

Quantum Computation

(In Brief)

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Exploiting Quantum Weirdness



“I think I can safely say that nobody understands quantum mechanics...”

Exploiting Quantum Weirdness

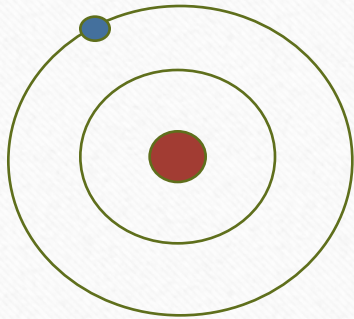


“I think I can safely say that nobody understands quantum mechanics...”

...BUT I know more about quantum mechanics than the generals do, believe me.”

Key Ideas About Quantum Physics

- Certain properties can take on discrete values. Examples:



Energy Levels
in atom:
{ground state,
1st excited
state,...}



Component of spin about any
given axis: $\{+1, -1\}$ for electrons

- State of a particle described by a vector of length one: $|E_0\rangle$, $|0\rangle$, $|1\rangle$

Important Idea for Quantum Computers

- Superposition: Particle can be in any linear combination of states between measurements.

$$\text{State} = a * \text{[blue circle with down arrow]} + b * \text{[blue circle with up arrow]}$$

State = $a|0\rangle + b|1\rangle$, where the $|a|^2 + |b|^2 = 1$ (unit vector)

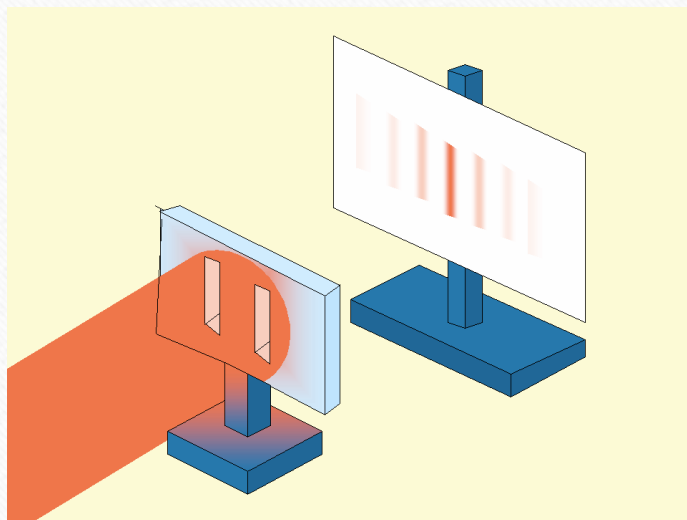
When a spin measurement is performed, State “collapses” to either $|0\rangle$ with probability $|a|^2$ or $|1\rangle$ with probability $|b|^2$.

Classical Computers vs Quantum Computers

- Unit of information: “bit”.....0 or 1.....high voltage or low voltage.....etc.
Physical implementation: 2-state system in either one state or another.
- Classical computers/Logic gates process bits. Bits in, bits out.
- **Quantum computers** process bits in SUPERPOSITION. These are “quantum bits”, or qubits. Picture: electron “spin up” + “spin down”:
Qubit state = $a|0\rangle + b|1\rangle$
- a and b are complex numbers (eg., $3 - 2i$, $5i$, -145 , 11) called “amplitudes”.
- Multiple qubits = multiple two-state quantum systems:
 - $|01\rangle$, or $|10\rangle$. In general: $|00\rangle + |01\rangle + |10\rangle + |11\rangle$ (superposition properly normalized)

Interference is a Good Thing!

- In quantum mechanics, states can interfere with each other, cancelling in some places, and reinforcing in others (double-slit experiment with light)



What if we had a device that took every possible answer to a problem, made them interfere so that only the correct answer got reinforced?

That's what Quantum Computers are for!

General Process

Step 1: Input quantum state. Example, $|00\rangle$. This represents a system of two particles: one spin down, the other also spin down.

Step 2: Apply a “quantum gate” turning the initial state into an equal combination of all the possible states: $\frac{1}{2}|00\rangle + \frac{1}{2}|01\rangle + \frac{1}{2}|10\rangle + \frac{1}{2}|11\rangle$

Step 3: Repeatedly apply another transformation on this new state so that the amplitude for the right answer grows with each application of the transformation.

Step 4: Perform a measurement on the system. You will observe the correct answer with high probability.

Grover's Search Algorithm

- Unordered list of N items. Want to match a search query.
- Classical computers can match with $O(N)$ at best.
- Quantum computers can do this with $O(\sqrt{N})$
- Suppose $N = 2^n$. We can write the i^{th} index of the list in binary. We can represent each index as a physical n qubit system.

Example: 8 entries in the list \rightarrow The list indices are can be written as:

$|000\rangle, |001\rangle, |010\rangle, |011\rangle, |100\rangle, |101\rangle, |110\rangle, |111\rangle$. Think of each as 3 electrons, each of which can be spin down (0) or spin up (1).

By putting these in a uniform superposition, applying certain transformations, then measuring the system, we can arrive at the desired index with high enough probability. I.E. Suppose the desired index was 6. $6 = 110$. So result of measurement will be the 3-qubit state $|110\rangle$

Limitations

- System must be kept in a superposition for as long as the transformations need to work their interference MAGIC.
- Interactions between the qubits and the outside world will destroy the superposition!
- Quantum computers beat classical computers hands down only for certain tasks (eg., searching – Grover's algorithm; factoring – Shor's algorithm)
- Other tasks don't run any faster on a QC than on a CC (eg, our routine use)
- Just protecting the quantum nature of the systems you use as qubits will likely make the QC's slower than CC's for a long, long time.
- NSA likely has nothing to worry about.

National Security

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By **Steven Rich** and **Barton Gellman** January 2, 2014 

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Nice blog post about Shor's algorithm for factoring large numbers and quantum computing:

<http://www.scottaaronson.com/blog/?p=208>

Scott Aaronson: Quantum Computing researcher at UT Austin – very cool blog if you're interested

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David L. Chandler | MIT News Office
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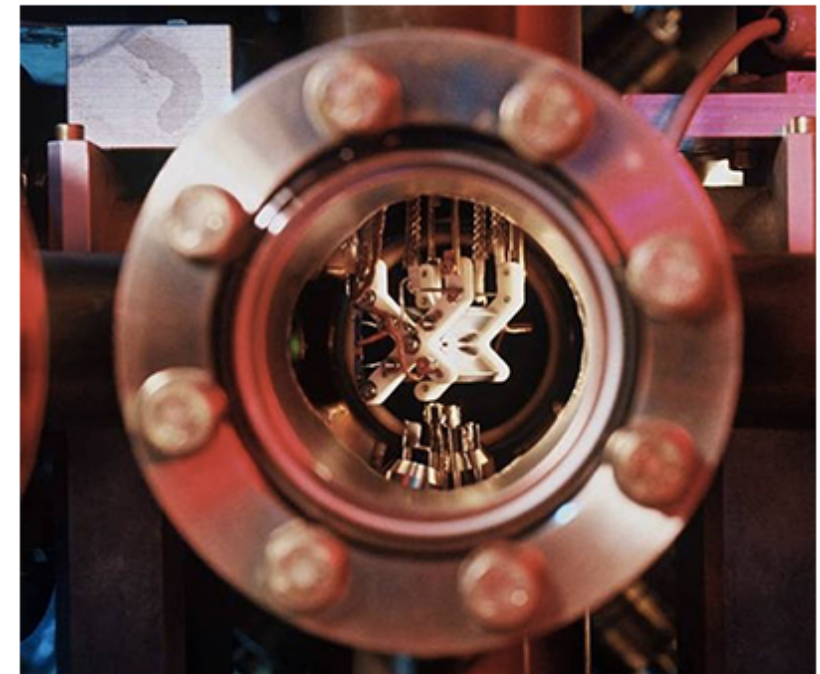
Programming Your Quantum Computer

The hardware doesn't yet exist, but languages for quantum coding are ready to go.

Brian Hayes

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