

maze-dataset: Maze Generation with Algorithmic Variety and Representational Flexibility

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Summary

Solving mazes is a classic problem in computer science and artificial intelligence, and humans have been constructing mazes for thousands of years. Although finding the shortest path through a maze is a solved problem, this very fact makes it an excellent testbed for studying how machine learning algorithms solve problems and represent spatial information. We introduce maze-dataset, a user-friendly Python library for generating, processing, and visualizing datasets of mazes. This library supports a variety of maze generation algorithms providing mazes with or without loops, mazes that are connected or not, and many other variations. These generation algorithms can be configured with various parameters, and the resulting mazes can be filtered to satisfy desired properties. Also provided are tools for converting mazes to and from various formats suitable for a variety of neural network architectures, such as rasterized images, tokenized text sequences, and various visualizations. As well as providing a simple interface for generating, storing, and loading these datasets, maze-dataset is extensively tested, type hinted, benchmarked, and documented.

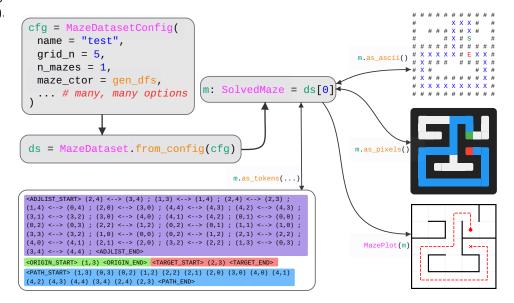


Figure 1: Usage of maze-dataset. We create a MazeDataset from a MazeDatasetConfig. This contains SolvedMaze objects which can be converted to and from a variety of formats. Code in the image contains clickable links to documentation. A variety of generated examples can be viewed here.



Statement of Need

While maze generation itself is straightforward, the architectural challenge comes from building a system supporting many algorithms with configurable parameters, property filtering, and representation transformation. This library aims to greatly streamline the process of generating and working with datasets of mazes that can be described as subgraphs of an $n \times n$ lattice with boolean connections and, optionally, start and end points that are nodes in the graph. Furthermore, we place emphasis on a wide variety of possible text output formats aimed at evaluating the spatial reasoning capabilities of Large Language Models (LLMs) and other text-based transformer models.

For interpretability and behavioral research, algorithmic tasks offer benefits by allowing systematic data generation and task decomposition, as well as simplifying the process of circuit discovery (Räuker et al., 2023). Although mazes are well suited for these investigations, we found that existing maze generation packages (Cobbe et al., 2019; Ehsan, 2022; Harries et al., n.d.; Németh, 2019; Schwarzschild, Borgnia, Gupta, Bansal, et al., 2021) lack support for transforming between multiple representations and provide limited control over the maze generation process.

Related Works

A multitude of public and open-source software packages exist for generating mazes (Ehsan, 2022; Németh, 2019; Schwarzschild, Borgnia, Gupta, Bansal, et al., 2021). However, nearly all of these packages produce mazes represented as rasterized images or other visual formats rather than the underlying graph structure, and this makes it difficult to work with these datasets.

- Most prior works provide mazes in visual or raster formats, and we provide a variety of similar output formats:
 - RasterizedMazeDataset, utilizing as_pixels(), which can exactly mimic the outputs provided in easy-to-hard-data(Schwarzschild, Borgnia, Gupta, Bansal, et al., 2021) and can be configured to be similar to the outputs of Németh (2019)
 - as_ascii() provides a format similar to (Oppenheim, 2018; Singla, 2023)
 - MazePlot provides a feature-rich plotting utility with support for multiple paths, heatmaps over positions, and more. This is similar to the outputs of (Alance AB, 2019; Ehsan, 2022; Guo et al., 2011; Nag, 2020)
- The text format provided by SolvedMaze(...).as_tokens() is similar to that of (Liu & Wu, 2023), but provides over 5.8 million unique formats for converting mazes to a text stream, detailed in section: *Tokenized Output Formats*.
- For rigorous investigations of the response of a model to various distributional shifts, preserving metadata about the generation algorithm with the dataset itself is essential. To this end, our package efficiently stores the dataset along with its metadata in a single human-readable file (M. Ivanitskiy, n.d.). As far as we are aware, no existing packages do this reliably.
- Storing mazes as images is not only difficult to work with, but also inefficient. We use a highly efficient method detailed in section: *Implementation*.
- Our package is easily installable with source code freely available. It is extensively tested, type hinted, benchmarked, and documented. Many other maze generation packages lack this level of rigor and scope, and some (Ayaz et al., 2008) appear to simply no longer be accessible.



Features

We direct readers to our examples, docs, and notebooks for more information.

Generation and Basic Usage

Our package can be installed from PyPi via pip install maze-dataset, or directly from the git repository (Michael I. Ivanitskiy et al., 2023a).

To create a dataset, we first create a MazeDatasetConfig configuration object, which specifies the seed, number, and size of mazes, as well as the generation algorithm and its corresponding parameters. This object is passed to a MazeDataset class to create a dataset. Crucially, this MazeDataset mimics the interface of a PyTorch (Paszke et al., 2019) Dataset, and can thus be easily incorporated into existing data pre-processing and training pipelines, e.g., through the use of a DataLoader class.

```
from maze_dataset import (
 {\tt MazeDataset}, {\tt MazeDatasetConfig}, {\tt LatticeMazeGenerators}
)
# create a config
cfg: MazeDatasetConfig = MazeDatasetConfig(
    name="example", # names need not be unique
    grid_n=3, # size of the maze
    n mazes=32, # number of mazes in the dataset
    maze ctor=LatticeMazeGenerators.gen dfs, # many algorithms available
    # (optional) algorithm-specific parameters
    maze_ctor_kwargs={"do_forks": True, ...},
    # (optional) many options for restricting start/end points
    endpoint_kwargs={"deadend_start": True, ...},
)
# create a dataset
dataset: MazeDataset = MazeDataset.from_config(
 cfq, # pass the config
  ..., # other options for disk loading, parallelization, etc.
```

When initializing a dataset, options which do not affect the mazes themselves can be specified through the <code>from_config()</code> factory method as necessary. These options allow for saving/loading existing datasets instead of re-generating, parallelization options for generation, and more. Available maze generation algorithms are static methods of the <code>LatticeMazeGenerators</code> namespace class and include generation algorithms based on randomized depth-first search, Wilson's algorithm (Wilson, 1996), percolation (Duminil-Copin, 2017; Fisher & Essam, 2004), Kruskal's algorithm (Kruskal, 1956), and others.

Furthermore, a dataset of mazes can be filtered to satisfy certain properties. Custom filters can be specified, and some filters are included in MazeDatasetFilters. For example, we can require a minimum path length of three steps from the origin to the target:

```
dataset_filtered: MazeDataset = dataset.filter_by.path_length(min_length=3)
```

All implemented maze generation algorithms are stochastic by nature. For reproducibility, the seed parameter of MazeDatasetConfig may be set. In practice, using provided deduplication filters, we find that exact duplicate mazes are generated very infrequently, even when generating very large datasets.

For use cases where mazes of different sizes, generation algorithms, or other parameter variations are required, we provide the MazeDatasetCollection class, which allows for creating a single iterable dataset from multiple independent configurations.



Visual Output Formats

Internally, mazes are SolvedMaze objects, which have path information and a tensor optimized for storing sub-graphs of a lattice. These objects can be converted to and from several formats to maximize their utility in different contexts.

as_ascii() as_pixels() MazePlot() Simple text format for disvamun οf feature-rich plotting utility arrav playing mazes, useful for with support for multiple dtype=uint8 and shape debugging in a terminal en-(height, width, 3). paths, heatmaps over posivironment. The last dimension is RGB tions, and more. color.

Figure 2: Various output formats. Top row (left to right): ASCII diagram, rasterized pixel grid, and advanced display tool.

In previous work, maze tasks have been used with Recurrent Convolutional Neural Network (RCNN) derived architectures (Schwarzschild, Borgnia, Gupta, Huang, et al., 2021). To facilitate the use of our package in this context, we replicate the format of (Schwarzschild, Borgnia, Gupta, Bansal, et al., 2021) and provide the RasterizedMazeDataset class which returns rasterized pairs of (input, target) mazes as shown in Figure 3 below.

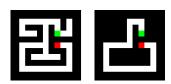


Figure 3: Input is the rasterized maze without the path marked (left), and provide as a target the maze with all but the correct path removed (right). Configuration options exist to adjust whether endpoints are included and if empty cells should be filled in.

Tokenized Output Formats

Autoregressive transformer models can be quite sensitive to the exact format of input data, and may even use delimiter tokens to perform reasoning steps (Pfau et al., 2024; Spies et al., 2024). To facilitate systematic investigation of the effects of different representations of data on text model performance, we provide a variety of tokenized text output formats.

We convert mazes to token sequences in two steps. First, the maze is stringified using as_tokens(). The MazeTokenizerModular class provides a powerful interface for configuring maze stringification behavior. Second, the sequence of strings is tokenized into integers using encode(). Tokenization uses a fixed vocabulary for simplicity. Mazes up to 50×50 are



supported when using a unique token for each position, and up to 128×128 are supported when positions in the maze are represented as a pair of coordinates.

There are many algorithms by which one might tokenize a 2D maze into a 1D format usable by autoregressive text models. Training multiple models on the encodings output from each of these algorithms may produce very different internal representations, learned solution algorithms, and levels of performance. To allow exploration of how different maze tokenization algorithms affect these models, the MazeTokenizerModular class contains a rich set of options to customize how mazes are stringified. This class contains 19 discrete parameters, resulting in over 5.8 million unique tokenizers. There are 6 additional parameters available whose functionality is not verified via automated testing, but further expand the the number of tokenizers by a factor of 44/3 to 86 million.

All output sequences consist of four token regions representing different features of the maze; an example output sequence is shown in Figure 4.

Figure 4: Example text output format with token regions highlighted. Adjacency list: text representation of the graph, Origin: starting coordinate, Target: ending coordinate, Path: maze solution sequence

Each MazeTokenizerModular is constructed from a set of several _TokenizerElement objects, each of which specifies how different token regions or other elements of the stringification are produced.

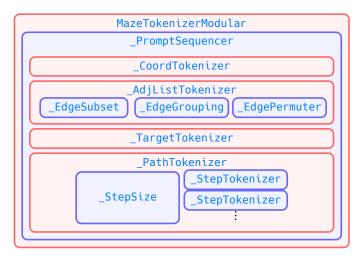


Figure 5: Nested internal structure of _TokenizerElement objects inside a typical MazeTokenizerModular.

The tokenizer architecture is purposefully designed such that adding and testing a wide variety of new tokenization algorithms is fast and minimizes disturbances to functioning code. This is enabled by the modular architecture and the automatic inclusion of any new tokenizers in integration tests. To create a new variety of tokenizer, developers forking the



library may simply create their own _TokenizerElement subclass and implement the abstract methods. If the behavior change is sufficiently small, simply adding a parameter to an existing _TokenizerElement subclass and updating its implementation will suffice.

The breadth of tokenizers is also easily scaled in the opposite direction. Due to the exponential scaling of parameter combinations, adding a small number of new features can significantly slow certain procedures which rely on constructing all possible tokenizers, such as integration tests. If any existing subclass contains features which aren't needed, a developer tool decorator <code>@mark_as_unsupported</code> is provided which can be applied to the unneeded <code>_TokenizerElement</code> subclasses to prune those features and compact the available space of tokenizers.

Benchmarks of Generation Speed

We provide approximate benchmarks for relative generation time across various algorithms, parameter choices, maze sizes, and dataset sizes in Table 1 and Figure 6. Experiments were performed on a standard GitHub runner without parallelism.

maze_ctor	keyword args	all sizes	$\begin{array}{c} small \\ g \leq 10 \end{array}$	$g \in (10, 32]$	large $g > 32$
	Reyword args			- , ,	
dfs		28.0	2.8	20.3	131.8
dfs	accessible_cells=20	2.3	2.2	2.4	2.2
dfs	do_forks=False	2.7	2.2	3.1	3.5
dfs	$max_tree_depth=0.5$	2.5	2.0	2.7	4.0
dfs_percolation	p=0.1	43.9	2.8	33.9	208.0
dfs_percolation	p=0.4	48.7	3.0	36.5	233.5
kruskal		12.8	1.9	10.3	55.8
percolation	p=1.0	50.2	2.6	37.2	242.5
recursive_div		10.2	1.7	8.9	42.1
wilson		676.5	7.8	188.6	3992.6
mean	·	559.9	13.0	223.5	3146.9
median		11.1	6.5	32.9	302.7

Table 1: Generation times for various algorithms and maze sizes. More information can be found on the benchmarks page.

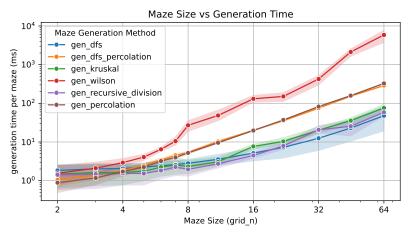


Figure 6: Plot of maze generation time. Generation time scales exponentially with maze size for all algorithms. Generation time per maze does not depend on the number of mazes being generated, and there is minimal overhead to initializing the generation process for a small dataset. Wilson's algorithm is notably less efficient than others and has high variance. Note that values are averaged across all parameter sets for that algorithm. More information can be found on the benchmarks page.



Success Rate Estimation

In order to replicate the exact dataset distribution of (Schwarzschild, Borgnia, Gupta, Bansal, et al., 2021), the parameter MazeDatasetConfig.endpoint_kwargs: EndpointKwargsType allows for additional constraints such as enforcing that the start or end point be in a "dead end" with only one accessible neighbor cell. However, combining these constraints with cyclic mazes (such as those generated with percolation), as was required for the work in (Knutson et al., 2024), can lead to an absence of valid start and end points. Placing theoretical bounds on this success rate is difficult, as it depends on the exact maze generation algorithm and parameters used. To deal with this, our package provides a way to estimate the success rate of a given configuration using a symbolic regression model trained with PySR (Cranmer, 2023). More details on this can be found in estimate_dataset_fractions.ipynb.

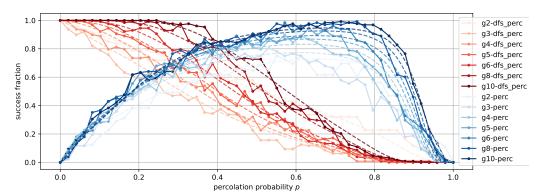


Figure 7: An example of both empirical and predicted success rates as a function of the percolation probability p for various maze sizes, percolation with and without depth first search, and endpoint_kwargs requiring that both the start and end be in unique dead ends. Empirical measures derived from a sample of 128 mazes. More information can be found on the benchmarks page.

Implementation

Using an adjacency matrix for storing mazes would be memory inefficient by failing to exploit the highly sparse structure, while using an adjacency list could lead to a poor lookup time. This package utilizes a simple, efficient representation of mazes as subgraphs of a finite lattice, which we call a LatticeMaze.

We describe mazes with the following representation: for a 2-dimensional lattice with r rows and c columns, we initialize a boolean array

$$A = \{0, 1\}^{2 \times r \times c}$$

which we refer to in the code as a connection_list. The value at A[0,i,j] determines whether a downward connection exists from node [i,j] to [i+1,j]. Likewise, the value at A[1,i,j] determines whether a rightward connection to [i,j+1] exists. Thus, we avoid duplication of data about the existence of connections and facilitate fast lookup time, at the cost of requiring additional care with indexing. Note that this setup allows for a periodic lattice. Generation of mazes is detailed in LatticeMazeGenerators.



Usage in Research

This package was originally built for the needs of the (Michael I. Ivanitskiy et al., 2023b) project, which aims to investigate spatial planning and world models in autoregressive transformer models trained on mazes (Michael Igorevich Ivanitskiy, Spies, et al., 2023; Michael Igorevich Ivanitskiy, Shah, et al., 2023; Spies et al., 2024). It was extended for work on understanding the mechanisms by which recurrent convolutional and implicit networks (Fung et al., 2022) solve mazes given a rasterized view (Knutson et al., 2024), which required matching the pixel-padded and endpoint constrained output format of (Schwarzschild, Borgnia, Gupta, Bansal, et al., 2021). Ongoing work using maze-dataset aims to investigate the effects of varying the tokenization format on the performance of pretrained LLMs on spatial reasoning.

This package has also been utilized in work by other groups:

- By (Nolte et al., 2024) to compare the effectiveness of transformers trained with the MLM-\$\mathcal{U}\$ (Kitouni et al., 2024) multistep prediction objective against standard autoregressive training for multi-step planning on our maze task.
- By (Wang et al., 2024) and (Chen et al., 2024) to study the effectiveness of imperative learning.
- By (Zhang et al., 2025) to introduce a novel framework for reasoning diffusion models.
- By (Dao & Vu, 2025) to improve spatial reasoning in LLMs with GRPO.

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