

Modified Causal Forest: Optimal Policy Estimation

Section 1: General information

Welcome to the mcf estimation and optimal policy package.

This report provides you with a summary of specifications and results. More detailed information can be found in the respective output files. Figures and data (in csv-format, partly to recreate the figures on your own) are provided in the output path as well.

Output information for OPTIMAL POLICY ANALYSIS

Path for all outputs:

Q:\SEW\Projekte\MLechner\Projekte und Angebote\Unicef\Kasachstan\Workshops\Astana\Wednesday_examples/example/outputOPTBPS_C LASSIF

Detailed text output:

Q:\SEW\Projekte\MLechner\Projekte und Angebote\Unicef\Kasachstan\Workshops\Astana\Wednesday_examples/example/outputOPTBPS_C LASSIF/OptPolicy.0.6.0.txt

Summary text output:

Q:\SEW\Projekte\MLechner\Projekte und Angebote\Unicef\Kasachstan\Workshops\Astana\Wednesday_examples/example/outputOPTBPS_C LASSIF/OptPolicy.0.6.0_Summary.txt

BACKGROUND

The optimal policy module offers three (basic) algorithms that can be used to exploit fine grained knowledge about effect heterogeneity to obtain decision rules. The current version is implemented for discrete treatments only.

The BEST_POLICY_SCORE algorithm is based on assigning the treatment that has the highest impact at the unit (e.g., individual) level. If the treatment heterogeneity is known (not estimated), this will lead to the best possible result. This algorithm is computationally not burdensome. However, it will not be easy to understand how the implied rules depends on the features of the unit. Its statistical properties are also not clear (for estimated treatment heterogeneity) and there is a certain danger of overfitting, which could lead to an unsatisfactory out-of-training-sample performance.

The BPS_CLASSIFIER classifier algorithm runs a classifier for each of the allocations obtained by the BEST_POLICY_SCORE algorithm. One advantage of this approach compared to the BEST_POLICY_SCORE algorithm is that prediction of the allocation of (new) observations is fast because it does not require to recompute the policy score (as it is the case with the BEST_POLICY_SCORE algorithm). The specific classifier is selected among four different classifiers from scikit-learn, namely a simple neural network, two classification random forests with minimum leaf size of 2 and 5, and ADDABOOST. The selection is made according to the out-of-sample performance of the Accuracy Score of scikit-learn.

The POLICY TREE algorithm builds optimal shallow decision trees. While these trees are unlikely to lead to globally optimal allocations, and are computationally much more expensive, they have the advantage that the decision rule is much easier to understand and that some statistical properties are known, at least for certain versions of such decision trees (e.g. Zhou, Athey, Wager, 2023). The basic algorithmic implementation follows the recursive algorithm suggested by Zhou, Athey, Wager

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(2023) with three (more substantial) deviations (=extensions).

Extension 1: Since using One Hot Encoding for categorical variables may lead to rather extreme leaves for such variables with many different values when building (shallow) trees (splitting one value against the rest), a more sophisticated procedure is used that allows to have with several values of the categorical variables on both sides of the split.

Extension 2: Constraints are allowed for. They are handled in a sequential manner: First, an approximate treatment-specific cost vector is obtained and used to adjust the policy score accordingly. Second, trees that violate the constraints are removed (to some extent, optional).

Extensions 3: There are a several options implemented to reduce the computational burden, which are discussed below in the section showing the implementation of the policy score.

References

-Zhou, Z., S. Athey, S. Wager (2023): Offline Multi-Action Policy Learning: Generalization and Optimization, Operations Research, INFORMS, 71(1), 148-183.

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Section 2: Optimal Policy

METHOD

The assignment rule is based on allocating units using a classifier (for all allocations considered by the `best_policy_score` algorithm).

VARIABLES provided

Policy scores: `y_pot0`, `y_pot1`, `y_pot2`

IATEs relative to first treatment state: `iate1vs0`, `iate2vs0`

Treatment dependent variables for descriptive analysis: `zero`, `ite1vs0`, `ite2vs0`, `x_cont0`, `iate1vs0`, `iate2vs0`

Variables determining prioritisation of units in case of binding constraints for the `best_policy_score` method: `x_unord0`

Treatment: `treat`

Identifier: `id`

Ordered features of units: `x_cont0`, `x_cont1`, `x_cont2`, `x_ord0`, `x_ord1`, `x_ord2`

Categorical / unordered features of units: `x_unord0`, `x_unord1`, `x_unord2`

Features used for variable importance statistics without transformations: `x_cont0`, `x_cont1`, `x_cont2`

Features that are transformed to indicator/dummy variables for variable importance computations (only): `x_unord0`

COSTS

No user provided costs of specific treatments.

RESTRICTIONS of treatment shares

The following restrictions on the treatment shares are specified 100%, 100%, 30.0%.

Section 2.1: Optimal Policy: Training

COMPUTATION

6 logical cores are used for processing.

DATA PREPARATION

Variables without variation are removed.

Variables that are perfectly correlated with other variables are removed.

Dummy variables with less than 10 observations in the smaller group are removed.

Rows with any missing values for variables needed for training are removed.

RESTRICTIONS on treatment shares

Restrictions are ignored if they are not binding.

If they are binding, then several methods are used to enforce them (almost) exactly:

- 1) Prioritize units that benefit most.
- 2) Deny a random selection of units their best option.
- 3) Prioritize units with higher values of `x_unord0`.

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Section 2.2: Optimal Policy: Evaluation of Allocation(s)

Main evaluation results.

Note: The output files contain relevant additional information, like a descriptive analysis of the treatment groups and variable importance statistics.

Evaluation of treatment allocation

Allocation	Value function	Share of 0 in %	Share of 1 in %	Share of 2 in %
All classif_bb	1.6512	18.6	41.1	40.3
All classif_bb_restrict_random	0.6164	23.8	75.2	1.0
All classif_bb_restrict_largest_gain	1.0806	19.6	57.9	22.5
All classif_bb_restrict_largest_gain_random_order	1.0610	13.0	80.0	7.0
All observed	0.5182	33.3	33.4	33.3
All random	0.6532	30.2	34.0	35.8
Switchers classif_bb	1.6853	19.18	40.26	40.56
Switchers classif_bb_restrict_random	0.6264	22.17	76.76	1.07
Switchers classif_bb_restrict_largest_gain	1.0510	20.49	54.8	24.71
Switchers classif_bb_restrict_largest_gain_random_order	1.0356	14.37	79.43	6.2
Switchers random	0.68	30.38	33.38	36.24

Note: Allocation analysed is the SAME as the one obtained from the training data.

Evaluation of treatment allocation

Allocation	Value function	Share of 0 in %	Share of 1 in %	Share of 2 in %
All classif_bb	0.9238	14.4	42.6	43.0
All classif_bb_restrict_random	0.6002	22.8	75.7	1.5
All classif_bb_restrict_largest_gain	0.9439	18.5	58.7	22.8
All classif_bb_restrict_largest_gain_random_order	0.9710	13.0	79.7	7.3
All observed	0.4973	33.3	33.4	33.3
All random	0.6461	30.2	34.0	35.8
Switchers classif_bb	0.9573	16.98	39.91	43.11
Switchers classif_bb_restrict_random	0.5961	21.05	77.55	1.39
Switchers classif_bb_restrict_largest_gain	0.9910	20.4	54.6	25.0
Switchers classif_bb_restrict_largest_gain_random_order	0.9755	15.32	77.17	7.51
Switchers random	0.7073	29.33	35.05	35.62

Note: Allocation analysed is DIFFERENT from the one obtained from the training data.