## Quantifying the non-reported new daily cases of COVID-2019 by region in Spain at a real-time

The present outbreak of COVID-19 disease, caused by the SARS-CoV-2 virus, has put the planet in quarantine. On January 30, 2020, the World Health Organization (WHO) declared the COVID-19 outbreak a "public health emergency of international concern", and then a pandemic on March 11.

Spain has become the fourth country worldwide with more infected cases, officially registering over thousands of cases in a short time. Although many critical and severe measures have been considered from the authorities to lessen the impact of the outbreak and help flatten the curve, they rely on numbers that could be unreliable and therefore misrepresent the implications of such pandemic.

Counts in Spain due to the protocols used for testing, mainly include individuals with severe symptoms. The authorities have juste announced a new protocol with rapid tests to be implemented in a few days elpais.com.

Given the nature of our data, we can guess that the estimated number of cases that we are finding are in fact potentially severe cases, and presumably the size of the infected population (asymptomatic) is even higher.

Accordingly, the current analysis aims to update the situation concerning COVID-19 daily, and particularly quantify the potential under-reporting in the official registered cases by region in Spain. Results herein can help to have a more realistic picture of the pandemic at a real time as well as to more accurately estimate essential measures such as the basic reproduction number or the fatality rate that are used for practitioners and politicians to make decisions.

The data for the analysis have been extracted from eldiario.es, where official data are gathered.

Notice that this analysis con be easily reproduced for other countries.

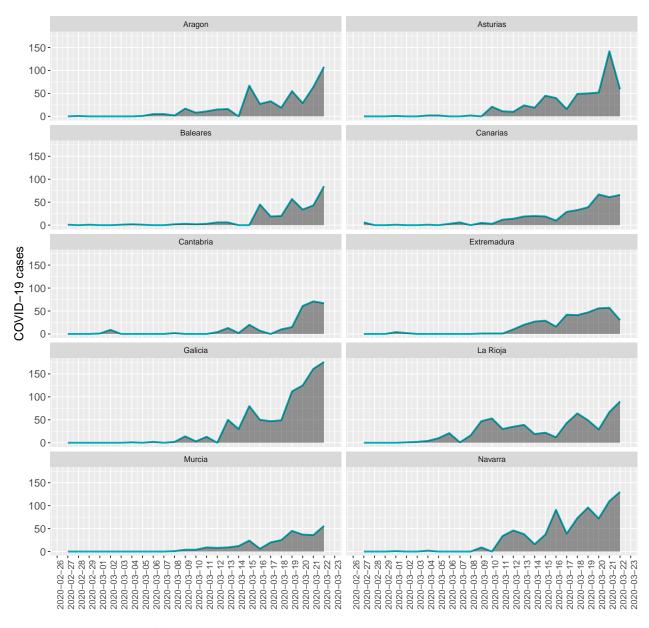


Figure 1 (a): Daily COVID-19 cases from 27-02-2020 to 22-03-2020

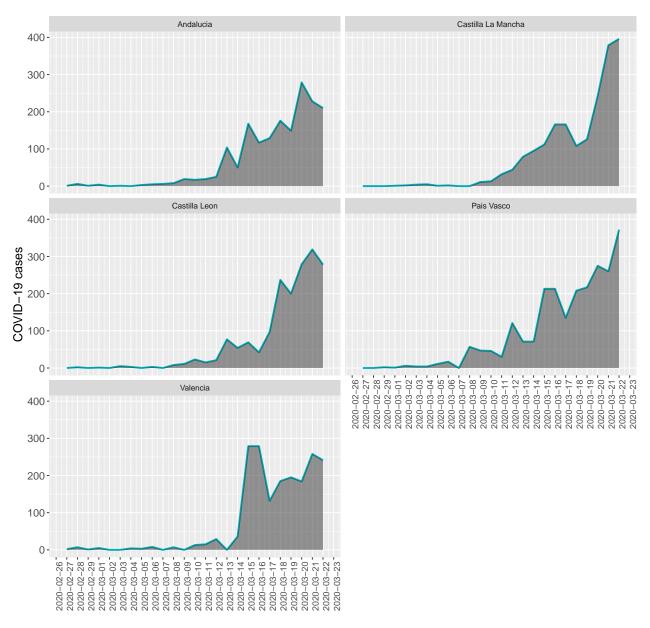


Figure 1 (b): Daily COVID-19 cases from 27-02-2020 to 22-03-2020

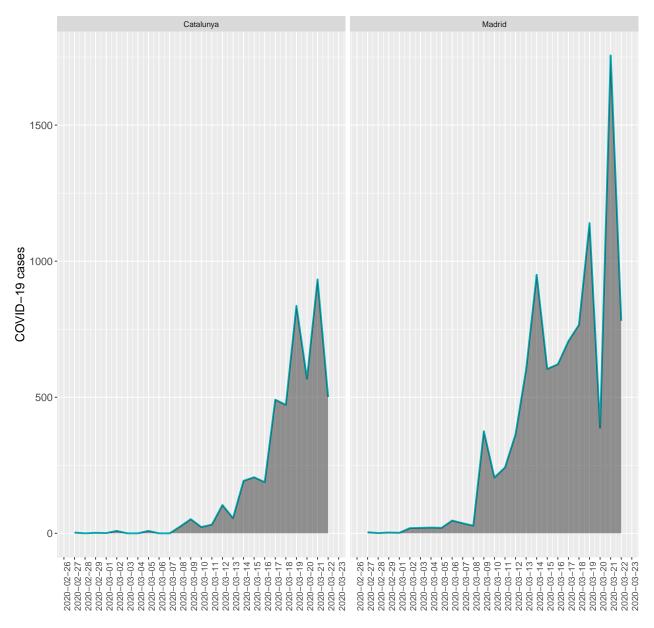


Figure 1 (c): Daily COVID-19 cases from 27-02-2020 to 22-03-2020

If the under-reporting is ignored, the daily counts can be appropriately modeled following:  $exp(\alpha_0 + \alpha_1 t)$ , since the number of daily COVID-19 cases overtime properly growths exponentially according to Figure 1.

However, if we consider that the official number of daily cases does not reflect the total number of cases (e.g., a proportion of the cases is not observed, and thus the data are misreported), the model above does not make any sense, and therefore a more appropriate alternative should be considered.

We shall base all the subsequent analysis in a model introduced by Fernández-Fontelo et al. (2016).

In that model, two different processes are considered:  $X_n$  which is the true process but unobserved (latent), and  $Y_n$  which is observed and potentially under-reported. In this application, the latent process is assumed to be Poisson distributed with time-dependent rate,  $\lambda_t = exp(\beta_0 + \beta_1 t)$ . The observed process will always be lower or equal than the latent process (due to the under-reporting) in such a way that  $Y_n$  will be equal than  $X_n$  (non under-reporting) with probability  $1 - \omega$ ; or  $Y_n$  is  $q \circ X_n$  with probability  $\omega$ . Parameters  $\omega$  and q quantify the overall frequency and intensity of the phenomenon, which roughly speaking describe respectively the number of times the observed counts are not equal to the real ones, and the distance between the real

-	minimum	mean	median	maximum	standard deviation	dispersion index
Andalucia	0.00	69.00	19.00	279.00	87.03	109.77
Aragon	0.00	19.32	8.00	108.00	27.37	38.76
Asturias	0.00	21.80	10.00	142.00	32.19	47.52
Baleares	0.00	13.24	2.00	85.00	22.35	37.73
Canarias	0.00	16.56	6.00	67.00	21.25	27.27
Cantabria	0.00	11.28	1.00	71.00	21.52	41.07
Castilla La Mancha	0.00	79.40	13.00	396.00	114.68	165.65
Castilla Leon	0.00	69.76	15.00	319.00	103.60	153.86
Catalunya	0.00	188.16	32.00	933.00	278.07	410.96
Extremadura	0.00	15.36	2.00	57.00	19.78	25.47
Galicia	0.00	36.60	3.00	176.00	53.57	78.40
La Rioja	0.00	26.16	21.00	90.00	25.12	24.11
Madrid	1.00	388.08	242.00	1756.00	449.94	521.66
Murcia	0.00	11.84	4.00	56.00	16.28	22.39
Navarra	0.00	31.76	9.00	130.00	40.69	52.14
Pais Vasco	0.00	95.24	47.00	372.00	109.51	125.93
Valencia	0.00	75.32	8.00	279.00	105.04	146.47

Table 1: Summary of the daily COVID-19 cases from 27-02-20 to 22-03-2020 by region in Spain

## and observed processes.

Using the Viterbi algorithm, the model also enables reconstructing the most likely sequence of real COVID-19 cases throughout the study. This allows us to have an estimated time series of truly daily cases and evaluate the impact of under-reporting over measures such as the basic reproduction number. Figure 2 shows the observed and reconstructed series over time by region.

	\$\alpha\$	\$\beta_0\$	\$\beta_1\$	\$\omega\$	\$q\$	AIC
Andalucia		0.8439	0.2121	0.7005	0.5133	258
s.e. (Andalucia)		0.1356	0.0064	0.099	0.0252	
Aragon		0.0722	0.2238	0.9047	0.2944	188.3
s.e. (Aragon)		0.2402	0.0105	0.0648	0.0224	
Asturias		-0.8338	0.24	0.545	0.4135	164.2
s.e. (Asturias)		0.3218	0.0149	0.1474	0.0402	
Baleares		-1.1326	0.2296	0.7799	0.4739	156.2
s.e. (Baleares)		0.4046	0.0172	0.1193	0.0491	
Canarias		-0.1145	0.1766	0.2876	0.287	147.3
s.e. (Canarias)		0.3007	0.0138	0.1271	0.0876	
Cantabria		-0.049	0.1763	0.7291	0.1717	143
s.e. (Cantabria)		0.4168	0.018	0.0967	0.0336	
Castilla La Mancha		-1.0139	0.3183	0.5221	0.412	212.4
s.e. (Castilla La Mancha)		0.2306	0.0124	0.127	0.0329	
Castilla Leon		-0.1367	0.2689	0.8715	0.5174	238.5
s.e. (Castilla Leon)		0.1687	0.0078	0.0846	0.0332	
Catalunya		0.3357	0.2867	0.5853	0.4746	578.4
s.e. (Catalunya)		0.1155	0.0057	0.1113	0.0162	
Extremadura		0.9265	0.1258	0.4776	0.0339	155.3
s.e. (Extremadura)		0.2981	0.014	0.1022	0.0204	
Galicia		-0.8216	0.285	0.8594	0.3751	176.4
s.e. (Galicia)		0.1996	0.0087	0.0768	0.0188	
La Rioja		2.1522	0.0927	0.5067	0.2914	236.6
s.e. (La Rioja)		0.1695	0.0083	0.1038	0.0338	
Madrid		3.5093	0.1606	0.52	0.3491	1015.8
s.e. (Madrid)		0.0469	0.0022	0.0999	0.009	
Murcia		-1.3113	0.2168	0.1909	0.2969	119.3
s.e. (Murcia)		0.384	0.0173	0.1541	0.1415	
Navarra		-0.2306	0.249	0.8141	0.3632	191.6
s.e. (Navarra)		0.1881	0.0085	0.0851	0.0193	
Pais Vasco		1.4514	0.2132	0.7903	0.4412	255.5
s.e. (Pais Vasco)		0.1192	0.0062	0.0847	0.0232	
Valencia		4.6996	0.032	0.68	0.0515	420
s.e. (Valencia)		0.1977	0.009	0.0933	0.0073	

Table 2: Estimates of under-reporting parameters by region in Spain

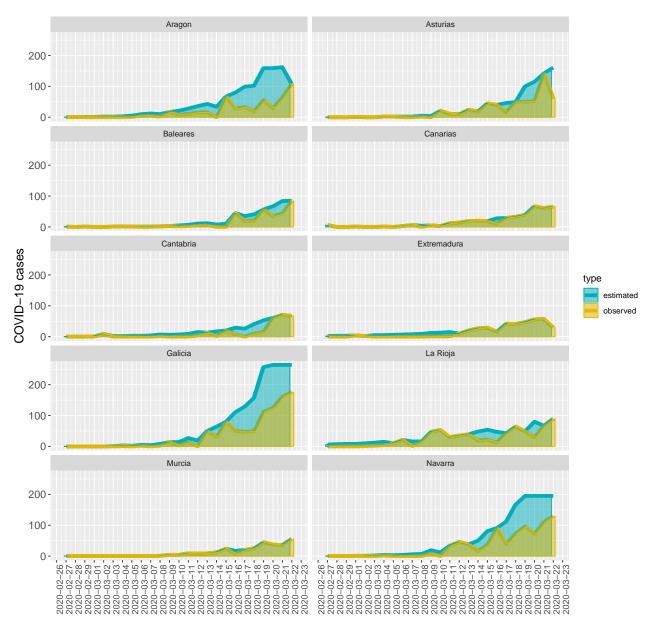


Figure 2 (a): Observed and truly daily cases

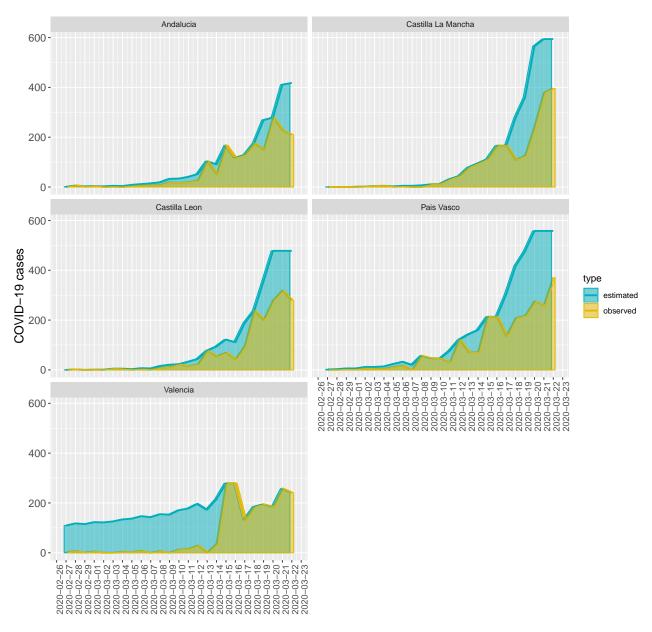


Figure 2 (b): Observed and truly daily cases

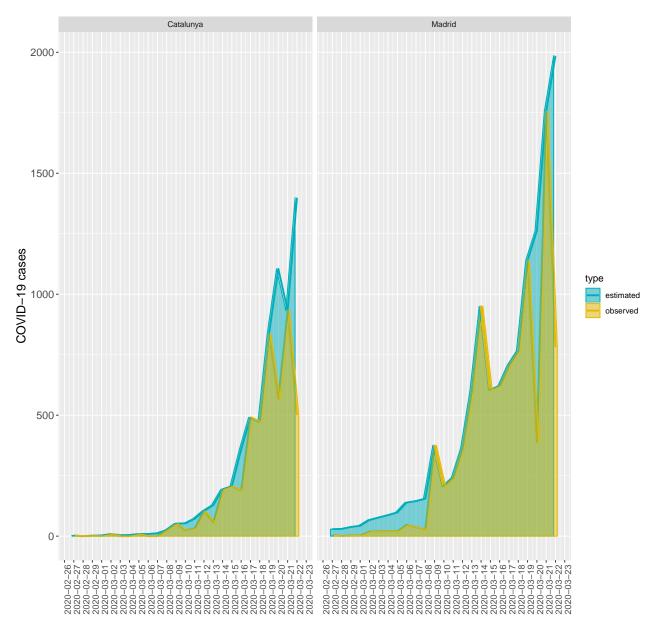


Figure 2 (c): Observed and estimated daily cases

Using the Viterbi algorithm, the model also enables reconstructing the most likely sequence of real COVID-19 cases throughout the study. This allows us to have an estimated time series of truly daily cases and evaluate the impact of under-reporting over measures such as the basic reproduction number. Figure 2 shows the observed and reconstructed series over time by region.

Table 3 shows the percentages of means counts that are not covered by the official registers. Thus, the highest the rate, the lower is the coverage, and therefore the severe is the impact of the under-reporting.

	observed mean	true mean	% not covered
Andalucia	69.00	96.12	28.21
Aragon	19.32	46.48	58.43
Asturias	21.80	32.04	31.96
Baleares	13.24	19.20	31.04
Canarias	16.56	17.44	5.05
Cantabria	11.28	18.64	39.48
Castilla La Mancha	79.40	125.64	36.80
Castilla Leon	69.76	111.44	37.40
Catalunya	188.16	259.32	27.44
Extremadura	15.36	18.76	18.12
Galicia	36.60	69.52	47.35
La Rioja	26.16	35.00	25.26
Madrid	388.08	499.48	22.30
Murcia	11.84	12.28	3.58
Navarra	31.76	58.32	45.54
Pais Vasco	95.24	163.20	41.64
Valencia	75.32	170.76	55.89

Table 3: Estimate mean of non-coverage of cases of COVID-19 in Spain

CCAA	estimated	observed	lethality-estimated	lethality-observed	mortality
Andalucia	2403.00	1725.00	1.96	2.72	0.56
Aragon	1162.00	483.00	2.07	4.97	1.82
Asturias	801.00	545.00	1.00	1.47	0.78
Baleares	480.00	331.00	0.83	1.21	0.35
Canarias	436.00	414.00	2.06	2.17	0.42
Cantabria	466.00	282.00	1.07	1.77	0.86
Castilla La Mancha	3141.00	1985.00	3.57	5.64	5.51
Castilla Leon	2786.00	1744.00	2.66	4.24	3.08
Catalunya	6483.00	4704.00	2.95	4.06	2.49
Extremadura	469.00	384.00	2.99	3.65	1.31
Galicia	1738.00	915.00	0.69	1.31	0.44
La Rioja	875.00	654.00	2.06	2.75	5.68
Madrid	12487.00	9702.00	8.18	10.52	15.32
Murcia	307.00	296.00	0.33	0.34	0.07
Navarra	1458.00	794.00	0.96	1.76	2.14
Pais Vasco	4080.00	2381.00	2.38	4.07	4.39
Valencia	4269.00	1883.00	1.62	3.66	1.38

Table 4: Estimated mortality and lethality rates