

team-friday-assignment

April 3, 2024

```
[ ]: import pandas as pd
from numpy.linalg import solve
import numpy as np

df = pd.read_csv('/content/current.csv')
```

```
[ ]: ##cleaning the dataset
df_cleaned = df.drop(index=0)
df_cleaned.reset_index(drop=True, inplace=True)
df_cleaned['sasdate'] = pd.to_datetime(df_cleaned['sasdate'], format='%m/%d/%Y')
df_cleaned
```

```
[ ]:      sasdate      RPI  W875RX1  DPCERA3M086SBEA      CMRMTSPLx  \
0   1959-01-01  2583.560   2426.0          15.188  2.766768e+05
1   1959-02-01  2593.596   2434.8          15.346  2.787140e+05
2   1959-03-01  2610.396   2452.7          15.491  2.777753e+05
3   1959-04-01  2627.446   2470.0          15.435  2.833627e+05
4   1959-05-01  2642.720   2486.4          15.622  2.853072e+05
..      ...      ...      ...      ...      ...
776 2023-09-01  19111.748  15741.9          116.594  1.507530e+06
777 2023-10-01  19145.402  15784.6          116.663  1.505477e+06
778 2023-11-01  19213.108  15859.9          117.127  1.514733e+06
779 2023-12-01  19251.946  15899.0          117.773  1.530296e+06
780 2024-01-01  19377.558  15948.8          117.639         NaN
```

```
      RETAILx      INDPRO      IPFPNSS      IPFINAL      IPCONGD  ...  \
0   18235.77392   21.9665   23.3891   22.2688   31.7011   ...
1   18369.56308   22.3966   23.7048   22.4617   31.9337   ...
2   18523.05762   22.7193   23.8483   22.5719   31.9337   ...
3   18534.46600   23.2032   24.1927   22.9026   32.4374   ...
4   18679.66354   23.5528   24.3936   23.1231   32.5925   ...
..      ...      ...      ...      ...      ...
776 705304.00000  103.2096  101.0935  101.3665  102.1034   ...
777 703528.00000  102.3722  100.5292  100.5527  101.1664   ...
778 703336.00000  102.6710  100.9362  101.2159  101.8557   ...
779 706180.00000  102.6715  100.8332  101.2843  101.9884   ...
780 700291.00000  102.5739  100.9984  101.7258  102.6235   ...
```

	DNDGRG3M086SBEA	DSERRG3M086SBEA	CES06000000008	CES20000000008	\
0	18.294	10.152	2.13	2.45	
1	18.302	10.167	2.14	2.46	
2	18.289	10.185	2.15	2.45	
3	18.300	10.221	2.16	2.47	
4	18.280	10.238	2.17	2.48	
..	
776	120.395	123.976	29.90	34.55	
777	120.040	124.228	29.97	34.67	
778	119.325	124.551	30.26	34.96	
779	119.193	124.917	30.45	35.01	
780	118.745	125.662	30.56	35.21	

	CES30000000008	UMCSENTx	DTCOLNVHFM	DTCTHFM	INVEST	VIXCLSx
0	2.04	NaN	6476.00	12298.00	84.2043	NaN
1	2.05	NaN	6476.00	12298.00	83.5280	NaN
2	2.07	NaN	6508.00	12349.00	81.6405	NaN
3	2.08	NaN	6620.00	12484.00	81.8099	NaN
4	2.08	95.3	6753.00	12646.00	80.7315	NaN
..
776	26.62	67.9	508808.61	913938.95	5074.6108	15.0424
777	26.65	63.8	513229.64	918210.64	5015.5456	19.0462
778	26.89	61.3	517434.30	922552.40	4999.7208	13.8563
779	27.14	69.7	522366.13	928336.14	5077.4222	12.6960
780	27.22	NaN	NaN	NaN	5105.3504	13.3453

[781 rows x 128 columns]

```
[ ]: ##extract transformation code
transformation_codes = df.iloc[0, 1:].to_frame().reset_index()
transformation_codes.columns = ['Series', 'Transformation_Code']

# Function to apply transformations based on the transformation code
def apply_transformation(series, code):
    if code == 1:
        # No transformation
        return series
    elif code == 2:
        # First difference
        return series.diff()
    elif code == 3:
        # Second difference
        return series.diff().diff()
    elif code == 4:
        # Log
        return np.log(series)
```

```

elif code == 5:
    # First difference of log
    return np.log(series).diff()
elif code == 6:
    # Second difference of log
    return np.log(series).diff().diff()
elif code == 7:
    # Delta ( $x_t/x_{t-1} - 1$ )
    return series.pct_change()
else:
    raise ValueError("Invalid transformation code")

for series_name, code in transformation_codes.values:
    df_cleaned[series_name] = apply_transformation(df_cleaned[series_name].
    ↪astype(float), float(code))

df_cleaned = df_cleaned[2:]
df_cleaned.reset_index(drop=True, inplace=True)
df_cleaned.head()

```

```

[ ]:
    sasdate      RPI    W875RX1  DPCERA3M086SBEA  CMRMTSPLx  RETAILx  \
0 1959-03-01  0.006457  0.007325          0.009404 -0.003374  0.008321
1 1959-04-01  0.006510  0.007029          -0.003622  0.019915  0.000616
2 1959-05-01  0.005796  0.006618          0.012043  0.006839  0.007803
3 1959-06-01  0.003068  0.003012          0.003642 -0.000097  0.009064
4 1959-07-01 -0.000580 -0.000762          -0.003386  0.012155 -0.000330

    INDPRO  IPFPNSS  IPFINAL  IPCONGD  ...  DNDGRG3M086SBEA  \
0  0.014306  0.006035  0.004894  0.000000  ...          -0.001148
1  0.021075  0.014338  0.014545  0.015650  ...           0.001312
2  0.014955  0.008270  0.009582  0.004770  ...          -0.001695
3  0.001141  0.007034  0.007128 -0.004767  ...           0.003334
4 -0.024240  0.001168  0.008249  0.013054  ...          -0.001204

    DSERRG3M086SBEA  CES0600000008  CES2000000008  CES3000000008  UMCSENTx  \
0          0.000292          -0.000022          -0.008147           0.004819      NaN
1          0.001760          -0.000022           0.012203          -0.004890      NaN
2          -0.001867          -0.000021          -0.004090          -0.004819      NaN
3          0.001946          -0.004619           0.003992           0.004796      NaN
4          -0.000013           0.000000          -0.004040          -0.004796      NaN

    DTCOLNVHFNM  DTCTHFNM  INVEST  VIXCLSx
0          0.004929  0.004138 -0.014792      NaN
1          0.012134  0.006734  0.024929      NaN
2          0.002828  0.002020 -0.015342      NaN

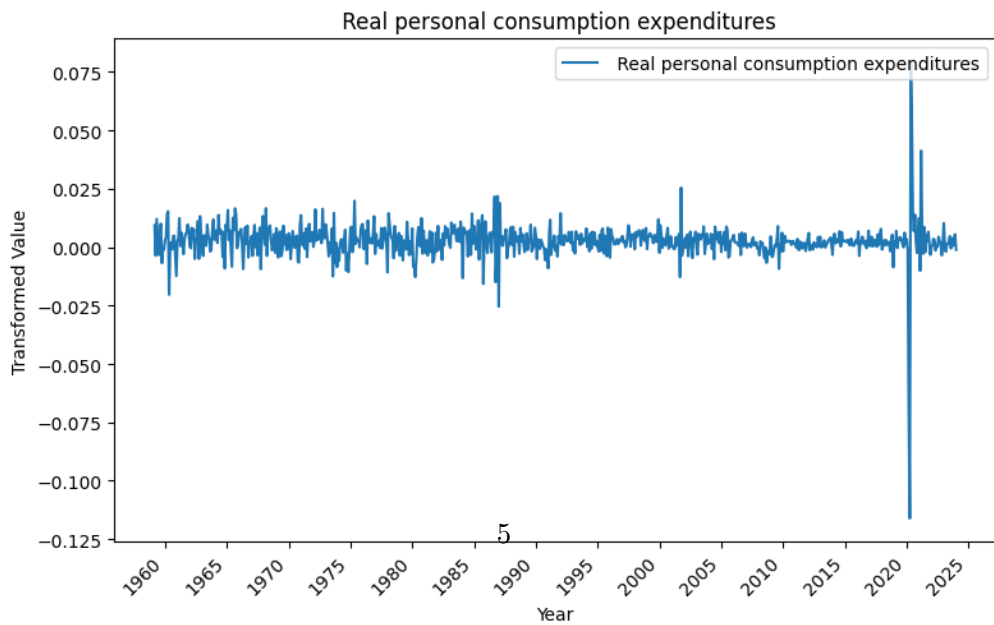
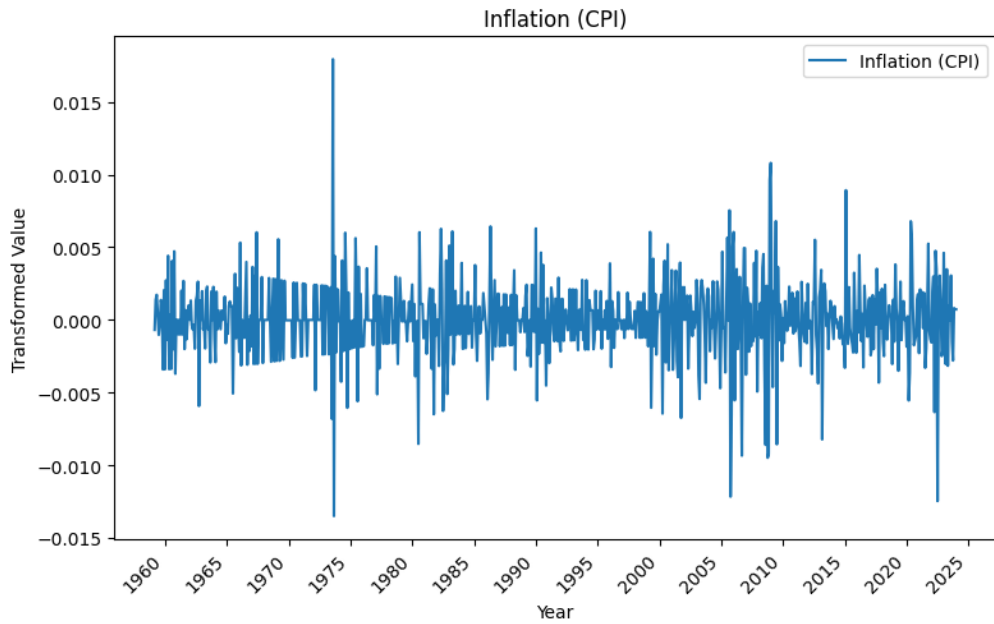
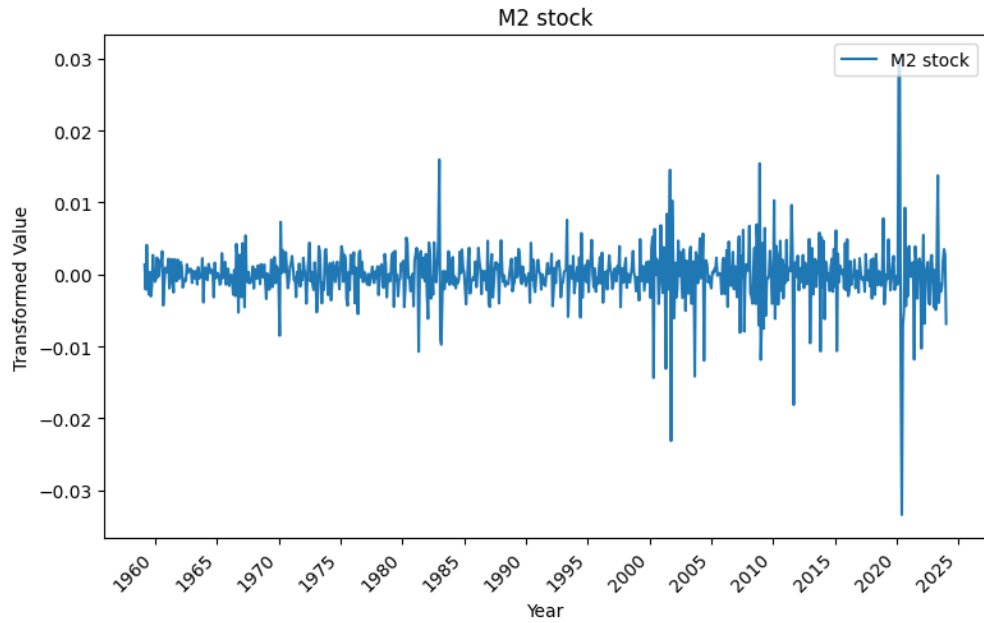
```

3	0.009726	0.009007	-0.012252	NaN
4	-0.004631	-0.001000	0.029341	NaN

[5 rows x 128 columns]

```
[ ]: #plot
import matplotlib.pyplot as plt
import matplotlib.dates as mdates
series_to_plot = ['M2SL', 'CPIAUCSL', 'DPCERA3M086SBEA']
series_names = ['M2 stock',
                 'Inflation (CPI)',
                 'Real personal consumption expenditures']
fig, axs = plt.subplots(len(series_to_plot), 1, figsize=(8, 15))
for ax, series_name, plot_title in zip(axs, series_to_plot, series_names):
    if series_name in df_cleaned.columns:
        dates = pd.to_datetime(df_cleaned['sasdate'], format='%m/%d/%Y')
        ax.plot(dates, df_cleaned[series_name], label=plot_title)
        ax.xaxis.set_major_locator(mdates.YearLocator(base=5))
        ax.xaxis.set_major_formatter(mdates.DateFormatter('%Y'))
        ax.set_title(plot_title)
        ax.set_xlabel('Year')
        ax.set_ylabel('Transformed Value')
        ax.legend(loc='upper right')
        plt.setp(ax.xaxis.get_majorticklabels(), rotation=45, ha='right')
    else:
        ax.set_visible(False) # Hide plots for which the data is not available

plt.tight_layout()
plt.show()
```



```
[ ]: #matrix X and vector Y
Yraw = df_cleaned['CPIAUCSL']
Xraw = df_cleaned[['M2SL', 'DNDGRG3M086SBEA']]
num_lags = 8
num_leads = 4
X = pd.DataFrame()
col = 'CPIAUCSL'
for lag in range (0, num_lags+1):
    X[f'{col}_lag{lag}'] = Yraw.shift(lag)
for col in Xraw.columns:
    for lag in range (0, num_lags+1):
        X[f'{col}_lag{lag}'] = Xraw[col].shift(lag)
X.insert(0, 'Ones', np.ones(len(X)))
X
```

```
[ ]:
```

	Ones	CPIAUCSL_lag0	CPIAUCSL_lag1	CPIAUCSL_lag2	CPIAUCSL_lag3	\
0	1.0	-0.000690	NaN	NaN	NaN	
1	1.0	0.001380	-0.000690	NaN	NaN	
2	1.0	0.001723	0.001380	-0.000690	NaN	
3	1.0	0.000339	0.001723	0.001380	-0.000690	
4	1.0	-0.001034	0.000339	0.001723	0.001380	
..	
774	1.0	-0.001515	0.003051	-0.000047	0.001003	
775	1.0	-0.002799	-0.001515	0.003051	-0.000047	
776	1.0	0.000811	-0.002799	-0.001515	0.003051	
777	1.0	0.000726	0.000811	-0.002799	-0.001515	
778	1.0	0.000721	0.000726	0.000811	-0.002799	

	CPIAUCSL_lag4	CPIAUCSL_lag5	CPIAUCSL_lag6	CPIAUCSL_lag7	\
0	NaN	NaN	NaN	NaN	
1	NaN	NaN	NaN	NaN	
2	NaN	NaN	NaN	NaN	
3	NaN	NaN	NaN	NaN	
4	-0.000690	NaN	NaN	NaN	
..	
774	-0.003161	0.003480	-0.003052	-0.001322	
775	0.001003	-0.003161	0.003480	-0.003052	
776	-0.000047	0.001003	-0.003161	0.003480	
777	0.003051	-0.000047	0.001003	-0.003161	
778	-0.001515	0.003051	-0.000047	0.001003	

	CPIAUCSL_lag8	...	M2SL_lag8	DNDGRG3M086SBEA_lag0	\
0	NaN	...	NaN	-0.001148	
1	NaN	...	NaN	0.001312	
2	NaN	...	NaN	-0.001695	

3	NaN	...	NaN	0.003334
4	NaN	...	NaN	-0.001204
..
774	0.004605	...	-0.004497	-0.010725
775	-0.001322	...	0.000641	-0.006139
776	-0.003052	...	-0.004907	-0.003021
777	0.003480	...	0.002439	0.004867
778	-0.003161	...	0.013769	-0.002659

	DNDGRG3M086SBEA_lag1	DNDGRG3M086SBEA_lag2	DNDGRG3M086SBEA_lag3	\
0	NaN	NaN	NaN	
1	-0.001148	NaN	NaN	
2	0.001312	-0.001148	NaN	
3	-0.001695	0.001312	-0.001148	
4	0.003334	-0.001695	0.001312	
..	
774	0.014038	-0.000887	0.004187	
775	-0.010725	0.014038	-0.000887	
776	-0.006139	-0.010725	0.014038	
777	-0.003021	-0.006139	-0.010725	
778	0.004867	-0.003021	-0.006139	

	DNDGRG3M086SBEA_lag4	DNDGRG3M086SBEA_lag5	DNDGRG3M086SBEA_lag6	\
0	NaN	NaN	NaN	
1	NaN	NaN	NaN	
2	NaN	NaN	NaN	
3	NaN	NaN	NaN	
4	-0.001148	NaN	NaN	
..	
774	-0.007022	0.006627	-0.006705	
775	0.004187	-0.007022	0.006627	
776	-0.000887	0.004187	-0.007022	
777	0.014038	-0.000887	0.004187	
778	-0.010725	0.014038	-0.000887	

	DNDGRG3M086SBEA_lag7	DNDGRG3M086SBEA_lag8
0	NaN	NaN
1	NaN	NaN
2	NaN	NaN
3	NaN	NaN
4	NaN	NaN
..
774	-0.003289	0.013510
775	-0.006705	-0.003289
776	0.006627	-0.006705
777	-0.007022	0.006627
778	0.004187	-0.007022

[779 rows x 28 columns]

```
[ ]: y = Yraw.shift(-num_leads)
      y
```

```
[ ]: 0      -0.001034
      1      -0.000345
      2       0.001367
      3       0.001017
      4     -0.003413
      ...
      774     0.000721
      775          NaN
      776          NaN
      777          NaN
      778          NaN
      Name: CPIAUCSL, Length: 779, dtype: float64
```

```
[ ]: X_T = X.iloc[-1:].values
      X_T
```

```
[ ]: array([[ 1.00000000e+00,  7.21400503e-04,  7.26467817e-04,
              8.11330254e-04, -2.79891559e-03, -1.51527417e-03,
              3.05087605e-03, -4.70784880e-05,  1.00257828e-03,
              -3.16114422e-03, -6.86011934e-03,  2.77062956e-03,
              3.51058387e-03,  1.99477265e-03, -1.51356295e-03,
              -2.37724874e-03, -1.26831670e-03, -3.92912202e-03,
              1.37692721e-02, -2.65885649e-03,  4.86732286e-03,
              -3.02117448e-03, -6.13924919e-03, -1.07253383e-02,
              1.40383347e-02, -8.87353808e-04,  4.18730761e-03,
              -7.02247442e-03]])
```

```
[ ]: y = y.iloc[num_lags:-num_leads]
      X = X.iloc[num_lags:-num_leads]
      y
```

```
[ ]: 8      -0.001361
      9       0.004411
     10     -0.003395
     11       0.000337
     12     -0.003380
      ...
     770     -0.001515
     771     -0.002799
     772       0.000811
     773       0.000726
```



```
774      0.000721
Name: CPIAUCSL, Length: 767, dtype: float64
```

```
[ ]: from numpy.linalg import solve
beta_ols = solve(X.T @ X, X.T @ y)
forecast = X_T@beta_ols*100
forecast
```

```
[ ]: array([0.01295211])
```

```
[ ]: #real test
def calculate_forecast(df_cleaned,
                        p = 4,
                        H = [1,4,8],
                        end_date = '12/01/1999',
                        target = 'CPIAUCSL',
                        xvars = ['M2SL', 'DNDGRG3M086SBEA']):
    rt_df = df_cleaned[df_cleaned['sasdate'] <= pd.Timestamp(end_date)]
    Y_actual = []
    for h in H:
        os = pd.Timestamp(end_date) + pd.DateOffset(months=h)
        Y_actual.append(df_cleaned[df_cleaned['sasdate'] == os][target]*100)
    Yraw = rt_df[target]
    Xraw = rt_df[xvars]
    X = pd.DataFrame()
    for lag in range(0,p):
        X[f'{target}_lag{lag}'] = Yraw.shift(lag)
    for col in Xraw.columns:
        for lag in range(0,p):
            X[f'{col}_lag{lag}'] = Xraw[col].shift(lag)
    X.insert(0, 'Ones', np.ones(len(X)))
    X_T = X.iloc[-1:].values
    Yhat = []
    for h in H:
        y_h = Yraw.shift(-h)
        y = y_h.iloc[p:-h].values
        X_ = X.iloc[p:-h].values
        beta_ols = solve(X_.T @ X_, X_.T @ y)
        Yhat.append(X_T@beta_ols*100)
    return np.array(Y_actual) - np.array(Yhat)
```

```
[ ]: t0 = pd.Timestamp('12/1/1999')
e = []
T = []
for j in range(0, 10):
    t0 = t0 + pd.DateOffset(months=1)
    print(f'Using data up to {t0}')
```

```
ehat = calculate_forecast(df_cleaned, p = 4, H = [1,4,8], end_date = t0)
e.append(ehat.flatten())
T.append(t0)
```

```
Using data up to 2000-01-01 00:00:00
Using data up to 2000-02-01 00:00:00
Using data up to 2000-03-01 00:00:00
Using data up to 2000-04-01 00:00:00
Using data up to 2000-05-01 00:00:00
Using data up to 2000-06-01 00:00:00
Using data up to 2000-07-01 00:00:00
Using data up to 2000-08-01 00:00:00
Using data up to 2000-09-01 00:00:00
Using data up to 2000-10-01 00:00:00
```

```
[ ]: edf = pd.DataFrame(e)
      np.sqrt(edf.apply(np.square).mean())
```

```
[ ]: 0    0.282944
      1    0.318535
      2    0.301497
      dtype: float64
```