No me Baño

24 de septiembre de 2019

Resumen

Repositorio 'Guardian de la tortuga' de 'No me baño' UNR FCEIA

1. Template

```
#include <bits/stdc++.h>
using namespace std;
#define forr(i,a,b) for(int i=(a); i<(b); i++)
#define forn(i,n) forr(i,0,n)
#define sz(c) ((int)c.size())
#define zero(v) memset(v, 0, sizeof(v))
#define forall(it,v) for(auto it=v.begin();it!=v.end();++it)
#define pb push_back
#define fst first
#define snd second
typedef unsigned long long ull;
typedef long long 11;
typedef pair<int,int> ii;
#define dforn(i,n) for(int i=n-1; i>=0; i--)
\#define dprint(v) cout << \#v"=" << v << endl
#define endl "\n"
const int MAXN=100100;
int main() {
    ios::sync_with_stdio(0);
    cin.tie(nullptr);
return 0;
}
```

2. DataStructure

Binary Search

```
//the following code counts how many times the key appears in the array.
//After the search, [p+1..q] is the range with value k.
int count(int x[], int n, int k) {
   int p = -1, q = -1;
   for (int a = n; a >= 1; a /= 2) {
      while (p+a < n && x[p+a] < k) p += a;
   while (q+a < n && x[q+a] <= k) q += a;
}
return q-p;
```

Disjoint Intervals Olaf

```
// stores disjoint intervals as [first, second)
struct disjoint_intervals {
set<pair<int,int> > s;
void insert(pair<int,int> v){
if(v.fst>=v.snd) return;
auto at=s.lower_bound(v);auto it=at;
if(at!=s.begin()&&(--at)->snd>=v.fst)v.fst=at->fst,--it;
for(;it!=s.end()&&it->fst<=v.snd;s.erase(it++))
v.snd=max(v.snd,it->snd);
segs.insert(v);
}
};
```

Binary Search

```
struct STree { // [cerrado-abierto), defininir "oper" y "NEUT"
   vector<1l> st;int n;
   STree(int n): st(4*n+5,NEUT), n(n) {}
   void upd(int k, int s, int e, int p, ll v){
      if(s+1==e){st[k]=v;return;}
      int m=(s+e)/2;
      if(p<m)upd(2*k,s,m,p,v);</pre>
```

```
else upd(2*k+1,m,e,p,v);
    st[k]=oper(st[2*k],st[2*k+1]);
}

ll query(int k, int s, int e, int a, int b){
    if(s>=b||e<=a)return NEUT;
    if(s>=a&&e<=b)return st[k];
    int m=(s+e)/2;
    return oper(query(2*k,s,m,a,b),query(2*k+1,m,e,a,b));
}

void upd(int p, ll v){upd(1,0,n,p,v);}

ll query(int a, int b){return query(1,0,n,a,b);}
}; // usage: STree st(n);st.upd(i,v);st.query(s,e);</pre>
```

3. Factorizacion

Divs

```
#define MAXP 100000 //no necesariamente primo
int criba[MAXP+1];
void crearcriba(){
int w[] = \{4,2,4,2,4,6,2,6\};
for(int p=25;p<=MAXP;p+=10) criba[p]=5;</pre>
for(int p=9;p<=MAXP;p+=6) criba[p]=3;</pre>
for(int p=4;p<=MAXP;p+=2) criba[p]=2;</pre>
for(int p=7,cur=0;p*p<=MAXP;p+=w[cur++&7]) if (!criba[p])
for(int j=p*p;j<=MAXP;j+=(p<<1)) if(!criba[j]) criba[j]=p;</pre>
}
vector<int> primos;
void buscarprimos(){
crearcriba();
forr (i,2,MAXP+1) if (!criba[i]) primos.push_back(i);
}
//factoriza bien numeros hasta MAXP^2
map<11,11> fact(11 n){ //0 (cant primos)
map<ll,ll> ret;
forall(p, primos){
while(!(n%*p)){
ret[*p]++;//divisor found
n/=*p;
}
}
if(n>1) ret[n]++;
return ret;
}
//factoriza bien numeros hasta MAXP
map<11,11> fact2(11 n){ //0 (lg n)}
map<11,11> ret;
```

```
while (criba[n]){
ret[criba[n]]++;
n/=criba[n];
if(n>1) ret[n]++;
return ret;
}
//Usar asi: divisores(fac, divs, fac.begin()); NO ESTA ORDENADO
void divisores(const map<11,11> &f, vector<11> &divs, map<11,11>::iterator it, 1
    if(it==f.begin()) divs.clear();
    if(it==f.end()) { divs.pb(n); return; }
    ll p=it->fst, k=it->snd; ++it;
    forn(_, k+1) divisores(f, divs, it, n), n*=p;
}
ll sumDiv (ll n){
  ll rta = 1;
  map<ll,ll> f=fact(n);
  forall(it, f) {
ll pot = 1, aux = 0;
forn(i, it->snd+1) aux += pot, pot *= it->fst;
rta*=aux;
  }
  return rta;
}
int main() {
buscarprimos();
return 0;
}
```

Fact Basic

```
vector<ll> factorize(ll m){
  if(m==1) return{};
  vector<ll> fact;
  for(ll a=2; a*a<=m; a++){
    while(m%a==0){
     fact.push_back(a);
}</pre>
```

```
m/=a;
}
if(m!=1) fact.push_back(m);
return fact;
}
```

Fact

```
#define MAXP 100000 //no necesariamente primo
int criba[MAXP+1];
void crearcriba(){
int w[] = \{4,2,4,2,4,6,2,6\};
for(int p=25;p<=MAXP;p+=10) criba[p]=5;</pre>
for(int p=9;p<=MAXP;p+=6) criba[p]=3;</pre>
for(int p=4;p<=MAXP;p+=2) criba[p]=2;</pre>
for(int p=7, cur=0; p*p \le MAXP; p+=w[cur++&7]) if (!criba[p])
for(int j=p*p; j<=MAXP; j+=(p<<1)) if(!criba[j]) criba[j]=p;</pre>
vector<int> primos;
void buscarprimos(){
crearcriba();
forr (i,2,MAXP+1) if (!criba[i]) primos.push_back(i);
}
//factoriza bien numeros hasta MAXP^2
map<11,11> fact(11 n){ //0 (cant primos)
map<11,11> ret;
forall(p, primos){
while(!(n%*p)){
ret[*p]++;//divisor found
n/=*p;
}
}
if(n>1) ret[n]++;
return ret;
```

```
//factoriza bien numeros hasta MAXP
map<11,11> fact2(11 n){ //0 (1g n)
map<11,11> ret;
while (criba[n]){
  ret[criba[n]]++;
  n/=criba[n];
}
if(n>1) ret[n]++;
return ret;
}
int main() {
  buscarprimos();
  return 0;
}
```

Rho

```
11 gcd(ll a, ll b){return a?gcd(b%a,a):b;}
ull mulmod(ull a, ull b, ull m){ // 0 <= a, b < m}
   long double x; ull c; ll r;
   x = a; c = x * b / m;
   r = (11)(a * b - c * m) % (11)m;
   return r < 0? r + m: r;
}
11 rho(11 n){
    if(!(n&1))return 2;
    11 x=2,y=2,d=1;
    11 c=rand()%n+1;
    while(d==1){
        x=(\text{mulmod}(x,x,n)+c)%n;
        y=(mulmod(y,y,n)+c)%n;
        y=(\text{mulmod}(y,y,n)+c)%n;
        if(x>=y)d=gcd(x-y,n);
        else d=gcd(y-x,n);
    }
    return d==n?rho(n):d;
```

```
}

void fact(ll n, map<ll,int>& f){ //0 (lg n)^3
if(n==1)return;
if(rabin(n)){f[n]++;return;}
ll q=rho(n);fact(q,f);fact(n/q,f);
}
```

4. Grafos

BFS List

```
const int MAXN=10010;
vector<ll> g[MAXN];
vector<int> BFS(int nodoInicial, int n){
queue<int> cola;
vector<int> distancias(n,n);
cola.push(nodoInicial);
distancias[nodoInicial] = 0;
while(!cola.empty()){
t = cola.front();
cola.pop();
for(unsigned int i = 0; i < g[t].size(); i++){
if(distancias[g[t][i]] == n){
distancias[g[t][i]] = distancias[t]+1;
cola.push(g[t][i]);
}
}
}
return distancias;
}
```

BFS Tablero

```
#define INF 1000000007
int n,m;
bool a[8][8];
int dist[8][8];
int CANT_MOVE = 4;
pair<int,int> mov[CANT_MOVE];

void inimove(void){
    mov[0].x = 0; mov[0].y = 1;
    mov[1].x = 0; mov[1].y = 0;
    mov[2].x = 1; mov[2].y = 1;
    mov[3].x = 1; mov[3].y = 0;
```

```
}
bool ok(pair<int,int> movement, pair<int,int> a){
    return movement.x+a.x>=0 and movement.x+a.x<n and movement.y+a.y>=0 and move
}
void bfs(void){
    bool visit[8][8];
    int nivel[8][8];
    pair<int,int> padre[8][8];
    memset(visit,false,sizeof(visit));
    queue<pair<int,int> > q;
    for(int i=0; i< n; i++) for(int j=0; j< m; j++) if(a[i][j]){
        pair<int,int> node = make_pair(i,j);
        q.push(make_pair(i,j));
        nivel[node.x][node.y] = -1;
        padre[node.x][node.y] = node;
        visit[node.x][node.y] = true;
    }
    while(q.size()){
        pair<int, int> current = q.front();
        pair<int,int> mi_padre = padre[current.x][current.y];
        nivel[current.x][current.y] = nivel[mi_padre.x][mi_padre.y]+1;
        dist[current.x][current.y] = min(dist[current.x][current.y], nivel[curren
        for(int i=0;i<CANT_MOVE;i++){</pre>
            if(ok(mov[i],current)){
                pair<int,int> vecino =make_pair(mov[i].x+current.x,mov[i].y+curr
                if(!visit[vecino.x][vecino.y]){
                     q.push(vecino);
                    padre[vecino.x][vecino.y] = current;
                    visit[vecino.x][vecino.y] = true;
                }
            }
        }
    }
}
int main(){
    inimove();
    forn(i,8) forn(j,8) dist[i][j] = INF;
```

```
n = m = 8;
bfs();
}
```

BFS Tablero Caballo

```
#define INF 100000007
int n,m;
bool a[8][8];
int dist[8][8];
int CANT_MOVE = 8;
pair<int,int> mov[CANT_MOVE];
void inimove(void){
    mov[0].x = -1; mov[0].y = 2;
    mov[1].x = 1; mov[1].y = 2;
    mov[2].x = -2; mov[2].y = 1;
    mov[3].x = 2; mov[3].y = 1;
    mov[4].x = -1; mov[4].y = -2;
    mov[5].x = 1; mov[5].y = -2;
    mov[6].x = 2; mov[6].y = -1;
    mov[7].x = -2; mov[7].y = -1;
}
bool ok(pair<int,int> movement, pair<int,int> a){
    return movement.x+a.x>=0 and movement.x+a.x<n and movement.y+a.y>=0 and move
}
void bfs(void){
    bool visit[8][8];
    int nivel[8][8];
    pair<int,int> padre[8][8];
    memset(visit,false,sizeof(visit));
    queue<pair<int,int> > q;
    for(int i=0; i< n; i++) for(int j=0; j< m; j++) if(a[i][j]){
        pair<int,int> node = make_pair(i,j);
        q.push(make_pair(i,j));
        nivel[node.x][node.y] = -1;
        padre[node.x][node.y] = node;
        visit[node.x][node.y] = true;
```

```
}
    while(q.size()){
        pair<int, int> current = q.front();
        q.pop();
        pair<int,int> mi_padre = padre[current.x][current.y];
        nivel[current.x][current.y] = nivel[mi_padre.x][mi_padre.y]+1;
        dist[current.x][current.y] = min(dist[current.x][current.y],nivel[curren
        for(int i=0;i<CANT_MOVE;i++){</pre>
            if(ok(mov[i],current)){
                pair<int,int> vecino =make_pair(mov[i].x+current.x,mov[i].y+curr
                if(!visit[vecino.x][vecino.y]){
                     q.push(vecino);
                    padre[vecino.x][vecino.y] = current;
                    visit[vecino.x][vecino.y] = true;
                }
            }
        }
    }
}
int main(){
    inimove();
    forn(i,8) forn(j,8) dist[i][j] = INF;
    n = m = 8;
    bfs();
}
```

Dijkstra Olaf

```
vector<pair<int,int> > g[MAXN];  // u->[(v,cost)]
ll dist[MAXN];
void dijkstra(int x){
memset(dist,-1,sizeof(dist));
priority_queue<pair<ll,int> > q;
dist[x]=0;q.push(mp(0,x));
while(!q.empty()){
x=q.top().snd;ll c=-q.top().fst;q.pop();
if(dist[x]!=c)continue;
forn(i,g[x].size()){
int y=g[x][i].fst,c=g[x][i].snd;
```

```
if(dist[y]<0||dist[x]+c<dist[y])
dist[y]=dist[x]+c,q.push(mp(-dist[y],y));
}
}</pre>
```

Floyd Warshall Olaf

```
// g[i][j]: weight of edge (i, j) or INF if there's no edge // g[i][i]=0  
ll g[MAXN] [MAXN]; int n;  
void floyd(){ // O(n^3) . Replaces g with min distances forn(k,n)forn(i,n)if(g[i][k]<INF)forn(j,n)if(g[k][j]<INF)  
g[i][j]=min(g[i][j],g[i][k]+g[k][j]);  
} bool inNegCycle(int v){return g[v][v]<0;}  
bool hasNegCycle(int a, int b){ // true iff there's neg cycle in between forn(i,n)if(g[a][i]<INF&&g[i][b]<INF&&g[i][i]<0)return true;  
return false;  
}
```

Kruskal Olaf

```
int uf[MAXN];
void uf_init(){memset(uf,-1,sizeof(uf));}
int uf_find(int x){return uf[x]<0?x:uf[x]=uf_find(uf[x]);}
bool uf_join(int x, int y){
    x=uf_find(x);y=uf_find(y);
    if(x==y)return false;
    if(uf[x]>uf[y])swap(x,y);
    uf[x]+=uf[y];uf[y]=x;
    return true;
}
vector<pair<ll,pair<int,int> > es; // edges (cost,(u,v))
ll kruskal(){ // assumes graph is connected
    sort(es.begin(),es.end());uf_init();
ll r=0;
forn(i,es.size()){
    int x=es[i].snd.fst,y=es[i].snd.snd;
```

```
if(uf_join(x,y))r+=es[i].fst; // (x,y,c) belongs to mst
}
return r; // total cost
}
```

5. Maths

Combinatoria

```
const int MAXN = 200;
#define MOD 100000007;
//Luego de llamar a combinatoria(), comb queda: (MÓDULO 10^9 +7)
//comb[i][k] = i tomados de a k
long long comb[MAXN+1][MAXN+2];
/* combinatoria : Void
 * Genera el triangulo de pascal hasta la fila MAXN
 * Como a partir de la fila ~60 los valores no entran en un long long
 * se guarda la información módulo 10^9+7
 * SE LLAMA UNA SOLA VEZ esta función
void combinatoria(){
forn(i, MAXN+1){ //comb[i][k]=i tomados de a k
comb[i][0]=comb[i][i]=1;
forr(k, 1, i)
comb[i][k] = (comb[i-1][k] + comb[i-1][k-1])%MOD;
}
}
void outputTrianguloPascal(){
forn(i, MAXN+1){
cout << "FILA: " << i << endl;</pre>
forn(k, i){
cout << comb[i][k] << "\t";</pre>
cout << endl;</pre>
}
}
int main(){
combinatoria();
outputTrianguloPascal();
return 0;
```

```
}
```

Exp Mod

```
11 expmod(11 b, 11 e, 11 m){
b%=m;
if(!e) return 1;
11 q = expmod(b, e/2, m); q = (q*q) % m;
return e%2 ? (b*q) % m : q;
}
```

Factorial

```
int factorial(int n){
  return (n == 1 || n == 0) ? 1 : factorial(n - 1) * n;
}
```

Fib

```
long long afib[10000000];
bool b[10000000] = {false};

//O(n)
long long fib(long long n){
   if(n == 1 || n == 2) {
      afib[n] = 1;
      b[n] = true;
   return 1;
}
if(b[n]) return afib[n];
b[n] = true;
afib[n] = fib(n-1) + afib[n-2];
return afib[n];
}
```

GCD-MCM

```
11 gcd(ll a, ll b){
   if(b<a) swap(a,b);
   if(a==0) return b;
   else{
     return gcd(b%a,a);
   }
}
11 mcm(ll a, ll b){
   return (a/gcd(a,b))*b;
}</pre>
```

GCD Array

```
int GCD(int n, int d[]){
int a = __gcd(d[0], d[1]);
forr(i, 1, n-1){
  if(__gcd(d[i], d[i+1]) < a)
  a = __gcd(d[i], d[i+1]);
}
return a;
}</pre>
```

6. Primos

Criba

```
#define MAXP 100000 //no necesariamente primo
int criba[MAXP+1];
void crearcriba(){
int w[] = \{4,2,4,2,4,6,2,6\};
for(int p=25;p<=MAXP;p+=10) criba[p]=5;</pre>
for(int p=9;p<=MAXP;p+=6) criba[p]=3;</pre>
for(int p=4;p<=MAXP;p+=2) criba[p]=2;</pre>
for(int p=7,cur=0;p*p<=MAXP;p+=w[cur++&7]) if (!criba[p])</pre>
for(int j=p*p;j<=MAXP;j+=(p<<1)) if(!criba[j]) criba[j]=p;</pre>
vector<int> primos;
void buscarprimos(){
crearcriba();
forr (i,2,MAXP+1) if (!criba[i]) primos.push_back(i);
int main() {
buscarprimos();
return 0;
}
                           Is Prime
```

```
bool is_prime(int m){
  for(int a=2; a*a<=m; a++){
    if(m%a==0)
      return false;
  }
  return true;
}</pre>
```

Rabin

```
ull mulmod(ull a, ull b, ull m){ // 0 <= a, b < m}
   long double x; ull c; ll r;
   x = a; c = x * b / m;
   r = (11)(a * b - c * m) \% (11)m;
   return r < 0? r + m: r;
}
ll expmod(ll b, ll e, ll m){
if(!e)return 1;
11 q=expmod(b,e/2,m);q=mulmod(q,q,m);
return e&1?mulmod(b,q,m):q;
}
bool is_prime_prob(ll n, int a){
if(n==a)return true;
11 s=0, d=n-1;
while (d\%2==0)s++,d/=2;
11 x=expmod(a,d,n);
if((x==1)||(x+1==n))return true;
forn(_,s-1){
x=mulmod(x,x,n);
if(x==1)return false;
if(x+1==n)return true;
}
return false;
bool rabin(ll n){ // true iff n is prime
if(n==1)return false;
int ar[]={2,3,5,7,11,13,17,19,23};
forn(i,9)if(!is_prime_prob(n,ar[i]))return false;
return true;
}
```

7. Random

Tiene X

```
int tieneX(int u, int x){
int g = u%10;
if(u%x == 0) return 1;
while (u > 0){
g=u%10;
if(u%10 == x)
return 1;
else
u = (u-g)/10;
}
return 0;
}
```