Exercise code provide by Instructor Alexander Booth, with some edits by the author.