## A TPTP Formalization of the Unified Foundational Ontology

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## Abstract

This document presents a formalization of the Unified Foundation Ontology (UFO) expressed in first-order logics through the TPTP syntax. This formalization is intended to support verification of UFO's theory through automated provers and consistency checkers.

## 1 Introduction

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## 2 UFO's TPTP Specification

```
18
20 fof(ax_taxonomy, axiom, (
21 ![X]: ((perdurant(X)|endurant(X))<=>(concreteIndividual(X))))).
22
23
24 fof(ax_taxonomy, axiom, (
25 ![X]: ((quale(X)|set(X))=>(abstractIndividual(X))))).
fof(ax_taxonomy, axiom, (
28 ![X]: ((object(X)|collective(X)|quantity(X))<=>(substantial(X))))).
31 fof(ax_taxonomy, axiom, (
32 ![X]: ((substantial(X)|moment(X)) <=>(endurant(X))))).
34 fof(ax_taxonomy, axiom, (
35 ![X]: ((intrinsicMoment(X)|relator(X)) <=>(moment(X))))).
37 fof(ax_taxonomy, axiom, (
38 ![X]: ((quality(X)|mode(X)) <=>(intrinsicMoment(X)))).
40 fof(ax_taxonomy, axiom, (
41 ![X]: ((externallyDependentMode(X)|disposition(X)) <=>(mode(X))))).
42
43 fof(ax_taxonomy, axiom, (
44 ![X]: ((quaIndividual(X)) <=>(externallyDependentMode(X))))).
46 fof(ax_taxonomy, axiom, (
47 ![X]: ((qualityStructure(X)) <=>(set(X))))).
49 fof(ax_taxonomy, axiom, (
50 ![X]: ((qualityDimension(X)|qualitySpace(X)) <=>(qualityStructure(X)
      )))).
51
fof(ax_taxonomy, axiom, (
54 ![X]: (world(X)=>(qualityStructure(X)))).
55
56
57 %%%%%Disjoitness axioms:
58
59 fof(ax_taxonomy, axiom, (
       ~?[X]: (concreteIndividual(X)&abstractIndividual(X)))).
60
61
62 fof(ax_taxonomy, axiom, (
      ~?[X]: (perdurant(X)&endurant(X)))).
63
64
65
66 fof(ax_taxonomy, axiom, (
       "?[X]: (substantial(X)&moment(X)))).
67
68
69 fof(ax_taxonomy, axiom, (
      ~?[X]: (quale(X)&set(X)))).
70
71
73 fof(ax_taxonomy, axiom, (
```

```
~?[X]: (object(X)&collective(X)))).
74
75
76
77 fof(ax_taxonomy, axiom, (
        ?[X]: (collective(X)&quantity(X)))).
78
79
80
81 fof(ax_taxonomy, axiom, (
       "?[X]: (object(X)&quantity(X)))).
83
84 fof(ax_taxonomy, axiom, (
       ~?[X]: (intrinsicMoment(X)&relator(X)))).
85
86
88 fof(ax_taxonomy, axiom, (
       ~?[X]: (quality(X)&mode(X)))).
89
90
91 fof(ax_taxonomy, axiom, (
92
       ~?[X]: (externallyDependentMode(X)&disposition(X)))).
93
   fof(ax_taxonomy, axiom, (
       ~?[X]: (qualityDimension(X)&qualitySpace(X)))).
95
96
97
98
99
100 %%%% Taxonomy of Types accoording to their instances
fof(ax_taxonomy, axiom, (
![X]: ((perdurantType(X)|endurantType(X))=>(type(X)))).
fof(ax_taxonomy, axiom, (
106 ![X]: ((substantialType(X)|momentType(X))<=>(endurantType(X)))).
108 fof(ax_taxonomy, axiom, (
109 ![X]: ((objectType(X)|collectiveType(X)|quantityType(X)) <=>(
       substantialType(X)))).
fof(ax_taxonomy, axiom, (
112 ![X]: ((intrinsicMomentType(X)|relatorType(X)) <=>(momentType(X)))))
114 fof(ax_taxonomy, axiom, (
115 ![X]: ((qualityType(X)|modeType(X))<=>(intrinsicMomentType(X))))).
117 %Disjointness axioms
118
119
fof(ax_taxonomy, axiom, (
       ~?[X]: (perdurantType(X)&endurantType(X)))).
121
122
fof(ax_taxonomy, axiom, (
       ~?[X]: (substantialType(X)&momentType(X)))).
124
125
126 fof(ax_taxonomy, axiom, (
      ~?[X]: (objectType(X)&collectiveType(X)))).
127
```

```
129
130 fof(ax_taxonomy, axiom, (
        ?[X]: (objectType(X)&quantityType(X)))).
131
132
133 fof(ax_taxonomy, axiom, (
       ~?[X]: (collectiveType(X)&quantityType(X)))).
134
135
136 fof(ax_taxonomy, axiom, (
           ~?[X]: (intrinsicMomentType(X)&relatorType(X)))).
137
138
139 fof(ax_taxonomy, axiom, (
           ~?[X]: (qualityType(X)&modeType(X)))).
140
141
142
143 %%%% Taxonomy accordint to metaproperty (sortality etc).
144
145
146 fof(ax_taxonomy, axiom, (
147 ![X]: ((sortal(X)|nonSortal(X)) <=>(endurantType(X))))).
148
149 fof(ax_taxonomy, axiom, (
150 ![X]: ((rigidSortal(X)|antiRigidSortal(X)) <=>(sortal(X))))).
152 fof(ax_taxonomy, axiom, (
153 ![X]: ((kind(X)|subkind(X)) <=>(rigidSortal(X))))).
155 fof(ax_taxonomy, axiom, (
156 ![X]: ((phase(X)|role(X)) <=>(antiRigidSortal(X))))).
157
fof(ax_taxonomy, axiom, (
159 ![X]: ((category(X)|antiRigidNonSortal(X)|mixin(X)) <=>(nonSortal(X)
       )))).
fof(ax_taxonomy, axiom, (
162 ![X]: ((phaseMixin(X)|roleMixin(X)) <=>(antiRigidNonSortal(X))))).
163
164
165 %%%Disjointness axioms:
166
167
   fof(ax_taxonomy, axiom, (
        "?[X]: (sortal(X)&nonSortal(X)))).
168
169
fof(ax_taxonomy, axiom, (
       ~?[X]: (rigidSortal(X)&antiRigidSortal(X)))).
171
172
fof(ax_taxonomy, axiom, (
           ~?[X]: (kind(X)&subKind(X)))).
174
175
176 fof(ax_taxonomy, axiom, (
            ~?[X]: (phase(X)&roles(X)))).
177
178
fof(ax_taxonomy, axiom, (
           ~?[X]: (category(X)&antiRigidNonSortal(X)))).
180
181
182 fof(ax_taxonomy, axiom, (
           ~?[X]: (category(X)&mixin(X)))).
183
184
```

```
185 fof(ax_taxonomy, axiom, (
          ~?[X]: (antiRigidNonSortal(X)&mixin(X)))).
186
187
  fof(ax_taxonomy, axiom, (
188
        ~?[X]: (phaseMixin(X)&roleMixin(X)))).
189
190
191
194 %
195 %Definition of instance of (iof), types, and individuals
196
198
  fof(ax_dtypea1, axiom, (
199
      ![X] : (type(X) <=> (?[W,Y] : (world(W) & (iof(Y,X,W))
200
201
      ))))),
202
_{203} %Note: we need to drop that individuals are not wordls, as now
      worlds are abstract.
205 fof(ax_dindividual_a2, axiom, (
         ![X] : (individual(X) <=> (![W] : (world(W) => ~?[Y] : (iof
206
      (Y, X, W)))))
         )).
207
208
209 fof(ax_multilevel_a3, axiom, (
      ![X,Y,W] : (iof(X,Y,W) \Rightarrow ((individual(X)|type(X)) & type(Y) &
210
      world(W)))).
211
  fof(ax_twolevels_a4, axiom, (
212
          "?[X,Y,Z,W]: (type(X) & iof(X,Y,W) & iof(Y,Z,W)))).
213
214
215
217
  %Specialization
219
220
  fof(ax_dspecialization_a5, axiom, (
221
    ![T1,T2] : (specializes(T1,T2) <=> (type(T1) & type(T2) &
222
                    ![W]: (world(W) => ![E]:(iof(E,T1,W) => iof(E,
223
      T2,W)))))).
224
   fof(ax_dspecialization_strict_d1, axiom, (
225
    ![T1,T2] : (strictlySpecializes(T1,T2) <=> (specializes(T1,T2) \&
226
       ~specializes(T2,T1))))).
227
    \% Whenever two types have a common instance, they must share a
228
      supertype or a subtype for this instance
    fof(ax_nondisjointSameTaxonomy_a6, axiom, (
229
        ![T1,T2]: (![X,W]: ((iof(X,T1,W)&iof(X,T2,W)&~specializes(T1,
230
      T2)&~specializes(T2,T1))=>
231
               (?[T3]: (specializes(T1,T3)&specializes(T2,T3)&iof(X,
232
      T3,W)))|
```

```
(?[T3]: (specializes(T3,T1)&specializes(T3,T2)&iof(X,
233
       T3,W)))
234
             ))
235
     )).
236
237
238
   239
241 %%Definition of rigidity, anitirigidity, semirigidity, sortality.
242
244
245
246 % Definition of rigid type
247 fof(ax_drigid_a7, axiom, (
248
       ![T]: (rigid(T) <=>(endurantType(T) &
                       (![X]: ((?[W]: (world(W) & iof(X,T,W))) => (![
249
       W2]: (world(W2)=>iof(X,T,W2))))))
250 )).
251
_{252} % Definition of antirigid type
fof(ax_dantirigid_a8, axiom, (
254
       ![T]: (antiRigid(T) <=>(endurantType(T) &
                       (![X]: ((?[W]: (world(W) & iof(X,T,W))) \Rightarrow (?[
255
       W2]: (world(W2) & ~iof(X,T,W2))))))).
256
257 % Implicit definition of semirigid type
fof(ax_semirigid_a9, axiom, (
       ![T]: (semiRigid(T) <=>(endurantType(T) &
259
                       ~antiRigid(T) & ~rigid(T)))
261 )).
262
263
   %%%%%%%%%%%%%%%%%%%%%%% Definition of sortality
264
265
266 % Every *individual* necessarily instantiates a kind // imply
       kinds are rigid!
267
268
   fof(ax_individualKindMin_a10_revised_to_endurants, axiom, (
       ![X] : (endurant(X) \Rightarrow ?[K]:(kind(K) & ![W]: (world(W) \Rightarrow iof(X,K)) \\
269
       ((((W,
       )).
270
271
   % Every thing instantiates at most one kind (whenever it
       instantiates a kind it does not
273 % possible instantiate a different one
274
fof(ax_individualKindMax_a11, axiom, (
       ![X,K,W] : ( ( kind(K) & iof(X,K,W)) =>
276
                   (~?[Z,W2]: (~(Z=K) & kind(Z) & iof(X,Z,W2))))
277
       )).
278
279
280 % Sortals definition, sortals are those types whose instances
       instantiate the same kind
282 fof(ax_dsortal_a12, axiom, (
```

```
![T] : (sortal(T) <=> (endurantType(T) &
283
                       (?[K] : (kind(K) & ![X,W]: (world(W)=>(iof(X,T,
      W) => iof(X,K,W) )))))
       )).
286
   % A non-sortal is a type that is not a sortal
287
288
   fof(ax_dnonsortal_a13, axiom, (
289
       ![T] : (nonSortal(T) <=> (endurantType(T) & ~sortal(T)) )
291
292
293
  %%%%%%%%%%%%%%%%%%%% Definitions
294
295
296
   fof(ax_rigidSortal, axiom, (
297
298
              ![T]: (rigidSortal(T) <=>(rigid(T) &sortal(T)))
299
300
   fof(ax_rigidNonSortal, axiom, (
301
       ![T]: (rigidNonSortal(T) <=>(rigid(T) & ~sortal(T)))
302
                  )).
303
   fof(ax_antiRigidSortal, axiom, (
304
                      ![T]: (antiRigidSortal(T) <=>(antiRigid(T)&
305
       sortal(T)))
                                  )).
306
307
   fof(ax_antiRigidNonSortal, axiom, (
308
              ![T]: (antiRigidNonSortal(T) <=>(antiRigid(T)&~sortal(T)
309
      )))).
311 fof(ax_semiRigidNonSortal, axiom, (
                           ![T]: (semiRigidNonSortal(T) <=>(semiRigid(T
312
      )&~sortal(T))))).
313
314
315
   317
   %Taxonomy of endurant types according to the ontological nature of
318
      their instances
319
   320
321
   % Endurant types are all those types whose instances are endurants
322
323
  fof(ax_dendurantType_a36, axiom, (
324
         ![T]: (endurantType(T) <=> (type(T) & (![X,W]: (iof(X,T,W) =>
325
        endurant(X))))
        )).
327
328 % Substantial types are all those types whose instances are
      substantials
329
fof(ax_dsubstantialType_a36, axiom, (
            ![T]: (substantialType(T) <=> (type(T) & (![X,W]: (iof(X,T)
331
       ,W)=>substantial(X)))))
```

```
)).
332
333
334 % Moment types are all those types whose instances are moments
335
fof(ax_dmomentType_a36, axiom, (
                     ![T]: (momentType(T) <=> (type(T) & (![X,W]: (iof(X,T,W)=>
337
                 moment(X))))
                     )).
338
339
^{340} % Relator types are all those types whose instances are relators
341
            fof(ax_drelatorType_a36, axiom, (
342
                                ![T]: (relatorType(T) <=> (type(T) & (![X,W]: (iof(X,T,W)
343
                 =>relator(X)))))
                     )).
344
345
346
       % Mode types are all those types whose instances are modes
347
348
                      fof(ax_dmodeType_a36, axiom, (
                                ![T]: (modeType(T) <=> (type(T) & (![X,W]: (iof(X,T,W)=>
349
                 mode(X))))
                     )).
350
351
       % Quality types are all those types whose instances are qualities
352
353
                      fof(ax_dqualityType_a36, axiom, (
354
                               ![T]: (qualityType(T) <=> (type(T) & (![X,W]: (iof(X,T,W)
355
                 =>quality(X))))
                     )).
356
357
358
       %%% Kinds are specialized according to the ontological nature of
359
                 their instances
360
                     % Substantial kinds are those kinds whose instances are
361
                 substantials
                     fof(ax_dsubstantialKind_a37, axiom, (
362
363
                                ![T]: (substantialKind(T) <=> (substantialType(T) & kind(T) <=> (substan
                 )))
                     )).
364
365
                      % Relator kinds are those kinds whose instances are relators
366
367
                      fof(ax_drelatorKind_a37, axiom, (
                               ![T]: (relatorKind(T) <=> (relatorType(T) & kind(T)))
368
                      )).
369
370
                      \% Mode kinds are those kinds whose instances are modes
371
                      fof(ax_dmodeKind_a37, axiom, (
372
                                ![T]: (modeKind(T) <=> (modeType(T) & kind(T)))
373
374
                     )).
375
                      % Quality kinds are those kinds whose instances are relators
376
377
                      fof(ax_dqualityKind_a37, axiom, (
                                ![T]: (qualityKind(T) <=> (qualityType(T) & kind(T)))
378
379
380
```

```
% every endurant is instance of one of the specific endurant
381
               kinds
                   fof(ax_everyEndurantInstantiatesSpecificKind_a38, axiom, (
382
                             ![X]: (endurant(X) \Rightarrow (?[W,K]: ((substantialkind(K)|
383
               relatorkind(K)|modekind(K)|qualitykind(K))& iof(X,K,W))))
384
385
386
387
388
      	ilde{N}
390
391
      %Mereology
392
       394
395
      fof(ax_part_arguments, axiom, (![X,Y]: (part(X,Y) => (
396
                concreteIndividual(X) & concreteIndividual(Y))))).
397
      fof(ax_part_rifl, axiom, (![X]: (concreteIndividual(X) => part(X,X)
398
               ))).
399
      fof(ax_part_antisymm, axiom, (![X,Y]: ((part(X,Y) & part(Y,X)) => (
              Y=X)))).
401
402 fof(ax_part_tran, axiom, (![X,Y,Z]: ((part(X,Y) & part(Y,Z)) =>
               part(X,Z)))).
403
404 fof(ax_part_overlappin, axiom, (![X,Y]: (overlap(X,Y) <=> ?[Z]:(
               part(Z,X) & part(Z,Y)))).
405
      \label{lem:concrete_strong_supp} \mbox{fof(ax\_part\_strong\_supp, axiom, (![X,Y]: ((concreteIndividual(Y) \& Axiom))))} \mbox{$\ell$ (ax\_part\_strong\_supp, axiom), (![X,Y]: ((concreteIndividual(Y) \& Axiom))))]} \mbox{$\ell$ (ax\_part\_strong\_supp, axiom), (![X,Y]: ((concreteIndividual(Y) \& Axiom)))]} \mbox{$\ell$ (ax\_part\_strong\_supp, axiom), (![X,Y]: ((concreteIndividual(Y) \& Axiom)))]} \mbox{$\ell$ (ax\_part\_strong\_supp, axiom), (![X,Y]: ((concreteIndividual(Y) \& Axiom)))]} \mbox{$\ell$ (ax\_part\_strong\_supp, axiom), (![X,Y]: ((concreteIndividual(Y) & Axiom))]} \mbox{$\ell$ (ax\_part\_strong\_strong\_strong\_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_strong_stron
406
               concreteIndividual(X) & ~part(Y,X)) => ?[Z]: (part(Z,Y) & ~
               overlap(Z,X)))).
407
      fof(ax_part_proper_part, axiom, (![X,Y]: (properPart(Y,X) <=> (part
408
                (Y,X) & ~part(X,Y)))).
409
fof(ax_part_sum, axiom, (![Z,X,Y]: (sum(Z,X,Y) \iff ![W]:((overlap(W)))
                ,Z) <=> (overlap(W,X) | overlap(W,X)))))).
411
      %Check how much fusion and existence of sum is needed.
412
413
414
416
417 %Composition
418
421
422 %Function as relations, "x function as y"
```

```
423
  fof(ax_function, axiom, (![X,Y]: (function(X,Y) => (endurant(X) &
      type(Y)))).
426 %Generic functional independence
427
  fof(ax_gfd_a47, axiom, (![X1,Y1,W]: (gfd(X1,Y1,W) <=> (![X]: ((iof(X1,Y1,W))))
428
      X,X1,W) & function(X,X1))
                                  => (?[Y]: (~(Y=X) & iof(Y,Y1,W) &
       function(Y,Y1)))))).
430
  %Individual functional dependence
431
432
433 fof(ax_ifd_a48, axiom, (![X,X1,Y,Y1,W]: (ifd(X,X1,Y,Y1,W) <=> (gfd(
      X1,Y1,W) & iof(X,X1,W) & iof(Y,Y1,W) &
                                 (function(X,X1) => function(Y,Y1)))
434
      ))).
435
436
437 %Component of
  fof(ax_ifd_a49, axiom, (![X,X1,Y,Y1,W]: (componentOf(X,X1,Y,Y1,W)
439
      <=> (properPart(X,Y) & ifd(X,X1,Y,Y1,W)))).
440
441
442
443
445
446
  %Constitution
447
  449
450
451 %%%ConstitutedBy
452
453 fof(ax_constituted_by_a58, axiom, (![X,Y,W]: (constitutedBy(X,Y,W)
        ((endurant(X) <=> endurant(Y)) & (perdurant(X) <=> perdurant(
454
      Y)) & world(W)))).
455
_{456} fof(ax_constituted_by_a59, axiom, (![X,Y,X1,Y1,W]: ((constitutedBy(
      X,Y,W) & iof(X,X1,W) & iof(Y,Y1,W) & kind(X1) & kind(Y1)) => ~(
      X1 = Y1)))).
457
458
  %%%%Generic constutional dependence (GCD).
459
  fof(ax_gcd_a60, axiom, (![X1,Y1]: ((gcd(X1,Y1) <=> (type(X1) & type
461
      (Y1) & ![X,W]:(iof(X,X1,W) =>
                         (?[Y]:(iof(Y,Y1,W) & constitutedBy(X,Y,W)))
462
      )))))).
463
464 %%%%Constitution
```

```
466 fof(ax_constitution_a61, axiom, (![X,Y,X1,Y1,W]: ((constitution(X,
                              X1,Y,Y1,W)
                                                                                            <=> (iof(X,X1,W) & iof(Y,Y1,W) & gcd(X1,Y1) &
467
                              consitutedBy(X,Y,W))))).
468
469
            \label{lem:constitution_perdurants_a62} \ , \ \  \text{axiom} \ , \ \ (\,!\,[\,X\,,\,Y\,,\,W\,]\, \colon \ (\,(\,\text{perdurant}\,(\,X\,,\,Y\,,\,W\,)\,) \ .
470
                              ) & constitutedBy(X,Y,W)) =>
                                                                                                     (![W1]: (exists(X,W1) => constitutedBy(X,Y,W1))
                              )))).
472
            fof(ax\_constitution\_a63, axiom, (![X,Y,W]: (constitutedBy(X,Y,W) =>
                                    ~(constitutedBy(Y,X,W)))).
474
475
            476
478 %Existence, existential dependence, existential independence
479 %
            481
482
            %Existence axiom.
483
485 fof(ax_existence, axiom, (\{[X,W]: (ex(X,W) => (thing(X) \& world(W))\}
                              ))).
486
           %existential dependence and independence
487
489 fof(ax_existential_dependence, axiom, (![X,Y]: (ed(X,Y) <=> ![W]:(
                              ex(X,W) => ex(Y,W)))).
490
             fof(ax_existential_independence, axiom, (![X,Y]: (ind(X,Y) <=> (~ed
491
                              (X,Y) & ~ed(Y,X)))).
492
493
494
495
            	ilde{\mathsf{X}} 	ild
497 %Inherence
            	imes 	ime
498
499
500
                     fof(ax_inherence_type, axiom, (![X,Y]: (inheresIn(X,Y) => (moment
501
                               (X) & (type(X) | concreteIndividual(Y)))))).
                                                fof(ax_inherence_ed, axiom, (![X,Y]: (inheresIn(X,Y) => ed(
                              X,Y))).
504
                                                fof(ax_inherence_irrifl, axiom, (![X]: ~inheresIn(X,X))).
506
                                                fof(ax_inherence_asymm, axiom, (![X,Y]: (inheresIn(X,Y) =>
507
                              ~inheresIn(Y,X))).
```

```
508
                                                    fof(ax_inherence_intrans, axiom, (![X,Y,Z]: ((inheresIn(X,Y)))
                                ) & inheresIn(Y,Z)) => ~inheresIn(X,Z)))).
                                                   fof(ax_inherence_unic, axiom, (![X,Y,Z]: ((inheresIn(X,Y) &
511
                                      inheresIn(X,Z)) \Rightarrow Y=Z))).
513
             	ilde{\mathsf{X}} 	ild
518 fof(ax_momentOf, axiom, (![M,X]: (momentOf(M,X) <=> (inheresIn(M,X)
                                      | (?[Y]:(ineheresIn(M,Y) & momentOf(Y,X))))).
519
             fof(ax_ulitmate_bearer, axiom, (![B,M]: (ultimateBearerOf(B,M) <=>
520
                                 (~moment(B) & momentOf(B,M)))).
521
             fof(ax_ulitmate_bearer_existence, axiom, (![M]: (moment(M) => (?[B
                                ]: (ulimateBererOf(B,M))))).
_{524} fof(ax_ulitmate_bearer_unicity, axiom, (![M,B,B1]: ((ulimateBererOf
                                 (B,M) & ultimateBearerOf(B1,M)) => (B=B1))).
526
             	ilde{	ide{	ilde{	id}}}}}}}}}}.}}}}} }} 
}} }} }} }} 
527
             	imes 	ime
531
             "Externally dependent (we avoid introducing here the function "
                                bearer of a moment", it is however unique)
534
fof(ax_externally_dependent, axiom, (![X,Y]: (externallyDependent(X
                                                                                                                                                                                                          (ed(X,Y) & (![Z]: (
                                inheresIn(X,Z) => ind(Y,Z)))))).
537
             %Externally dependent modes
538
             fof(ax_externally_dependent_mode, axiom, (![X]: (
540
                                 externallyDependentMode(X) <=> (mode(X) & (?[Y]: (
                                 externallyDependent(X,Y)))))).
541
543 %Founded by
544
fof(ax_founded_by, axiom, (![X,Y]: (foundedBy(X,Y) => ((
                                 externallyDependentMode(X) | relator(X)) & perdurant(Y))))).
{\tt 547} \ \ {\tt fof(ax\_foundation\_existence, axiom, (![X]: (externallyDependentMode)))} \\
                             (X) \Rightarrow (?[Y]: (foundedBy(X,Y)))).
```

```
548
  fof(ax_foundation_unicity, axiom, (![X,Y,Z]: ((foundedBy(X,Y) &
      foundedBy(X,Z)) \Rightarrow (Y=Z))).
  %Qua individual of
551
552
553
  fof(ax_qua_individual_of, axiom, (![X,Y]: (quaIndividualOf(X,Y) <=>
                                      (![Z]:(overlap(Z,X) <=>
554
      externallyDependentMode(Z) & inheresIn(Z,Y) &
                                            (![P]: (foundedBy(X,P)
      => foundedBy(Z,P))))))).
557
  fof(ax_qua_individual_of_unicity, axiom, (![X,Y,Y1]: ((
      quaIndividualOf(X,Y) & quaIndividualOf(X,Y1)) => (Y=Y1)))).
559
560
  %Qua individual
561
  fof(ax_qua_individual_def, axiom, (![X]: ((quaIndividual(X) <=> (?[
      Y]: (quaIndividualOf(X,Y))))).
564
565
566
567
568
569
  570
571
  572
573
574 %Instances
%Taxonomy of types 1.
%fof(ax_instance, axiom, perdurantType(pt1)).
%fof(ax_instance, axiom, axiom,objectType(ot1)).
581 %fof(ax_instance, axiom, collectiveType(ct1)).
%fof(ax_instance, axiom, quantityType(qnt1)).
883 %fof(ax_instance, axiom, relatorType(rt1)).
584 %fof(ax_instance, axiom, qualityType(qlt1)).
585 %fof(ax_instance, axiom, modeType(mot1)).
586
588 %Taxonomy of types 2
589
590 %fof(ax_instance, axiom, kind(k1)).
%fof(ax_instance, axiom, subKind(sk1)).
592 %fof(ax_instance, axiom, phase(phase1)).
593 %fof(ax_instance, axiom, role(role1)).
594 %fof(ax_instance, axiom, category(cat1)).
%fof(ax_instance, axiom, phaseMixin(pm1)).
596 %fof(ax_instance, axiom, roleMixin(rmi1)).
597 %fof(ax_instance, axiom, mixin(mix1)).
598
```

```
%Taxnomy of individuals

%Tof(ax_instance, axiom, perdurant(p1)).

%fof(ax_instance, axiom, object(o1)).

%fof(ax_instance, axiom, collective(c1)).

%fof(ax_instance, axiom, quantity(quan1)).

%fof(ax_instance, axiom, relator(r1)).

%fof(ax_instance, axiom, quality(qual1)).

%fof(ax_instance, axiom, quality(qual1)).

%fof(ax_instance, axiom, qualitydual(qi1)).

%fof(ax_instance, axiom, qualityDimension(qd1)).

%fof(ax_instance, axiom, qualityDimension(qd1)).

%fof(ax_instance, axiom, qualitySpace(qs1)).

%fof(ax_instance, axiom, qualitySpace(qs1)).
```