A First-Order Logic Formalization of the Unified Foundational Ontology

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Abstract

This document presents a formalization of the Unified Foundational Ontology (UFO) in first-order logic. This formalization is documented by means of three complementary representations: (i) a representation in standard Common Logic using the CLIF syntax; (ii) a representation in natural language; and, when applicable, a (iii) UML-based diagrammatic representation. The presented formalization is supported by consistency and satisfiability checks performed through automated proofing tools.

1 Introduction

This document presents a formalization of the Unified Foundational Ontology (UFO) in first-order logic. This formalization is documented by means of three complementary representations: (i) a representation in standard Common Logic using the CLIF syntax; (ii) a representation in natural language; and, when applicable, a (iii) UML-based diagrammatic representation. The presented formalization is supported by consistency and satisfiability checks performed through automated proofing tools.

The remainder of this document is organized as a single formalization section (Section 2), which contains subsections for each submodule of the ontology.

2 Formalization

This section contains the formalization of the Unified Foundational Ontology (UFO) in first-order logics. This formalization is organized in several subsections where each presents the formalization of a portion of the whole ontology. The formalization is presented through different equivalent representations, designed to support the understanding of its contents: (i) a representation in standard Common Logic using the CLIF syntax; (ii) a representation in natural language; and, when applicable, a (iii) UML-based diagrammatic representation.

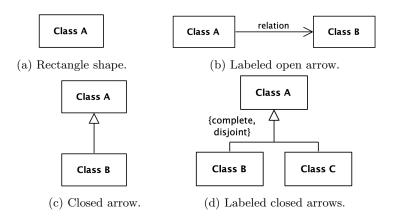


Figure 1: UML-based representation of first-order logic axioms.

The UML-based diagrammatic representation serves as a visual representation certain predicates and axioms, being each element in Figure 1 being translated as follows:

- Rectangle shape (Figure 1a): visual representation of unary predicates associated to types in the ontology; the associated predicate is shown in lower camel case with no spaces.

 classA(x)
- Open arrow (Figure 1b): visual representation of binary predicates; the predicate associated to the arrows' label is shown in lower camel case with no spaces; the predicate can only be true for any x and y if it is also true predicates associated to the types of each end (keeping the order of the arrow in the binary predicate's positions); this representation may also be associated to ternary predicates if if its third position represents a

```
\forall x, y (relation(x, y) \rightarrow (classA(x) \land classB(y)))
\forall x, y, w (relation(x, y, w) \rightarrow (classA(x) \land classB(y) \land world(w)))
```

• Closed arrow (Figure 1c): visual representation of specializations between ontology's types, where the type in the tail of the arrow is a subtype of the type in the head of the arrow.

```
\forall x(classB(x) \rightarrow classA(x))
```

time-index.

• Labeled closed arrow (Figure 1d): visual representation of disjoint and/or complete constraints over sets specializations between ontology's types.

```
 \forall x (classB(x) \rightarrow classA(x)) 
 \forall x (classC(x) \rightarrow classA(x)) 
 \forall x (classA(x) \rightarrow (classB(x) \lor classC(x))) 
 \neg \exists x (classB(x) \land classC(x))  {disjoint}
```

2.1 UFO Taxonomy

2.1.1 Partial Taxonomy of Thing

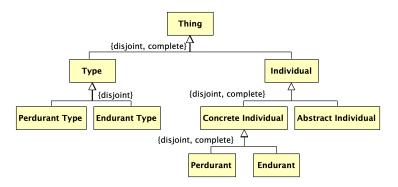


Figure 2: Partial Taxonomy of UFO - Thing.

```
4 % Thing
6 fof(ax_thing_taxonomy, axiom, (
  ![X]: ((type_(X) | individual(X)) <=> (thing(X)))
8 )).
9
fof(ax_thing_partition, axiom, (
"?[X]: (type_(X) & individual(X))
12 )).
13
14 % Individual
fof(ax_individual_taxonomy, axiom, (
    ![X]: ((concreteIndividual(X) | abstractIndividual(X)) <=> (
      individual(X)))
18 )).
19
_{\rm 20} fof(ax_individual_partition, axiom, (
    ~?[X]: (concreteIndividual(X) & abstractIndividual(X))
22 )).
23
24 % Concrete Individual
fof(ax_concreteIndividual_taxonomy, axiom, (
![X]: ((endurant(X) | perdurant(X)) <=> (concreteIndividual(X)))
28 )).
30 fof(ax_concreteIndividual_partition, axiom, (
    "?[X]: (endurant(X) & perdurant(X))
32 )).
33
34 % Type
36 fof(ax_type_taxonomy, axiom, (
37 ![X]: ((endurantType(X) | perdurantType(X)) => (type_(X)))
```

2.1.2 Partial Taxonomy of Abstract Individual

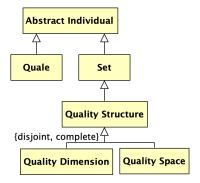


Figure 3: Partial Taxonomy of UFO – Abstract Individual.

```
51 % Abstract Individual
fof(ax_abstractIndividual_taxonomy_quale, axiom, (
![X]: (quale(X) => (abstractIndividual(X)))
55 )).
fof(ax_abstractIndividual_taxonomy_set, axiom, (
  ![X]: (set_(X) => (abstractIndividual(X)))
59 )).
60
fof(ax_abstractIndividual_taxonomy_world, axiom, (
  ![X]: (world(X) => (abstractIndividual(X)))
62
63 )).
64
65 fof(ax_abstractIndividual_pairwiseDisjoint, axiom, (
     ~?[X]: ((quale(X) & set_(X)) | (quale(X) & world(X)) | (set_(X) &
66
       world(X)))
67 )).
68
69 % Set
```

```
70
71 fof(ax_set_taxonomy_qualityStructure, axiom, (
  ![X]: (qualityStructure(X) => (set_(X)))
72
73 )).
74
75 % Quality Structure
fof(ax_qualityStructure_taxonomy, axiom, (
    ![X]: ((qualityDimension(X) | qualitySpace(X)) <=> (
      qualityStructure(X)))
79 )).
80
  fof(ax_qualityStructure_partition, axiom, (
81
    ~?[X]: (qualityDimension(X) & qualitySpace(X))
83 )).
84
85 % Abstract Individual partial taxonomy instances
86 % (tested to rule out trivial models)
```

2.1.3 Partial Taxonomy of Endurant

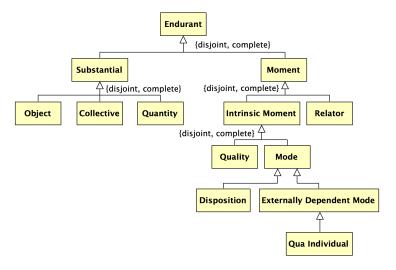


Figure 4: Partial Taxonomy of UFO – Endurant.

```
88 % fof(ax_abstractIndividual_instances, axiom, (
89 % set_(set1) & quale(quale1) & qualityStructure(qualityStructure1
       ) & qualityDimension(qualityDimension1) & qualitySpace(
            qualitySpace1) & world(world1)
90 % )).
91
92 % Endurant
93
94 fof(ax_endurant_taxonomy, axiom, (
95   ![X]: ((substantial(X) | moment(X)) <=> (endurant(X)))
96 )).
```

```
97
98 fof(ax_endurant_partition, axiom, (
    "?[X]: (substantial(X) & moment(X))
99
102 % Substantial
103
fof(ax_substantial_taxonomy, axiom, (
   ![X]: ((object(X) | collective(X) | quantity(X)) <=> (substantial
       (X)))
106 )).
fof(ax_substantial_partition, axiom, (
     ~?[X]: ((object(X) & collective(X)) | (object(X) & quantity(X)) |
        (collective(X) & quantity(X)))
110 )).
111
112 % Moment
113
_{\rm 114} fof(ax_moment_taxonomy, axiom, (
115
    ![X]: ((intrinsicMoment(X) | relator(X)) <=> (moment(X)))
116 )).
117
118 fof(ax_moment_partition, axiom, (
   "?[X]: (intrinsicMoment(X) & relator(X))
119
120 )).
122 % Intrinsic Moment
123
{\tt 124} fof(ax_intrinsicMoment_taxonomy, axiom, (
   ![X]: ((quality(X) | mode(X)) <=> (intrinsicMoment(X)))
125
126 )).
127
128 fof(ax_intrinsicMoment_partition, axiom, (
    ~?[X]: (quality(X) & mode(X))
129
130 )).
131
132 % Mode
133
134 fof(ax_mode_taxonomy_externallyDependentMode, axiom, (
   ![X]: (externallyDependentMode(X) => (mode(X)))
135
136 )).
137
138 % Externally Dependent Mode
140 fof(ax_externallyDependentMode_taxonomy_quaIndividual, axiom, (
   ![X]: (quaIndividual(X) => (externallyDependentMode(X)))
141
142 )).
143
144 % Endurant partial taxonomy instances
145 % (tested to rule out trivial models)
```

2.1.4 Partial Taxonomy of Endurant Type (on ontological natures)

```
% fof(ax_endurant_instances, axiom, (
```

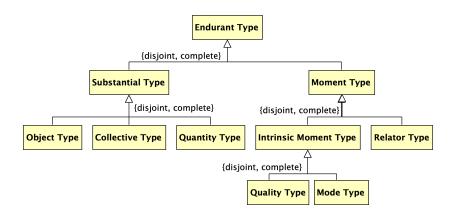


Figure 5: Partial Taxonomy of UFO – Endurant Types (by ontological nature).

```
substantial(substantial1) & moment(moment1) & object(object1) &
       collective(collective1) & quantity(quantity1) &
       intrinsicMoment(intrinsicMoment1) & relator(relator1) & quality
       (quality1) & mode(mode1) & disposition(disposition1) &
       externallyDependentMode(externallyDependentMode1) &
       quaIndividual(quaIndividual1)
149 % )).
150
  % Endurant Type (by ontological nature)
152
fof(ax_endurantType_taxonomy_nature, axiom, (
     ![X]: ((substantialType(X) | momentType(X)) <=> (endurantType(X))
  )).
155
  fof(ax_endurantType_partition_nature, axiom, (
157
     ~?[X]: (substantialType(X) & momentType(X))
158
159 )).
160
161
   % Substantial Type
   fof(ax_substantialType_taxonomy, axiom, (
163
     ![X]: ((objectType(X) | collectiveType(X) | quantityType(X)) <=>
       (substantialType(X)))
165 )).
166
   fof(ax_substantialType_partition, axiom, (
     ~?[X]: ((objectType(X) & collectiveType(X)) | (objectType(X) &
168
       quantityType(X)) | (collectiveType(X) & quantityType(X)))
169 )).
171
   % Moment Type
   fof(ax_momentType_taxonomy, axiom, (
173
     ![X]: ((intrinsicMomentType(X) | relatorType(X)) <=> (momentType(
       X)))
175 )).
176
```

```
177 fof(ax_momentType_partition, axiom, (
     ~?[X]: (intrinsicMomentType(X) & relatorType(X))
   )).
179
180
   % Intrinsic Moment Type
181
182
   fof(ax_intrinsicMomentType_taxonomy, axiom, (
     ![X]: ((qualityType(X) | modeType(X)) <=> (intrinsicMomentType(X)
184
185
   )).
186
   {\tt fof(ax\_intrinsicMomentType\_partition, axiom,} \ (
     ~?[X]: (qualityType(X) & modeType(X))
188
189 )).
190
   % Endurant Type (by ontological nature) partial taxonomy instances
192 % (tested to rule out trivial models)
```

2.1.5 Partial Taxonomy of Endurant Type (on modal properties of types)

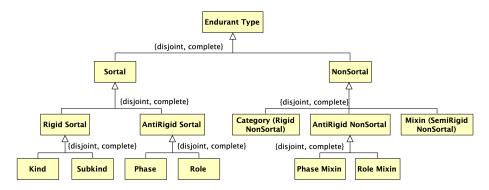


Figure 6: Partial Taxonomy of UFO – Endurant Types (by modal properties of types).

```
_{194} % fof(ax_endurantType_instances_natures, axiom, (
195
       substantialType(substantialType1) & momentType(momentType1) &
       objectType(objectType1) & collectiveType(collectiveType1) &
       quantityType(quantityType1) & intrinsicMomentType(
       intrinsicMomentType1) & relatorType(relatorType1) & qualityType
       (qualityType1) & modeType(modeType1)
196 % )).
197
   % Endurant Type (by modal properties of types)
198
  fof(ax_endurantType_taxonomy_properties, axiom, (
200
     ![X]: ((sortal(X) | nonSortal(X)) <=> (endurantType(X)))
201
202
  )).
203
204 fof(ax_endurantType_partition_properties, axiom, (
   ~?[X]: (sortal(X) & nonSortal(X))
205
206 )).
```

```
207
208 % Sortal
fof(ax_sortal_taxonomy, axiom, (
211 ![X]: ((rigidSortal(X) | antiRigidSortal(X)) <=> (sortal(X)))
212 )).
214 fof(ax_sortal_partition, axiom, (
~?[X]: (rigidSortal(X) & antiRigidSortal(X))
216 )).
217
218 % Rigid Sortal
219
220 fof(ax_rigidSortal_taxonomy, axiom, (
221 ![X]: ((kind(X) | subkind(X)) <=> (rigidSortal(X)))
223
224 fof(ax_rigidSortal_partition, axiom, (
225 ~?[X]: (kind(X) & subkind(X))
226 )).
227
228 % Anti-Rigid Sortal
fof(ax_antiRigidSortal_taxonomy, axiom, (
![X]: ((phase(X) | role(X)) <=> (antiRigidSortal(X)))
232 )).
233
fof(ax_antiRigidSortal_partition, axiom, (
    ~?[X]: (phase(X) & role(X))
235
236 )).
237
238 % Non-Sortal
240 fof(ax_nonSortal_taxonomy, axiom, (
    ![X]: ((rigidNonSortal(X) | semiRigidNonSortal(X) |
       antiRigidNonSortal(X)) <=> (nonSortal(X)))
242 )).
fof(ax_nonSortal_partition, axiom, (
     ~?[X]: ((rigidNonSortal(X) & semiRigidNonSortal(X)) | (
       rigidNonSortal(X) & antiRigidNonSortal(X)) | (
       semiRigidNonSortal(X) & antiRigidNonSortal(X)))
246 )).
247
248 % Category
249
fof(ax_rigidNonSortal_taxonomy, axiom, (
![X]: (rigidNonSortal(X) <=> (category(X)))
252 )).
253
254 % Mixin
fof(ax_semiRigidNonSortal_taxonomy, axiom, (
![X]: (semiRigidNonSortal(X) <=> (mixin(X)))
258 )).
259
260 % Anti-Rigid Non-Sortal
```

```
261
262  fof(ax_antiRigidNonSortal_taxonomy, axiom, (
    ![X]: ((phaseMixin(X) | roleMixin(X)) <=> (antiRigidNonSortal(X))
    )
264  )).
265  fof(ax_antiRigidNonSortal_partition, axiom, (
    ~?[X]: (phaseMixin(X) & roleMixin(X))
    )).
268  )).
269  // Endurant Type (by modal properties of types) partial taxonomy instances
271  % (tested to rule out trivial models)
```

2.1.6 Defining Types, Individuals, and Specialization

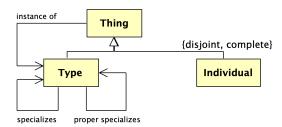


Figure 7: Types, individuals, instantiation, and specialization.

```
_{\rm 273} % fof(ax_endurantType_instances_properties, axiom, (
       sortal(sortal1) & nonSortal(nonSortal1) & rigidSortal(
       rigidSortal1) & antiRigidSortal(antiRigidSortal1) & kind(kind1)
        & subkind(subkind1) & phase(phase1) & role(role1) & category(
       category1) & mixin(mixin1) & antiRigidNonSortal(
       antiRigidNonSortal1) & phaseMixin(phaseMixin1) & roleMixin(
       roleMixin1)
275 % )).
276
277 %%%%%%%%% Instance of, Types, and Individuals %%%%%%%%%%%
278
   fof(ax_dIof, axiom, (
    ![X,Y,W]: (iof(X,Y,W) => (type_(Y) & world(W)))
280
281
282
fof(ax_dType_a1, axiom, (
    ![X]: (type_(X) <=> (?[Y,W]: iof(Y,X,W)))
284
285 )).
fof(ax_dIndividual_a2, axiom, (
    ![X]: (individual(X) <=> (~?[Y,W]: iof(Y,X,W)))
288
289 )).
290
291 fof(ax_multiLevel_a3, axiom, (
292 ![X,Y,W]: (iof(X,Y,W) => (type_(X) | individual(X)))
293 )).
```

```
294
295 fof(ax_twoLevelConstrained_a4, axiom, (
   ~?[X,Y,Z,W]: (type_(X) & iof(X,Y,W) & iof(Y,Z,W))
296
298
299 % Instantiation relations
300 % (tested to rule out trivial models)
301
302 % fof(ax_iofInUse, axiom, (
303 % type_(t2) & individual(i2) & world(w2) & iof(i2,t2,w2)
304 % )).
305
306 % Ax |= "th_everythingIsAThing_t1"; conjecture commented for
       convenience
307
308 % fof(th_everythingIsAThing_t1, conjecture, (
309 % ![X]: (type_(X) | individual(X))
310 % )).
311
312 % Ax |= "th_thingPartition_t2"; conjecture commented for
       convenience
313
314 % fof(th_thingPartition_t2, conjecture, (
      "?[X]: (type_(X) & individual(X))
316 % )).
317
318 %%%%%%% Specialization and Proper Specialization %%%%%%%%
319
320 fof(ax_dSpecializes, axiom, (
    ![X,Y]: (specializes(X,Y) => (type_(X) & type_(Y)))
321
322 )).
323
324 fof(ax_specialization_a5, axiom, (
     ![T1,T2]: (specializes(T1,T2) <=> (
325
       type_(T1) & type_(T2) & ![W]: (world(W) => ![E]: (iof(E,T1,W)
326
       => iof(E,T2,W)))
     ))
327
328 )).
329
fof(ax_properSpecializes_d1, axiom, (
     ![X,Y]: (properSpecializes(X,Y) <=> (specializes(X,Y) & ~
       specializes(Y,X)))
332 )).
333
334 % Ax |= "th_cyclicSpecializations_t3"; conjecture commented for
       convenience
336 % fof(th_cyclicSpecializations_t3, conjecture, (
       ![X,Y]: (specializes(X,Y) => (specializes(X,X) & specializes(Y,
337 %
       Y)))
338 % )).
339
340 % Ax |= "th_transitiveSpecializations_t4"; conjecture commented for
       convenience
342 % fof(th_transitiveSpecializations_t4, conjecture, (
343 % ![X,Y,Z]: ((specializes(X,Y) & specializes(Y,Z)) => (
```

```
specializes(X,Z)))
344 % )).
345
346 fof(ax_sharedSpecializations_a6, axiom, (
     ![T1,T2]: (![X,W]: ((iof(X,T1,W) & iof(X,T2,W) & ~specializes(T1,
347
       T2) & ~specializes(T2,T1)) => (
         (?[T3]: (specializes(T1,T3) & specializes(T2,T3) & iof(X,T3,W
         | (?[T3]: (specializes(T3,T1) & specializes(T3,T2) & iof(X,T3
       ,W)))
     )))
350
351 )).
352
353 % Specialization relations
354 % (tested to rule out trivial models)
356 % fof(ax_specializesInUse, axiom, (
```

2.1.7 Defining Rigidity and Sortality

```
360 %%%%%%%%%%%%%%%%%% Sortality and Rigidity %%%%%%%%%%%%%%%%%%%%%%
361
362 % Rigidity
363
364 fof(ax_dRigid_a18, axiom, (
     ![T]: (rigid(T) <=> (endurantType(T) & (
       ![X]: ((?[W1]: (world(W1) & iof(X,T,W1))) => (![W2]: (world(W2)
366
        => iof(X,T,W2))))
     )))
367
   )).
368
369
fof(ax_dAntiRigid_a19, axiom, (
     ![T]: (antiRigid(T) <=> (endurantType(T) & (
       ![X]: ((?[W1]: (world(W1) & iof(X,T,W1))) => (?[W2]: (world(W2)))
372
        % ~iof(X,T,W2)))
    ))))
373
374 )).
fof(ax_dSemiRigid_a20, axiom, (
     ![T]: (semiRigid(T) <=> (endurantType(T) & ~rigid(T) & ~antiRigid
       (T)))
378 )).
380 % Ax |= "th_thEndurantTypeHaveRigidity_t5"; conjecture commented
       for convenience
381
382 % fof(th_thEndurantTypeHaveRigidity_t5, conjecture, (
       ![T]: (endurantType(T) <=> (rigid(T) | semiRigid(T) | antiRigid
384 % )).
385
386 % Ax |= "th_pairwiseDisjointRigidities_t6"; conjecture commented
       for convenience
387
388 % fof(th_pairwiseDisjointRigidities_t6, conjecture, (
```

```
389 % ~ [T]: ((rigid(T) & semiRigid(T)) | (semiRigid(T) & antiRigid(T
      )) | (rigid(T) & antiRigid(T)))
390 % )).
391
392 % Ax |= "th_rigidAntiRigidSpecializationConstraint_t7"; conjecture
       commented for convenience
394 % fof(th_rigidAntiRigidSpecializationConstraint_t7, conjecture, (
     ~![T1,T2]: (rigid(T1) & antiRigid(T2) & specializes(T1,T2))
396 % )).
397
398 % Ax |= "th_semiRigidAntiRigidSpecializationConstraint_t8";
       conjecture commented for convenience
_{400} % fof(th_semiRigidAntiRigidSpecializationConstraint_t8, conjecture,
       ~![T1,T2]: (semiRigid(T1) & antiRigid(T2) & specializes(T1,T2))
401
402 % )).
403
404 % Rigidity properties
405 % (tested to rule out trivial models)
407 % fof(ax_rigidityInUse, axiom, (
       endurantType(t4_1) & endurantType(t4_2) & endurantType(t4_3) &
       rigid(t4_1) & semiRigid(t4_2) & antiRigid(t4_3) &
       properSpecializes (t4\_1,t4\_2) \& properSpecializes (t4\_3,t4\_1)
409 % )).
410
411 % Sortality
412
fof(ax_endurantsKind_a21, axiom, (
     ![E]: (endurant(E) => (
414
       ?[U]: (kind(U) & (![W]: (world(W) => iof(E,U,W))))
415
     ))
416
417 )).
418
419 fof(ax_uniqueKind_a22, axiom, (
   ![E,U,W]: ((world(W) & kind(U) & iof(E,U,W)) => (
        ~?[U2,W2]: (kind(U2) & iof(E,U2,W2) & ~(U = U2))
421
422
423 )).
424
425 % Changing "ax_dSortal_a23" from the form it was defined in the
       paper to "sortals are endurant types that specialize some
       ultimate sortal" seem to express the same concept while
       speeding up the execution of SPASS considerably
426
427 % fof(ax_dSortal_a23, axiom, (
       ![S]: (sortal(S) <=> (endurantType(S) & (?[U]: (kind(U) & (![E,
428 %
       W]: (iof(E,S,W) \Rightarrow iof(E,U,W))))))
429 % )).
430
fof(ax_dSortal_a23, axiom, (
    ![S]: ((sortal(S)) <=> (endurantType(S) & (?[U]: (kind(U) &
       specializes(S,U)))))
433 )).
434
```

```
^{435} % If we have the taxonomy's axiomatization, then a24 becomes a
436 % Ax |= "th nonSortalsAreEndurantsThatAreNotSortals a24":
       conjecture commented for convenience
437
438 % fof(th_nonSortalsAreEndurantsThatAreNotSortals_a24, conjecture, (
439 % ![NS]: ((nonSortal(NS)) <=> (endurantType(NS) & ~sortal(NS)))
440 % )).
442 % Ax |= "th_kindsAreRigid_t9"; conjecture commented for convenience
444 % fof(th_kindsAreRigid_t9, conjecture, (
445 % ![U]: ((kind(U)) => (rigid(U)))
446 % )).
447
448 % Ax |= "th_kindsHaveDisjointExtensions_t10"; conjecture commented
       for convenience
450 % fof(th_kindsHaveDisjointExtensions_t10, conjecture, (
      ![K1,K2]: ((kind(K1) & kind(K2) & ~(K1=K2)) => (
451 %
         ~?[X,W1,W2]: (world(W1) & world(W2) & iof(X,K1,W1) & iof(X,K2
       ,W2)))
453 %
454 % )).
455
456 % Ax |= "th_kindsHaveDisjointTaxonomies_t11"; conjecture commented
       for convenience
458 % fof(th_kindsHaveDisjointTaxonomies_t11, conjecture, (
      ![K1,K2]: ((kind(K1) & kind(K2) & ~(K1=K2)) => (
460 %
         ~?[T]: (specializes(T,K1) & specializes(T,K2)))
461 %
462 % )).
463
464 % Ax |= "th_kindsAreSortal_t12"; conjecture commented for
       convenience
465
466 % fof(th_kindsAreSortal_t12, conjecture, (
467 % ![K]: ((kind(K)) => (sortal(K)))
469
470 % Ax |= "th_sortalSpecializeKinds_t13"; conjecture commented for
       convenience
471
472 % fof(th_sortalSpecializeKinds_t13, conjecture, (
473 % ![S]: ((sortal(S)) => (?[K]: (kind(K) & specializes(S,K))))
474 % )).
475
476 % Ax |= "th_sortalsSpecializeAUniqueKind_t14"; conjecture commented
        for convenience
478 % fof(th_sortalsSpecializeAUniqueKind_t14, conjecture, (
      ![S]: ((sortal(S)) => (~?[U,U2]: (kind(U) & kind(U2) &
       specializes(S,U) & specializes(S,U2) & ~(U=U2))))
480 % )).
482 % Sortality properties
```

```
483 % (tested to rule out trivial models)
485 % fof(ax_sortalityInUse, axiom, (
       endurant(e5_1) & endurant(e5_2) & world(w5) & kind(k5_1) & kind
       (k5_2) & iof(e5_1,k5_1,w5) & iof(e5_1,k5_1,w5) & ~(k5_1=k5_2)
487 % )).
488
489 % Sortality + Rigidity
491 fof(ax_rigidSortalsAreRigidAndSortal_xx, axiom, (
    ![T]: ((rigidSortal(T)) <=> (rigid(T) & sortal(T)))
492
493 )).
494
495 fof(ax_antiRigidSortalsAreAntiRigidAndSortal_xx, axiom, (
496 ![T]: ((antiRigidSortal(T)) <=> (antiRigid(T) & sortal(T)))
498
499 fof(ax_rigidNonSortalsAreRigidAndNonSortal_xx, axiom, (
![T]: ((rigidNonSortal(T)) <=> (rigid(T) & nonSortal(T)))
501 )).
503 fof(ax_antiRigidNonSortalsAreAntiRigidAndNonSortal_xx, axiom, (
504 ![T]: ((antiRigidNonSortal(T)) <=> (antiRigid(T) & nonSortal(T)))
505 )).
506
507 fof(ax_semiRigidNonSortalsAreSemiRigidAndNonSortal_xx, axiom, (
   ![T]: ((semiRigidNonSortal(T)) <=> (semiRigid(T) & nonSortal(T)))
508
509 )).
510
511 % If we have the taxonomy's axiomatization, then a25 becomes a
512 % Ax |= "th_kindAndSubkindAreDisjoint_a25"; conjecture commented
       for convenience
513
514 % fof(th_kindAndSubkindAreDisjoint_a25, conjecture, (
515 % ~?[T]: (kind(T) & subkind(T))
516 % )).
517
518 % If we have the taxonomy's axiomatization, then a26 becomes a
519 % Ax |= "th_kindAndSubkindAreRigidSortals_a26"; conjecture
       commented for convenience
521 % fof(th_kindAndSubkindAreRigidSortals_a26, conjecture, (
522 % ![T]: ((kind(T) | subkind(T)) <=> (rigid(T) & sortal(T)))
523 % )).
524
525 % If we have the taxonomy's axiomatization, then a27 becomes a
       theorem
526 % Ax |= "th_phaseAndRoleAreDisjoint_a27"; conjecture commented for
       convenience
528 % fof(th_phaseAndRoleAreDisjoint_a27, conjecture, (
529 % ~?[T]: (phase(T) & role(T))
530 % )).
532 % If we have the taxonomy's axiomatization, then a28 becomes a
```

```
theorem
533 % Ax |= "th_phaseAndRoleAreAntiRigidSortals_a28"; conjecture
       commented for convenience
535 % fof(th_phaseAndRoleAreAntiRigidSortals_a28, conjecture, (
      ![T]: ((phase(T) | role(T)) <=> (antiRigid(T) & sortal(T)))
537 % )).
538
539 % Skipping (a29) because we leave the concept of semi-rigid sortals
        out of this ontology.
540
541 % If we have the taxonomy's axiomatization, then a 30 becomes a
       theorem
542 % Ax |= "th_categoriesAreRigidNonSortals_a30"; conjecture commented
       for convenience
543
544 % fof(th_categoriesAreRigidNonSortals_a30, conjecture, (
545 % ![T]: ((category(T)) <=> (rigid(T) & nonSortal(T)))
546 % )).
547
548 % If we have the taxonomy's axiomatization, then a31 becomes a
       theorem
549 % Ax |= "th_mixinsAreSemiRigidNonSortals_a31"; conjecture commented
       for convenience
550
551 % fof(th_mixinsAreSemiRigidNonSortals_a31, conjecture, (
552 % ![T]: ((mixin(T)) <=> (semiRigid(T) & nonSortal(T)))
553 % )).
554
_{555} % If we have the taxonomy's axiomatization, then a32 becomes a
556 % Ax |= "th_phaseMixinAndRoleMixinAreDisjoint_a32"; conjecture
       commented for convenience
557
558 % fof(th_phaseMixinAndRoleMixinAreDisjoint_a32, conjecture, (
559 % ~?[T]: (phaseMixin(T) & roleMixin(T))
560 % )).
561
_{562} % If we have the taxonomy's axiomatization, then a33 becomes a
563 % Ax |= "ax_phaseMixinAndRoleMixinAreAntiRigidSortals_a33";
       conjecture commented for convenience
565 % fof(th_phaseMixinAndRoleMixinAreAntiRigidSortals_a33, conjecture,
       ![T]: ((phaseMixin(T) | roleMixin(T)) <=> (antiRigid(T) &
566 %
       nonSortal(T)))
567 % )).
568
569 % Ax |= "th_leafCategoriesArePairwiseDisjoint_t18"; conjecture
       commented for convenience
571 % fof(th_leafCategoriesArePairwiseDisjoint_t18, conjecture, (
       ~?[T]: (endurantType(T) & (
572 %
573 %
           (kind(T) & subkind(T))
574 %
575 %
          | (kind(T) & phase(T))
```

```
| (kind(T) & role(T))
576 %
577
   %
              (kind(T) & category(T))
            | (kind(T) & mixin(T))
578 %
            | (kind(T) & phaseMixin(T))
            | (kind(T) & roleMixin(T))
580 %
581 %
         ) | (
            (subkind(T) & phase(T))
582
   %
583 %
            | (subkind(T) & role(T))
584 %
            | (subkind(T) & category(T))
            | (subkind(T) & mixin(T))
585 %
   %
            | (subkind(T) & phaseMixin(T))
586
   %
587
            | (subkind(T) & roleMixin(T))
   %
         ) | (
588
589 %
            (phase(T) & role(T))
590 %
            | (phase(T) & category(T))
   %
              (phase(T) & mixin(T))
591
592 %
            | (phase(T) & phaseMixin(T))
593 %
            | (phase(T) & roleMixin(T))
594 %
         ) | (
595 %
            (role(T) & category(T))
596
            | (role(T) & mixin(T))
            | (role(T) & phaseMixin(T))
   %
597
598 %
            | (role(T) & roleMixin(T))
599 %
         ) | (
   %
            (category(T) & mixin(T))
600
   %
601
            | (category(T) & phaseMixin(T))
            | (category(T) & roleMixin(T))
602 %
603
         ) | (
            (mixin(T) & phaseMixin(T))
604 %
            | (mixin(T) & roleMixin(T))
605
   %
606
         ) | (
            (phaseMixin(T) & roleMixin(T))
607
   %
         )
608
       ))
609 %
610 % )).
611
612 % Ax |= "th_leafCategoriesCompletelyCategorizeAllEndurantTypes_t19
        "; conjecture commented for convenience
613
_{614} % fof(th_leafCategoriesCompletelyCategorizeAllEndurantTypes_t19,
       conjecture, (
615 %
        ![T]: (endurantType(T) => (
         kind(T) | subkind(T) | phase(T) | role(T) | category(T) |
       mixin(T) \mid phaseMixin(T) \mid roleMixin(T)
617
618 % )).
619
620 % Sortality and rigidity properties combined
621 % (tested to rule out trivial models)
_{\rm 623} % fof(ax_sortalityAndRigidityInUse, axiom, (
        endurant(e6_1) & endurant(e6_2) & world(w6) & kind(k6_1) & kind
624 %
        (k6_2) \& iof(e6_1,k6_1,w6) \& iof(e6_1,k6_1,w6) \& ~(k6_1=k6_2)
625 % )).
```

2.1.8 Defining Endurant Types

628

```
629 % Defining the taxonomy of types of ontological natures through the
        categorization of the taxonomy of concrete individuals
630
631 fof(ax_perdurantTypeDefinition_a44, axiom, (
     ![T]: (perdurantType(T) <=> (
632
       type_{T}(T) & (![P,W]: ((world(W) & iof(P,T,W)) => (perdurant(P)))
633
     ))
634
   )).
635
636
   fof(ax_endurantTypeDefinition_a44, axiom, (
637
     ![T]: (endurantType(T) <=> (
638
       type_(T) & (![E,W]: ((world(W) & iof(E,T,W)) => (endurant(E))))
639
     ))
640
641 )).
642
643
   fof(ax_substantialTypeDefinition_a44, axiom, (
     ![T]: (substantialType(T) <=> (
644
       type_{-}(T) & (![E,W]: ((world(W) & iof(E,T,W)) => (substantial(E))) \\
       )))
     ))
647 )).
648
649 fof(ax_momentTypeDefinition_a44, axiom, (
     ![T]: (momentType(T) <=> (
650
       type_{-}(T) \& (![E,W]: ((world(W) \& iof(E,T,W)) \Rightarrow (moment(E))))
651
652
653 )).
654
655 fof(ax_objectTypeDefinition_a44, axiom, (
     ![T]: (objectType(T) <=> (
656
       type_{T}(T) & (![E,W]: ((world(W) & iof(E,T,W)) => (object(E))))
657
     ))
658
659 )).
660
   fof(ax_collectiveTypeDefinition_a44, axiom, (
661
     ![T]: (collectiveType(T) <=> (
662
       type_{-}(T) & (![E,W]: ((world(W) & iof(E,T,W)) \Rightarrow (collective(E))
       ))
     ))
664
665 )).
666
667 fof(ax_quantityTypeDefinition_a44, axiom, (
     ![T]: (quantityType(T) <=> (
668
       type_{T}(T) & (![E,W]: ((world(W) & iof(E,T,W)) => (quantity(E))))
669
670
671 )).
672
673 fof(ax_intrinsicMomentTypeDefinition_a44, axiom, (
     ![T]: (intrinsicMomentType(T) <=> (
674
       type_(T) & (![E,W]: ((world(W) & iof(E,T,W)) => (
675
       intrinsicMoment(E))))
     ))
676
677 )).
678
fof(ax_relatorTypeDefinition_a44, axiom, (
680 ![T]: (relatorType(T) <=> (
```

```
type_(T) & (![E,W]: ((world(W) & iof(E,T,W)) => (relator(E))))
681
    ))
682
683 )).
684
685 fof(ax_qualityTypeDefinition_a44, axiom, (
     ![T]: (qualityType(T) <=> (
686
       type_(T) & (![E,W]: ((world(W) & iof(E,T,W)) => (quality(E))))
687
688
689 )).
690
   fof(ax_modeTypeDefinition_a44, axiom, (
691
     ![T]: (modeType(T) <=> (
692
       type_{-}(T) & (![E,W]: ((world(W) & iof(E,T,W)) \Rightarrow (mode(E))))
693
     ))
694
695 )).
696
697 % Types Definition
698 % (tested to rule out trivial models)
_{699} % TODO: investigate why we cannot list four different endurant
       types (it may have something to do with "intrinsicMoment" and " \,
       intrinsicMomentType")
700
701 % fof(ax_typesDefinitionsInstances, axiom, (
       objectType(ot7) & collectiveType(ct7) & modeType(mt7)
703 % )).
704
705 % Ax |= "th_leafCategoriesArePairwiseDisjoint_t21"; conjecture
       commented for convenience
706 % Having the previously defined taxonomy, this should be quite
       trivial
708 % fof(th_leafCategoriesArePairwiseDisjoint_t21, conjecture, (
       ~?[T]: (type_(T) & (
709 %
710 %
           (objectType(T) & collectiveType(T)) | (objectType(T) &
711 %
       quantityType(T)) | (objectType(T) & modeType(T)) | (objectType(
       T) & qualityType(T)) | (objectType(T) & relatorType(T)) | (
       objectType(T) & perdurantType(T))
         ) | (
712 %
713 %
            (collectiveType(T) & quantityType(T)) | (collectiveType(T)
       & modeType(T)) | (collectiveType(T) & qualityType(T)) | (
       collectiveType(T) & relatorType(T)) | (collectiveType(T) &
       perdurantType(T))
714 %
         ) | (
            (quantityType(T) & modeType(T)) | (quantityType(T) &
715
       qualityType(T)) | (quantityType(T) & relatorType(T)) | (
       quantityType(T) & perdurantType(T))
716 %
         ) | (
           (modeType(T) & qualityType(T)) | (modeType(T) & relatorType
717 %
       (T)) | (modeType(T) & perdurantType(T))
         ) | (
718 %
719 %
            (qualityType(T) & relatorType(T)) | (qualityType(T) &
       perdurantType(T))
         ) | (
720 %
721 %
           relatorType(T) & perdurantType(T)
722 %
723 %
```

```
724 % )).
726 % Ultimate Sortals Definitions (by ontological nature)
fof(ax_objectKindDefinition_a45, axiom, (
   ![T]: (objectKind(T) <=> (objectType(T) & kind(T)))
729
730 )).
731
fof(ax_collectiveKindDefinition_a45, axiom, (
734 )).
735
fof(ax_quantityKindDefinition_a45, axiom, (
![T]: (quantityKind(T) <=> (quantityType(T) & kind(T)))
738 )).
740 fof(ax_modeKindDefinition_a45, axiom, (
   ![T]: (modeKind(T) <=> (modeType(T) & kind(T)))
741
742 )).
743
744 fof(ax_qualityKindDefinition_a45, axiom, (
![T]: (qualityKind(T) <=> (qualityType(T) & kind(T)))
746 )).
747
fof(ax_relatorKindDefinition_a45, axiom, (
749 ![T]: (relatorKind(T) <=> (relatorType(T) & kind(T)))
750 )).
751
752 % Ultimate sortals (by ontological nature) instances
753 % (tested to rule out trivial models)
_{754} % TODO: investigate why we cannot list all different types of
      ultimate sortals at once
756 % fof(ax_typesDefinitionsInstances, axiom, (
      objectKind(ok9) & collectiveKind(ck9) & quantityKind(quank9) &
       relatorKind(rk9) & modeKind(mk9) & qualityKind(qualk9)
758 % )).
759
760 % Skipping (t22) because (a21) makes it trivial
761
762 % Ax |= "th_endurantsInstantiateEndurantKindsOfSomeNature_a46";
       conjecture commented for convenience
_{763} % This axiom is actually a theorem in this version of the
      axiomatization
_{765} % fof(th_endurantsInstantiateEndurantKindsOfSomeNature_a46,
       conjecture, (
766 %
       ![E]: (endurant(E) => (
        ?[K,W]: ((objectKind(K) | collectiveKind(K) | quantityKind(K)
767 %
        | modeKind(K) | qualityKind(K) | relatorKind(K))
768 %
        & iof(E,K,W))
     ))
769 %
770 % )).
771
772 % Ax |= "th_endurantSortalsCompleteness_t23"; conjecture commented
      for convenience
773 % Thanks to the taxonomy, we already have "sortal(T) =>
```

```
endurantType(T)", but I leave it like this to be consistent
       with the paper
774
775 % fof(th_endurantSortalsCompleteness_t23, conjecture, (
      ![T]: ((endurantType(T) & sortal(T)) => (objectKind(T) |
       collectiveKind(T) | quantityKind(T) | qualityKind(T) | modeKind
       (T) | relatorKind(T) | phase(T) | role(T)))
777 % )).
779 % Ax |= "th_objectTypesSpecializeAKindOfSameNature_t24"; conjecture
        commented for convenience
_{781} % fof(th_objectTypesSpecializeAKindOfSameNature_t24, conjecture, (
      ![T]: ((objectType(T) \& sortal(T)) <=> (?[K]: (objectKind(K) &
       specializes(T,K))))
783 % )).
784
785 % Ax |= "th_collectiveTypesSpecializeAKindOfSameNature_t24";
       conjecture commented for convenience
786
  % fof(th_collectiveTypesSpecializeAKindOfSameNature_t24, conjecture
       ![T]: ((collectiveType(T) & sortal(T)) <=> (?[K]: (
       collectiveKind(K) & specializes(T,K))))
789 % )).
790
791 % Ax |= "th_quantityTypesSpecializeAKindOfSameNature_t24";
       conjecture commented for convenience
793 % fof(th_quantityTypesSpecializeAKindOfSameNature_t24, conjecture,
       ![T]: ((quantityType(T) & sortal(T)) <=> (?[K]: (quantityKind(K
      ) & specializes(T,K))))
795 % )).
796
797 % Ax |= "th_modeTypesSpecializeAKindOfSameNature_t24"; conjecture
       commented for convenience
^{799} % fof(th_modeTypesSpecializeAKindOfSameNature_t24, conjecture, (
800 %
       ![T]: ((modeType(T) & sortal(T)) <=> (?[K]: (modeKind(K) &
       specializes(T,K))))
801 % )).
802
803 % Ax |= "th_qualityTypesSpecializeAKindOfSameNature_t24";
       conjecture commented for convenience
804
805 % fof(th_qualityTypesSpecializeAKindOfSameNature_t24, conjecture, (
      ![T]: ((qualityType(T) & sortal(T)) <=> (?[K]: (qualityKind(K)
       & specializes(T,K))))
807 % )).
808
809 % Ax |= "th_relatorTypesSpecializeAKindOfSameNature_t24";
       conjecture commented for convenience
810
811 % fof(th_relatorTypesSpecializeAKindOfSameNature_t24, conjecture, (
812 % ![T]: ((relatorType(T) & sortal(T)) <=> (?[K]: (relatorKind(K)
       & specializes(T,K))))
```

```
813 % )).
814
815 % Ax |= "th_sortalLeafCategoriesAreDisjoint_t25"; conjecture
       commented for convenience
816
817 % fof(th_sortalLeafCategoriesAreDisjoint_t25, conjecture, (
       ![T]: (objectKind(T) => (~(collectiveKind(T) | quantityKind(T)
818
       | modeKind(T) | qualityKind(T) | relatorKind(T) | category(T) |
        mixin(T) | phaseMixin(T) | roleMixin(T))))
       & ![T]: (collectiveKind(T) => (~(objectKind(T) | quantityKind(T
819 %
         | modeKind(T) | qualityKind(T) | relatorKind(T) | category(T)
        | mixin(T) | phaseMixin(T) | roleMixin(T))))
       & ![T]: (quantityKind(T) => (~(objectKind(T) | collectiveKind(T
820 %
       ) | modeKind(T) | qualityKind(T) | relatorKind(T) | category(T)
        | mixin(T) | phaseMixin(T) | roleMixin(T))))
       & ![T]: (modeKind(T) => (~(objectKind(T) | quantityKind(T) |
       collectiveKind(T) | qualityKind(T) | relatorKind(T) | category(
       T) | mixin(T) | phaseMixin(T) | roleMixin(T))))
       & ![T]: (qualityKind(T) \Rightarrow (~(objectKind(T) | quantityKind(T) |
822 %
        modeKind(T) | collectiveKind(T) | relatorKind(T) | category(T)
        | mixin(T) | phaseMixin(T) | roleMixin(T))))
       & ![T]: (relatorKind(T) => (~(objectKind(T) | quantityKind(T) |
823 %
        modeKind(T) | qualityKind(T) | collectiveKind(T) | category(T)
        | mixin(T) | phaseMixin(T) | roleMixin(T))))
       & ![T]: (category(T) => (~(objectKind(T) | quantityKind(T) |
824 %
       \verb|modeKind(T)| qualityKind(T)| relatorKind(T)| collectiveKind(T)|
       T) | mixin(T) | phaseMixin(T) | roleMixin(T))))
       & ![T]: (mixin(T) => (~(objectKind(T) | quantityKind(T) |
825 %
       modeKind(T) | qualityKind(T) | relatorKind(T) | category(T) |
       \verb|collectiveKind(T)|| phaseMixin(T)|| roleMixin(T)))|
       & ![T]: (phaseMixin(T) => (~(objectKind(T) | quantityKind(T) |
826
       modeKind(T) | qualityKind(T) | relatorKind(T) | category(T) |
       mixin(T) | collectiveKind(T) | roleMixin(T))))
827 %
       & ![T]: (roleMixin(T) \Rightarrow (~(objectKind(T) | quantityKind(T) |
       modeKind(T) | qualityKind(T) | relatorKind(T) | category(T) |
       mixin(T) | phaseMixin(T) | collectiveKind(T))))
828 % )).
830 % Ax |= "th_sortalLeafCategoriesAreComplete_t26"; conjecture
       commented for convenience
831
832 % fof(th_sortalLeafCategoriesAreComplete_t26, conjecture, (
       ![T]: ((endurantType(T)) => (objectKind(T) | collectiveKind(T)
       |\ quantity \texttt{Kind}(\texttt{T})\ |\ quality \texttt{Kind}(\texttt{T})\ |\ mode \texttt{Kind}(\texttt{T})\ |\ relator \texttt{Kind}(
       T) | phase(T) | role(T) | category(T) | mixin(T) | phaseMixin(T
       ) | roleMixin(T)))
834 % )).
```

2.1.9 Mereology

```
837
838 % TODO: review whether it is necessary to reduce mereology to concrete individuals; I am leaving this axiom out for the moment
839
840 % fof(ax_partArguments, axiom, (
841 % ![X,Y]: (part(X,Y) => (concreteIndividual(X) & concreteIndividual(Y)))
```

```
842 % )).
843
844 fof(ax_reflexiveParthood, axiom, (
   ![X]: (partOf(X,X))
846 )).
847
848 fof(ax_antiSymmetricParthood_a47, axiom, (
   ![X,Y]: ((partOf(X,Y) & partOf(Y,X)) => (X=Y))
849
851
852 fof(ax_antiSymmetricParthood_a48, axiom, (
   ![X,Y]: ((partOf(X,Y) & partOf(Y,X)) => (X=Y))
853
854 )).
fof(ax_transitiveParthood_a49, axiom, (
    ![X,Y,Z]: ((partOf(X,Y) & partOf(Y,Z)) => (partOf(X,Z)))
857
858 )).
859
fof(ax_overlappingWholes_a50, axiom, (
   ![X,Y]: ((overlap(X,Y)) <=> (?[Z]: (partOf(Z,X) & partOf(Z,Y))))
861
862 )).
863
864 fof(ax_strongSupplementation_a51, axiom, (
865 ![X,Y]: (~partOf(X,Y) <=> ?[Z]: (partOf(Z,X) & ~overlap(Z,Y)))
866 )).
867
s68 fof(ax_properPart_a52, axiom, (
    ![X,Y]: (properPartOf(X,Y) <=> (partOf(X,Y) & ~partOf(Y,X)))
869
870 )).
871
872 fof(ax_binarySum_a53, axiom, (
    ![X,Y,Z]: (sum(Z,X,Y) \iff ![W]: (overlap(W,Z) \iff (overlap(W,X) |
873
        overlap(W,Y))))
874 )).
875
876 % Mereology in use
877 % (tested to rule out trivial models)
879 % fof(ax_mereologyInUse, axiom, (
880 %
      concreteIndividual(ci10_1) & concreteIndividual(ci10_2) &
       concreteIndividual(ci10_3) & concreteIndividual(ci10_4) &
       concreteIndividual(ci10_5) & ~(ci10_1=ci10_2) & ~(ci10_2=ci10_3
      ) & ~(ci10_3=ci10_4) & ~(ci10_4=ci10_5) & properPart(ci10_1,
       ci10_2) & properPart(ci10_3,ci10_4) & sum(ci10_5,ci10_3,ci10_4)
   % )).
882
fof(ax_function, axiom, (
    ![X,Y]: (functionsAs(X,Y) => (endurant(X) & type_(Y)))
887 )).
```

2.1.10 Composition

```
886 ![X,Y]: (functionsAs(X,Y) => (endurant(X) & type_(Y)))
887 )).
888
fof(ax_genericFunctionalDependence_a55, axiom, (
```

```
![T1,T2,W]: (gfd(T1,T2,W) <=>
       ![E1]: ((iof(T1,E1,W) & functionsAs(T1,E1)) => ?[E2]: (~(E1=E2)
       & iof(T2,E2,W) & functionsAs(T2,E2))))
893
  fof(ax_individualFunctionalDependence_a56, axiom, (
894
    895
      gfd(T1,T2,W) & iof(E1,T1,W) & iof(E2,T2,W) & (functionsAs(E1,T1
896
       => functionsAs(E2,T2))
    ))
897
898 )).
899
900 fof(ax_componentOf_a57, axiom, (
    ![E1,T1,E2,T2,W]: (componentOf(E1,T1,E2,T2,W) <=> (properPartOf(
      E1,E2) & ifd(E1,T1,E2,T2,W)))
902 )).
903
904 % Composition in use
905 % (tested to rule out trivial models)
906
907 % fof(ax_compositionInUse, axiom, (
      componentOf(e11_1,t11_1,e11_2,t11_2,w11) & ~(e11_1=e11_2) & ~(
908 %
      e11_1=t11_1) & ~(e11_2=t11_2) & ~(e11_1=t11_2) & ~(e11_2=t11_1)
       & ~(t11_1=t11_2)
909 % )).
910
912
913 fof(ax_constitutedByInvolvedNatures_a58, axiom, (
    ![X,Y,W]: (constitutedBy(X,Y,W) => ((endurant(X) <=> endurant(Y))
       & (perdurant(X) <=> perdurant(Y)) & world(W)))
```

2.1.11 Constitution

```
917 fof(ax_constitutedByDifferentKinds_a59, axiom, (
     ![E1,E2,T1,T2,W]: ((constitutedBy(E1,E2,W) & iof(E1,T1,W) & iof(
       E2,T2,W) & kind(T1) & kind(T2)) => (~(T1=T2)))
919 )).
920
921 % Ax |= "th_noSelfConstitution_t27"; conjecture commented for
       convenience
922
923 % fof(th_noSelfConstitution_t27, conjecture, (
924 %
     ~?[X,W]: (endurant(X) & constitutedBy(X,X,W))
925 % )).
fof(ax_genericConstitutionalDependence_a60, axiom, (
     ![T1,T2]: (genericConstitutionalDependence(T1,T2) <=> (
928
929
       type_(T1) & type_(T2) & ![E1,W]: (iof(E1,T1,W) => (
         ?[E2]: (constitutedBy(E1,E2,W) & iof(E2,T2,W)
930
931
       )))
    ))
932
933 )).
934
935 fof(ax_constitution_a61, axiom, (
   ![E1,T1,E2,T2,W]: (constitution(E1,T1,E2,T2,W) <=> (
```

```
iof(E1,T1,W) & iof(E2,T2,W) & genericConstitutionalDependence(
                     T1,T2) & constitutedBy(E1,E2,W)
              ))
938
939 )).
940
941 fof(
                      \verb|ax_wheneverAC| on stituted Perdurant Exists The Constituted By Relation Holds\_a62| and the Constituted By R
                        . axiom. (
                ![P1,P2,W1]: ((constitutedBy(P1,P2,W1) & perdurant(P1)) => (![W2
                      ]: (exists(P1,W2) => constitutedBy(P1,P2,W2))))
943 )).
944
945 fof(ax_constitutedByIsAsymmetric_a63, axiom, (
              ![E1,E2,W]: (constitutedBy(E1,E2,W) => ~constitutedBy(E2,E1,W))
947 )).
949 % Constitution in use
950 % (tested to rule out trivial models)
951
_{952} % fof(ax_constitutionInUse, axiom, (
                      object(e12_1) & object(e12_2) & objectKind(k12_1) & objectKind(
953
                      k12_2) & world(w12) & ~(k12_1=k12_2) & iof(e12_1,k12_1,w12) &
                      iof(e12_2,k12_2,w12) & constitutedBy(e12_1,e12_2,w12) &
                      genericConstitutionalDependence(k12_1,k12_2) & constitution(
                      e12_1, k12_1, e12_2, k12_2, w12)
954 % )).
955
956 %%%%%%%%%%%%%%%% Existential Dependence %%%%%%%%%%%%%%%%%%%%
957
958 fof(ax_exists_a64, axiom, (
         ![X,W]: (exists(X,W) => (thing(X) & world(W)))
```

2.1.12 Existential Dependence

```
961
962 fof(ax_existentiallyDependsOn_a65, axiom, (
                   ![X,Y]: (existentiallyDependsOn(X,Y) \iff (![W]: (exists(X,W) => (![W
                          exists(Y,W))))
964 )).
965
966 fof(ax_existentiallyIndependentOf_a66, axiom, (
                  ![X,Y]: (existentiallyIndependentOf(X,Y) <=> (~
                          \tt existentiallyDependsOn(X,Y) \& ~~existentiallyDependsOn(Y,X)))
968 )).
969
970 % Existential dependence in use
971 % (tested to rule out trivial models)
972
973 % fof(ax_constitutionInUse, axiom, (
                         object(e13_1) & object(e13_2) & object(e13_3) & ~(e13_1=e13_2)
974 %
                         & ~(e13_1=e13_3) & ~(e13_2=e13_3) & existentiallyDependsOn(
                         e13_2,e13_1) & existentiallyIndependentOf(e13_3,e13_1)
975 % )).
976
977 % TODO: introduce transitivity and anti-symmetry of existential
                          dependence
_{978} % TODO: introduce continuity of existence with perdurants never
                        ceasing to exist
```

2.1.13 Moments and Inherence

```
985 ![M,X]: (inheresIn(M,X) => existentiallyDependsOn(M,X))
986 )).
987
988 fof(ax_thingsInvolvedInInherence_a68, axiom, (
989
    ![M,X]: (inheresIn(M,X) => (moment(M) & (type_(X) | endurant(X)))
990 )).
991
992 % TODO: add definition (d5) for the "bearer" axiom
994 fof(ax irreflexiveInherence, axiom, (
995
    ![X]: (~inheresIn(X,X))
996 )).
997
998 fof(ax_asymmetricInherence, axiom, (
999 ![X,Y]: (inheresIn(X,Y) => ~inheresIn(Y,X))
1000 )).
1002 fof(ax_intransitiveInherence, axiom, (
![X,Y,Z]: ((inheresIn(X,Y) & inheresIn(Y,Z)) => ~inheresIn(X,Z))
1004 )).
fof(ax_uniqueInherence_a69, axiom, (
   ![X,Y,Z]: ((inheresIn(X,Y) \& inheresIn(X,Z)) \Rightarrow (Y=Z))
1007
1008 )).
1009
1010 % Moments
1011
1012 fof(ax_dMomentOf_d6, axiom, (
![M,X]: (momentOf(M,X) \iff (inheresIn(M,X) | (
        ?[M2]: (inheresIn(M,M2) & momentOf(M2,X))
1014
1015
     )))
1016 )).
1017
1018 fof(ax_dUltimateBearerOf_d7, axiom, (
![B,M]: (ultimateBearerOf(B,M) <=> (~moment(B) & momentOf(M,B)))
1020 )).
1021
1022 fof(ax_everyMomentHasUniqueAUltimateBearer_a70, axiom, (
![M]: (moment(M) => (?[B]: (ultimateBearerOf(B,M) & (
1024
        ![B2]: (ultimateBearerOf(B2,M) <=> (B=B2))
     ))))
1025
1026 )).
1027
1028 fof(ax_noMomentOfCycles, axiom, (
     ~?[M]: momentOf(M,M)
1029
1030 )).
1031
1032 % Ax |= "th_irreflexiveInherence_t28"; conjecture commented for
       convenience
```

```
1034 % fof(th_irreflexiveInherence_t28, conjecture, (
1035 % ~?[X]: (inheresIn(X,X))
1036 % )).
1037
1038 % Ax |= "th_asymmetricInherence_t29"; conjecture commented for
       convenience
1040 % fof(th_asymmetricInherence_t29, conjecture, (
      ~?[X,Y]: (inheresIn(X,Y) & inheresIn(Y,X))
1042 % )).
1043
_{1044} % Ax |= "th_antiTransitiveInherence_t30"; conjecture commented for
       convenience
1045
1046 % fof(th_antiTransitiveInherence_t30, conjecture, (
1047 % ![X,Y,Z]: ((inheresIn(X,Y) \& inheresIn(Y,Z)) => (~inheresIn(X,Z))
       )))
1048 % )).
1049
1050 % TODO: add instances
1054 % External Dependence and Externally Dependent Modes
```

2.1.14 Relators

```
~?[M,X]: (externallyDependsOn(M,X) <=> (existentiallyDependsOn(M,
       X) & (![Y]: (inheresIn(M,Y) => existentiallyIndependentOf(X,Y))
       )))
1058 )).
1059
_{1060} fof(ax_dExternallyDependentMode_a72, axiom, (
     ![M]: (externallyDependentMode(M) <=> (mode(M) & (?[X]: (
       externallyDependsOn(M,X))))
1062 )).
1063
1064 % Founded by
fof(ax_foundedByInvolvedThings_a73, axiom, (
     ![M,P]: (foundedBy(M,P) <=> ((externallyDependentMode(M) |
1067
       relator(M)) & perdurant(P)))
1068 )).
fof(ax_relationalModesHaveAFoundationEvent_a74, axiom, (
     ![M]: ((externallyDependentMode(M) | relator(M)) => (?[P]: (
       foundedBy(M,P))))
1072 )).
1074 fof(ax_uniqueFoundationEvents_a74, axiom, (
![M,P1,P2]: ((foundedBy(M,P1) & foundedBy(M,P2)) => (P1=P2))
1076 )).
1078 % TODO: add definition (d8) for the "foundationOf" axiom
1079
1080 % Qua Individual
1081
fof(ax_dQuaIndividualOf_a75, axiom, (
```

```
![X,Y]: (quaIndividualOf(X,Y) \iff (![Z]: (overlap(Z,X) \iff (
        externallyDependentMode(Z) & inheresIn(Z,Y) & (![P]: (foundedBy
        (X,P) \Rightarrow foundedBy(Z,P))
     ))))
1086 )).
1087
1088 % Ax |= "
       th_thePartsOfAQuaIndividualShareTheFoundationOfTheWhole_t31";
        conjecture commented for convenience
1089
_{1090} % fof(th_thePartsOfAQuaIndividualShareTheFoundationOfTheWhole_t31,
        conjecture, (
        ![X,Y,Z]: ((quaIndividual(X) & partOf(Z,X)) \Rightarrow (![P]: (
1091 %
        foundedBy(Z,P) => foundedBy(X,P))))
1092 % )).
1094 fof(ax_dQuaIndividual_a76, axiom, (
     ![X]: (quaIndividual(X) <=> ?[Y]: (quaIndividualOf(X,Y)))
1095
1096 )).
1097
1098 % Qua Individual is already defined as a subtype of Externally
        Dependent Mode in the taxonomy; skipping (a78)
1099
1100 % Skipping (a79); already defined in (a74)
1102 fof(ax_thePartsOfARelatorShareTheFoundationOfTheWhole_a80, axiom, (
     ![X,Y,Z]: ((relator(X) \& partOf(Z,X)) \Rightarrow (![P]: (foundedBy(Z,P))
1103
        => foundedBy(X,P))))
1104 )).
fof(ax_dRelator_a81, axiom, (
      ![R]: (relator(R) <=> (
1107
        (?[X]: (properPartOf(X,R))
1108
        & (![Y,Z]: ((properPartOf(Y,R) & properPartOf(Z,R)) => (
1109
        quaIndividual(Y) & quaIndividual(Z) & existentiallyDependsOn(Y,
        Z) & existentiallyDependsOn(Z,Y) & (![P]: (foundedBy(Y,P) <=>
        foundedBy(Z,P)))))
        & (![Y2,Z2]: ((properPartOf(Y2,R) & quaIndividual(Z2) &
        existentiallyDependsOn(Y2,Z2) & existentiallyDependsOn(Z2,Y2) &
         (![P2]: (foundedBy(Y2,P2) <=> foundedBy(Z2,P2)))) => (
        properPartOf(Z2,R))))
1111
     )))
1112 )).
1113
   \% Ax |= "th_relatorsImplyTheExistenceOfAtLeastTwoQuaIndividuals_t32
        "; conjecture commented for convenience
1116 % fof(th_relatorsImplyTheExistenceOfAtLeastTwoQuaIndividuals_t32,
        conjecture, (
        ![R]: (relator(R) => (?[Q1,X,Q2,Y]: (quaIndividualOf(Q1,X) &
        quaIndividualOf(Q2,Y) & ~(Q1=Q2))))
1118 % )).
1119
fof(ax_dMediates_a82, axiom, (
      ![R,E]: (mediates(R,E) \iff (relator(R) \& endurant(E) \& (?[Q]: (
        quaIndividualOf(Q,E) & partOf(Q,R)))))
1122 )).
```

```
1123
1124 % Ax |= "th_relatorsMediateAtLeastTwoThings_t33"; conjecture
      commented for convenience
\% fof(th_relatorsMediateAtLeastTwoThings_t33, conjecture, (
      ![R]: (relator(R) => (?[E1,E2]: (~(E1=E2) & mediates(R,E1) &
      mediates(R,E2))))
1128 % )).
1129
1130 % TODO: add definition (d9) for the "relator bearer" axiom
1131
1132 % TODO: add instances
1133
1135
1136 fof(ax_endurantTypeCharacterizationByMomentTypes_a83, axiom, (
![ET,MT]: (characterizes(MT,ET) => (
```

2.1.15 Characterization

```
1139
       & momentType(M)
       & (![E,W]: (iof(E,ET,W) => (?[M]: (iof(M,MT,W) & inheresIn(M,E)
1140
       ))))
       & (![M2,W2]: (iof(M2,MT,W2) => (?[E2]: (iof(E2,ET,W2) &
1141
       inheresIn(M2,E2)))))
     ))
1142
1143 )).
1144
1145 % Ax |= "
        th\_qualities Inheres In \verb|AUniqueEndurantConnectThroughCharacteization\_a84|
       "; conjecture commented for convenience
1146
1147 % fof(
       \verb|th_qualitiesInheresInAU| niqueEndurantConnectThroughCharacteization_a84| \\
        ![QT,ET]: ((characterizes(QT,ET) & qualityType(QT)) => (![Q,W]:
1148 %
         (iof(Q,QT,W) \Rightarrow (?[E]: (iof(E,ET,W) & inheresIn(Q,E) & (![E2]:
         (inheresIn(Q,E2) <=> (E=E2)))))))))
1149 % )).
1150
1151 % TODO: add instances
1154
^{1155} % Skipping (a85); previously introduced in the taxonomy
1156 % Skipping (a86); previously introduced in the taxonomy
```

2.1.16 Qualities and Quality Structures

2.1.17 Endurants and Perdurants