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# **Machine Learning Overview**

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# **Introduction to Machine Learning**

# Machine Learning is...

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**Machine learning is a subset of artificial intelligence in the field of computer science that often uses statistical techniques to give computers the ability to "learn" (i.e., progressively improve performance on a specific task) with data, without being explicitly programmed.**



# Machine Learning is...

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A computer program is said to learn from experience E with respect to some class of tasks T and performance measure P if its performance at tasks in T, as measured by P, improves with experience E.

Tom Mitchell

$$E * T = P$$

Experience

\*

Task

=

Performance

**Input Data:**

- Housing prices
- Customer transactions
- Clickstream data
- Images

**Task:**

- Predict prices
- Segment customers
- Optimize user flows
- Categorize images

**Performance:**

- Accurate prices
- Coherent groupings
- KPI lifts
- Correctly sorted images

# Machine Learning is...

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Machine learning is programming computers to optimize a performance criterion using example data or past experience.

-- Ethem Alpaydin

The goal of machine learning is to develop methods that can automatically detect patterns in data, and then to use the uncovered patterns to predict future data or other outcomes of interest.

-- Kevin P. Murphy

The field of pattern recognition is concerned with the automatic discovery of regularities in data through the use of computer algorithms and with the use of these regularities to take actions.

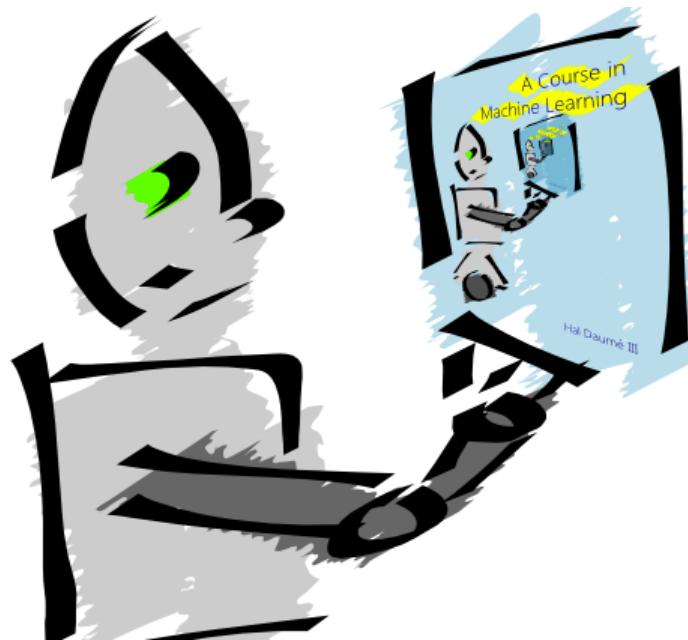
-- Christopher M. Bishop

# Machine Learning is...

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**Machine learning is about predicting the future based on the past.**

-- Hal Daume III

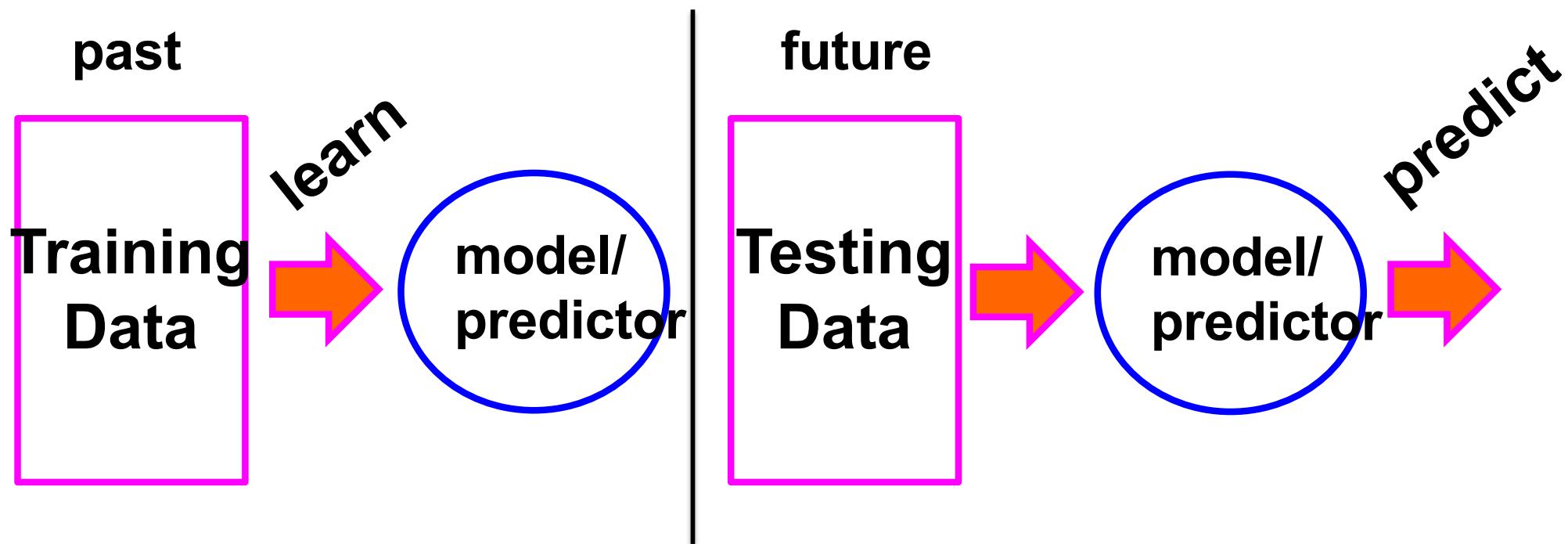


# Machine Learning is...

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Machine learning is about predicting the future based on the past.

-- Hal Daume III



# The machine learning framework

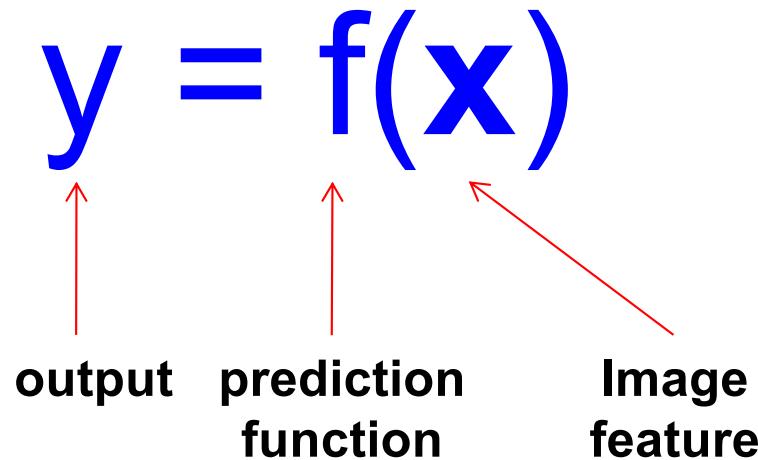
---

- Apply a prediction function to a feature representation of the image to get the desired output:

$$f(\text{apple}) = \text{"apple"}$$
$$f(\text{tomato}) = \text{"tomato"}$$
$$f(\text{cow}) = \text{"cow"}$$

# The machine learning framework

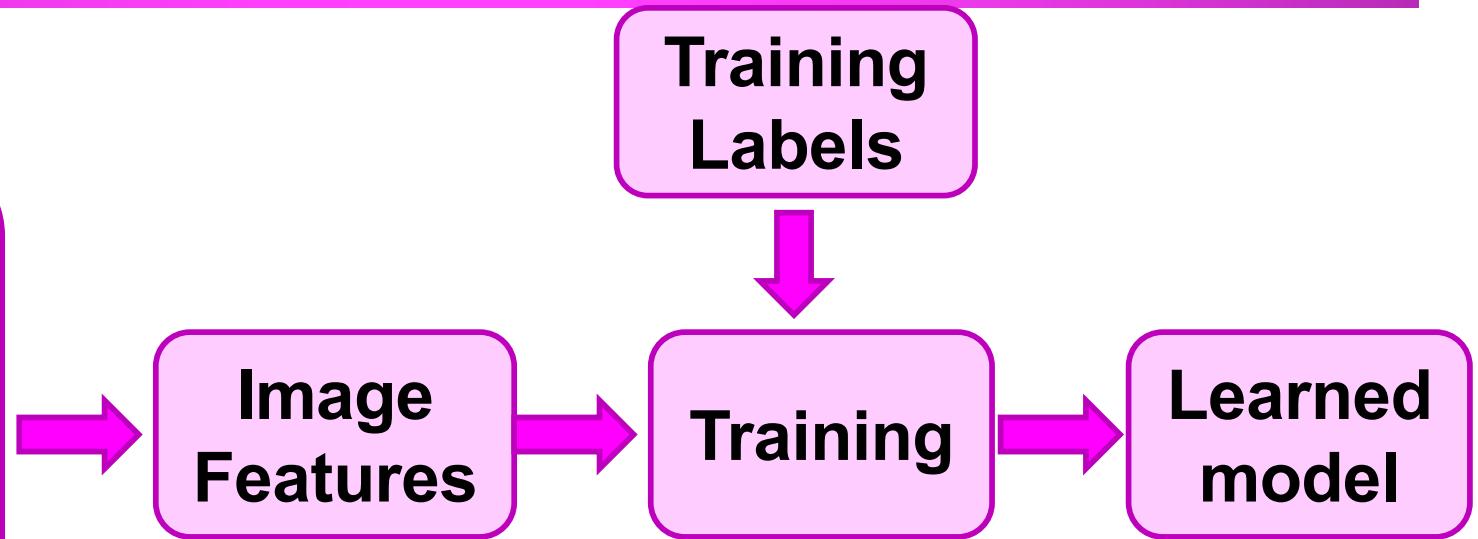
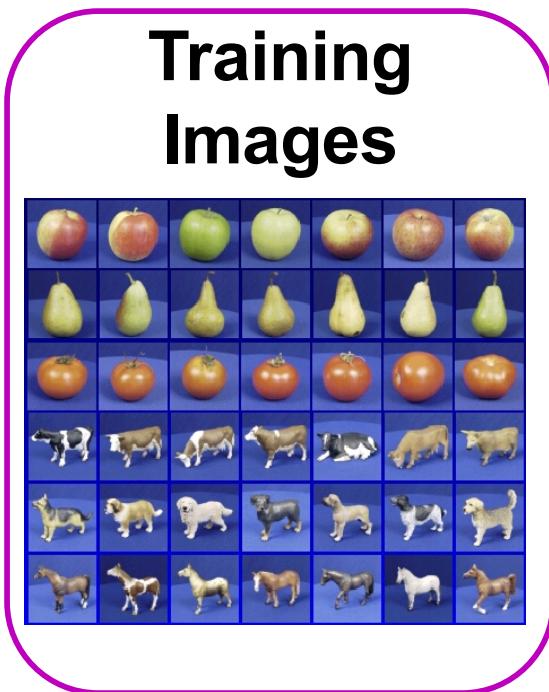
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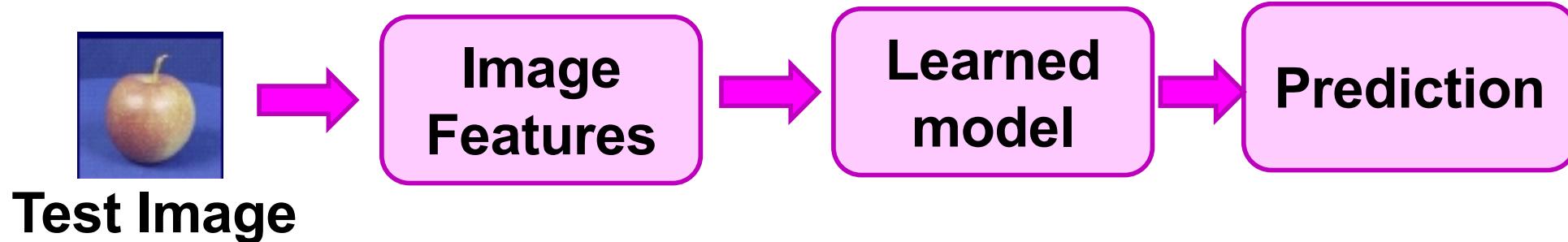
- **Training:** given a *training set* of labeled examples  $\{(\mathbf{x}_1, y_1), \dots, (\mathbf{x}_N, y_N)\}$ , estimate the prediction function  $f$  by minimizing the prediction error on the training set
- **Testing:** apply  $f$  to a never before seen *test example*  $\mathbf{x}$  and output the predicted value  $y = f(\mathbf{x})$

# Steps

## Training



## Testing



# Great opportunities to improve productivity in all walks of life

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McKinsey Global Institute

## Big data: The next frontier for innovation, competition, and productivity

### *Big data—a growing torrent*

\$600 to buy a disk drive that can store all of the world's music

5 billion mobile phones in use in 2010

30 billion pieces of content shared on Facebook every month

40% projected growth in global data generated per year vs. 5% growth in global IT spending

235 terabytes data collected by the US Library of Congress in April 2011

15 out of 17 sectors in the United States have more data stored per company than the US Library of Congress

### *Big data—capturing its value*

\$300 billion potential annual value to US health care—more than double the total annual health care spending in Spain

€250 billion potential annual value to Europe's public sector administration—more than GDP of Greece

\$600 billion potential annual consumer surplus from using personal location data globally

60% potential increase in retailers' operating margins possible with big data

140,000–190,000 more deep analytical talent positions, and

1.5 million more data-savvy managers needed to take full advantage of big data in the United States

# Great Opportunities to Solve Society's Major Problems

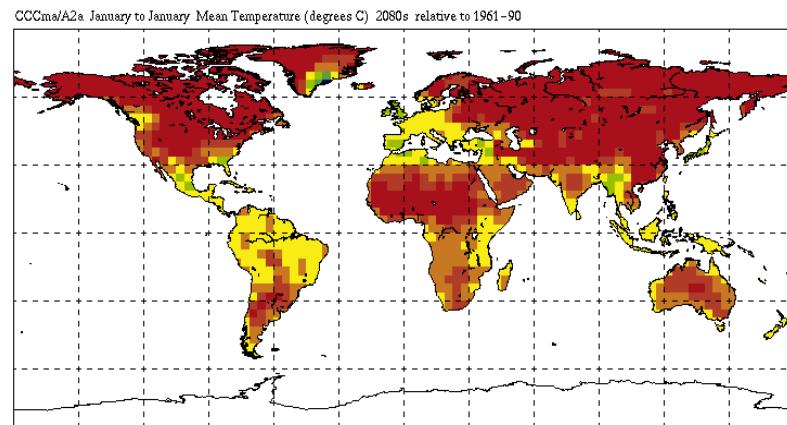
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Improving health care and reducing costs



Finding alternative/ green energy sources



Predicting the impact of climate change



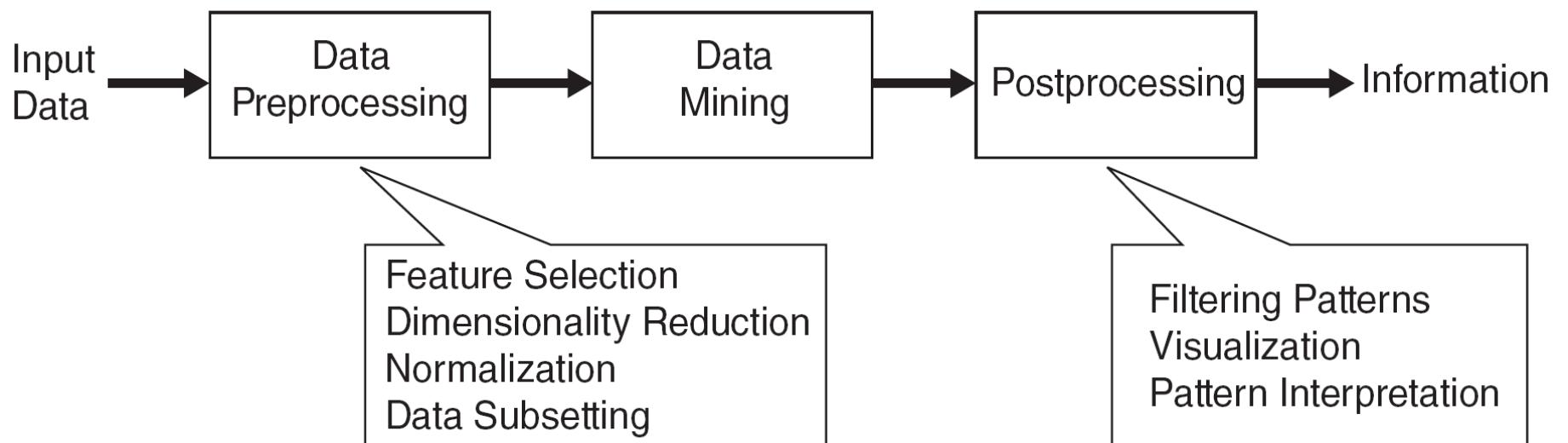
Reducing hunger and poverty by increasing agriculture production

# What is Data Mining?

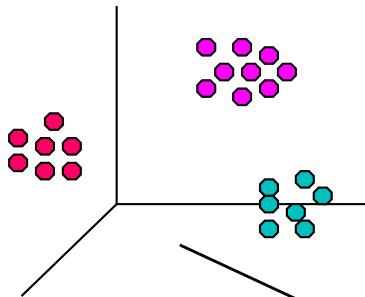
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## ● Many Definitions

- Non-trivial extraction of implicit, previously unknown and potentially useful information from data
- Exploration & analysis, by automatic or semi-automatic means, of large quantities of data in order to discover meaningful patterns



# ML Tasks ...



*Clustering*

**Data**

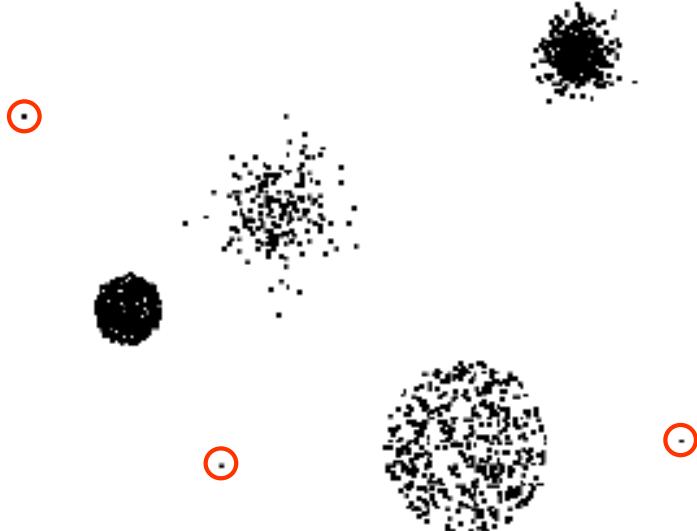
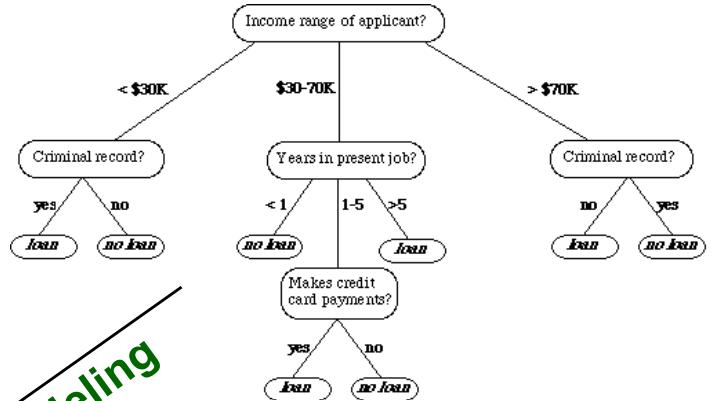
Tid	Refund	Marital Status	Taxable Income	Cheat
1	Yes	Single	125K	No
2	No	Married	100K	No
3	No	Single	70K	No
4	Yes	Married	120K	No
5	No	Divorced	95K	Yes
6	No	Married	60K	No
7	Yes	Divorced	220K	No
8	No	Single	85K	Yes
9	No	Married	75K	No
10	No	Single	90K	Yes
11	No	Married	60K	No
12	Yes	Divorced	220K	No
13	No	Single	85K	Yes
14	No	Married	75K	No
15	No	Single	90K	Yes



*Association Rules*

*Predictive Modeling*

*Anomaly Detection*



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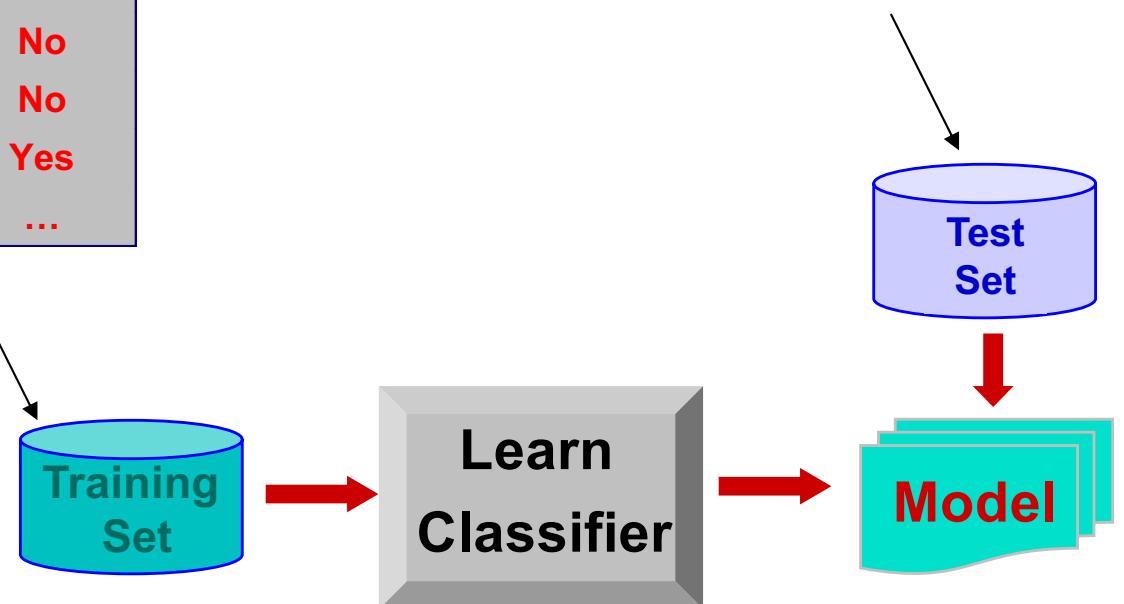
# **Classification**

# Classification Example

categorical categorical quantitative class

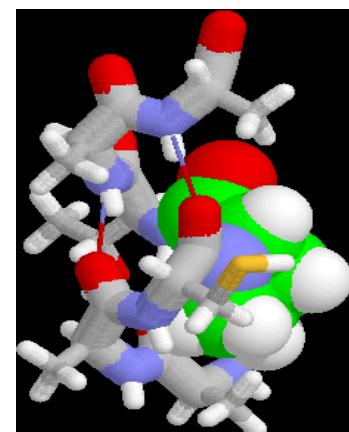
Tid	Employed	Level of Education	# years at present address	Credit Worthy
1	Yes	Graduate	5	Yes
2	Yes	High School	2	No
3	No	Undergrad	1	No
4	Yes	High School	10	Yes
...	...	...	...	...

Tid	Employed	Level of Education	# years at present address	Credit Worthy
1	Yes	Undergrad	7	?
2	No	Graduate	3	?
3	Yes	High School	2	?
...	...	...	...	...



# Examples of Classification Task

- Classifying credit card transactions as legitimate or fraudulent
- Classifying land covers (water bodies, urban areas, forests, etc.) using satellite data
- Categorizing news stories as finance, weather, entertainment, sports, etc
- Identifying intruders in the cyberspace
- Predicting tumor cells as benign or malignant
- Classifying secondary structures of protein as alpha-helix, beta-sheet, or random coil



# Classification: Application 1

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- Fraud Detection
  - **Goal:** Predict fraudulent cases in credit card transactions.
  - **Approach:**
    - ◆ Use credit card transactions and the information on its account-holder as attributes.
      - When does a customer buy, what does he buy, how often he pays on time, etc
    - ◆ Label past transactions as fraud or fair transactions. This forms the class attribute.
    - ◆ Learn a model for the class of the transactions.
    - ◆ Use this model to detect fraud by observing credit card transactions on an account.

# Classification: Application 2

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- Churn prediction for telephone customers
  - **Goal:** To predict whether a customer is likely to be lost to a competitor.
  - **Approach:**
    - ◆ Use detailed record of transactions with each of the past and present customers, to find attributes.
      - How often the customer calls, where he calls, what time-of-the day he calls most, his financial status, marital status, etc.
    - ◆ Label the customers as loyal or disloyal.
    - ◆ Find a model for loyalty.

From [Berry & Linoff] Data Mining Techniques, 1997

# Classification: Application 3

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## ● Sky Survey Cataloging

- **Goal:** To predict class (star or galaxy) of sky objects, especially visually faint ones, based on the telescopic survey images (from Palomar Observatory).
  - 3000 images with 23,040 x 23,040 pixels per image.
- **Approach:**
  - ◆ Segment the image.
  - ◆ Measure image attributes (features) - 40 of them per object.
  - ◆ Model the class based on these features.
  - ◆ Success Story: Could find 16 new high red-shift quasars, some of the farthest objects that are difficult to find!

From [Fayyad, et.al.] Advances in Knowledge Discovery and Data Mining, 1996

# Classifiers in MLlib

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## Linear models

- classification (SVMs, logistic regression)
- linear regression (least squares, Lasso, ridge)

## Decision trees

## Ensembles of decision trees

- random forests
- gradient-boosted trees

## Naive Bayes

## Isotonic regression

# Mathematical Foundation

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- Most classifiers can be expressed as finding the minimum of a convex objective function

$$f(\mathbf{w}) = \lambda R(\mathbf{w}) + \frac{1}{n} \sum_{i=1}^n L(\mathbf{w}; \mathbf{x}_i, y_i)$$

Where

$f(\mathbf{w})$  is the objective function

$L(\mathbf{w}; \mathbf{x}_i, y_i)$  is the loss function - difference between actual ( $y_i$ ) and predicted value using set of feature vector ( $\mathbf{x}_i$ ), using the choice of weights ( $\mathbf{w}$ )

$\lambda R(\mathbf{w})$  regularization term that controls tradeoff between minimizing loss and model complexity.

# Loss Functions

## Types of Loss functions:

	loss function $L(\mathbf{w}; \mathbf{x}, y)$	gradient or sub-gradient
hinge loss	$\max\{0, 1 - y\mathbf{w}^T \mathbf{x}\}, \quad y \in \{-1, +1\}$	$\begin{cases} -y \cdot \mathbf{x} & \text{if } y\mathbf{w}^T \mathbf{x} < 1, \\ 0 & \text{otherwise.} \end{cases}$
logistic loss	$\log(1 + \exp(-y\mathbf{w}^T \mathbf{x})), \quad y \in \{-1, +1\}$	$-y \left(1 - \frac{1}{1+\exp(-y\mathbf{w}^T \mathbf{x})}\right) \cdot \mathbf{x}$
squared loss	$\frac{1}{2}(\mathbf{w}^T \mathbf{x} - y)^2, \quad y \in \mathbb{R}$	$(\mathbf{w}^T \mathbf{x} - y) \cdot \mathbf{x}$

## Types of Regularizer

	regularizer $R(\mathbf{w})$	gradient or sub-gradient
zero (unregularized)	0	0
L2	$\frac{1}{2} \ \mathbf{w}\ _2^2$	$\mathbf{w}$
L1	$\ \mathbf{w}\ _1$	$\text{sign}(\mathbf{w})$
elastic net	$\alpha \ \mathbf{w}\ _1 + (1 - \alpha) \frac{1}{2} \ \mathbf{w}\ _2^2$	$\alpha \text{sign}(\mathbf{w}) + (1 - \alpha)\mathbf{w}$

# Logistic Regression

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Logistic Regression is a linear classifier with following loss function:

$$L(\mathbf{w}; \mathbf{x}, y) := \log(1 + \exp(-y\mathbf{w}^T \mathbf{x})).$$

Given a data point, classification is done by evaluating:

$$f(z) = \frac{1}{1 + e^{-z}}$$

where  $z = \mathbf{w}^T \mathbf{x}$

If  $f(z) > 0.5$ , assign class 0, otherwise class 1

More details at:

<https://spark.apache.org/docs/2.2.0/mllib-linear-methods.html#logistic-regression>

# Logistic Regression in Spark MLLib

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Easiest way to get started:  
LogisticRegressionWithLBFGS  
- limited memory BFGS algorithm

```
val lr = new LogisticRegression()  
    .setMaxIter(10)  
    .setRegParam(0.3)  
    .setElasticNetParam(0.8)
```

- should be tried first as base model
- More details at:

<https://spark.apache.org/docs/2.2.1/api/java/org/apache/spark/ml/classification/LogisticRegressionWithLBFGS.html>

# Logistic Regression in Spark MLlib

```
def setElasticNetParam(value: Double): LogisticRegression.this.type
  Set the ElasticNet mixing parameter.

def setFamily(value: String): LogisticRegression.this.type
  Sets the value of param family.

def setFeaturesCol(value: String): LogisticRegression

def setFitIntercept(value: Boolean): LogisticRegression.this.type
  Whether to fit an intercept term.

def setLabelCol(value: String): LogisticRegression

def setMaxIter(value: Int): LogisticRegression.this.type
  Set the maximum number of iterations.

def setPredictionCol(value: String): LogisticRegression

def setProbabilityCol(value: String): LogisticRegression

def setRawPredictionCol(value: String): LogisticRegression

def setRegParam(value: Double): LogisticRegression.this.type
  Set the regularization parameter.

def setStandardization(value: Boolean): LogisticRegression.this.type
  Whether to standardize the training features before fitting the model.

def setThreshold(value: Double): LogisticRegression.this.type
  Set threshold in binary classification, in range [0, 1].
```

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```
def setThresholds(value: Array[Double]): LogisticRegression.this.type
  Set thresholds in multiclass (or binary) classification to adjust the probability of predicting each class.
```

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```
def setTol(value: Double): LogisticRegression.this.type
  Set the convergence tolerance of iterations.
```

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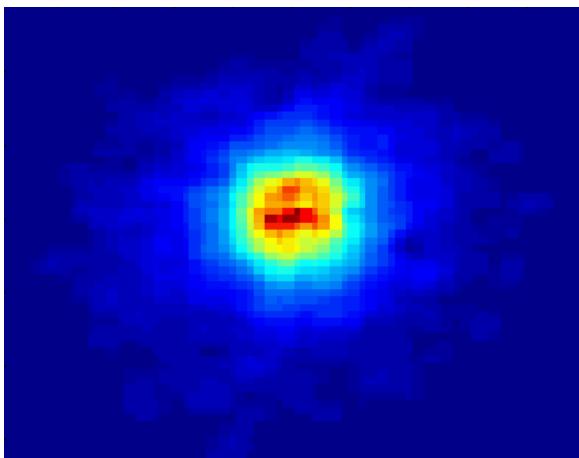
```
def setWeightCol(value: String): LogisticRegression.this.type
  Sets the value of param weightCol.
```

**More details**

# Classifying Galaxies

Courtesy: <http://aps.umn.edu>

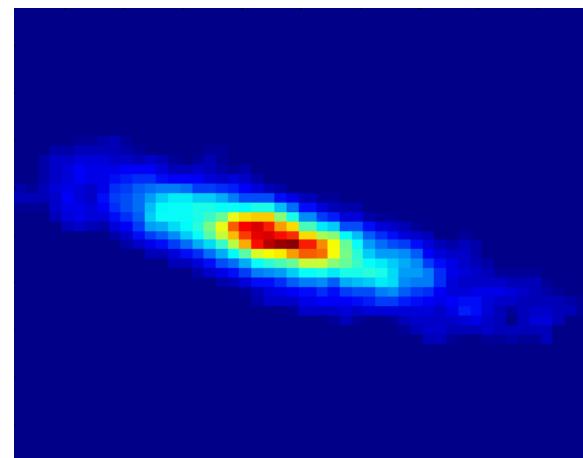
*Early*



**Class:**

- Stages of Formation

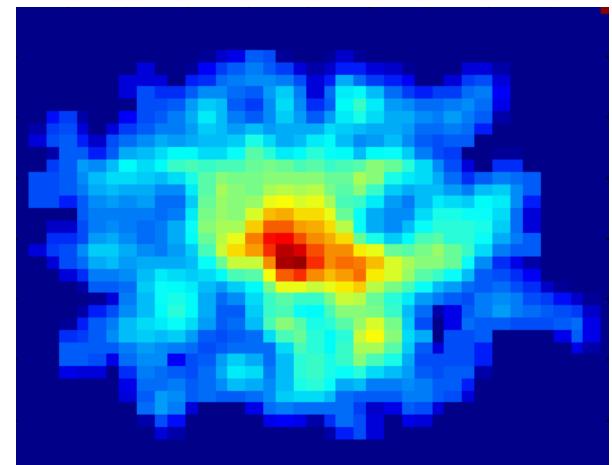
*Intermediate*



**Attributes:**

- Image features,
- Characteristics of light waves received, etc.

*Late*



**Data Size:**

- 72 million stars, 20 million galaxies
- Object Catalog: 9 GB
- Image Database: 150 GB

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# Regression

# Regression

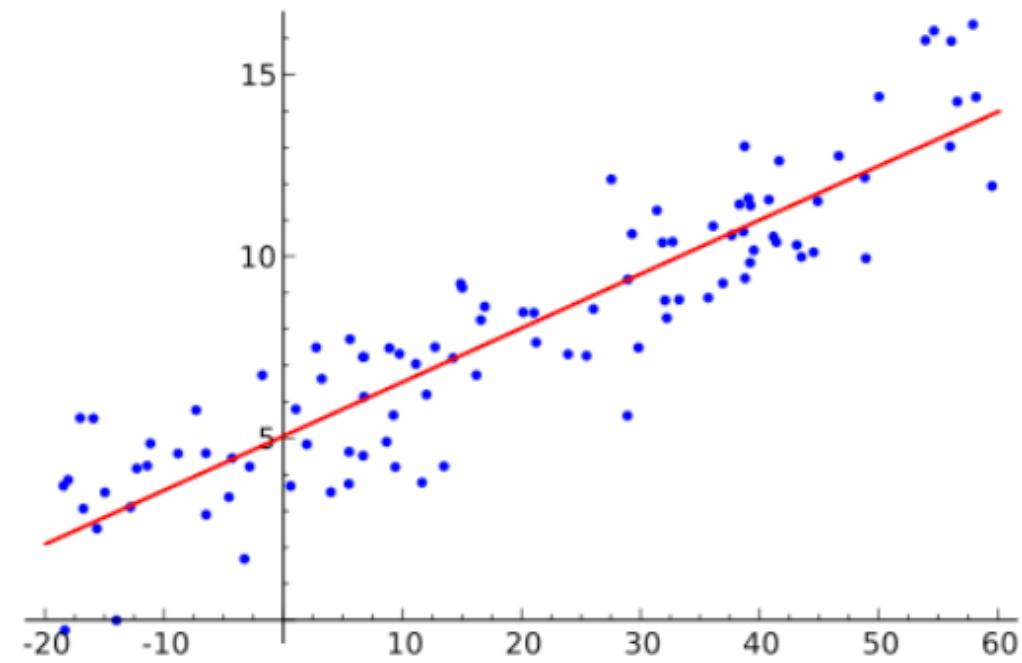
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- Predict a value of a given continuous valued variable based on the values of other variables, assuming a linear or nonlinear model of dependency.
- Extensively studied in statistics, neural network fields.
- Examples:
  - Predicting sales amounts of new product based on advertising expenditure.
  - Predicting wind velocities as a function of temperature, humidity, air pressure, etc.
  - Time series prediction of stock market indices.

# Regression

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Linear regression tries to fit the best linear model to a set of data points and their continuous (real-valued) label.



# Regression with Spark MLlib

## Parameters

A list of (hyper-)parameter keys this algorithm can take. Users can set and get the parameter values through setters and getters, respectively.

- ▶ `final val elasticNetParam: DoubleParam` [https://en.wikipedia.org/wiki/Elastic\\_net\\_regularization](https://en.wikipedia.org/wiki/Elastic_net_regularization)  
Param for the ElasticNet mixing parameter, in range [0, 1].[https://web.stanford.edu/~hastie/TALKS/enet\\_talk.pdf](https://web.stanford.edu/~hastie/TALKS/enet_talk.pdf)
- ▶ `final val featuresCol: Param[String]`  
Param for features column name.
- ▶ `final val fitIntercept: BooleanParam`  
Param for whether to fit an intercept term.
- ▶ `final val labelCol: Param[String]`  
Param for label column name.
- ▶ `final val loss: Param[String]`  
The loss function to be optimized.
- ▶ `final val maxIter: IntParam`  
Param for maximum number of iterations ( $\geq 0$ ).
- ▶ `final val predictionCol: Param[String]`  
Param for prediction column name.
- ▶ `final val regParam: DoubleParam`  
Param for regularization parameter ( $\geq 0$ ).
- ▶ `final val solver: Param[String]`  
The solver algorithm for optimization.
- ▶ `final val standardization: BooleanParam`  
Param for whether to standardize the training features before fitting the model.
- ▶ `final val tol: DoubleParam`  
Param for the convergence tolerance for iterative algorithms ( $\geq 0$ ).
- ▶ `final val weightCol: Param[String]`  
Param for weight column name.

More details at:

<https://spark.apache.org/docs/latest/ml-classification-regression.html#linear-regression>

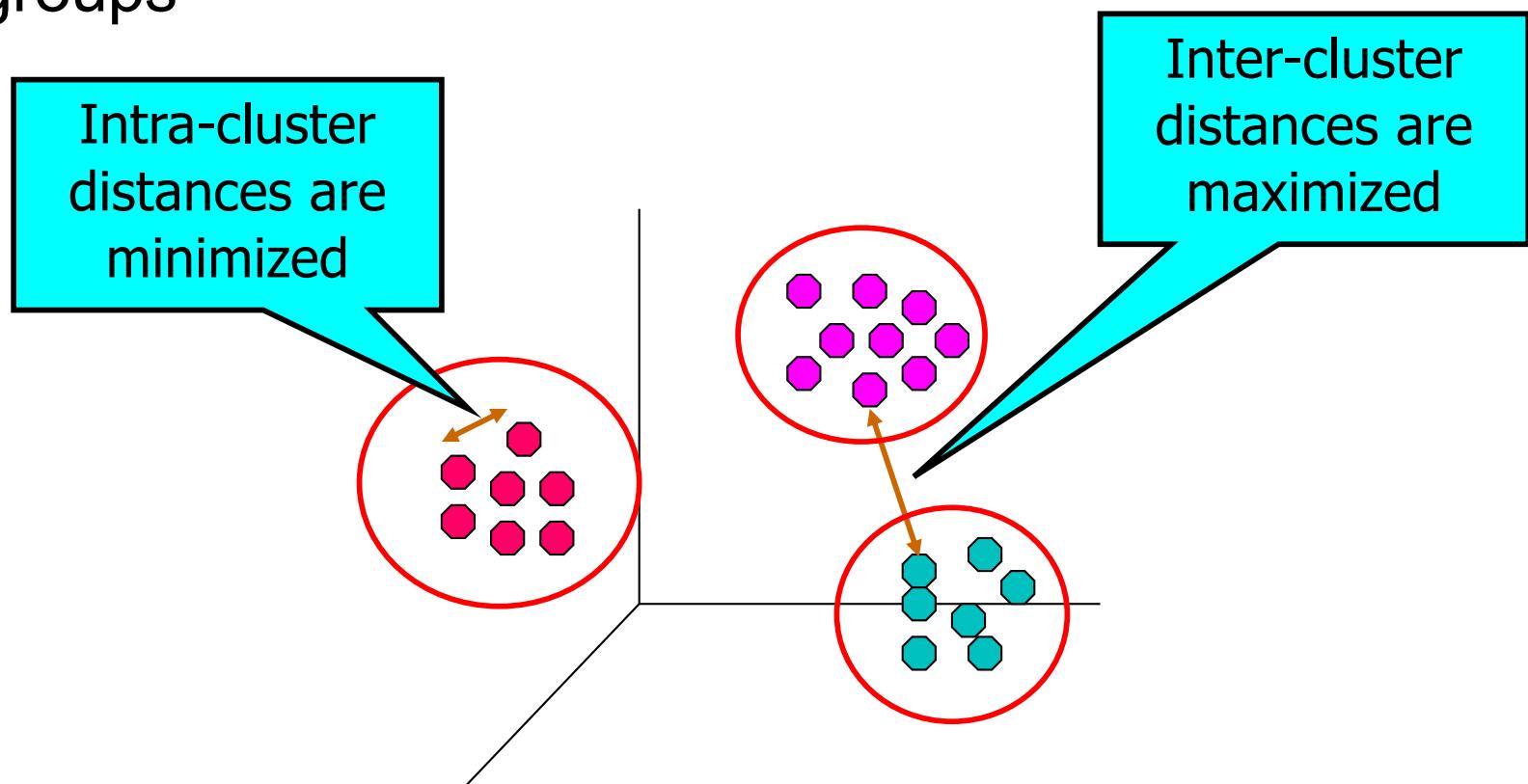


# Clustering

# Clustering

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- Finding groups of objects such that the objects in a group will be similar (or related) to one another and different from (or unrelated to) the objects in other groups



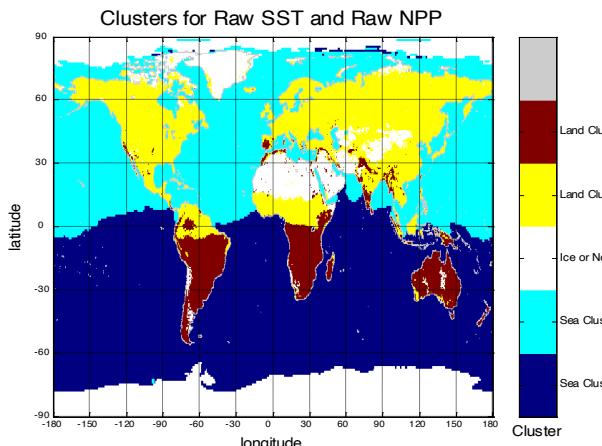
# Applications of Cluster Analysis

## ● Understanding

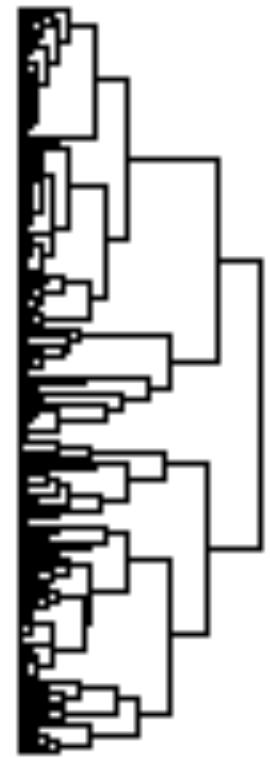
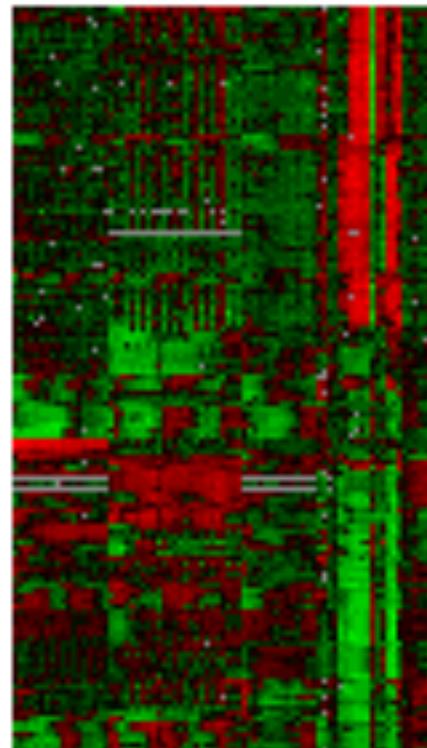
- Custom profiling for targeted marketing
- Group related documents for browsing
- Group genes and proteins that have similar functionality
- Group stocks with similar price fluctuations

## ● Summarization

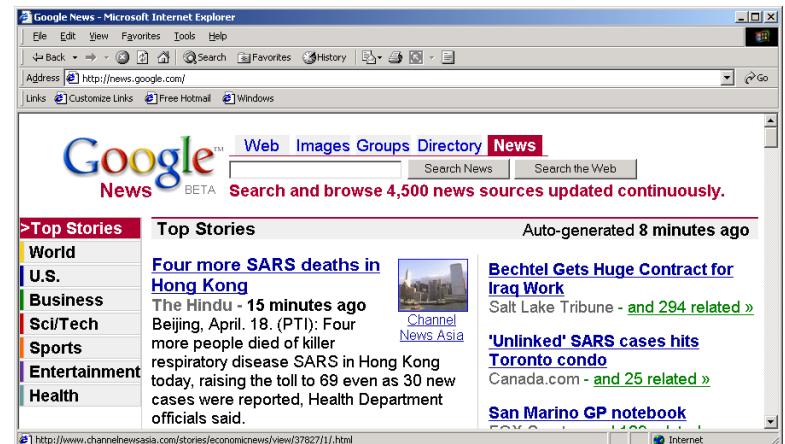
- Reduce the size of large data sets



**Use of K-means to partition Sea Surface Temperature (SST) and Net Primary Production (NPP) into clusters that reflect the Northern and Southern Hemispheres.**



Courtesy: Michael Eisen



# Clustering: Application 1

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- Market Segmentation:

- **Goal:** subdivide a market into distinct subsets of customers where any subset may conceivably be selected as a market target to be reached with a distinct marketing mix.
- **Approach:**
  - ◆ Collect different attributes of customers based on their geographical and lifestyle related information.
  - ◆ Find clusters of similar customers.
  - ◆ Measure the clustering quality by observing buying patterns of customers in same cluster vs. those from different clusters.

# Clustering: Application 2

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- Document Clustering:

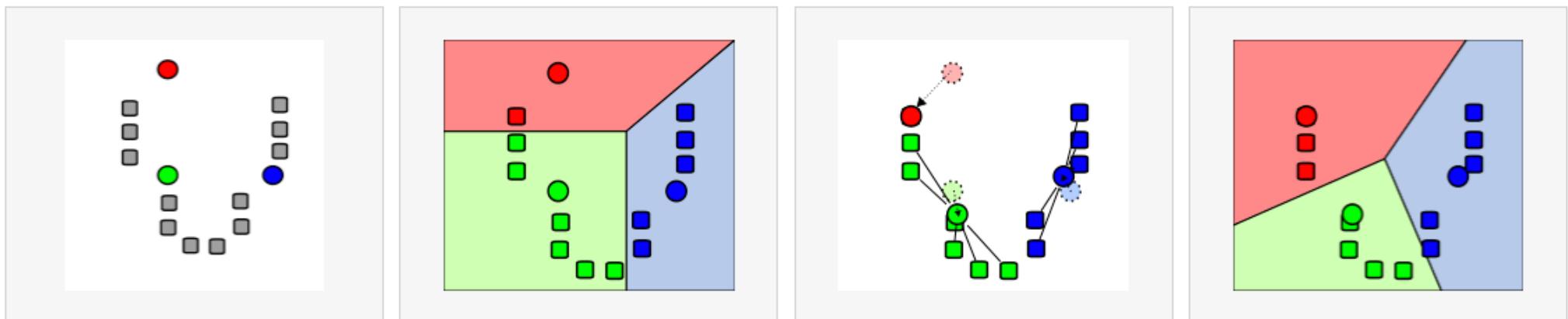
- **Goal:** To find groups of documents that are similar to each other based on the important terms appearing in them.
- **Approach:** To identify frequently occurring terms in each document. Form a similarity measure based on the frequencies of different terms. Use it to cluster.

Enron email dataset



# k-means Clustering

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need to specify  $k$  (how many clusters)

# k-means Clustering

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```
import org.apache.spark.ml.clustering.KMeans
import org.apache.spark.mllib.linalg.Vectors

// Creates a DataFrame
val dataset: DataFrame = sqlContext.createDataFrame(Seq(
  (1, Vectors.dense(0.0, 0.0, 0.0)),
  (2, Vectors.dense(0.1, 0.1, 0.1)),
  (3, Vectors.dense(0.2, 0.2, 0.2)),
  (4, Vectors.dense(9.0, 9.0, 9.0)),
  (5, Vectors.dense(9.1, 9.1, 9.1)),
  (6, Vectors.dense(9.2, 9.2, 9.2))
)).toDF("id", "features")

// Trains a k-means model
val kmeans = new KMeans()
  .setK(2)
  .setFeaturesCol("features")
  .setPredictionCol("prediction")
val model = kmeans.fit(dataset)

// Shows the result
println("Final Centers: ")
model.clusterCenters.foreach(println)
```

# Latent Dirichlet allocation

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- Part of clustering library.
- Example Application: Topic discovery in a group of documents.
  - Can be a very interesting project topic
  - Read more at:

[https://en.wikipedia.org/wiki/Latent\\_Dirichlet\\_allocation](https://en.wikipedia.org/wiki/Latent_Dirichlet_allocation)

[https://en.wikipedia.org/wiki/Topic\\_model](https://en.wikipedia.org/wiki/Topic_model)

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# **Dimensionality Reduction**

# Dimensionality Reduction

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- Aim: Given a dataset with large number of features (dimensions), we wish to explain/summarize the underlying **variance-covariance structure** of variables through a **few linear combinations of these variables**.
- Principal component analysis (PCA) is a statistical procedure that uses an orthogonal transformation to convert a set of observations of possibly correlated variables into a set of values of linearly uncorrelated variables called principal components.

# Dimensionality Reduction

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- Very useful technique in image processing, factor analysis, etc
- Spark has dimensionality reductions using SVD and PCA
- See details at:  
<http://spark.apache.org/docs/latest/ml-dimensionality-reduction.html>

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# **Collaborative Filtering**

# Explicit Matrix Factorization Approach

Suppose you have following dataset :  
(user, movie, review)

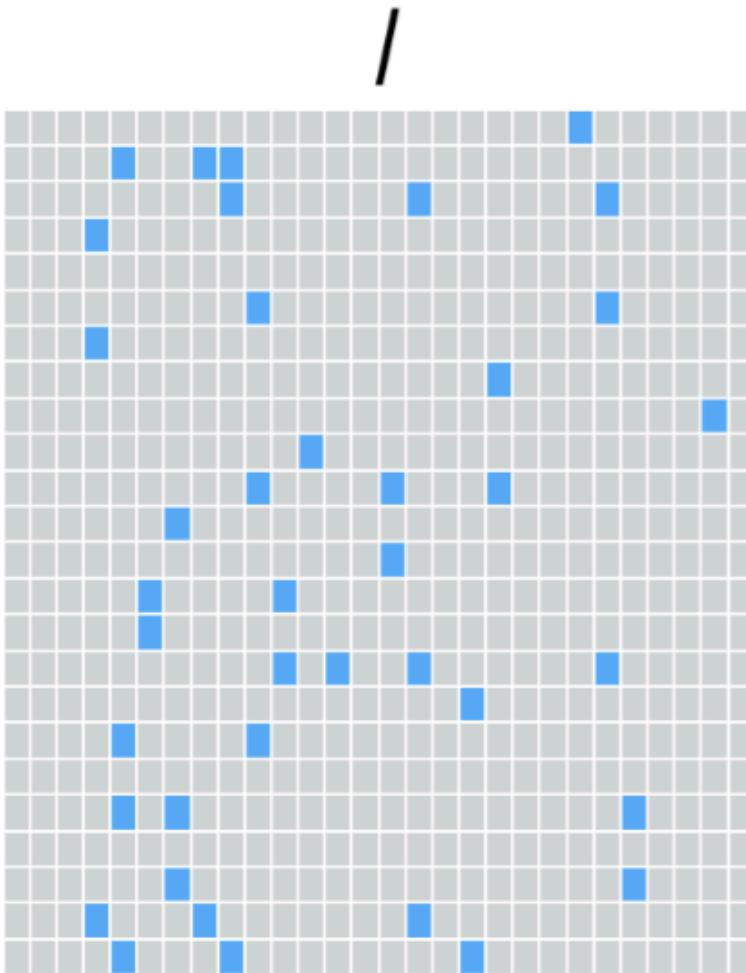
Tom, Star Wars, 5  
Jane, Titanic, 4  
Bill, Batman, 3  
Jane, Star Wars, 2  
Bill, Titanic, 3

It can be converted to a matrix:

User / Item	Batman	Star Wars	Titanic
Bill	3	3	
Jane		2	4
Tom		5	

For large number of data points,  
this would be a **sparse** matrix

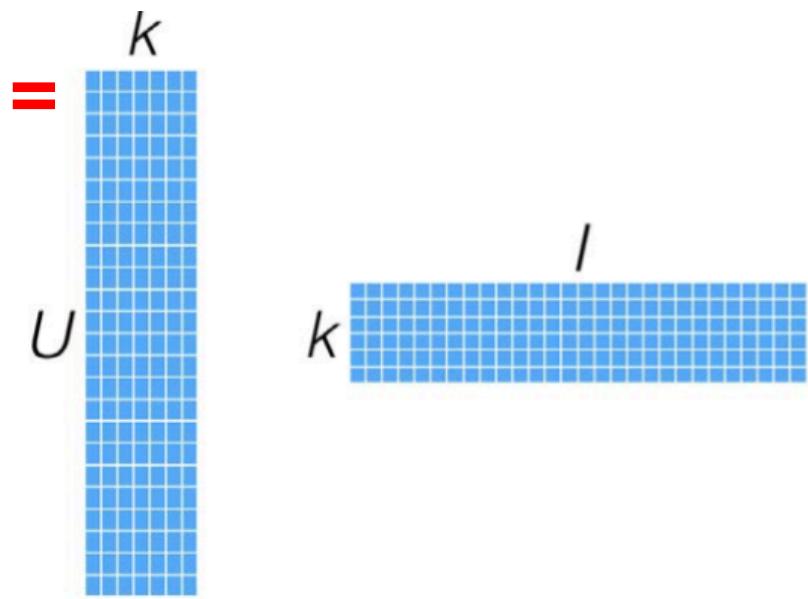
# Factor Matrices



A sparse ratings matrix

Do we really need to store it like this?

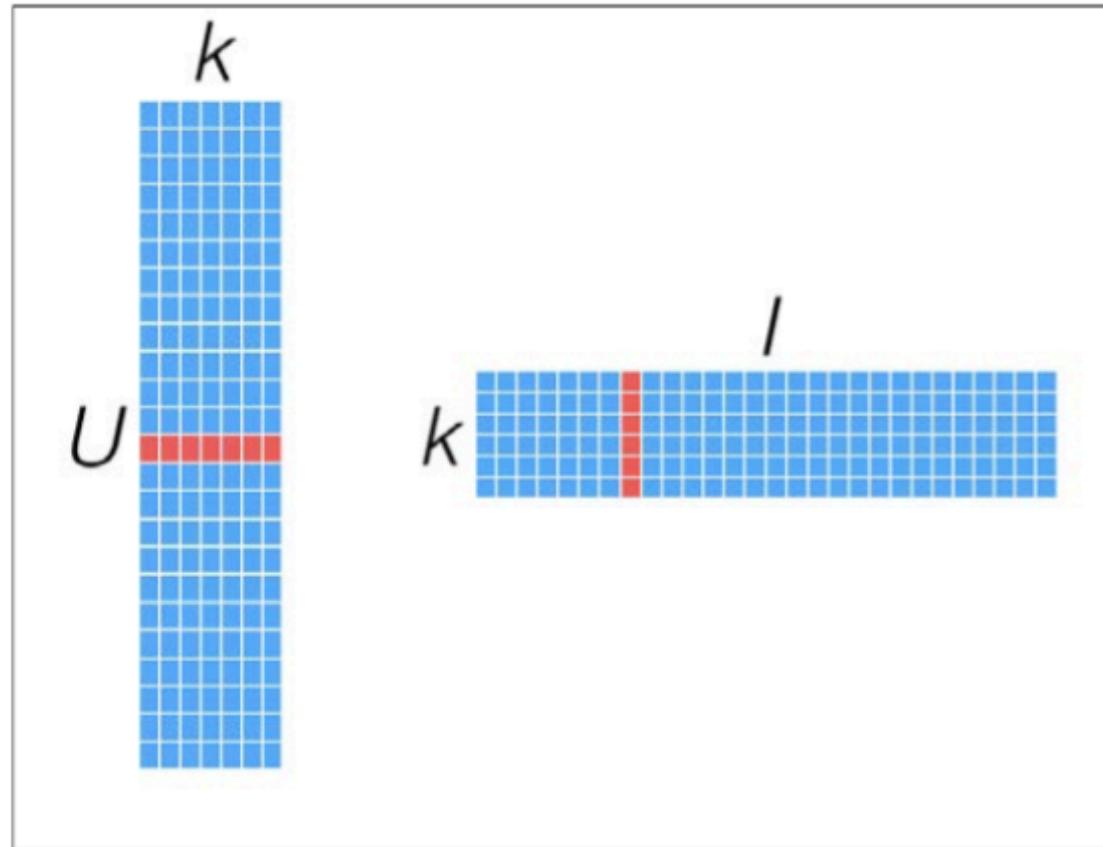
- How about dimensionality reduction.
- Representing it as a product of two smaller **matrices (factor matrices)**



# Prediction using factor matrices

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To find the prediction between a user and an item, simply take the dot product of corresponding row and column:



Computing recommendations from user- and item-factor vectors

# Implicit Feedback

User / Item	Batman	Star Wars	Titanic
Bill	1	1	
Jane		1	1
Tom		1	

User / Item	Batman	Star Wars	Titanic
Bill	3	3	
Jane		2	4
Tom		5	

Representation of an implicit preference and confidence matrix

You can still factorize the P matrix into users and items.  
The C matrix indicates the "confidence" of the Preferences (P) matrix.

# How is this achieved in Spark

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- Spark has a library that implements ALS method for Matrix Factorization.
- See details at:  
<http://spark.apache.org/docs/latest/mllib-collaborative-filtering.html>
- Good source of datasets for Recommender Systems:  
<https://gist.github.com/entaroadun/1653794>

# Spark Collaborative Filtering

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- Use ALS.train to train the model. Parameters are:

- rank: This refers to the number of factors in our ALS model, that is, the number of hidden features in our low-rank approximation matrices. Generally, the greater the number of factors, the better, but this has a direct impact on memory usage, both for computation and to store models for serving, particularly for large number of users or items. Hence, this is often a trade-off in real-world use cases. A rank in the range of 10 to 200 is usually reasonable.

Also look at `trainImplicit` method

<https://databricks-training.s3.amazonaws.com/movie-recommendation-with-mllib.html>

- iterations: This refers to the number of iterations to run. While each iteration in ALS is guaranteed to decrease the reconstruction error of the ratings matrix, ALS models will converge to a reasonably good solution after relatively few iterations. So, we don't need to run for too many iterations in most cases (around 10 is often a good default).

- lambda: This parameter controls the regularization of our model. Thus, lambda controls over fitting. The higher the value of lambda, the more is the regularization applied. What constitutes a sensible value is very dependent on the size, nature, and sparsity of the underlying data, and as with almost all machine learning models, the regularization parameter is something that should be tuned using out-of-sample test data and cross-validation approaches.

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# **Frequent Pattern Mining**

# The Market-Basket Model

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- A large set of *items*, e.g., things sold in a supermarket.
- A large set of *baskets*, each of which is a **small** set of the items, e.g., the things one customer buys on one day.

# Support

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- Simplest question: find sets of items that appear “frequently” in the baskets.
- *Support* for itemset  $I$  = the number of baskets containing all items in  $I$ .
  - Sometimes given as a percentage of the baskets.
- Given a *support threshold*  $s$ , a set of items appearing in at least  $s$  baskets is called a *frequent itemset*.

## Example: Frequent Itemsets

- Items={milk, coke, pepsi, beer, juice}.
- Support = 3 baskets.

$$B_1 = \{m, c, b\}$$

$$B_3 = \{m, b\}$$

$$B_5 = \{m, p, b\}$$

$$B_7 = \{c, b, j\}$$

$$B_2 = \{m, p, j\}$$

$$B_4 = \{c, j\}$$

$$B_6 = \{m, c, b, j\}$$

$$B_8 = \{b, c\}$$

- Frequent itemsets: {m}, {c}, {b}, {j},

{m,b}, {b,c}, {c,j}.

# Applications

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- “Classic” application was analyzing what people bought together in a brick-and-mortar store.
  - Apocryphal story of “diapers and beer” discovery.
  - Used to position potato chips between diapers and beer to enhance sales of potato chips.
- Many other applications, including plagiarism detection; see MMDS.

# Association Rules

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- If-then rules about the contents of baskets.
- $\{i_1, i_2, \dots, i_k\} \rightarrow j$  means: “if a basket contains all of  $i_1, \dots, i_k$  then it is *likely* to contain  $j$ .”
- *Confidence* of this association rule is the probability of  $j$  given  $i_1, \dots, i_k$ .
  - That is, the fraction of the baskets with  $i_1, \dots, i_k$  that also contain  $j$ .
- Generally want both high confidence and high support for the set of items involved.

## Example: Confidence

$$\begin{array}{ll} + & B_1 = \{m, c, b\} \qquad \qquad B_2 = \{m, p, j\} \\ - & B_3 = \{m, b\} \qquad \qquad B_4 = \{c, j\} \\ - & B_5 = \{m, p, b\} \qquad + \qquad B_6 = \{m, c, b, j\} \\ - & B_7 = \{c, b, j\} \qquad \qquad B_8 = \{b, c\} \end{array}$$

- An association rule:  $\{m, b\} \rightarrow c$ .
  - Confidence =  $2/4 = 50\%$ .

# Frequent Pattern using Spark

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- Spark has built-in implementation for the FP Growth algorithm.
- Details are at:  
<http://spark.apache.org/docs/latest/ml-frequent-pattern-mining.html>

# Association Rule Discovery: Definition

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- Given a set of records each of which contain some number of items from a given collection
  - Produce dependency rules which will predict occurrence of an item based on occurrences of other items.

TID	Items
1	Bread, Coke, Milk
2	Beer, Bread
3	Beer, Coke, Diaper, Milk
4	Beer, Bread, Diaper, Milk
5	Coke, Diaper, Milk

Rules Discovered:

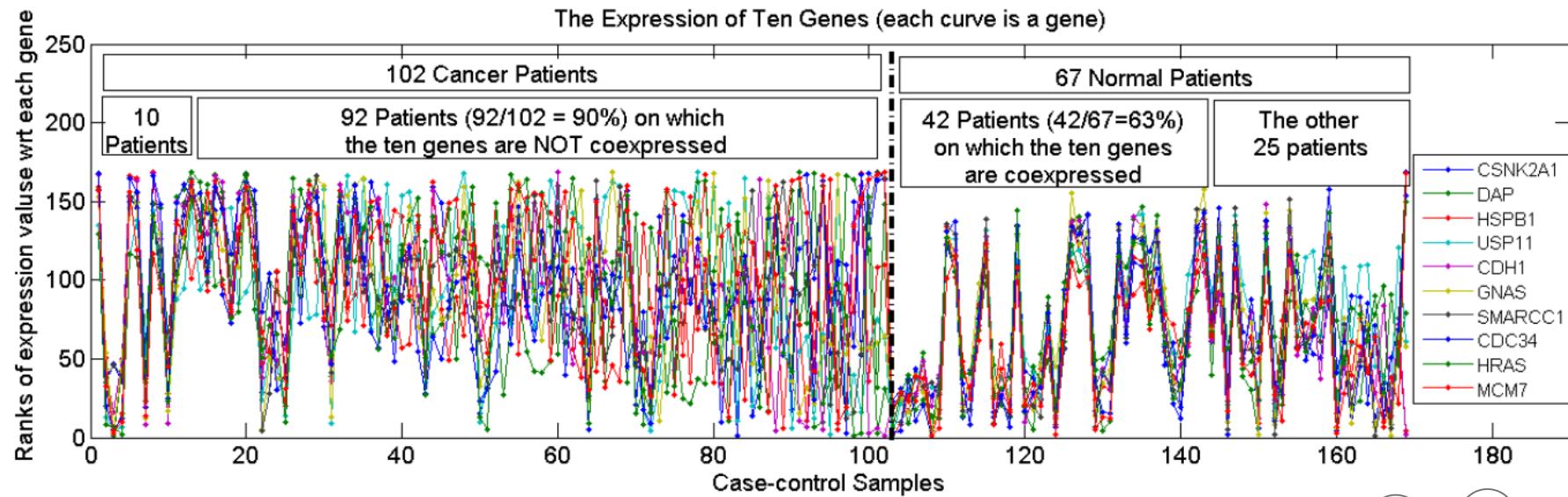
$\{\text{Milk}\} \rightarrow \{\text{Coke}\}$

$\{\text{Diaper}, \text{Milk}\} \rightarrow \{\text{Beer}\}$

# Association Analysis: Applications

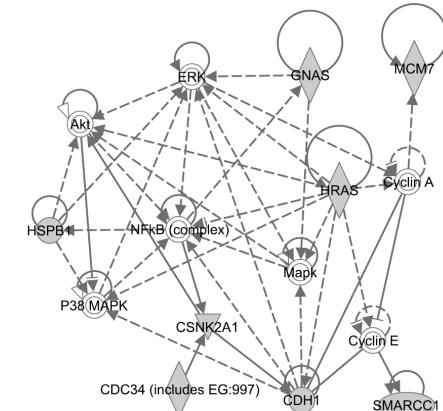
- An Example Subspace Differential Coexpression Pattern from lung cancer dataset

Three lung cancer datasets [Bhattacharjee et al. 2001], [Stearman et al. 2005], [Su et al. 2007]



Enriched with the TNF/NFB signaling pathway  
which is well-known to be related to lung cancer  
P-value:  $1.4 \times 10^{-5}$  (6/10 overlap with the pathway)

[Fang et al PSB 2010]



# Association Analysis: Applications

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- Market-basket analysis
  - Rules are used for sales promotion, shelf management, and inventory management
- Telecommunication alarm diagnosis
  - Rules are used to find combination of alarms that occur together frequently in the same time period
- Medical Informatics
  - Rules are used to find combination of patient symptoms and test results associated with certain diseases

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# Evaluation Metrics

# Model Evaluation and Selection

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- Evaluation metrics: How can we measure accuracy? Other metrics to consider?
- Use **validation test set** of class-labeled tuples instead of training set when assessing accuracy
- Methods for estimating a classifier's accuracy:
  - Holdout method, random subsampling
  - Cross-validation
  - Bootstrap
- Comparing classifiers:
  - Confidence intervals
  - Cost-benefit analysis and ROC Curves

# Classifier Evaluation Metrics: Confusion Matrix

Confusion Matrix:

Actual class\Predicted class	$C_1$	$\neg C_1$
$C_1$	True Positives (TP)	False Negatives (FN)
$\neg C_1$	False Positives (FP)	True Negatives (TN)

Example of Confusion Matrix:

Actual class\Predicted class	buy_computer = yes	buy_computer = no	Total
buy_computer = yes	6954	46	7000
buy_computer = no	412	2588	3000
Total	7366	2634	10000

- Given  $m$  classes, an entry,  $CM_{i,j}$  in a **confusion matrix** indicates # of tuples in class  $i$  that were labeled by the classifier as class  $j$
- May have extra rows/columns to provide totals

# Classifier Evaluation Metrics: Accuracy, Error Rate, Sensitivity and Specificity

A\P	C	$\neg C$	
C	TP	FN	P
$\neg C$	FP	TN	N
	P'	N'	All

- **Classifier Accuracy**, or recognition rate: percentage of test set tuples that are correctly classified

$$\text{Accuracy} = (TP + TN)/\text{All}$$

- **Error rate**:  $1 - \text{accuracy}$ , or  
$$\text{Error rate} = (FP + FN)/\text{All}$$

- **Class Imbalance Problem**:
  - One class may be *rare*, e.g. fraud, or HIV-positive
  - Significant *majority of the negative class* and minority of the positive class
- **Sensitivity**: True Positive recognition rate
  - $$\text{Sensitivity} = TP/P$$

# Classifier Evaluation Metrics: Precision and Recall, and F-measures

- **Precision:** exactness – what % of tuples that the classifier labeled as positive are actually positive

$$precision = \frac{TP}{TP + FP}$$

- **Recall:** completeness – what % of positive tuples did the classifier label as positive?

$$recall = \frac{TP}{TP + FN}$$

- Perfect score is 1.0
- Inverse relationship between precision & recall
- **F measure ( $F_1$  or F-score):** harmonic mean of precision and recall,

$$F = \frac{2 \times precision \times recall}{precision + recall}$$

- $F_\beta$ : weighted measure of precision and recall
  - assigns  $\beta$  times as much weight to recall as to precision

$$F_\beta = \frac{(1 + \beta^2) \times precision \times recall}{\beta^2 \times precision + recall}$$

# Classifier Evaluation Metrics: Example

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Actual Class\Predicted class	cancer = yes	cancer = no	Total	Recognition(%)
cancer = yes	<b>90</b>	<b>210</b>	300	30.00 ( <i>sensitivity</i> )
cancer = no	<b>140</b>	<b>9560</b>	9700	98.56 ( <i>specificity</i> )
Total	230	9770	10000	96.40 ( <i>accuracy</i> )

- $Precision = 90/230 = 39.13\%$        $Recall = 90/300 = 30.00\%$

# Evaluating Classifier Accuracy: Holdout & Cross-Validation Methods

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- **Holdout method**
  - Given data is randomly partitioned into two independent sets
    - Training set (e.g., 2/3) for model construction
    - Test set (e.g., 1/3) for accuracy estimation
  - Random sampling: a variation of holdout
    - Repeat holdout  $k$  times, accuracy = avg. of the accuracies obtained
- **Cross-validation ( $k$ -fold, where  $k = 10$  is most popular)**
  - Randomly partition the data into  $k$  *mutually exclusive* subsets, each approximately equal size
  - At  $i$ -th iteration, use  $D_i$  as test set and others as training set
  - Leave-one-out:  $k$  folds where  $k = \#$  of tuples, for small sized data
  - **\*Stratified cross-validation\***: folds are stratified so that class dist. in each fold is approx. the same as that in the initial data

# Evaluating Classifier Accuracy: Bootstrap

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- **Bootstrap**
  - Works well with small data sets
  - Samples the given training tuples uniformly *with replacement*
    - i.e., each time a tuple is selected, it is equally likely to be selected again and re-added to the training set
- Several bootstrap methods, and a common one is **.632 bootstrap**
  - A data set with  $d$  tuples is sampled  $d$  times, with replacement, resulting in a training set of  $d$  samples. The data tuples that did not make it into the training set end up forming the test set. About 63.2% of the original data end up in the bootstrap, and the remaining 36.8% form the test set (since  $(1 - 1/d)^d \approx e^{-1} = 0.368$ )
  - Repeat the sampling procedure  $k$  times, overall accuracy of the model:

$$Acc(M) = \frac{1}{k} \sum_{i=1}^k (0.632 \times Acc(M_i)_{test\_set} + 0.368 \times Acc(M_i)_{train\_set})$$

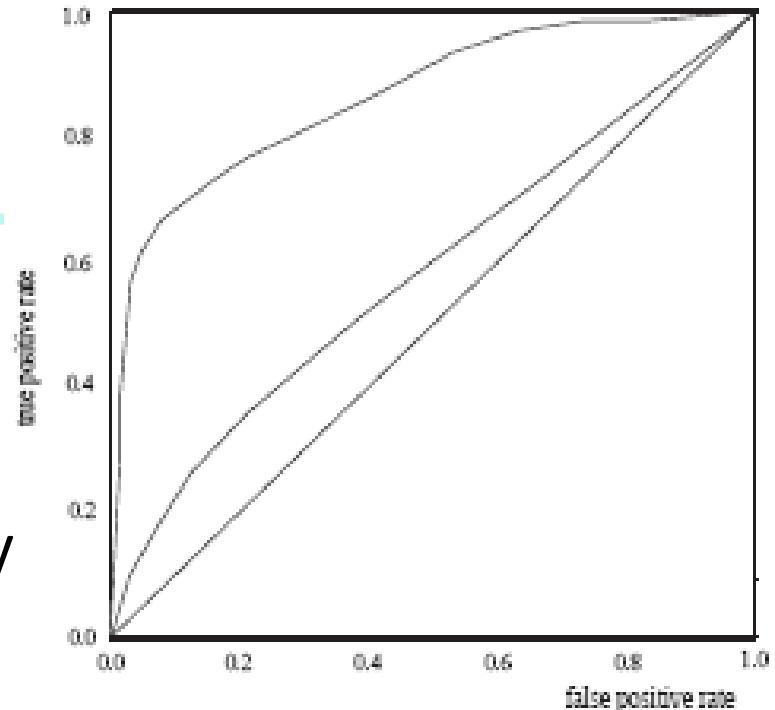
# Estimating Confidence Intervals: Classifier Models $M_1$ vs. $M_2$

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- Suppose we have 2 classifiers,  $M_1$  and  $M_2$ , which one is better?
- Use 10-fold cross-validation to obtain  $\overline{err}(M_1)$  and  $\overline{err}(M_2)$
- These mean error rates are just *estimates* of error on the true population of *future* data cases
- What if the difference between the 2 error rates is just attributed to *chance*?
  - Use a **test of statistical significance**
  - Obtain **confidence limits** for our error estimates

# Model Selection: ROC Curves

- ROC (Receiver Operating Characteristics) curves: for visual comparison of classification models
- Originated from signal detection theory
- Shows the trade-off between the true positive rate and the false positive rate
- The area under the ROC curve is a measure of the accuracy of the model
- Rank the test tuples in decreasing order: the one that is most likely to belong to the positive class appears at the top of the list
- The closer to the diagonal line (i.e., the closer the area is to 0.5), the less accurate is the model



- Vertical axis represents the true positive rate
- Horizontal axis rep. the false positive rate
- The plot also shows a diagonal line
- A model with perfect accuracy will have an area of 1.0

# Issues Affecting Model Selection

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- **Accuracy**
  - classifier accuracy: predicting class label
- **Speed**
  - time to construct the model (training time)
  - time to use the model (classification/prediction time)
- **Robustness:** handling noise and missing values
- **Scalability:** efficiency in disk-resident databases
- **Interpretability**
  - understanding and insight provided by the model
- Other measures, e.g., goodness of rules, such as decision tree size or compactness of classification rules

# Evaluation Metrics

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- For ML projects, it is definitely a good idea to present evaluation metrics.
- Details are at:  
<http://spark.apache.org/docs/latest/mllib-evaluation-metrics.html>

# Motivating Challenges

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- Scalability
- High Dimensionality
- Heterogeneous and Complex Data
- Data Ownership and Distribution
- Non-traditional Analysis