A TPTP Formalization of the Unified Foundational Ontology

Daniele Porelo, João Paulo A. Almeida, Giancarlo Guizzardi,
Claudenir M. Fonseca, Tiago Prince Sales

October 16, 2021

Abstract

This document presents a formalization of the Unified Foundation Ontology (UFO) expressed in first-order logics through the TPTP syntax. This formalization is intended to support verification of UFO's theory through automated provers and consistency checkers.

1 Introduction

This document presents a formalization of the Unified Foundation Ontology (UFO) expressed in first-order logics through the TPTP syntax. This formalization is intended to support verification of UFO's theory through automated provers and consistency checkers.

2 UFO's TPTP Specification

2.1 UFO Taxonomy

2.1.1 Partial Taxonomy of Thing

```
% Thing

fof(ax_thing_taxonomy, axiom, (
  ![X]: ((type_(X) | individual(X)) <=> (thing(X)))
)).

fof(ax_thing_partition, axiom, (
  ~?[X]: (type_(X) & individual(X))
)).

% Individual

fof(ax_individual_taxonomy, axiom, (
  ![X]: ((concreteIndividual(X) | abstractIndividual(X)) <=> (
    individual(X)))
```

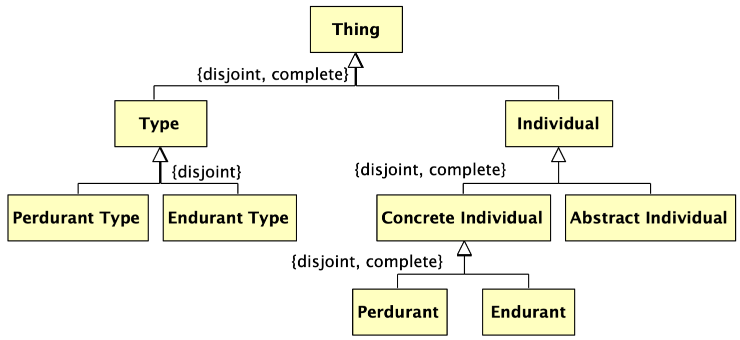

Figure 1: Partial Taxonomy of UFO – Thing.

```
)).

fof(ax_individual_partition, axiom, (
  ~?[X]: (concreteIndividual(X) & abstractIndividual(X))
)).

% Concrete Individual

fof(ax_concreteIndividual_taxonomy, axiom, (
  ![X]: ((endurant(X) | perdurant(X)) <=> (concreteIndividual(X)))
)).

fof(ax_concreteIndividual_partition, axiom, (
  ~?[X]: (endurant(X) & perdurant(X))
)).

% Type

fof(ax_type_taxonomy, axiom, (
  ![X]: ((endurantType(X) | perdurantType(X)) => (type_(X)))
)).

fof(ax_type_partition, axiom, (
  ~?[X]: (endurantType(X) & perdurantType(X))
)).

% Thing partial taxonomy instances
% (tested to rule out trivial models)

% fof(ax_thing_instances, axiom, (
%   type_(type1) & individual(individual1) & concreteIndividual(concreteIndividual1) & abstractIndividual(abstractIndividual1) & endurant(endurant1) & perdurant(perdurant1) & endurantType(endurantType1) & perdurantType(perdurantType1)
% )).
```

2.1.2 Partial Taxonomy of Abstract Individual

```
% Abstract Individual

```

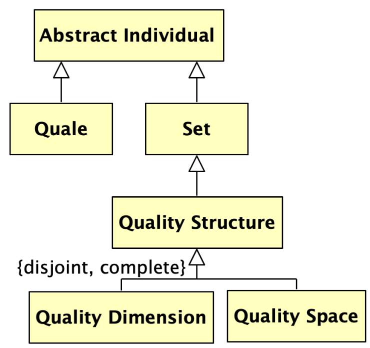

Figure 2: Partial Taxonomy of UFO – Abstract Individual.

```
fof(ax_abstractIndividual_taxonomy_quale, axiom, (
  ![X]: (quale(X) => (abstractIndividual(X)))
)).

fof(ax_abstractIndividual_taxonomy_set, axiom, (
  ![X]: (set_(X) => (abstractIndividual(X)))
)).

fof(ax_abstractIndividual_taxonomy_world, axiom, (
  ![X]: (world(X) => (abstractIndividual(X)))
)).

% Set

fof(ax_set_taxonomy_qualityStructure, axiom, (
  ![X]: (qualityStructure(X) => (set_(X)))
)).

% Quality Structure

fof(ax_qualityStructure_taxonomy, axiom, (
  ![X]: ((qualityDimension(X) | qualitySpace(X)) <=> (
    qualityStructure(X)))
)).

fof(ax_qualityStructure_partition, axiom, (
  ~?[X]: (qualityDimension(X) & qualitySpace(X))
)).

% Abstract Individual partial taxonomy instances
% (tested to rule out trivial models)

% fof(ax_abstractIndividual_instances, axiom, (
%   set_(set1) & quale(quale1) & qualityStructure(qualityStructure1
    ) & qualityDimension(qualityDimension1) & qualitySpace(
    qualitySpace1) & world(world1)
% )).
```

2.1.3 Partial Taxonomy of Endurant

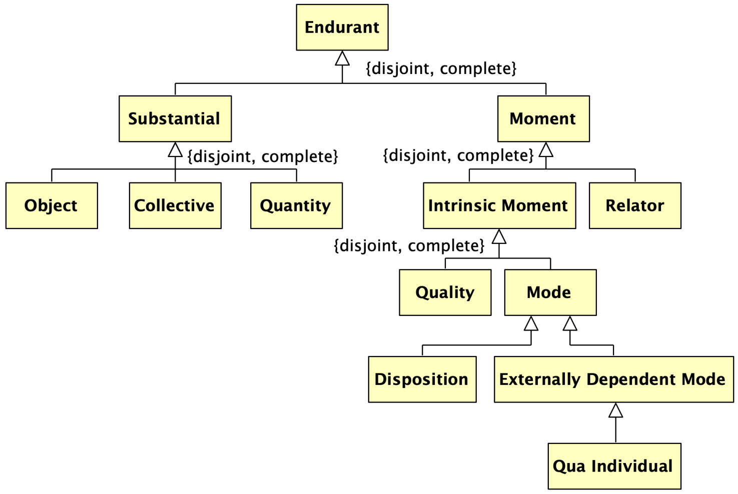

Figure 3: Partial Taxonomy of UFO – Endurant.

```
% Endurant

fof(ax_endurant_taxonomy, axiom, (
  ![X]: ((substantial(X) | moment(X)) <=> (endurant(X)))
)).

fof(ax_endurant_partition, axiom, (
  ~?[X]: (substantial(X) & moment(X))
)).

% Substantial

fof(ax_substantial_taxonomy, axiom, (
  ![X]: ((object(X) | collective(X) | quantity(X)) <=> (substantial
    (X)))
)).

fof(ax_substantial_partition, axiom, (
  ~?[X]: ((object(X) & collective(X)) | (object(X) & quantity(X)) |
     (collective(X) & quantity(X)))
)).

% Moment

fof(ax_moment_taxonomy, axiom, (
  ![X]: ((intrinsicMoment(X) | relator(X)) <=> (moment(X)))
)).

fof(ax_moment_partition, axiom, (
  ~?[X]: (intrinsicMoment(X) & relator(X))
)).

% Intrinsic Moment
```

```
fof(ax_intrinsicMoment_taxonomy, axiom, (
  ![X]: ((quality(X) | mode(X)) <=> (intrinsicMoment(X)))
)).

fof(ax_intrinsicMoment_partition, axiom, (
  ~?[X]: (quality(X) & mode(X))
)).

% Mode

fof(ax_mode_taxonomy_externallyDependentMode, axiom, (
  ![X]: (externallyDependentMode(X) => (mode(X)))
)).

% Externally Dependent Mode

fof(ax_externallyDependentMode_taxonomy_quaIndividual, axiom, (
  ![X]: (quaIndividual(X) => (externallyDependentMode(X)))
)).

% Endurant partial taxonomy instances
% (tested to rule out trivial models)

% fof(ax_endurant_instances, axiom, (
%   substantial(substantial1) & moment(moment1) & object(object1) &
     collective(collective1) & quantity(quantity1) &
    intrinsicMoment(intrinsicMoment1) & relator(relator1) & quality
    (quality1) & mode(mode1) & disposition(disposition1) &
    externallyDependentMode(externallyDependentMode1) &
    quaIndividual(quaIndividual1)
% )).
```

2.1.4 Partial Taxonomy of Endurant Type (on ontological natures)

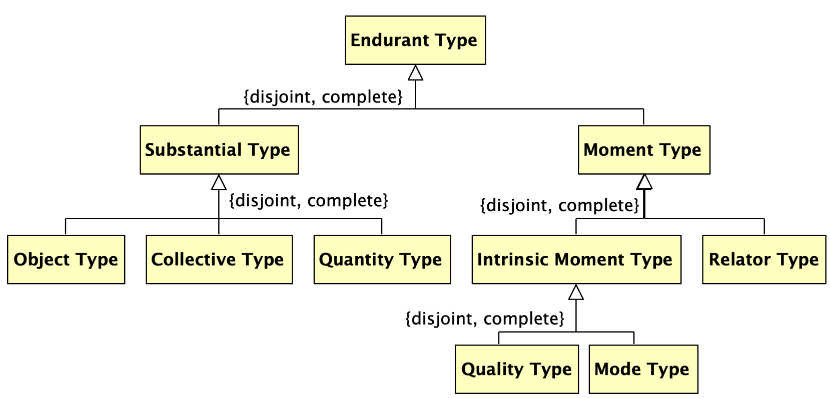

Figure 4: Partial Taxonomy of UFO – Endurant Types (by ontological nature).

```
% Endurant Type (by ontological nature)

```

```
fof(ax_endurantType_taxonomy_nature, axiom, (
  ![X]: ((substantialType(X) | momentType(X)) <=> (endurantType(X))
    )
)).

fof(ax_endurantType_partition_nature, axiom, (
  ~?[X]: (substantialType(X) & momentType(X))
)).

% Substantial Type

fof(ax_substantialType_taxonomy, axiom, (
  ![X]: ((objectType(X) | collectiveType(X) | quantityType(X)) <=>
    (substantialType(X)))
)).

fof(ax_substantialType_partition, axiom, (
  ~?[X]: ((objectType(X) & collectiveType(X)) | (objectType(X) &
    quantityType(X)) | (collectiveType(X) & quantityType(X)))
)).

% Moment Type

fof(ax_momentType_taxonomy, axiom, (
  ![X]: ((intrinsicMomentType(X) | relatorType(X)) <=> (momentType(
    X)))
)).

fof(ax_momentType_partition, axiom, (
  ~?[X]: (intrinsicMomentType(X) & relatorType(X))
)).

% Intrinsic Moment Type

fof(ax_intrinsicMomentType_taxonomy, axiom, (
  ![X]: ((qualityType(X) | modeType(X)) <=> (intrinsicMomentType(X)
    ))
)).

fof(ax_intrinsicMomentType_partition, axiom, (
  ~?[X]: (qualityType(X) & modeType(X))
)).

% Endurant Type (by ontological nature) partial taxonomy instances
% (tested to rule out trivial models)

% fof(ax_endurantType_instances_natures, axiom, (
%   substantialType(substantialType1) & momentType(momentType1) &
    objectType(objectType1) & collectiveType(collectiveType1) &
    quantityType(quantityType1) & intrinsicMomentType(
    intrinsicMomentType1) & relatorType(relatorType1) & qualityType
    (qualityType1) & modeType(modeType1)
% )).
```

2.1.5 Partial Taxonomy of Endurant Type (on modal properties of types)

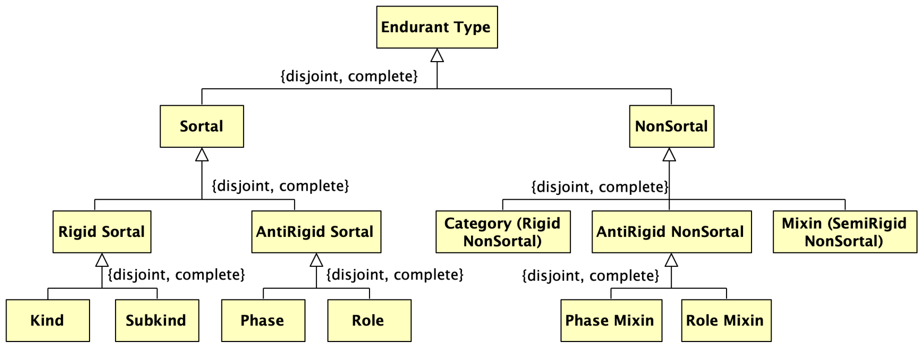

Figure 5: Partial Taxonomy of UFO – Endurant Types (by modal properties of types).

```
% Endurant Type (by modal properties of types)

fof(ax_endurantType_taxonomy_properties, axiom, (
  ![X]: ((sortal(X) | nonSortal(X)) <=> (endurantType(X)))
)).

fof(ax_endurantType_partition_properties, axiom, (
  ~?[X]: (sortal(X) & nonSortal(X))
)).

% Sortal

fof(ax_sortal_taxonomy, axiom, (
  ![X]: ((rigidSortal(X) | antiRigidSortal(X)) <=> (sortal(X)))
)).

fof(ax_sortal_partition, axiom, (
  ~?[X]: (rigidSortal(X) & antiRigidSortal(X))
)).

% Rigid Sortal

fof(ax_rigidSortal_taxonomy, axiom, (
  ![X]: ((kind(X) | subkind(X)) <=> (rigidSortal(X)))
)).

fof(ax_rigidSortal_partition, axiom, (
  ~?[X]: (kind(X) & subkind(X))
)).

% Anti-Rigid Sortal

fof(ax_antiRigidSortal_taxonomy, axiom, (
  ![X]: ((phase(X) | role(X)) <=> (antiRigidSortal(X)))
```

```
)).

fof(ax_antiRigidSortal_partition, axiom, (
  ~?[X]: (phase(X) & role(X))
)).

% Non-Sortal

fof(ax_nonSortal_taxonomy, axiom, (
  ![X]: ((rigidNonSortal(X) | semiRigidNonSortal(X) | antiRigidNonSortal(X)) <=> (nonSortal(X)))
)).

fof(ax_nonSortal_partition, axiom, (
  ~?[X]: ((rigidNonSortal(X) & semiRigidNonSortal(X)) | (rigidNonSortal(X) & antiRigidNonSortal(X)) | (semiRigidNonSortal(X) & antiRigidNonSortal(X)))
)).

% Category

fof(ax_rigidNonSortal_taxonomy, axiom, (
  ![X]: (rigidNonSortal(X) <=> (category(X)))
)).

% Mixin

fof(ax_semiRigidNonSortal_taxonomy, axiom, (
  ![X]: (semiRigidNonSortal(X) <=> (mixin(X)))
)).

% Anti-Rigid Non-Sortal

fof(ax_antiRigidNonSortal_taxonomy, axiom, (
  ![X]: ((phaseMixin(X) | roleMixin(X)) <=> (antiRigidNonSortal(X)))
)).

fof(ax_antiRigidNonSortal_partition, axiom, (
  ~?[X]: (phaseMixin(X) & roleMixin(X))
)).

% Endurant Type (by modal properties of types) partial taxonomy instances
% (tested to rule out trivial models)

% fof(ax_endurantType_instances_properties, axiom, (
%   sortal(sortal1) & nonSortal(nonSortal1) & rigidSortal(rigidSortal1) & antiRigidSortal(antiRigidSortal1) & kind(kind1) & subkind(subkind1) & phase(phase1) & role(role1) & category(category1) & mixin(mixin1) & antiRigidNonSortal(antiRigidNonSortal1) & phaseMixin(phaseMixin1) & roleMixin(roleMixin1)
% )).
```

2.1.6 Defining Types, Individuals, and Specialization

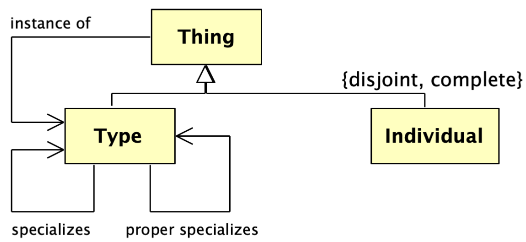

Figure 6: Types, individuals, instantiation, and specialization.

```
%%%%%%%%%%% Instance of, Types, and Individuals %%%%%%%%%%

fof(ax_dIof, axiom, (
  ![X,Y,W]: (iof(X,Y,W) => (type_(Y) & world(W)))
)).

fof(ax_dType_a1, axiom, (
  ![X]: (type_(X) <=> (?[Y,W]: iof(Y,X,W)))
)).

fof(ax_dIndividual_a2, axiom, (
  ![X]: (individual(X) <=> (~?[Y,W]: iof(Y,X,W)))
)).

% TODO: confirm whether we are including second-order types in this
     formalization

fof(ax_multiLevel_a3, axiom, (
  ![X,Y,W]: (iof(X,Y,W) => (type_(X) | individual(X)))
)).

fof(ax_twoLevelConstrained_a4, axiom, (
  ~?[X,Y,Z,W]: (type_(X) & iof(X,Y,W) & iof(Y,Z,W))
)).

% Instantiation relations
% (tested to rule out trivial models)

% fof(ax_iofInUse, axiom, (
%   type_(t2) & individual(i2) & world(w2) & iof(i2,t2,w2)
% )).

% Ax |= "th_everythingIsAThing_t1"; conjecture commented for
    convenience

% fof(th_everythingIsAThing_t1, conjecture, (
%   ![X]: (type_(X) | individual(X))
% )).

% Ax |= "th_thingPartition_t2"; conjecture commented for
    convenience
```

```
% fof(th_thingPartition_t2, conjecture, (
%   ~?[X]: (type_(X) & individual(X))
% )).

%%%%%%%% Specialization and Proper Specialization %%%%%%%%

fof(ax_dSpecializes, axiom, (
  ![X,Y]: (specializes(X,Y) => (type_(X) & type_(Y)))
)).

fof(ax_specialization_a5, axiom, (
  ![T1,T2]: (specializes(T1,T2) <=> (
    type_(T1) & type_(T2) & ![W]: (world(W) => ![E]: (iof(E,T1,W) => iof(E,T2,W)))
  ))
)).

fof(ax_properSpecializes_d1, axiom, (
  ![X,Y]: (properSpecializes(X,Y) <=> (specializes(X,Y) & ~specializes(Y,X)))
)).

% Ax |= "th_cyclicSpecializations_t3"; conjecture commented for convenience

% fof(th_cyclicSpecializations_t3, conjecture, (
%   ![X,Y]: (specializes(X,Y) => (specializes(X,X) & specializes(Y,Y)))
% )).

% Ax |= "th_transitiveSpecializations_t4"; conjecture commented for convenience

% fof(th_transitiveSpecializations_t4, conjecture, (
%   ![X,Y,Z]: ((specializes(X,Y) & specializes(Y,Z)) => (specializes(X,Z)))
% )).

fof(ax_sharedSpecializations_a6, axiom, (
  ![T1,T2]: (?[X,W]: ((iof(X,T1,W) & iof(X,T2,W) & ~specializes(T1,T2) & ~specializes(T2,T1)) => (
      (?[T3]: (specializes(T1,T3) & specializes(T2,T3) & iof(X,T3,W)))|
      (?[T3]: (specializes(T3,T1) & specializes(T3,T2) & iof(X,T3,W)))
  )))
)).

% Specialization relations
% (tested to rule out trivial models)

% fof(ax_specializesInUse, axiom, (
%   endurantType(t3_1) & endurantType(t3_2) & specializes(t3_1,t3_2) & properSpecializes(t3_1,t3_2) & specializes(t3_1,t3_1) & endurant(e3) & world(w3) & iof(e3,t3_1,w3)
% )).
```

2.1.7 Defining Rigidity and Sortality

```
% Rigidity

% TODO: I don't find we need to attach the "rigid(T)" predicate to the "endurant(T)" predicate like the paper does, so let's review this idea.
% TODO: verify whether it is a problem not to introduce predicates "world(W1) &" and "world(W2) &" before each instantiation

fof(ax_dRigid_a18, axiom, (
  ![T]: (rigid(T) <=> (endurantType(T) & (
    ![X]: ((?[W1]: (world(W1) & iof(X,T,W1))) => (![W2]: (world(W2) => iof(X,T,W2))))
  )))
)).

fof(ax_dAntiRigid_a19, axiom, (
  ![T]: (antiRigid(T) <=> (endurantType(T) & (
    ![X]: ((?[W1]: (world(W1) & iof(X,T,W1))) => (?[W2]: (world(W2) & ~iof(X,T,W2)))
  ))))
)).

fof(ax_dSemiRigid_a20, axiom, (
  ![T]: (semiRigid(T) <=> (endurantType(T) & ~rigid(T) & ~antiRigid(T)))
)).

% Ax |= "th_thEndurantTypeHaveRigidity_t5"; conjecture commented for convenience

% fof(th_thEndurantTypeHaveRigidity_t5, conjecture, (
%   ![T]: (endurantType(T) <=> (rigid(T) | semiRigid(T) | antiRigid(T)))
% )).

% Ax |= "th_pairwiseDisjointRigidities_t6"; conjecture commented for convenience

% fof(th_pairwiseDisjointRigidities_t6, conjecture, (
%   ~![T]: ((rigid(T) & semiRigid(T)) | (semiRigid(T) & antiRigid(T)) | (rigid(T) & antiRigid(T)))
% )).

% Ax |= "th_rigidAntiRigidSpecializationConstraint_t7"; conjecture commented for convenience

% fof(th_rigidAntiRigidSpecializationConstraint_t7, conjecture, (
%   ~![T1,T2]: (rigid(T1) & antiRigid(T2) & specializes(T1,T2))
% )).

% Ax |= "th_semiRigidAntiRigidSpecializationConstraint_t8"; conjecture commented for convenience

% fof(th_semiRigidAntiRigidSpecializationConstraint_t8, conjecture, (
```

```
%   ~![T1,T2]: (semiRigid(T1) & antiRigid(T2) & specializes(T1,T2))
% )).

% Rigidity properties
% (tested to rule out trivial models)

% fof(ax_rigidityInUse, axiom, (
%   endurantType(t4_1) & endurantType(t4_2) & endurantType(t4_3) & rigid(t4_1) & semiRigid(t4_2) & antiRigid(t4_3) & properSpecializes(t4_1,t4_2) & properSpecializes(t4_3,t4_1)
% )).

% Sortality

fof(ax_endurantsKind_a21, axiom, (
  ![E]: (endurant(E) => (
    ?[U]: (kind(U) & (![W]: (world(W) => iof(E,U,W))))
  ))
)).

fof(ax_uniqueKind_a22, axiom, (
  ![E,U,W]: ((world(W) & kind(U) & iof(E,U,W)) => (
    ~?[U2,W2]: (kind(U2) & iof(E,U2,W2) & ~(U = U2))
  ))
)).

% Changing "ax_dSortal_a23" from the form it was defined in the paper to "sortals are endurant types that specialize some ultimate sortal" seem to express the same concept while speeding up the execution of SPASS considerably

% fof(ax_dSortal_a23, axiom, (
%   ![S]: (sortal(S) <=> (endurantType(S) & (?[U]: (kind(U) & (![E,W]: (iof(E,S,W) => iof(E,U,W)))))))
% )).

fof(ax_dSortal_a23, axiom, (
  ![S]: ((sortal(S)) <=> (endurantType(S) & (?[U]: (kind(U) & specializes(S,U)))))
)).

% If we have the taxonomy's axiomatization, then a24 becomes a theorem
% Ax |= "th_nonSortalsAreEndurantsThatAreNotSortals_a24"; conjecture commented for convenience

% fof(th_nonSortalsAreEndurantsThatAreNotSortals_a24, conjecture, (
%   ![NS]: ((nonSortal(NS)) <=> (endurantType(NS) & ~sortal(NS)))
% )).

% Ax |= "th_kindsAreRigid_t9"; conjecture commented for convenience

% fof(th_kindsAreRigid_t9, conjecture, (
%   ![U]: ((kind(U)) => (rigid(U)))
% )).

% Ax |= "th_kindsHaveDisjointExtensions_t10"; conjecture commented
```

```
    for convenience

% fof(th_kindsHaveDisjointExtensions_t10, conjecture, (
%   ![K1,K2]: ((kind(K1) & kind(K2) & ~(K1=K2)) => (
%     ~?[X,W1,W2]: (world(W1) & world(W2) & iof(X,K1,W1) & iof(X,K2
    ,W2)))
%   )
% )).

% Ax |= "th_kindsHaveDisjointTaxonomies_t11"; conjecture commented
    for convenience

% fof(th_kindsHaveDisjointTaxonomies_t11, conjecture, (
%   ![K1,K2]: ((kind(K1) & kind(K2) & ~(K1=K2)) => (
%     ~?[T]: (specializes(T,K1) & specializes(T,K2)))
%   )
% )).

% Ax |= "th_kindsAreSortal_t12"; conjecture commented for
    convenience

% fof(th_kindsAreSortal_t12, conjecture, (
%   ![K]: ((kind(K)) => (sortal(K)))
% )).

% Ax |= "th_sortalSpecializeKinds_t13"; conjecture commented for
    convenience

% fof(th_sortalSpecializeKinds_t13, conjecture, (
%   ![S]: ((sortal(S)) => (?[K]: (kind(K) & specializes(S,K))))
% )).

% Ax |= "th_sortalsSpecializeAUniqueKind_t14"; conjecture commented
     for convenience

% fof(th_sortalsSpecializeAUniqueKind_t14, conjecture, (
%   ![S]: ((sortal(S)) => (~?[U,U2]: (kind(U) & kind(U2) &
    specializes(S,U) & specializes(S,U2) & ~(U=U2))))
% )).

% Sortality properties
% (tested to rule out trivial models)

% fof(ax_sortalityInUse, axiom, (
%   endurant(e5_1) & endurant(e5_2) & world(w5) & kind(k5_1) & kind
    (k5_2) & iof(e5_1,k5_1,w5) & iof(e5_1,k5_1,w5) & ~(k5_1=k5_2)
% )).

% Sortality + Rigidity

fof(ax_rigidSortalsAreRigidAndSortal_xx, axiom, (
  ![T]: ((rigidSortal(T)) <=> (rigid(T) & sortal(T)))
)).

fof(ax_antiRigidSortalsAreAntiRigidAndSortal_xx, axiom, (
  ![T]: ((antiRigidSortal(T)) <=> (antiRigid(T) & sortal(T)))
)).
```

```

fof(ax_rigidNonSortalsAreRigidAndNonSortal_xx, axiom, (
  ![T]: ((rigidNonSortal(T)) <=> (rigid(T) & nonSortal(T)))
)).

fof(ax_antiRigidNonSortalsAreAntiRigidAndNonSortal_xx, axiom, (
  ![T]: ((antiRigidNonSortal(T)) <=> (antiRigid(T) & nonSortal(T)))
)).

fof(ax_semiRigidNonSortalsAreSemiRigidAndNonSortal_xx, axiom, (
  ![T]: ((semiRigidNonSortal(T)) <=> (semiRigid(T) & nonSortal(T)))
)).

% If we have the taxonomy's axiomatization, then a25 becomes a theorem
% Ax |= "th_kindAndSubkindAreDisjoint_a25"; conjecture commented for convenience

% fof(th_kindAndSubkindAreDisjoint_a25, conjecture, (
%   ~?[T]: (kind(T) & subkind(T))
% )).

% If we have the taxonomy's axiomatization, then a26 becomes a theorem
% Ax |= "th_kindAndSubkindAreRigidSortals_a26"; conjecture commented for convenience

% fof(th_kindAndSubkindAreRigidSortals_a26, conjecture, (
%   ![T]: ((kind(T) | subkind(T)) <=> (rigid(T) & sortal(T)))
% )).

% If we have the taxonomy's axiomatization, then a27 becomes a theorem
% Ax |= "th_phaseAndRoleAreDisjoint_a27"; conjecture commented for convenience

% fof(th_phaseAndRoleAreDisjoint_a27, conjecture, (
%   ~?[T]: (phase(T) & role(T))
% )).

% If we have the taxonomy's axiomatization, then a28 becomes a theorem
% Ax |= "th_phaseAndRoleAreAntiRigidSortals_a28"; conjecture commented for convenience

% fof(th_phaseAndRoleAreAntiRigidSortals_a28, conjecture, (
%   ![T]: ((phase(T) | role(T)) <=> (antiRigid(T) & sortal(T)))
% )).

% Skipping (a29) because we leave the concept of semi-rigid sortals out of this ontology.

% If we have the taxonomy's axiomatization, then a30 becomes a theorem
% Ax |= "th_categoriesAreRigidNonSortals_a30"; conjecture commented for convenience

```

```
% fof(th_categoriesAreRigidNonSortals_a30, conjecture, (
%   ![T]: ((category(T)) <=> (rigid(T) & nonSortal(T)))
% )).

% If we have the taxonomy's axiomatization, then a31 becomes a theorem
% Ax |= "th_mixinsAreSemiRigidNonSortals_a31"; conjecture commented for convenience

% fof(th_mixinsAreSemiRigidNonSortals_a31, conjecture, (
%   ![T]: ((mixin(T)) <=> (semiRigid(T) & nonSortal(T)))
% )).

% If we have the taxonomy's axiomatization, then a32 becomes a theorem
% Ax |= "th_phaseMixinAndRoleMixinAreDisjoint_a32"; conjecture commented for convenience

% fof(th_phaseMixinAndRoleMixinAreDisjoint_a32, conjecture, (
%   ~?[T]: (phaseMixin(T) & roleMixin(T))
% )).

% If we have the taxonomy's axiomatization, then a33 becomes a theorem
% Ax |= "ax_phaseMixinAndRoleMixinAreAntiRigidSortals_a33"; conjecture commented for convenience

% fof(th_phaseMixinAndRoleMixinAreAntiRigidSortals_a33, conjecture, (
%   ![T]: ((phaseMixin(T) | roleMixin(T)) <=> (antiRigid(T) & nonSortal(T)))
% )).

% Ax |= "th_leafCategoriesArePairwiseDisjoint_t18"; conjecture commented for convenience

% fof(th_leafCategoriesArePairwiseDisjoint_t18, conjecture, (
%   ~?[T]: (endurantType(T) & (
%     (
%       (kind(T) & subkind(T))
%       | (kind(T) & phase(T))
%       | (kind(T) & role(T))
%       | (kind(T) & category(T))
%       | (kind(T) & mixin(T))
%       | (kind(T) & phaseMixin(T))
%       | (kind(T) & roleMixin(T))
%     ) | (
%       (subkind(T) & phase(T))
%       | (subkind(T) & role(T))
%       | (subkind(T) & category(T))
%       | (subkind(T) & mixin(T))
%       | (subkind(T) & phaseMixin(T))
%       | (subkind(T) & roleMixin(T))
%     ) | (
%       (phase(T) & role(T))
%       | (phase(T) & category(T))
%       | (phase(T) & mixin(T))
```

```
%       | (phase(T) & phaseMixin(T))
%       | (phase(T) & roleMixin(T))
%     ) | (
%       (role(T) & category(T))
%       | (role(T) & mixin(T))
%       | (role(T) & phaseMixin(T))
%       | (role(T) & roleMixin(T))
%     ) | (
%       (category(T) & mixin(T))
%       | (category(T) & phaseMixin(T))
%       | (category(T) & roleMixin(T))
%     ) | (
%       (mixin(T) & phaseMixin(T))
%       | (mixin(T) & roleMixin(T))
%     ) | (
%       (phaseMixin(T) & roleMixin(T))
%     )
%   ))
% )).

% Ax |= "th_leafCategoriesCompletelyCategorizeAllEndurantTypes_t19"; conjecture commented for convenience

% fof(th_leafCategoriesCompletelyCategorizeAllEndurantTypes_t19, conjecture, (
%   ![T]: (endurantType(T) => (
%     kind(T) | subkind(T) | phase(T) | role(T) | category(T) | mixin(T) | phaseMixin(T) | roleMixin(T)
%   ))
% )).

% Sortality and rigidity properties combined
% (tested to rule out trivial models)

% fof(ax_sortalityAndRigidityInUse, axiom, (
%   endurant(e6_1) & endurant(e6_2) & world(w6) & kind(k6_1) & kind(k6_2) & iof(e6_1,k6_1,w6) & iof(e6_1,k6_1,w6) & ~(k6_1=k6_2)
% )).
```

2.1.8 Defining Endurant Types

```
%%%%%%%%%%%%%%%%%%% Types Definition %%%%%%%%%%%%%%%%%%%

% Defining the taxonomy of types of ontological natures through the categorization of the taxonomy of concrete individuals

fof(ax_perdurantTypeDefinition_a44, axiom, (
  ![T]: (perdurantType(T) <=> (
    type_(T) & (![P,W]: ((world(W) & iof(P,T,W)) => (perdurant(P))))
  ))
)).

fof(ax_endurantTypeDefinition_a44, axiom, (
  ![T]: (endurantType(T) <=> (
    type_(T) & (![E,W]: ((world(W) & iof(E,T,W)) => (endurant(E))))
  ))
)).
```

```
fof(ax_substantialTypeDefinition_a44, axiom, (
  ![T]: (substantialType(T) <=> (
    type_(T) & (![E,W]: ((world(W) & iof(E,T,W)) => (substantial(E)
    )))
  ))
)).

fof(ax_momentTypeDefinition_a44, axiom, (
  ![T]: (momentType(T) <=> (
    type_(T) & (![E,W]: ((world(W) & iof(E,T,W)) => (moment(E))))
  ))
)).

fof(ax_objectTypeDefinition_a44, axiom, (
  ![T]: (objectType(T) <=> (
    type_(T) & (![E,W]: ((world(W) & iof(E,T,W)) => (object(E))))
  ))
)).

fof(ax_collectiveTypeDefinition_a44, axiom, (
  ![T]: (collectiveType(T) <=> (
    type_(T) & (![E,W]: ((world(W) & iof(E,T,W)) => (collective(E))
    ))
  ))
)).

fof(ax_quantityTypeDefinition_a44, axiom, (
  ![T]: (quantityType(T) <=> (
    type_(T) & (![E,W]: ((world(W) & iof(E,T,W)) => (quantity(E))))
  ))
)).

fof(ax_intrinsicMomentTypeDefinition_a44, axiom, (
  ![T]: (intrinsicMomentType(T) <=> (
    type_(T) & (![E,W]: ((world(W) & iof(E,T,W)) => (
    intrinsicMoment(E))))
  ))
)).

fof(ax_relatorTypeDefinition_a44, axiom, (
  ![T]: (relatorType(T) <=> (
    type_(T) & (![E,W]: ((world(W) & iof(E,T,W)) => (relator(E))))
  ))
)).

fof(ax_qualityTypeDefinition_a44, axiom, (
  ![T]: (qualityType(T) <=> (
    type_(T) & (![E,W]: ((world(W) & iof(E,T,W)) => (quality(E))))
  ))
)).

fof(ax_modeTypeDefinition_a44, axiom, (
  ![T]: (modeType(T) <=> (
    type_(T) & (![E,W]: ((world(W) & iof(E,T,W)) => (mode(E))))
  ))
)).
```

```
% Types Definition
% (tested to rule out trivial models)
% TODO: investigate why we cannot list four different endurant types (it may have something to do with "intrinsicMoment" and "intrinsicMomentType")

% fof(ax_typesDefinitionsInstances, axiom, (
%   objectType(ot7) & collectiveType(ct7) & modeType(mt7)
% )).

% Ax |= "th_leafCategoriesArePairwiseDisjoint_t21"; conjecture commented for convenience
% Having the previously defined taxonomy, this should be quite trivial

% fof(th_leafCategoriesArePairwiseDisjoint_t21, conjecture, (
%   ~?[T]: (type_(T) & (
%     (
%       (objectType(T) & collectiveType(T)) | (objectType(T) & quantityType(T)) | (objectType(T) & modeType(T)) | (objectType(T) & qualityType(T)) | (objectType(T) & relatorType(T)) | (objectType(T) & perdurantType(T))
%     ) | (
%       (collectiveType(T) & quantityType(T)) | (collectiveType(T) & modeType(T)) | (collectiveType(T) & qualityType(T)) | (collectiveType(T) & relatorType(T)) | (collectiveType(T) & perdurantType(T))
%     ) | (
%       (quantityType(T) & modeType(T)) | (quantityType(T) & qualityType(T)) | (quantityType(T) & relatorType(T)) | (quantityType(T) & perdurantType(T))
%     ) | (
%       (modeType(T) & qualityType(T)) | (modeType(T) & relatorType(T)) | (modeType(T) & perdurantType(T))
%     ) | (
%       (qualityType(T) & relatorType(T)) | (qualityType(T) & perdurantType(T))
%     ) | (
%       relatorType(T) & perdurantType(T)
%     )
%   ))
% )).

% Ultimate Sortals Definitions (by ontological nature)

fof(ax_objectKindDefinition_a45, axiom, (
  ![T]: (objectKind(T) <=> (objectType(T) & kind(T)))
)).

fof(ax_collectiveKindDefinition_a45, axiom, (
  ![T]: (collectiveKind(T) <=> (collectiveType(T) & kind(T)))
)).

fof(ax_quantityKindDefinition_a45, axiom, (
  ![T]: (quantityKind(T) <=> (quantityType(T) & kind(T)))
)).
```

```

fof(ax_modeKindDefinition_a45, axiom, (
  ![T]: (modeKind(T) <=> (modeType(T) & kind(T)))
)).

fof(ax_qualityKindDefinition_a45, axiom, (
  ![T]: (qualityKind(T) <=> (qualityType(T) & kind(T)))
)).

fof(ax_relatorKindDefinition_a45, axiom, (
  ![T]: (relatorKind(T) <=> (relatorType(T) & kind(T)))
)).

% Ultimate sortals (by ontological nature) instances
% (tested to rule out trivial models)
% TODO: investigate why we cannot list all different types of ultimate sortals at once

% fof(ax_typesDefinitionsInstances, axiom, (
%   objectKind(ok9) & collectiveKind(ck9) & quantityKind(quank9) & relatorKind(rk9) & modeKind(mk9) & qualityKind(qualk9)
% )).

% Skipping (t22) because (a21) makes it trivial

% Ax |= "th_endurantsInstantiateEndurantKindsOfSomeNature_a46"; conjecture commented for convenience
% This axiom is actually a theorem in this version of the axiomatization

% fof(th_endurantsInstantiateEndurantKindsOfSomeNature_a46, conjecture, (
%   ![E]: (endurant(E) => (
%     ?[K,W]: ((objectKind(K) | collectiveKind(K) | quantityKind(K) | modeKind(K) | qualityKind(K) | relatorKind(K))
%     & iof(E,K,W))
%   ))
% )).

% Ax |= "th_endurantSortalsCompleteness_t23"; conjecture commented for convenience
% Thanks to the taxonomy, we already have "sortal(T) => endurantType(T)", but I leave it like this to be consistent with the paper

% fof(th_endurantSortalsCompleteness_t23, conjecture, (
%   ![T]: ((endurantType(T) & sortal(T)) => (objectKind(T) | collectiveKind(T) | quantityKind(T) | qualityKind(T) | modeKind(T) | relatorKind(T) | phase(T) | role(T)))
% )).

% Ax |= "th_objectTypesSpecializeAKindOfSameNature_t24"; conjecture commented for convenience

% fof(th_objectTypesSpecializeAKindOfSameNature_t24, conjecture, (
%   ![T]: ((objectType(T) & sortal(T)) <=> (?[K]: (objectKind(K) & specializes(T,K))))
```

```
% )).

% Ax |= "th_collectiveTypesSpecializeAKindOfSameNature_t24"; conjecture commented for convenience

% fof(th_collectiveTypesSpecializeAKindOfSameNature_t24, conjecture, (
%   ![T]: ((collectiveType(T) & sortal(T)) <=> (?[K]: (collectiveKind(K) & specializes(T,K))))
% )).

% Ax |= "th_quantityTypesSpecializeAKindOfSameNature_t24"; conjecture commented for convenience

% fof(th_quantityTypesSpecializeAKindOfSameNature_t24, conjecture, (
%   ![T]: ((quantityType(T) & sortal(T)) <=> (?[K]: (quantityKind(K) & specializes(T,K))))
% )).

% Ax |= "th_modeTypesSpecializeAKindOfSameNature_t24"; conjecture commented for convenience

% fof(th_modeTypesSpecializeAKindOfSameNature_t24, conjecture, (
%   ![T]: ((modeType(T) & sortal(T)) <=> (?[K]: (modeKind(K) & specializes(T,K))))
% )).

% Ax |= "th_qualityTypesSpecializeAKindOfSameNature_t24"; conjecture commented for convenience

% fof(th_qualityTypesSpecializeAKindOfSameNature_t24, conjecture, (
%   ![T]: ((qualityType(T) & sortal(T)) <=> (?[K]: (qualityKind(K) & specializes(T,K))))
% )).

% Ax |= "th_relatorTypesSpecializeAKindOfSameNature_t24"; conjecture commented for convenience

% fof(th_relatorTypesSpecializeAKindOfSameNature_t24, conjecture, (
%   ![T]: ((relatorType(T) & sortal(T)) <=> (?[K]: (relatorKind(K) & specializes(T,K))))
% )).

% Ax |= "th_sortalLeafCategoriesAreDisjoint_t25"; conjecture commented for convenience

% fof(th_sortalLeafCategoriesAreDisjoint_t25, conjecture, (
%   ![T]: (objectKind(T) => (~(collectiveKind(T) | quantityKind(T) | modeKind(T) | qualityKind(T) | relatorKind(T) | category(T) | mixin(T) | phaseMixin(T) | roleMixin(T))))
%   & ![T]: (collectiveKind(T) => (~(objectKind(T) | quantityKind(T) | modeKind(T) | qualityKind(T) | relatorKind(T) | category(T) | mixin(T) | phaseMixin(T) | roleMixin(T))))
%   & ![T]: (quantityKind(T) => (~(objectKind(T) | collectiveKind(T) | modeKind(T) | qualityKind(T) | relatorKind(T) | category(T) | mixin(T) | phaseMixin(T) | roleMixin(T))))
```

```
%   & ![T]: (modeKind(T) => (~(objectKind(T) | quantityKind(T) |
    collectiveKind(T) | qualityKind(T) | relatorKind(T) | category(
    T) | mixin(T) | phaseMixin(T) | roleMixin(T))))
%   & ![T]: (qualityKind(T) => (~(objectKind(T) | quantityKind(T) |
     modeKind(T) | collectiveKind(T) | relatorKind(T) | category(T)
     | mixin(T) | phaseMixin(T) | roleMixin(T))))
%   & ![T]: (relatorKind(T) => (~(objectKind(T) | quantityKind(T) |
     modeKind(T) | qualityKind(T) | collectiveKind(T) | category(T)
     | mixin(T) | phaseMixin(T) | roleMixin(T))))
%   & ![T]: (category(T) => (~(objectKind(T) | quantityKind(T) |
    modeKind(T) | qualityKind(T) | relatorKind(T) | collectiveKind(
    T) | mixin(T) | phaseMixin(T) | roleMixin(T))))
%   & ![T]: (mixin(T) => (~(objectKind(T) | quantityKind(T) |
    modeKind(T) | qualityKind(T) | relatorKind(T) | category(T) |
    collectiveKind(T) | phaseMixin(T) | roleMixin(T))))
%   & ![T]: (phaseMixin(T) => (~(objectKind(T) | quantityKind(T) |
    modeKind(T) | qualityKind(T) | relatorKind(T) | category(T) |
    mixin(T) | collectiveKind(T) | roleMixin(T))))
%   & ![T]: (roleMixin(T) => (~(objectKind(T) | quantityKind(T) |
    modeKind(T) | qualityKind(T) | relatorKind(T) | category(T) |
    mixin(T) | phaseMixin(T) | collectiveKind(T))))
% )).

% Ax |= "th_sortalLeafCategoriesAreComplete_t26"; conjecture
    commented for convenience

% fof(th_sortalLeafCategoriesAreComplete_t26, conjecture, (
%   ![T]: ((endurantType(T)) => (objectKind(T) | collectiveKind(T)
    | quantityKind(T) | qualityKind(T) | modeKind(T) | relatorKind(
    T) | phase(T) | role(T) | category(T) | mixin(T) | phaseMixin(T
    ) | roleMixin(T)))
% )).
```

2.1.9 Mereology

```
%%%%%%%%%%%%%%%%%%%%%%% Mereology %%%%%%%%%%%%%%%%%%%%%%%%%

% TODO: review whether it is necessary to reduce mereology to
    concrete individuals; I am leaving this axiom out for the
    moment

% fof(ax_partArguments, axiom, (
%   ![X,Y]: (part(X,Y) => (concreteIndividual(X) &
    concreteIndividual(Y)))
% )).

fof(ax_reflexiveParthood, axiom, (
  ![X]: (partOf(X,X))
)).

fof(ax_antiSymmetricParthood_a47, axiom, (
  ![X,Y]: ((partOf(X,Y) & partOf(Y,X)) => (X=Y))
)).

fof(ax_antiSymmetricParthood_a48, axiom, (
  ![X,Y]: ((partOf(X,Y) & partOf(Y,X)) => (X=Y))
)).

```

```
fof(ax_transitiveParthood_a49, axiom, (
  ![X,Y,Z]: ((partOf(X,Y) & partOf(Y,Z)) => (partOf(X,Z)))
)).

fof(ax_overlappingWholes_a50, axiom, (
  ![X,Y]: ((overlap(X,Y)) <=> (?[Z]: (partOf(Z,X) & partOf(Z,Y))))
)).

fof(ax_strongSupplementation_a51, axiom, (
  ![X,Y]: (~partOf(X,Y) <=> ?[Z]: (partOf(Z,X) & ~overlap(Z,Y)))
)).

fof(ax_properPart_a52, axiom, (
  ![X,Y]: (~properPartOf(X,Y) <=> (partOf(X,Y) & ~partOf(Y,X)))
)).

fof(ax_binarySum_a53, axiom, (
  ![X,Y,Z]: (sum(Z,X,Y) <=> ![W]: (overlap(W,Z) <=> (overlap(W,X) |
     overlap(W,Y))))
)).

fof(ax_binarySum_a53, axiom, (
  ![X,Y,Z]: (sum(Z,X,Y) <=> ![W]: (overlap(W,Z) <=> (overlap(W,X) |
     overlap(W,Y))))
)).

% TODO: check whether it is necessary to introduce fusion and
    existence of sums, and how to do it

% Mereology in use
% (tested to rule out trivial models)

% fof(ax_mereologyInUse, axiom, (
%   concreteIndividual(ci10_1) & concreteIndividual(ci10_2) &
    concreteIndividual(ci10_3) & concreteIndividual(ci10_4) &
    concreteIndividual(ci10_5) & ~(ci10_1=ci10_2) & ~(ci10_2=ci10_3
    ) & ~(ci10_3=ci10_4) & ~(ci10_4=ci10_5) & properPart(ci10_1,
    ci10_2) & properPart(ci10_3,ci10_4) & sum(ci10_5,ci10_3,ci10_4)
% )).
```

2.1.10 Composition

```
%%%%%%%%%%%%%%%%%%%%%% Composition %%%%%%%%%%%%%%%%%%%%%

% TODO: review why we need to constrain functions to hold between
    endurants and types only (not even "endurant types")

fof(ax_function, axiom,  (
  ![X,Y]: (function(X,Y) => (endurant(X) & type_(Y)))
)).

fof(ax_genericFunctionalDependence_a55, axiom, (
  ![T1,T2,W]: (gfd(T1,T2,W) <=>
    ![E1]: ((iof(T1,E1,W) & function(T1,E1)) => ?[E2]: (~(E1=E2) &
    iof(T2,E2,W) & function(T2,E2))))
)).

fof(ax_individualFunctionalDependence_a56, axiom, (
```

```
  ![E1,T1,E2,T2,W]: (ifd(E1,T1,E2,T2,W) <=> (
    gfd(T1,T2,W) & iof(E1,T1,W) & iof(E2,T2,W) & (function(E1,T1) => function(E2,T2))
  ))
)).

fof(ax_componentOf_a57, axiom, (
  ![E1,T1,E2,T2,W]: (componentOf(E1,T1,E2,T2,W) <=> (properPartOf(E1,E2) & ifd(E1,T1,E2,T2,W)))
)).

% Composition in use
% (tested to rule out trivial models)

% fof(ax_compositionInUse, axiom, (
%   componentOf(e11_1,t11_1,e11_2,t11_2,w11) & ~(e11_1=e11_2) & ~(e11_1=t11_1) & ~(e11_2=t11_2) & ~(e11_1=t11_2) & ~(e11_2=t11_1) & ~(t11_1=t11_2)
% )).
```

2.1.11 Constitution

```
%%%%%%%%%%%%%%%%%%%%% Constitution %%%%%%%%%%%%%%%%%%%%%

fof(ax_constitutedByInvolvedNatures_a58, axiom, (
  ![X,Y,W]: (constitutedBy(X,Y,W) => ((endurant(X) <=> endurant(Y)) & (perdurant(X) <=> perdurant(Y)) & world(W)))
)).

fof(ax_constitutedByDifferentKinds_a59, axiom, (
  ![E1,E2,T1,T2,W]: ((constitutedBy(E1,E2,W) & iof(E1,T1,W) & iof(E2,T2,W) & kind(T1) & kind(T2)) => (~(T1=T2)))
)).

% Ax |= "th_noSelfConstitution_t27"; conjecture commented for convenience

% fof(th_noSelfConstitution_t27, conjecture, (
%   ~?[X,W]: (endurant(X) & constitutedBy(X,X,W))
% )).

fof(ax_genericConstitutionalDependence_a60, axiom, (
  ![T1,T2]: (genericConstitutionalDependence(T1,T2) <=> (
    type_(T1) & type_(T2) & ![E1,W]: (iof(E1,T1,W) => (
      ?[E2]: (constitutedBy(E1,E2,W) & iof(E2,T2,W)
    )))
  ))
)).

fof(ax_constitution_a61, axiom, (
  ![E1,T1,E2,T2,W]: (constitution(E1,T1,E2,T2,W) <=> (
    iof(E1,T1,W) & iof(E2,T2,W) & genericConstitutionalDependence(T1,T2) & constitutedBy(E1,E2,W)
  ))
)).

fof(
    ax_wheneverAConstitutedPerdurantExistsTheConstitutedByRelationHolds_a62
```

```
, axiom, (
  ![P1,P2,W1]: ((constitutedBy(P1,P2,W1) & perdurant(P1)) => (![W2]: (exists(P1,W2) => constitutedBy(P1,P2,W2))))
)).

fof(ax_constitutedByIsAsymmetric_a63, axiom, (
  ![E1,E2,W]: (constitutedBy(E1,E2,W) => ~constitutedBy(E2,E1,W))
)).

% Constitution in use
% (tested to rule out trivial models)

% fof(ax_constitutionInUse, axiom, (
%   object(e12_1) & object(e12_2) & objectKind(k12_1) & objectKind(k12_2) & world(w12) & ~(k12_1=k12_2) & iof(e12_1,k12_1,w12) & iof(e12_2,k12_2,w12) & constitutedBy(e12_1,e12_2,w12) & genericConstitutionalDependence(k12_1,k12_2) & constitution(e12_1,k12_1,e12_2,k12_2,w12)
% )).
```

2.1.12 Existential Dependence

```
%%%%%%%%%%%%%%%%% Existential Dependence %%%%%%%%%%%%%%%%%

fof(ax_exists_a64, axiom, (
  ![X,W]: (exists(X,W) => (thing(X) & world(W)))
)).

fof(ax_existentiallyDependsOn_a65, axiom, (
  ![X,Y]: (existentiallyDependsOn(X,Y) <=> (![W]: (exists(X,W) => exists(Y,W))))
)).

fof(ax_existentiallyIndependentOf_a66, axiom, (
  ![X,Y]: (existentiallyIndependentOf(X,Y) <=> (~existentiallyDependsOn(X,Y) & ~existentiallyDependsOn(Y,X)))
)).

% Existential dependence in use
% (tested to rule out trivial models)

% fof(ax_constitutionInUse, axiom, (
%   object(e13_1) & object(e13_2) & object(e13_3) & ~(e13_1=e13_2) & ~(e13_1=e13_3) & ~(e13_2=e13_3) & existentiallyDependsOn(e13_2,e13_1) & existentiallyIndependentOf(e13_3,e13_1)
% )).

% TODO: introduce transitivity and anti-symmetry of existential dependence
% TODO: introduce continuity of existence with perdurants never ceasing to exist
```

2.1.13 Moments and Inherence

```
%%%%%%%%%%%%%%%%%% Moments and Inherence %%%%%%%%%%%%%%%%%

%  Inherence
```

```
fof(ax_inherenceImpliesExistentialDependence_a67, axiom, (
  ![M,X]: (inheresIn(M,X) => existentiallyDependsOn(M,X))
)).

fof(ax_thingsInvolvedInInherence_a68, axiom, (
  ![M,X]: (inheresIn(M,X) => (moment(M) & (type_(X) | endurant(X))))
)).

% TODO: add definition (d5) for the "bearer" axiom

fof(ax_irreflexiveInherence, axiom, (
  ![X]: (~inheresIn(X,X))
)).

fof(ax_asymmetricInherence, axiom, (
  ![X,Y]: (inheresIn(X,Y) => ~inheresIn(Y,X))
)).

fof(ax_intransitiveInherence, axiom, (
  ![X,Y,Z]: ((inheresIn(X,Y) & inheresIn(Y,Z)) => ~inheresIn(X,Z))
)).

fof(ax_uniqueInherence_a69, axiom, (
  ![X,Y,Z]: ((inheresIn(X,Y) & inheresIn(X,Z)) => (Y=Z))
)).

% Moments

fof(ax_dMomentOf_d6, axiom, (
  ![M,X]: (momentOf(M,X) <=> (inheresIn(M,X) | (
    ?[M2]: (inheresIn(M,M2) & momentOf(M2,X))
  )))
)).

fof(ax_dUltimateBearerOf_d7, axiom, (
  ![B,M]: (ultimateBearerOf(B,M) <=> (~moment(B) & momentOf(M,B)))
)).

fof(ax_everyMomentHasUniqueAUltimateBearer_a70, axiom, (
  ![M]: (moment(M) => (?[B]: (ultimateBearerOf(B,M) & (
    ![B2]: (ultimateBearerOf(B2,M) <=> (B=B2))
  ))))
)).

fof(ax_noMomentOfCycles, axiom, (
  ~?[M]: momentOf(M,M)
)).

% Ax |= "th_irreflexiveInherence_t28"; conjecture commented for convenience

% fof(th_irreflexiveInherence_t28, conjecture, (
%   ~?[X]: (inheresIn(X,X))
% )).
```

```
% Ax |= "th_asymmetricInherence_t29"; conjecture commented for
    convenience

% fof(th_asymmetricInherence_t29, conjecture, (
%   ~?[X,Y]: (inheresIn(X,Y) & inheresIn(Y,X))
% )).

% Ax |= "th_antiTransitiveInherence_t30"; conjecture commented for
    convenience

% fof(th_antiTransitiveInherence_t30, conjecture, (
%   ![X,Y,Z]: ((inheresIn(X,Y) & inheresIn(Y,Z)) => (~inheresIn(X,Z
    )))
% )).
```

2.1.14 Relators

```
%%%%%%%%%%%%%%%%%%%%%%%% Relators %%%%%%%%%%%%%%%%%%%%%%%%



%%%%%%%%%%%%%%%%%%%% Characterization %%%%%%%%%%%%%%%%%%%



%%%%%%%%%%%% Qualities and Quality Structures %%%%%%%%%%%



%%%%%%%%%%%%%%%% Endurants and Perdurants %%%%%%%%%%%%%%%
```