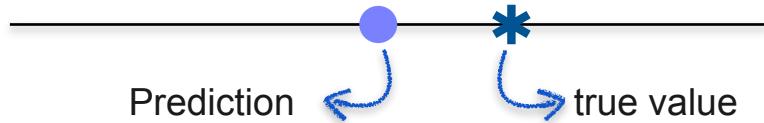


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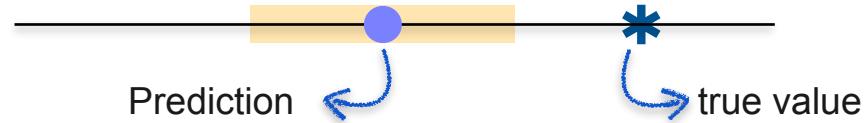
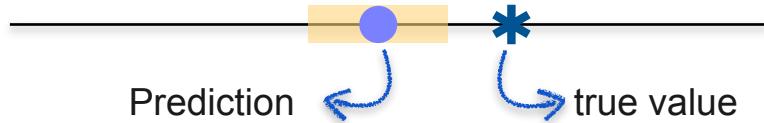
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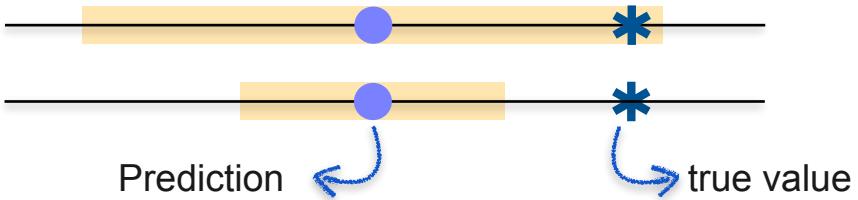
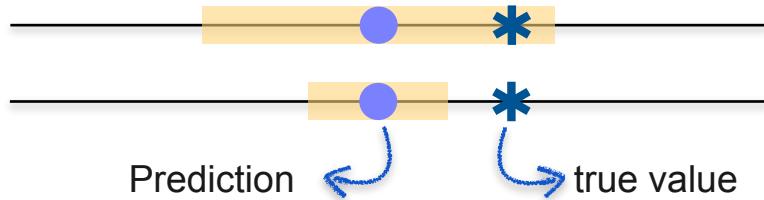
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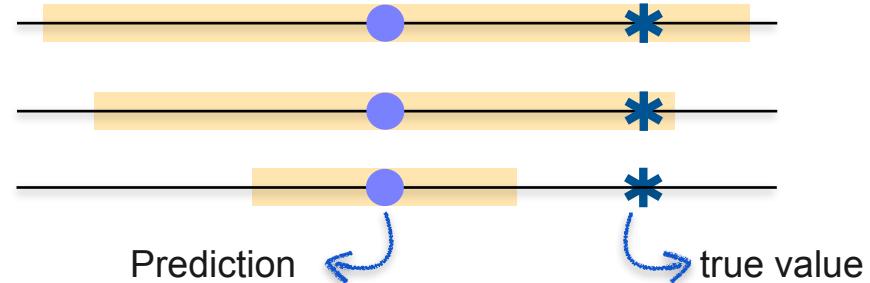
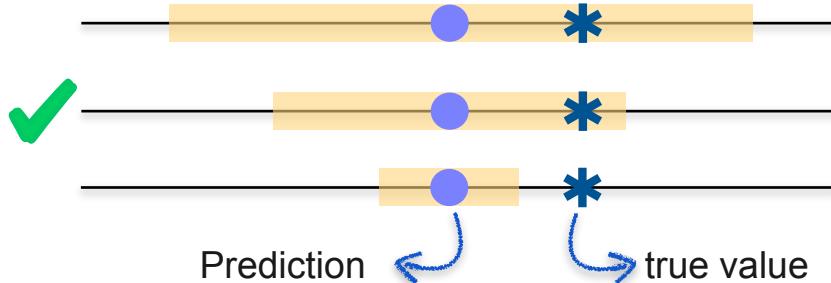
# Evaluation

Width - Sharpness

Tight intervals - peaky distributions

Coverage

Including the true label in the confidence interval



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Width - Sharpness

Tight intervals - peaky distributions

Coverage

Including the true label in the confidence interval



Robustness

Robust to noise injection - adversarial attacks

Prediction ↙ true value

Prediction ↙ true value



# Evaluation

Width - Sharpness

Tight intervals - peaky distributions

Coverage

Including the true label in the confidence interval



Robustness

Robust to noise injection - adversarial attacks

Fairness

Similar behaviour across attributes



Prediction



true value



Prediction



true value

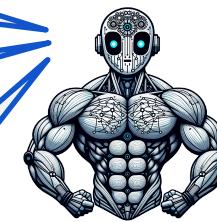
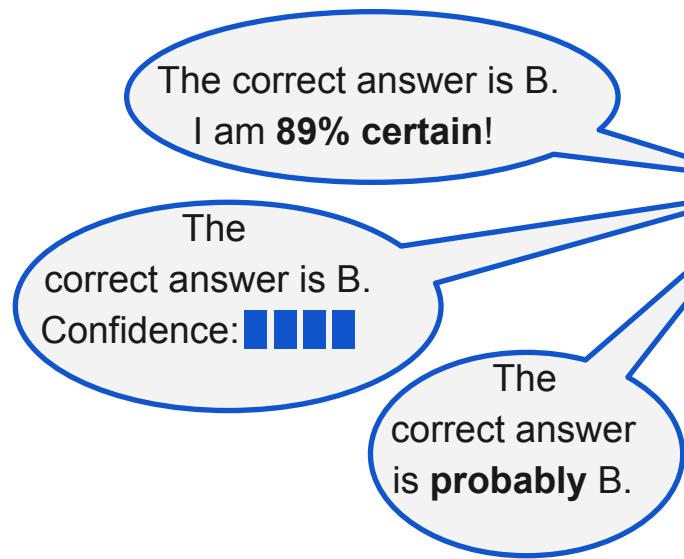
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Do people have a shared notion of risk/uncertainty/confidence?



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# Turning to conformal prediction

and coverage

# Conformal prediction



## Ingredients:

- Test set  $\{X_{\text{test}}, Y_{\text{test}}\}$
- Held-out calibration set
- $S^{\text{cal}} = \{X_{\text{cal}}, Y_{\text{cal}}\} = \{(x_i, y_i)\}_{i=1}^n$
- Non-conformity score for each data point:  
 $s_i := s(x_i, y_i)$
- Desired coverage  $1-\alpha$

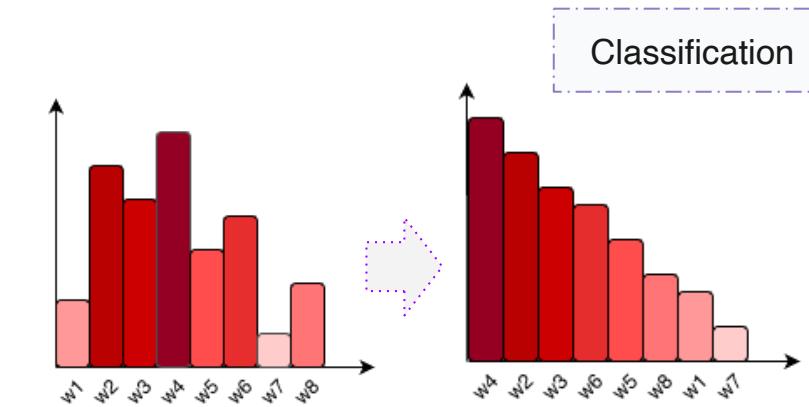


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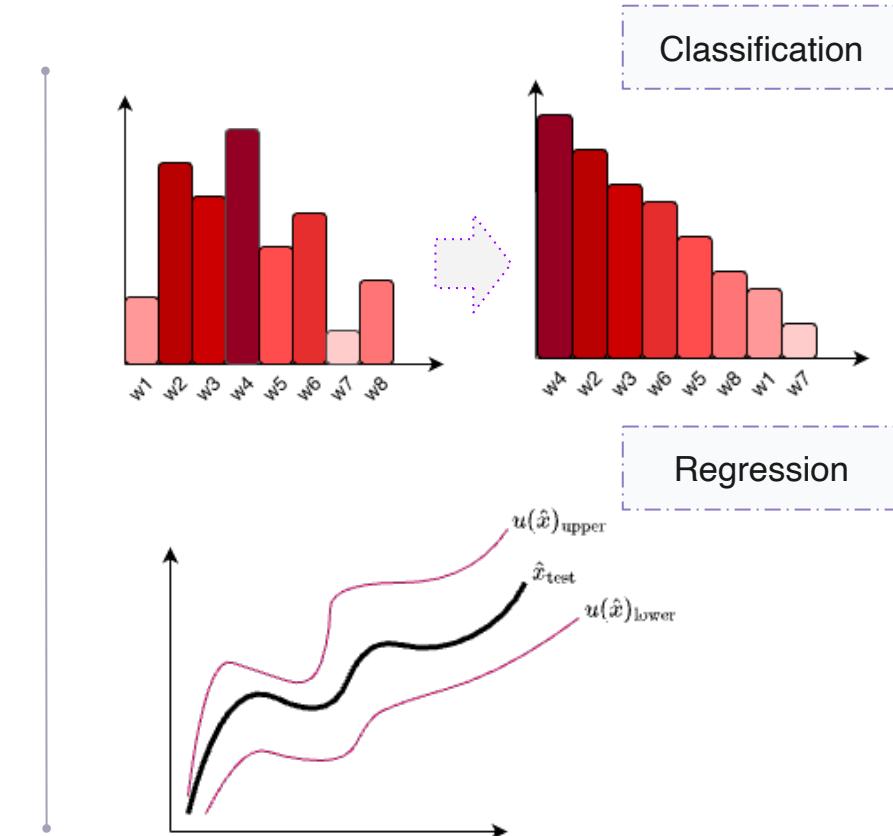
Classification

# Conformal prediction



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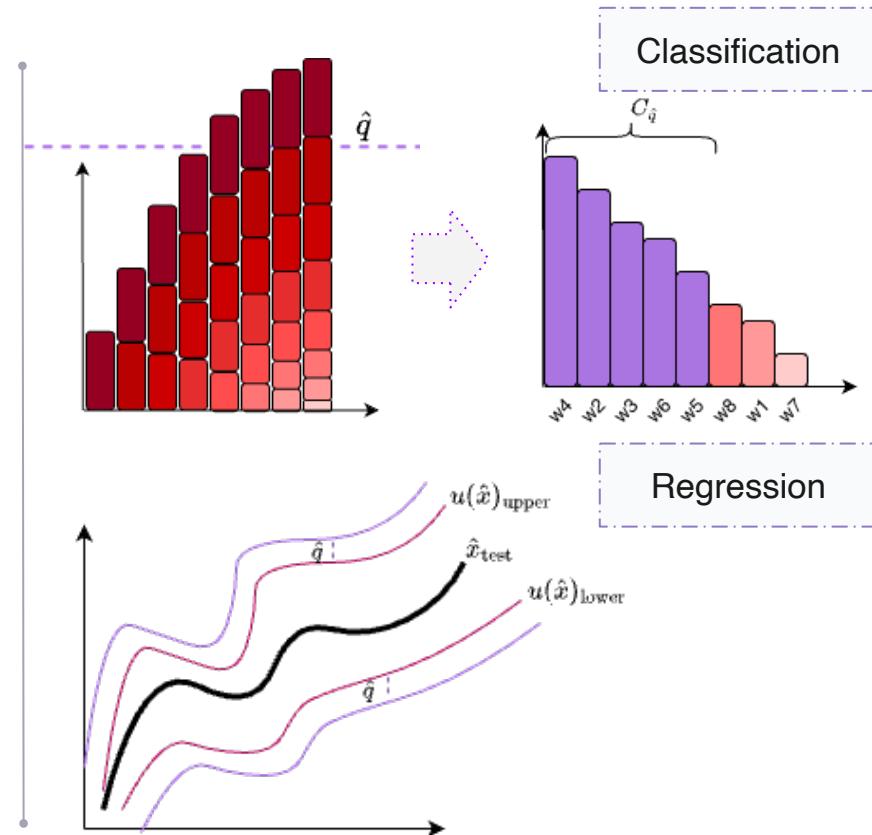


# Conformal prediction



## Process:

- Compute the  $\frac{[(n + 1)(1 - \alpha)]}{n}$  quantile  $\hat{q}$  over the non-conformity scores  $s_i := s(x_i, y_i)$  of the calibration set
- We can now compute the confidence intervals  $C_{\hat{q}}(x_{\text{test}}) = \{y \in Y : s(x_{\text{test}}, y) \leq \hat{q}\}$



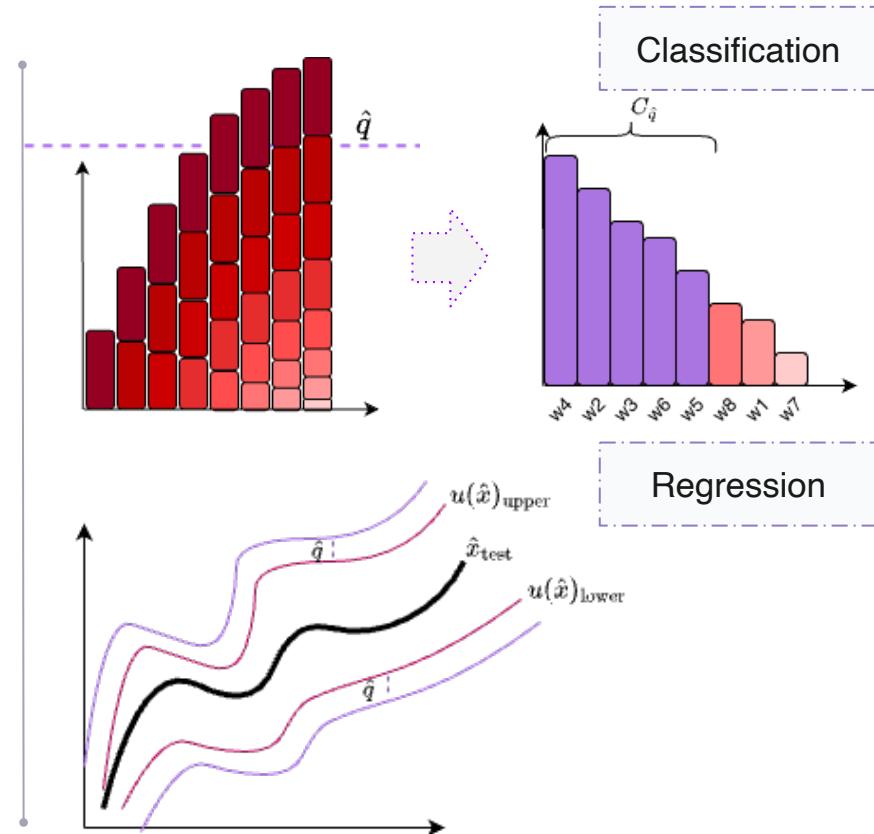
# Conformal prediction



## Process:

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# Conformal prediction



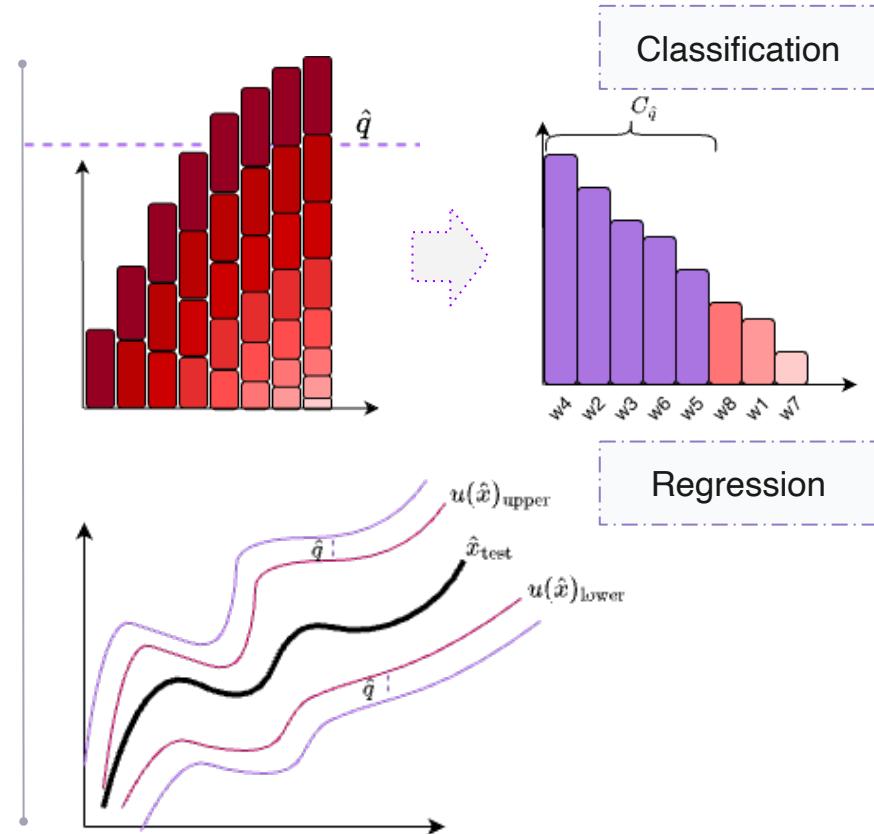
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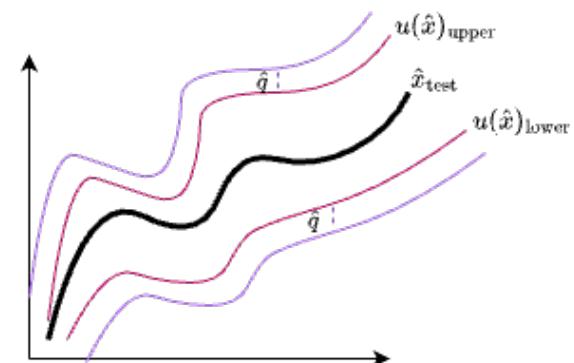
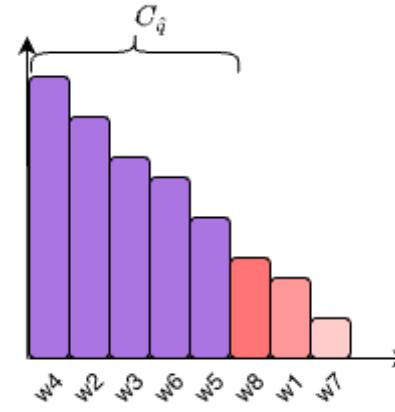


Guarantee on **marginal** coverage



# Interpretation

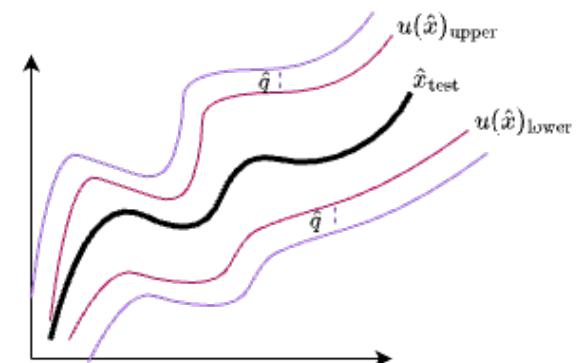
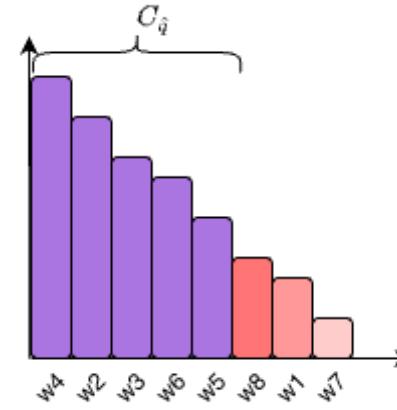
- width scaled with respect to desired coverage
- ✓ easier comparison between instances
- ✓ Meaningful intervals across tasks
- ✓ Non-parametric



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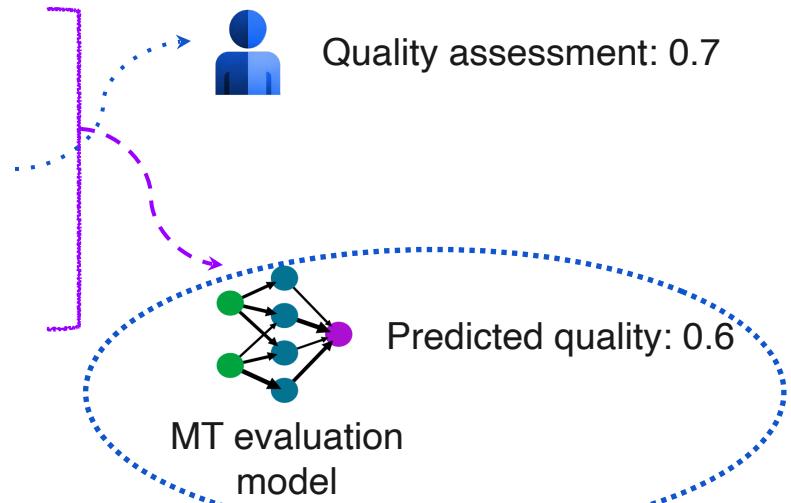
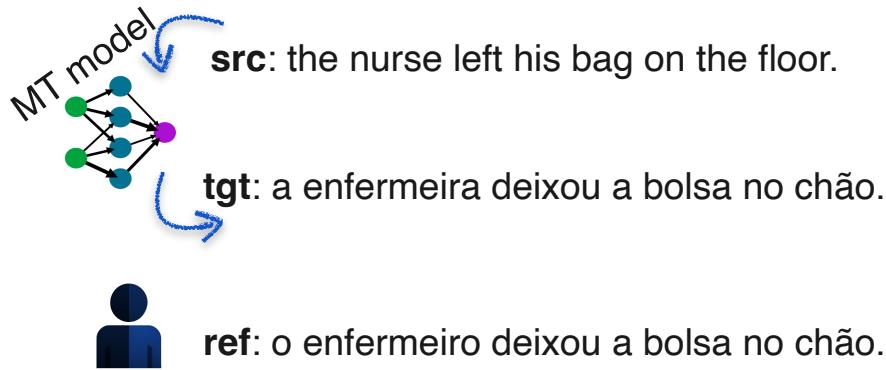
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Holds only for exchangeable data!



# Conformalising MT evaluation

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# Conformal prediction for MT evaluation

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MC Dropout

Deep Ensembles

$$\mathcal{N}(\hat{\mu}(x), \hat{\sigma}^2(x))$$

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Heteroscedastic Regression

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Regress on the residuals!

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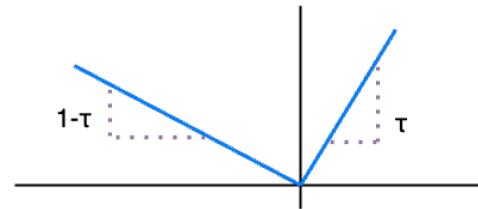
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Quantile regression



$$\mathcal{L}_\tau(\hat{y}; y) = (\hat{y} - y)(\mathbb{1}\{y \leq \hat{y}\} - \tau)$$

Optimise to predict selected quantiles instead of mean!

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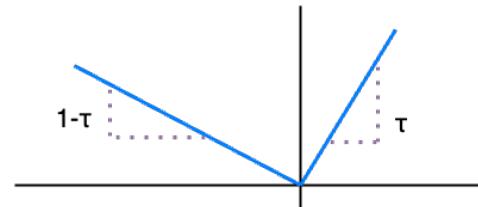
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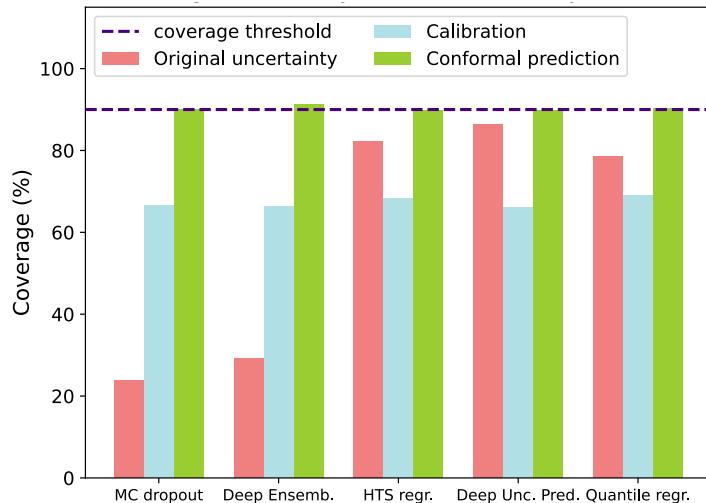
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Optimise to predict selected quantiles instead of mean!

$$s(x, y) = \frac{|y - \hat{y}(x)|}{u(x)}$$

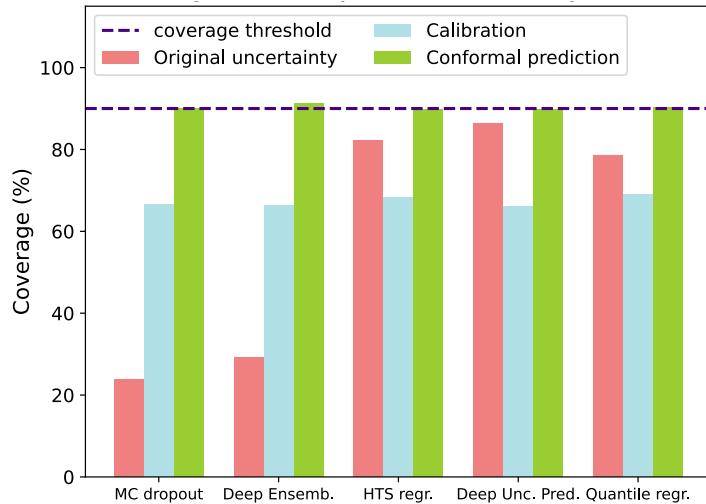
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# Selecting the most suitable UQ



Coverage for different UQ on COMET  
tested on WMT 2021 Metrics data

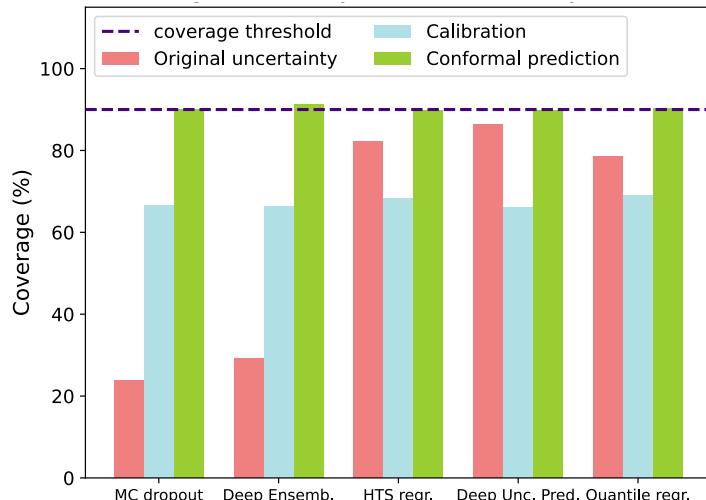
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Coverage (and  $\hat{q}$ ) aligns well with error correlation

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Coverage (and  $\hat{q}$ ) aligns well with error correlation

	$\hat{q} \downarrow$	$r \uparrow$
<i>MC Dropout</i>	8.08	0.04
<i>Deep Ensembles</i>	6.99	0.07
<i>Heteroscedastic reg.</i>	2.69	0.24
<i>Direct uncertainty pred.</i>	1.81	0.27
<i>Quantile regression</i>	1.28	0.34

# Access to fairness

What if we compute coverage with respect to specific attributes?

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	MCD	DE	HTS	DUP	QNT
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English-Japanese					
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English-Russian					
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German-English					
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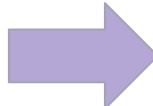
	MCD	DE	HTS	DUP	QNT
English-Czech	0.982	0.959	0.939	0.875	0.931
English-German	0.973	0.971	0.925	0.863	0.927
English-Japanese	0.990	0.978	0.987	0.886	0.972
English-Polish	0.977	0.948	0.914	0.882	0.914
English-Russian	0.974	0.958	0.936	0.862	0.926
English-Tamil	0.970	0.952	0.949	0.892	0.858
English-Chinese	0.934	0.983	0.991	0.919	0.945
Czech-English	0.890	0.871	0.884	0.898	0.875
German-English	0.880	0.888	0.867	0.896	0.902
Japanese-English	0.883	0.856	0.921	0.910	0.887
Khmer-English	0.881	0.875	0.948	0.943	0.840
Polish-English	0.862	0.833	0.825	0.873	0.849
Pashto-English	0.851	0.854	0.932	0.922	0.786
Russian-English	0.851	0.828	0.831	0.879	0.888
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Language-wise  
recalibration

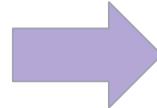


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English-German	0.902	0.902	0.902	0.896	0.893
English-Japanese	0.909	0.891	0.900	0.891	0.904
English-Polish	0.882	0.905	0.895	0.900	0.898
English-Russian	0.900	0.898	0.908	0.906	0.903
English-Tamil	0.903	0.895	0.883	0.886	0.903
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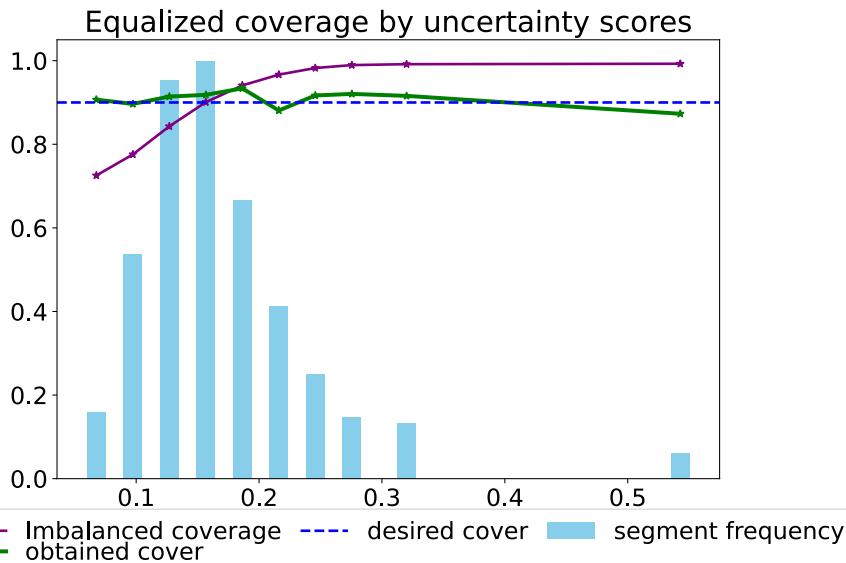
# Fairness

**Beyond language**

# Fairness

## Beyond language

Can also be applied on continuous attributes

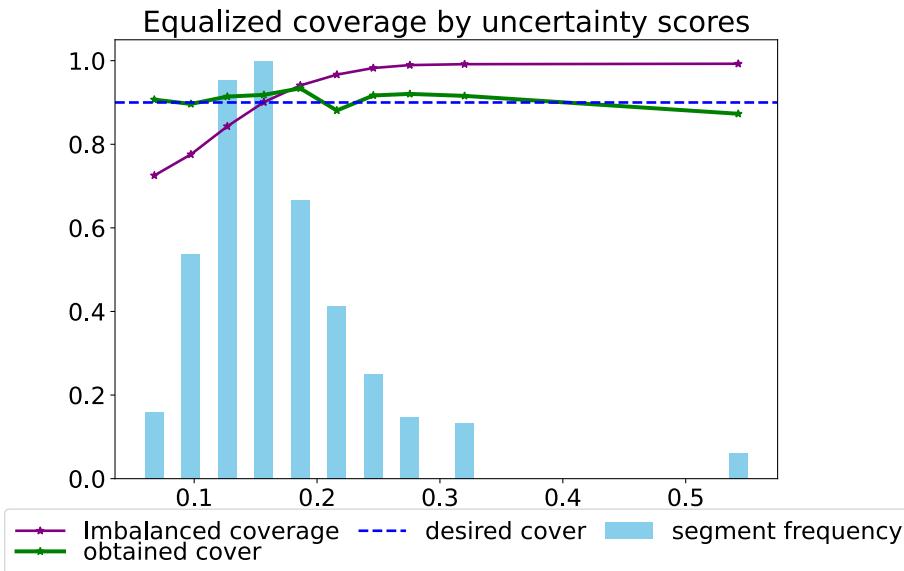


# Fairness

## Beyond language

Can also be applied on continuous attributes

... sensitive, demographic attributes



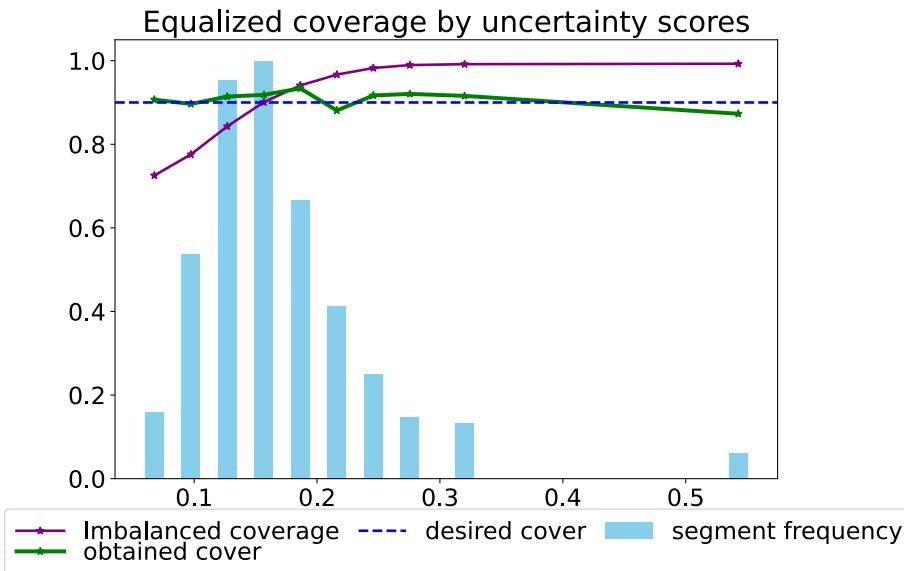
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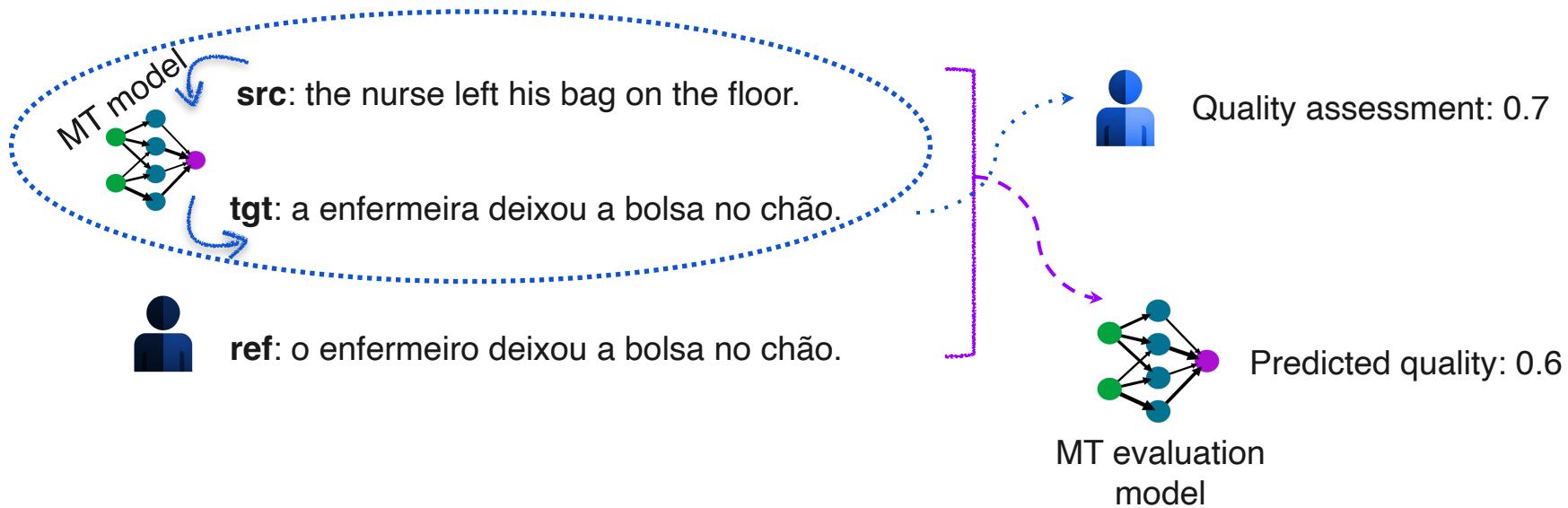
- Gender bias
- Racial bias
- Religious bias
- Age bias
- ...

... other linguistic aspects

- Style preference
- Formality
- Example difficulty
- Syntactic complexity

# Conformalising MT

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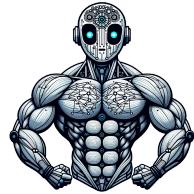


# What about generation?

the nurse left his bag on the floor.   ⇒   a enfermeira deixou a bolsa no chão.

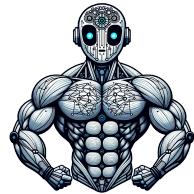
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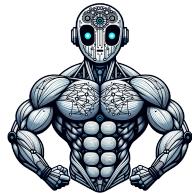
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→ sample →

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→ sample →

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o enfermeiro deixou a bolsa no chão  
a enfermeira deixou a mochila dele no chão

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sample

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## Sentence level uncertainty

Access to output probabilities?

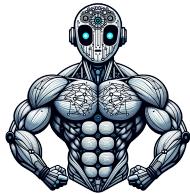
- Entropy-based uncertainty

No access to output probabilities?

- Deviation of output tokens
- Ask the model!

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## Sentence level conformal prediction

- As a sentence classification task
  - Treat each sample as a label
- Use one of the uncertainty estimates as non-conformity

# What about generation?

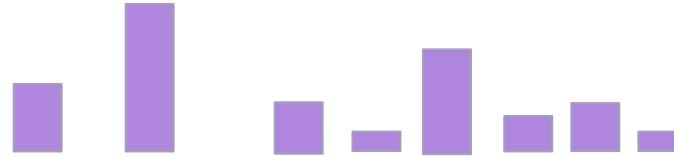
the nurse left his bag on the floor. ➔

# What about generation?

the nurse left his bag on the floor.



a enfermeira deixou a bolsa no chão .

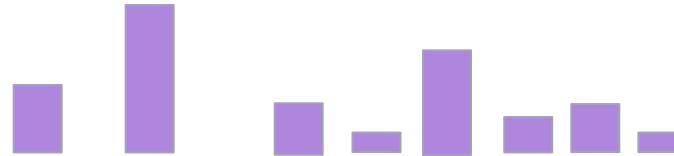


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## Word level uncertainty

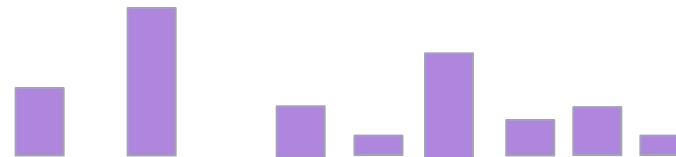
- Output probabilities
- Entropy-based methods
- Sampling + semantic entropy

# What about generation?

the nurse left his bag on the floor.



a enfermeira deixou a bolsa no chão .



## Word level uncertainty

- Output probabilities
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## Word level conformal prediction

✗ exchangeability assumption

# Conformalised Generation

Non-exchangeable CP bound (Barber et al., 2023)

# Conformalised Generation

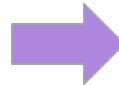
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non ex.

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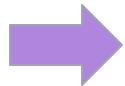
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non ex.

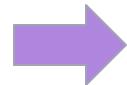
coverage gap



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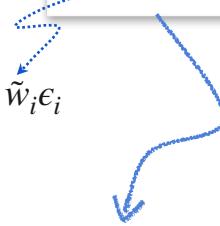
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non ex.

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coverage gap

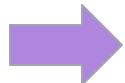


We want this to be small!

# Conformalised Generation

Non-exchangeable CP bound (Barber et al., 2023)

$$\mathbb{P}(Y_{\text{test}} \in C_{\hat{q}}(X_{\text{test}})) \geq 1 - \alpha$$



non ex.

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$$\epsilon_i = d_{TV}((x_i, y_i), (x_{\text{test}}, y_{\text{test}}))$$

... not that easy to compute

coverage gap

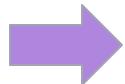


We want this to be small!

# Conformalised Generation

Non-exchangeable CP bound (Barber et al., 2023)

$$\mathbb{P}(Y_{\text{test}} \in C_{\hat{q}}(X_{\text{test}})) \geq 1 - \alpha$$



non ex.

$$\mathbb{P}(Y_{\text{test}} \in C_{\hat{q}}(X_{\text{test}})) \geq 1 - \alpha - \sum_{i=1}^n \tilde{w}_i \epsilon_i$$

coverage gap

... not that easy to compute

We want this to be small!

meaningful weights  $\Rightarrow$  small coverage gap

# Conformalised Generation

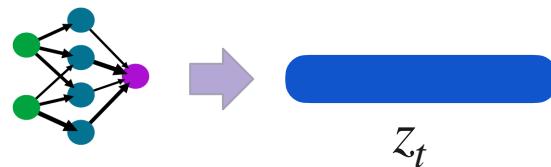
## Our solution:

- Use the hidden representation of our LM
- Select a calibration set at every step of generation
- kNN to dynamically select the calibration set from a datastore
- distance metric to compute the weights

# Conformalised Generation

## Our solution:

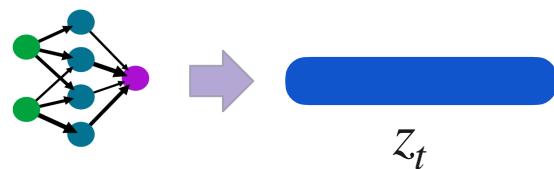
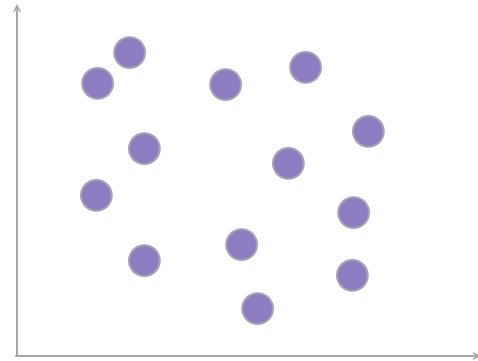
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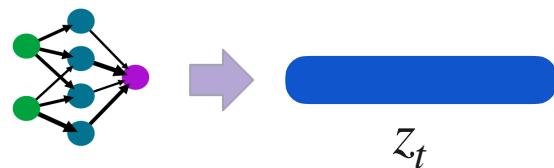
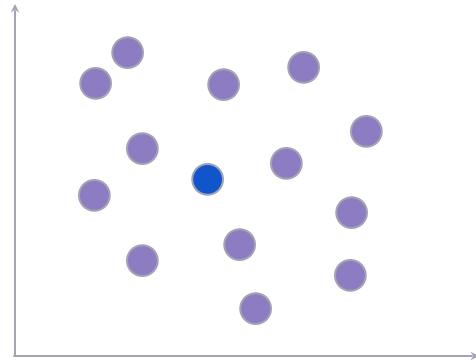
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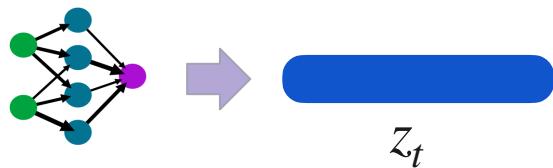
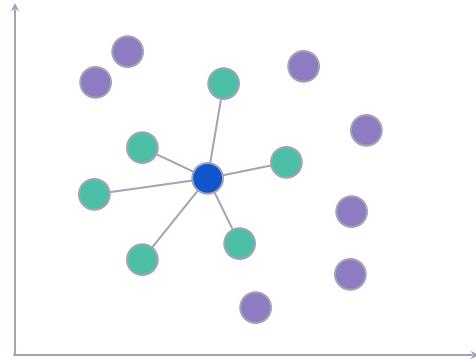
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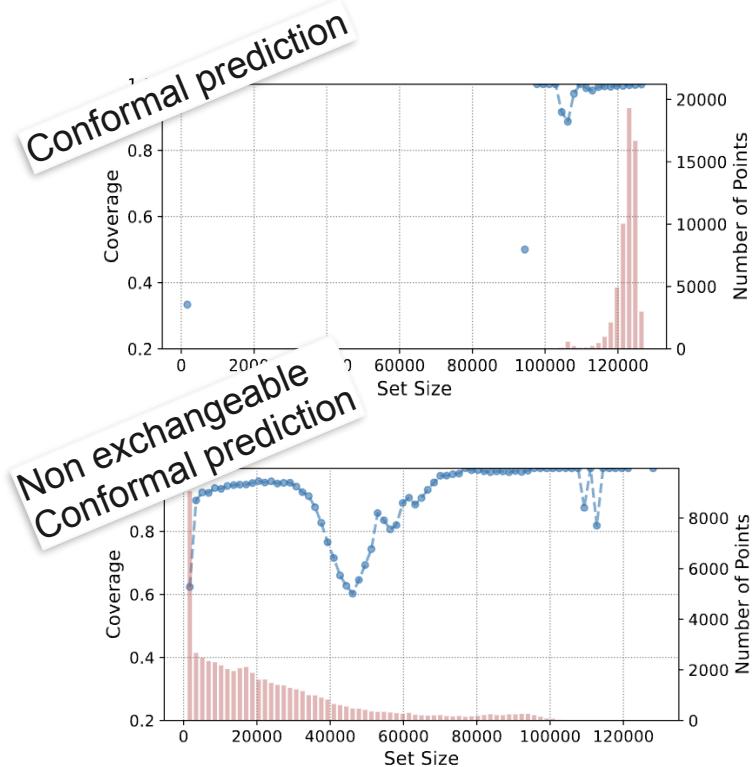
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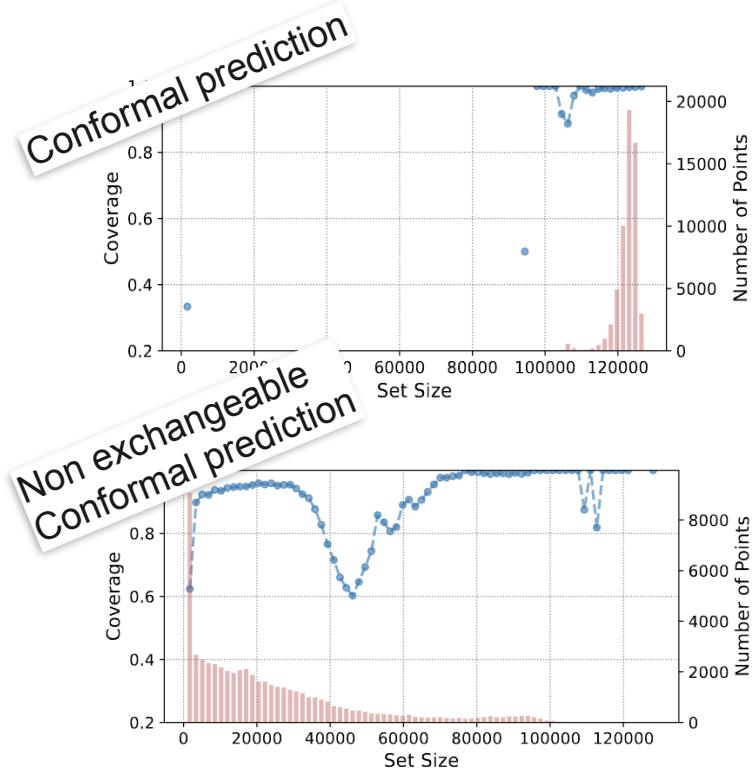
# Conformalising Machine Translation

# Conformalising Machine Translation



# Conformalising Machine Translation

- ✓ Tighter confidence intervals
- ✓ Better “worst-case” coverage

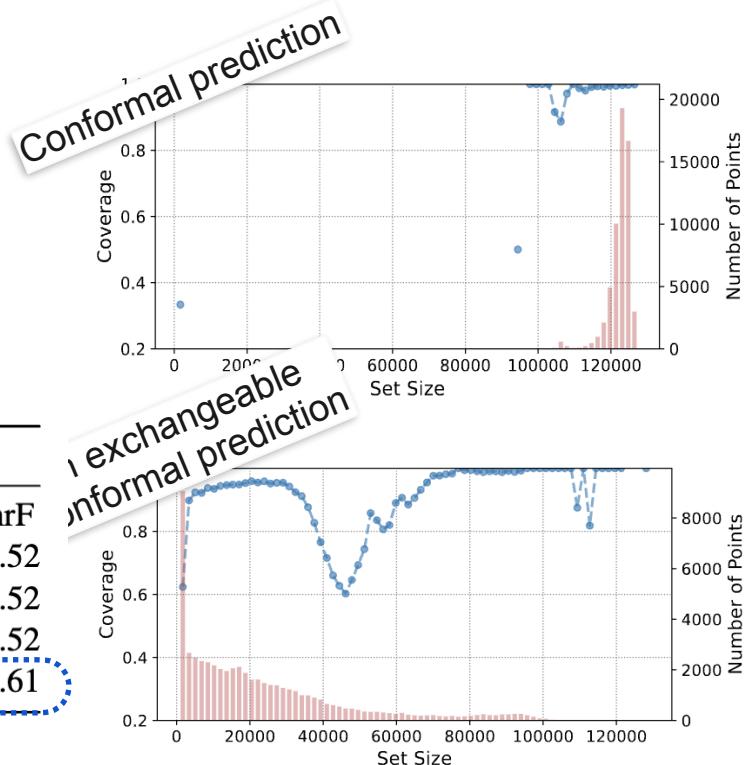


# Conformalising Machine Translation

- ✓ Tighter confidence intervals
- ✓ Better “worst-case” coverage
- ✓ Comparable or even better performance to nucleus and top-k sampling

	En-De			En-Ja		
	BLEU	COMET	ChrF	BLEU	COMET	ChrF
Nucleus	27.63	0.89	54.8	10.61	0.59	36.52
Top-k	27.63	0.89	54.79	10.61	0.59	36.52
Conformal	27.63	0.89	54.8	10.61	0.59	36.52
Non-Ex Conformal	27.65	0.9	54.82	10.74	0.59	36.61

M2M100 - WMT 2022

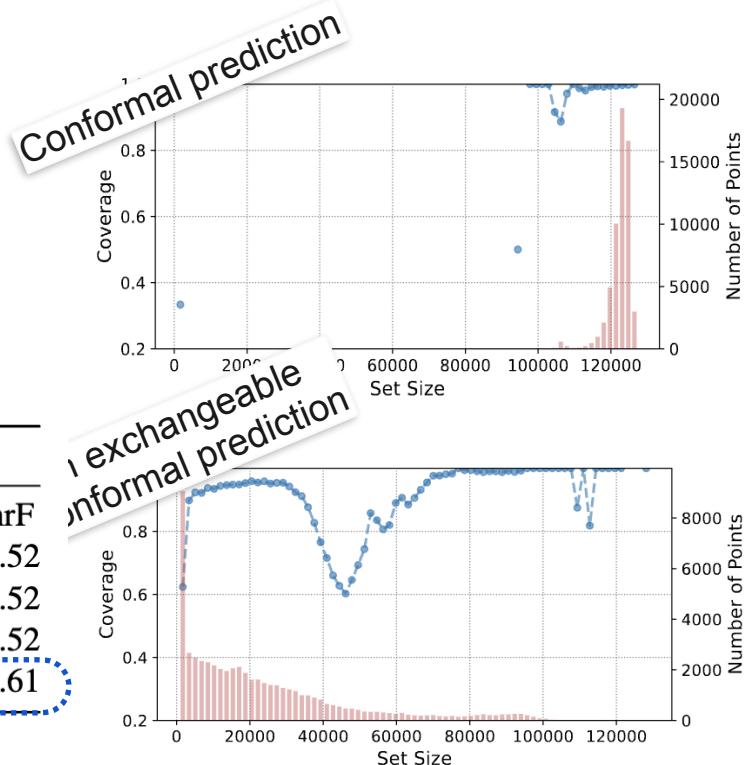


# Conformalising Machine Translation

- ✓ Tighter confidence intervals
- ✓ Better “worst-case” coverage
- ✓ Comparable or even better performance to nucleus and top-k sampling
- ✓ Robust to noise injection!

	En-De			En-Ja		
	BLEU	COMET	ChrF	BLEU	COMET	ChrF
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M2M100 - WMT 2022



# Beyond coverage

We can calibrate for any loss function

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⋮

**monotone  
bounded**

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- ❖ False negative rate
- ❖ Token-level F1 score
- ❖  $\lambda$ -insensitive absolute loss

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Robust method

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- ❖ Token-level F1 score
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- ✓ Distribution shifts
- ✓ Changepoints

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width **adapted** to the distribution shifts while maintaining performance for the controlled value

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⋮

**monotone  
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- ❖ Token-level F1 score
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Robust method

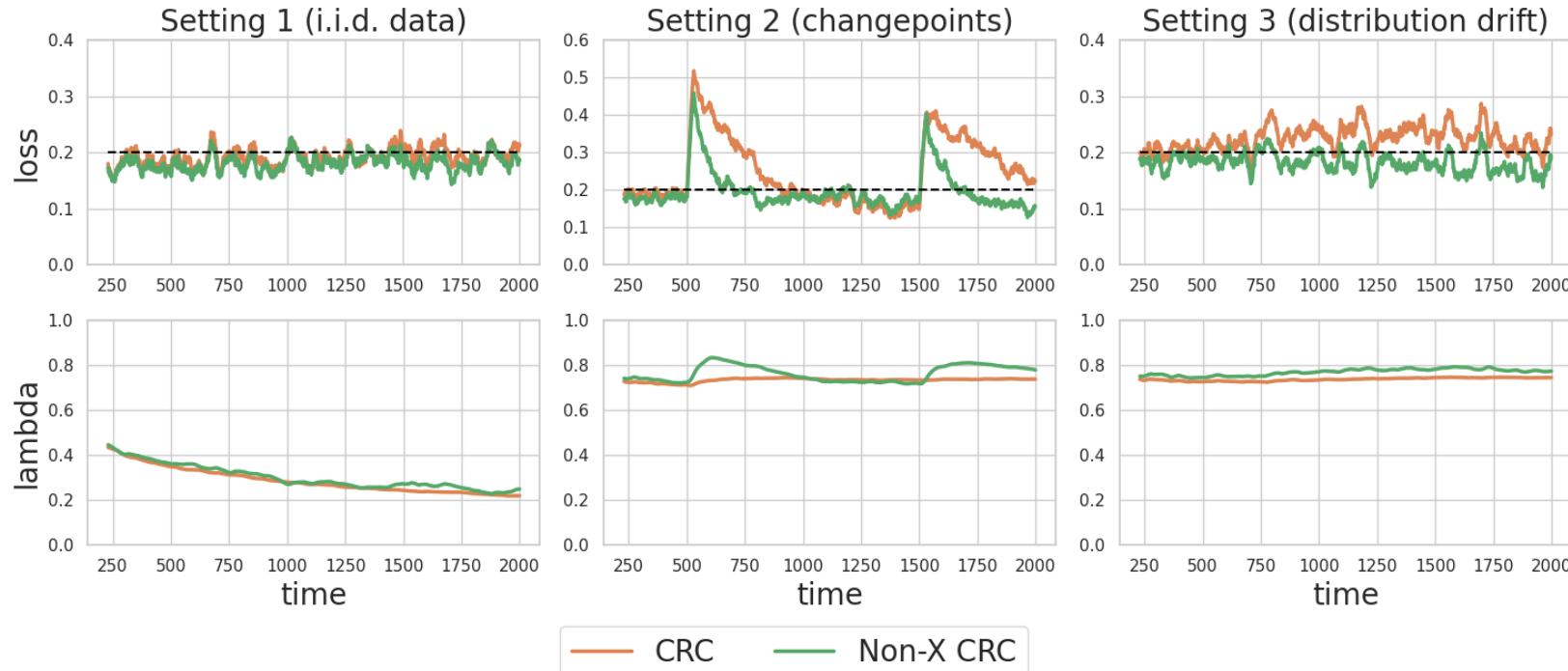
- ✓ Distribution shifts
- ✓ Changepoints

Efficient method

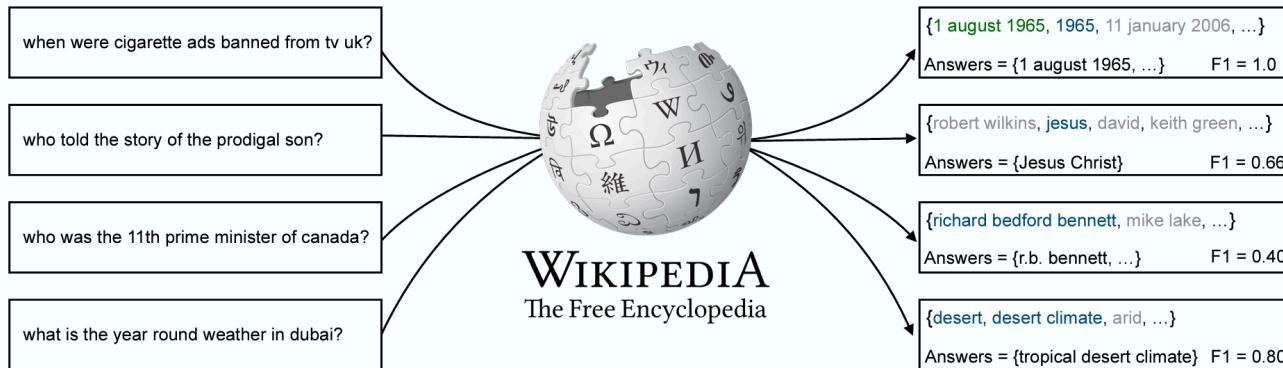
- ✓ Tighter prediction sets

width **adapted** to the distribution shifts while maintaining performance for the controlled value

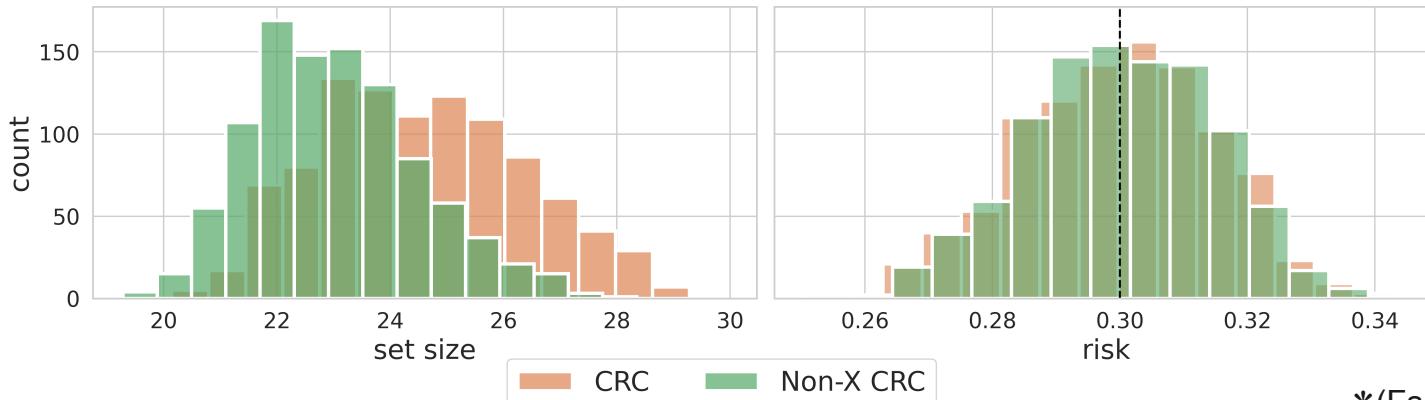
# Simulated time-series data



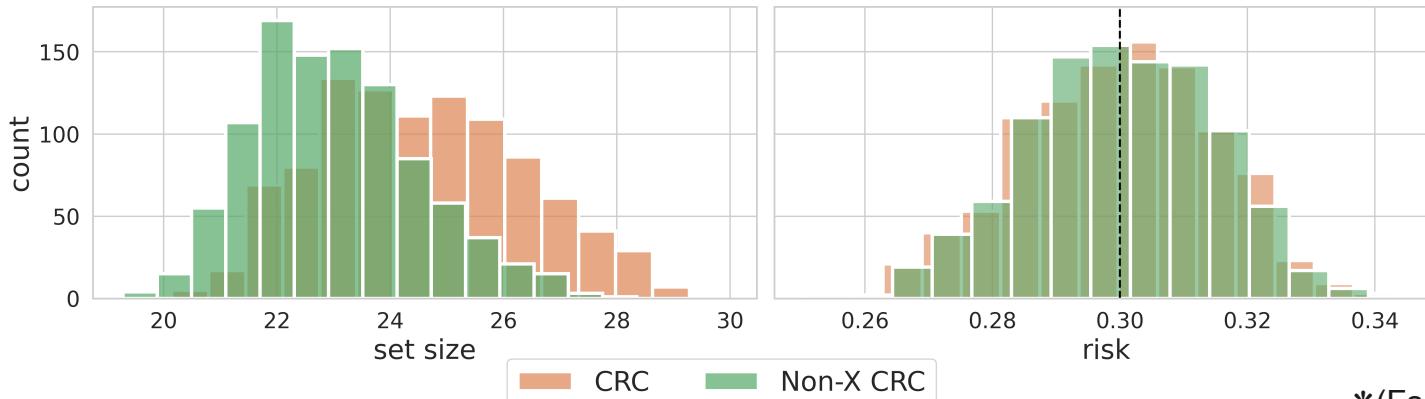
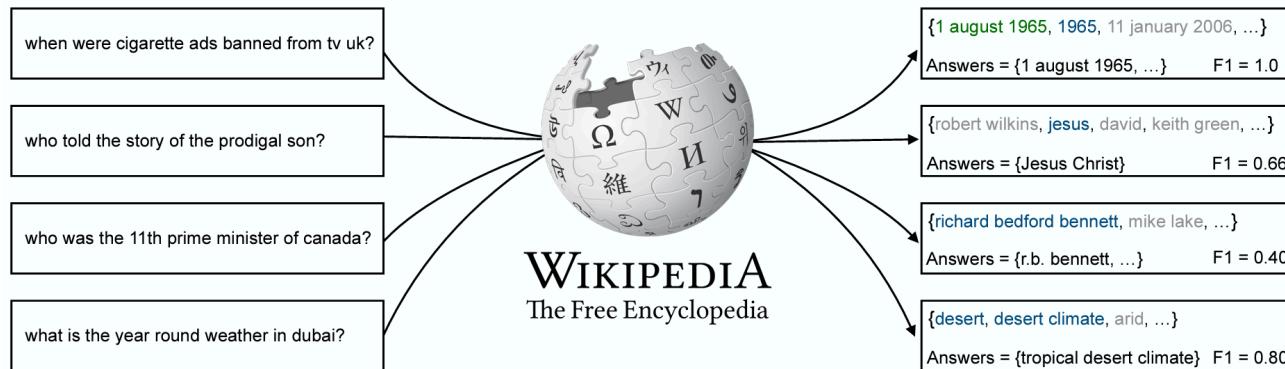
# Open QA



Token level  
F1-score

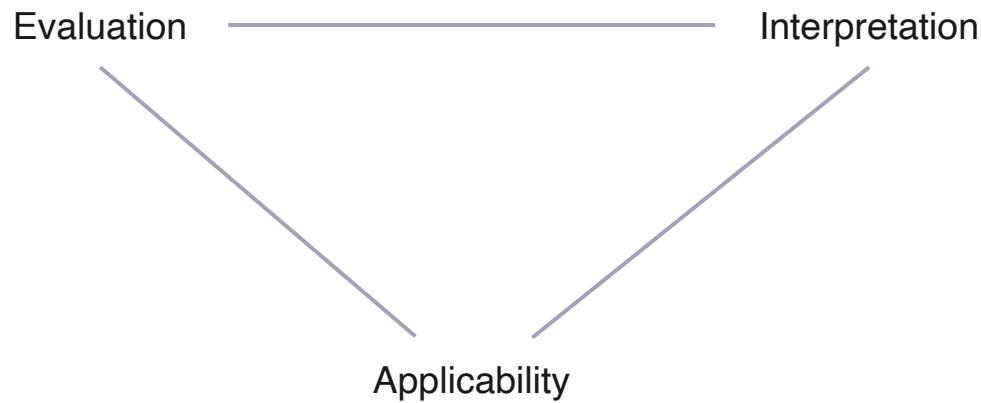


# Open QA

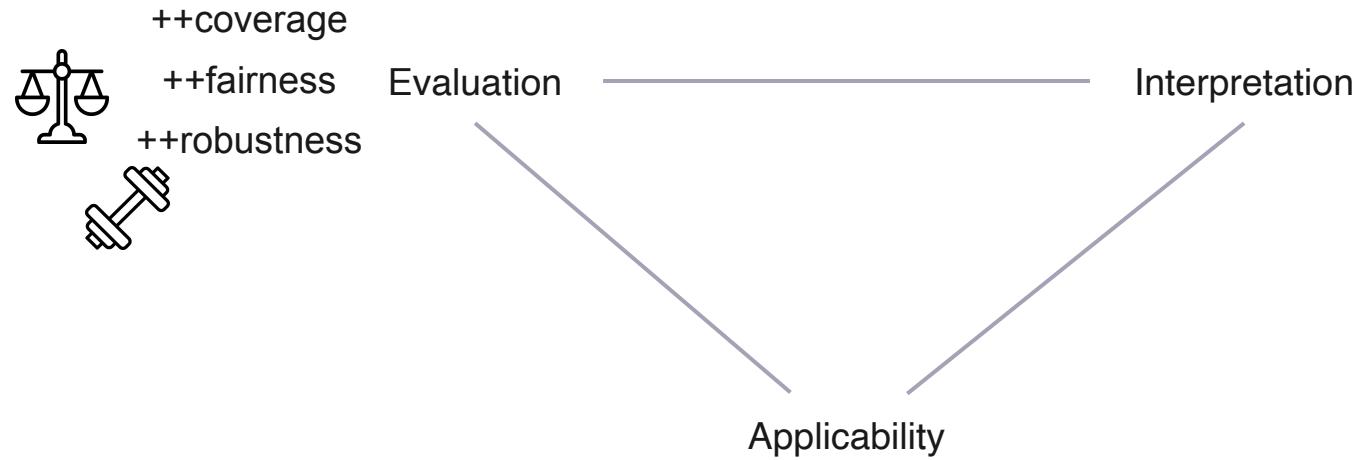


# Conformal prediction

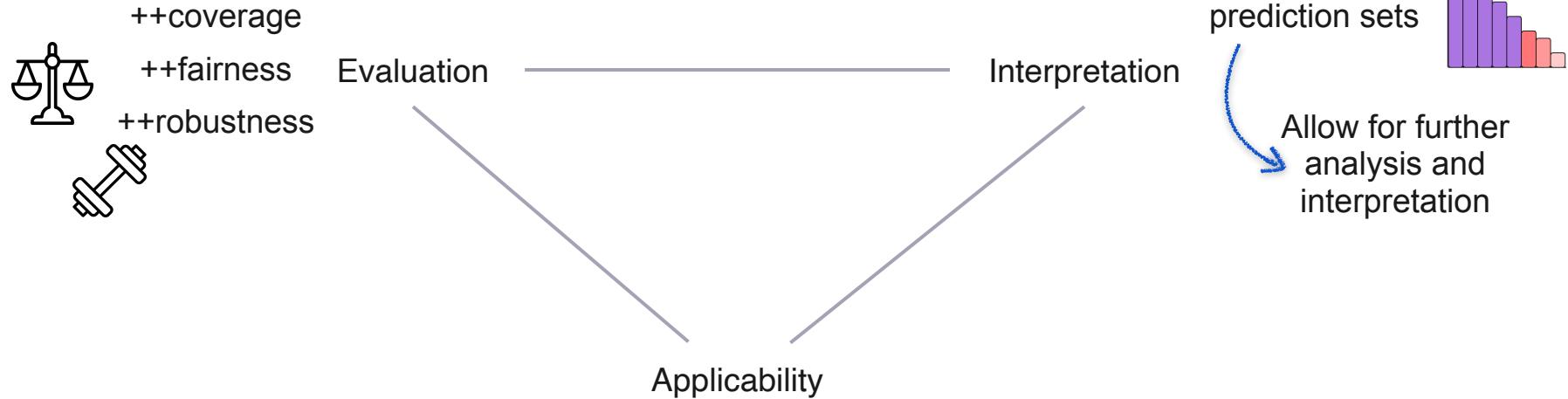
# Conformal prediction



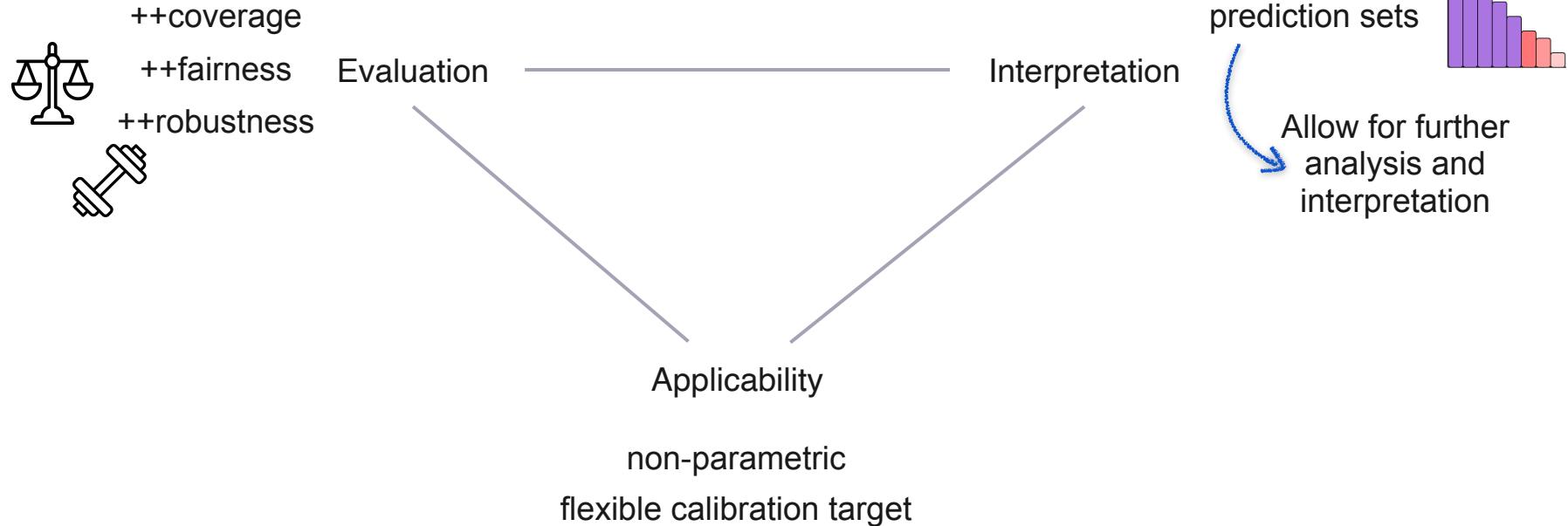
# Conformal prediction



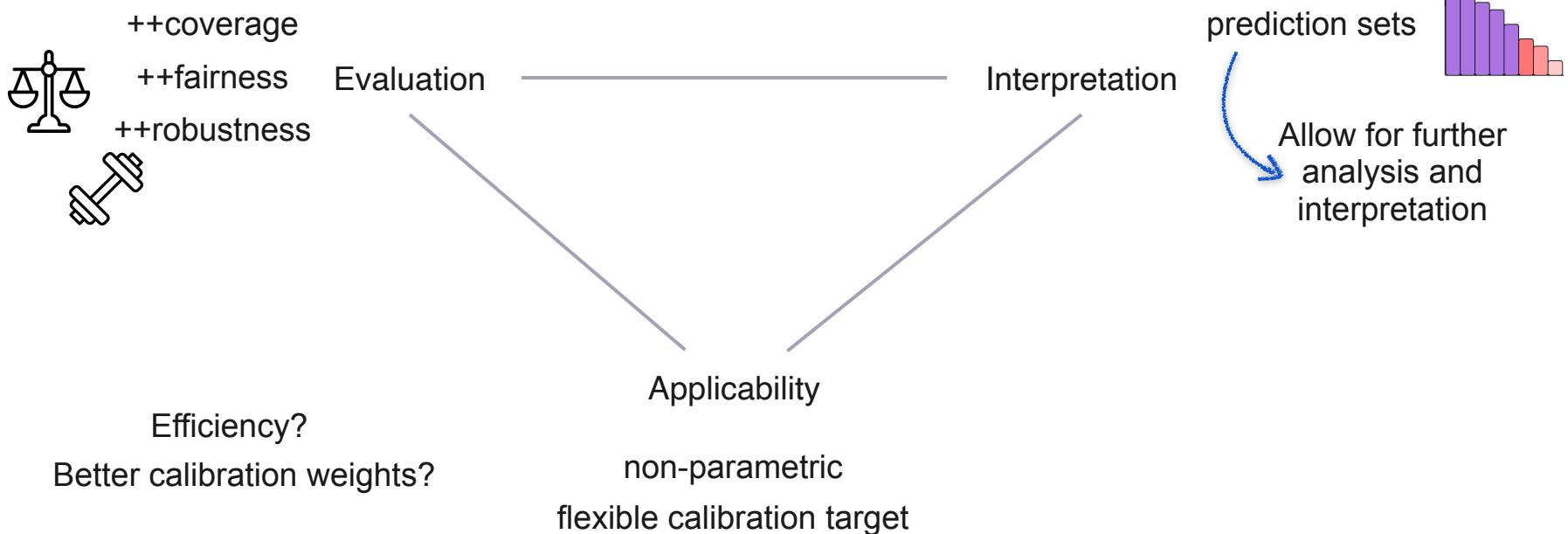
# Conformal prediction



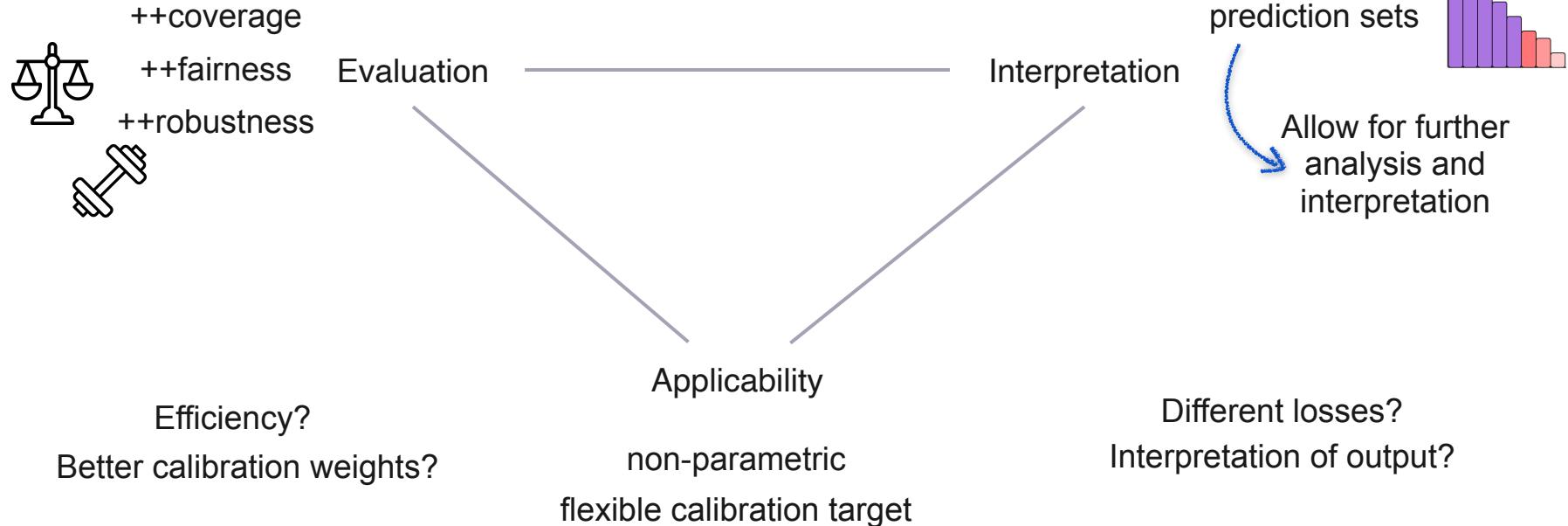
# Conformal prediction



# Conformal prediction

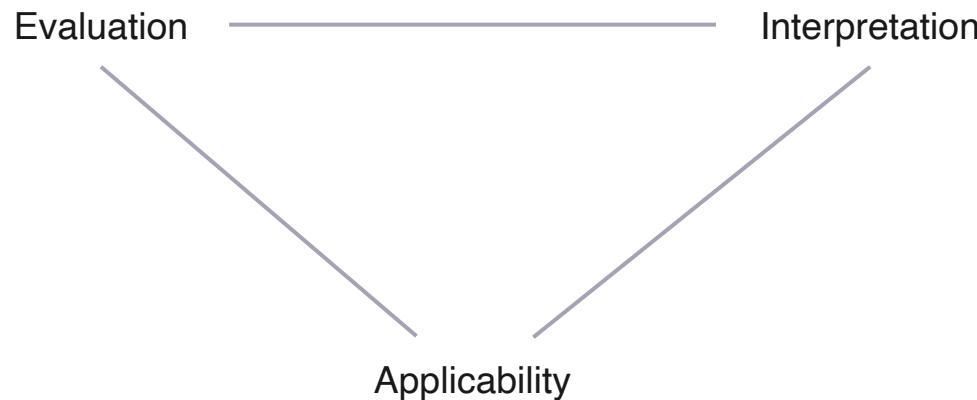


# Conformal prediction



# Overall

Towards a more accessible version of uncertainty



# Thank you!



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