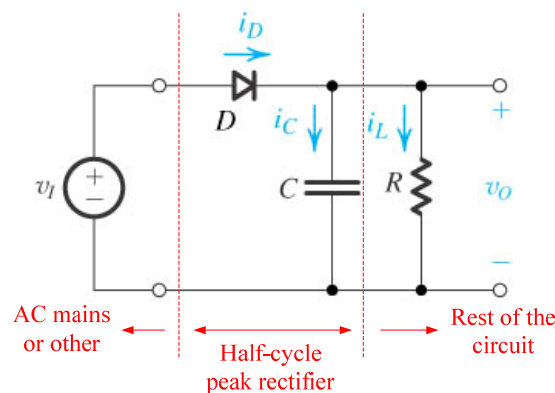


## Lecture 8: Peak Rectifiers.

The output of the rectifier circuits discussed in the last lecture is pulsating significantly with time. Hence, it's not useful as the output from a DC power supply.

One way to reduce this ripple is to use a **filtering capacitor**.

Consider the half-cycle rectifier again, but now add a capacitor in parallel with the load:

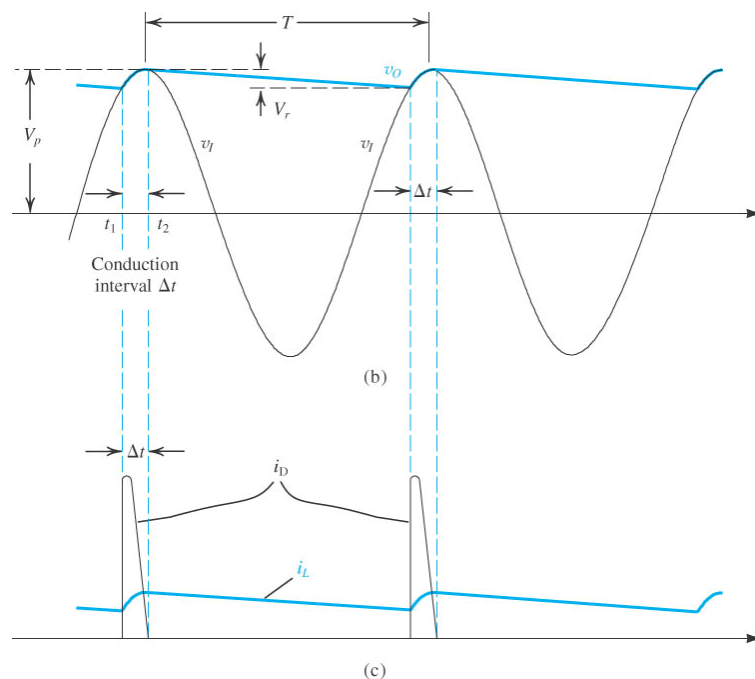


(Fig. 3.29a)

We expect that as soon as we turn on the source, the capacitor will **charge up** on “+” cycles of  $v_I$  and discharge on the “-” cycles.

To **smooth out** the voltage, we need this discharge to occur slowly in time. This means we need to choose  $C$  large enough to make this happen, presuming that  $R$  is a given quantity (the Thévenin resistance of the rest of the circuit).

The output voltage  $v_o$  will then be a smoothed-out signal that pulsates with time:

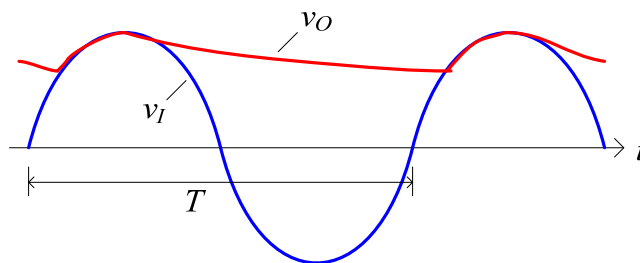


(Fig. 3.29)

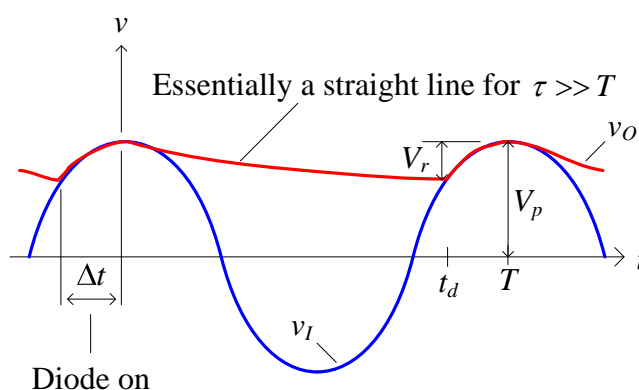
Notice the diode current and the capacitor voltage. They display behavior much different than what one would find in an AC circuit.

## Analysis of Peak Rectifier Circuits

We'll require that  $\tau = RC \gg T$ , which means that the time constant of the RC circuit must be **much greater** than the period of the input sinusoidal signal:



Now, our quest is to approximately **determine the ripple voltage  $V_r$** , assuming  $\tau \gg T$ :



Not sketched to scale.

When  $D$  is off, and assuming it is an ideal diode

$$v_o(t) = V_p e^{-t/\tau} \quad (1)$$

[If  $D$  is not ideal then  $v_o(t) \approx (V_p - 0.7)e^{-t/\tau}$ .]

At the end of the **discharge time**,  $t_d$ , the output voltage equals

$$v_o(t_d) = V_p - V_r \quad (2)$$

Substituting for  $v_o$  from (1) at this time  $t_d$  leads to

$$V_p e^{-t_d/\tau} = V_p - V_r \quad \text{or} \quad \frac{V_r}{V_p} = (1 - e^{-t_d/\tau}) \quad (3)$$

This equation has the two unknowns  $V_r$  and  $t_d$ , assuming  $\tau$  is known. If we can determine  $t_d$ , then we can find  $V_r$ . Finding  $t_d$  can be done numerically by equating (1) to the expression for the input voltage

$$v_I(t) = V_p \cos(\omega t) \quad (4)$$

and solving for the time  $t_d$  when the two are equal as

$$V_p \cos(\omega t_d) = V_p e^{-t_d/\tau} \quad \text{or} \quad \cos(\omega t_d) = e^{-t_d/\tau} \quad (5)$$

This needs to be **done numerically** since (5) is a “transcendental equation.”

Alternatively, if  $\Delta t$  is small compared to  $T$  (true when  $\tau \gg T$ , as assumed), then from (3)

$$\frac{V_r}{V_p} = 1 - e^{-(T-\Delta t)/\tau} \approx 1 - e^{-T/\tau} \quad (6)$$

Again, because  $\tau \gg T$  then we can truncate the series expansion of the exponential function to two terms (see Lecture 4) giving

$$\boxed{\frac{V_r}{V_p} \approx \frac{T}{\tau}} \quad (\tau \gg T) \quad (7)$$

This simple equation gives the ratio of the ripple voltage to the peak voltage of the input sinusoidal signal for the **half-cycle rectifier**. It's worth memorizing, or knowing how to derive.

Often  $R$  and  $T$  are fixed quantities. So from (7)

$$\boxed{V_r \approx V_p \frac{T}{RC}} \quad (\tau \gg T) \quad (3.28), (8)$$

to obtain a small ripple voltage we need a **large  $C$**  in this case.

## Conduction Interval

Lastly, the **conduction interval**  $\Delta t$  is defined as the time interval in which the diode is actually conducting current. This time period is sketched in the preceding two figures.

The diode conducts current beginning at time  $t_d$  and ending at  $T$ , within each period. Using equation (4) at time  $t_d$

$$V_p \cos[\omega(T - t_d)] = V_p - V_r \quad \text{or} \quad V_p \cos(\omega\Delta t) = V_p - V_r \quad (9)$$

We expect the conduction interval to be small. So truncating the series expansion of cosine to two terms, (9) gives

$$\omega\Delta t \approx \sqrt{\frac{2V_r}{V_p}} \quad (3.30), (10)$$

The factor  $\omega\Delta t$  is sometimes called the conduction angle,  $\theta$ . For  $V_r \ll V_p$  this conduction angle (and conduction interval) will be small, as expected.

## Discussion

To reiterate, the objective of the peak rectifier is to charge the shunt  $C$  when  $D$  is on, and **slowly discharge** it during those times when  $D$  is off.

When does  $D$  conduct? During the  $\Delta t$  periods in the previous figure. Also see Fig. 3.29(c).

Note that this peak rectifier is **not** a linear circuit.  $i_D$  is a very complicated waveform and not a sinusoid, as seen earlier in Fig. 3.29(c). There are no simple exact formulas for the solution to this problem. The text only shows approximate solutions for **peak  $i_D$** :

$$i_D|_{\max} \approx \frac{V_p}{R} \left( 1 + 2\pi \sqrt{\frac{2V_p}{V_r}} \right) \text{ [A]} \quad (V_r \ll V_p) \quad (3.32), (11)$$

**Example N8.1** (similar to text example 3.9). A **half-cycle peak rectifier** with  $R = 10 \text{ k}\Omega$  is fed by a 60-Hz sinusoidal voltage with a peak amplitude of 100 V.

(a) Determine  $C$  for a ripple voltage of  $2 \text{ V}_{pp}$ . From (8):

$$C = \frac{T}{R} \frac{V_p}{V_r} = \frac{1}{60 \cdot 10,000} \frac{100}{2}$$

or  **$C = 83.3 \text{ }\mu\text{F}$ .**

For a “factor of safety” of two, make  $C$  twice as large. Remember, a bigger  $C$  translates to smaller ripple.

(b) Determine the peak diode current. Using (11):

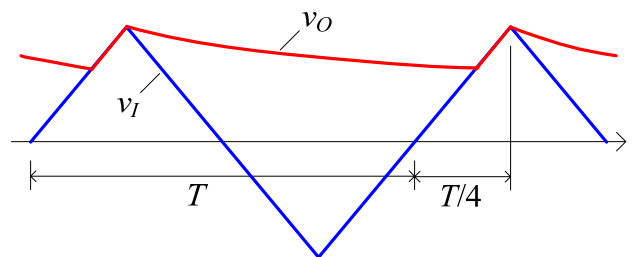
$$i_D|_{\max} \approx \frac{V_p}{R} \left( 1 + 2\pi \sqrt{\frac{2V_p}{V_r}} \right) = \frac{100}{10,000} \left( 1 + 2\pi \sqrt{\frac{2 \cdot 100}{2}} \right)$$

or

$$i_D|_{\max} \approx 638 \text{ mA.}$$

When specifying a diode for your circuit design, you would need to find one that could safely handle this amount of current.

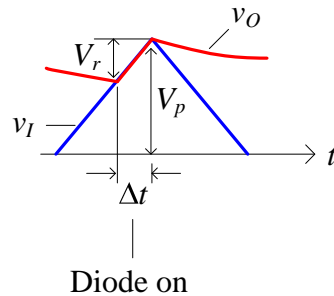
**Example N8.2.** A half-cycle peak rectifier with  $R = 10 \text{ k}\Omega$  is fed by a 60-Hz **triangular** voltage with a peak amplitude of 100 V.



- (a) Determine  $C$  for a ripple voltage of  $2 V_{pp}$ . If you go back and look at the derivation of (8) you'll find that there were no approximations made that **required a sinusoidal** waveform. Consequently, (8) applies to this triangular waveform as well, provided  $\tau \gg T$ . Hence, as before

$$C = 83.3 \text{ }\mu\text{F.}$$

- (b) Determine the diode conduction time,  $\Delta t$ . Referring to this sketch of the region near the positive peak voltage for  $v_I$ :



Because the rising portion of the waveform is a straight line:

$$v_I = \frac{\text{rise}}{\text{run}} t = \frac{V_p}{T/4} t$$

To find  $\Delta t$ , equate

$$\Delta v_I = \frac{4V_p}{T} \Delta t \quad \text{or} \quad V_r = \frac{4V_p}{T} \Delta t$$

Therefore, for a triangular waveform

$$\Delta t = \frac{T}{4} \frac{V_r}{V_p} \quad (12)$$

In this particular case,

$$\Delta t = \frac{1/60}{4} \frac{2}{100} = 83.3 \mu\text{s}$$

Compare this time to a sinusoidal waveform:

$$\Delta t = \frac{T}{2\pi} \sqrt{\frac{2V_r}{V_p}} = \frac{1/60}{2\pi} \sqrt{\frac{2 \cdot 2}{100}} = 530.5 \mu\text{s}$$

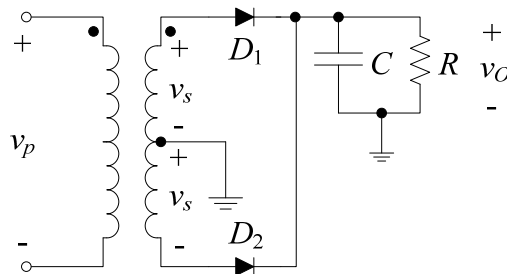
This time is **much longer** than for the triangular waveform. Consequently, we would expect  $i_D|_{\max}$  for  $D$  to be **much larger** for the triangular waveform than for the sinusoid!



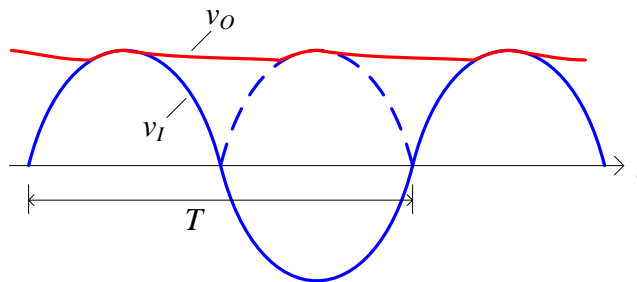
## Full-Cycle Peak Rectifiers

In a similar fashion, we can also add a shunt  $C$  to full cycle and bridge rectifiers to convert them to peak rectifiers.

For example, for a **full-cycle peak rectifier**:



The output voltage has less ripple than from a half-cycle peak rectifier (actually **one half** less ripple).



The “ripple frequency” is **twice** that of a half-cycle peak rectifier. Using the same derivation procedure as before with the half cycle, but with  $T \rightarrow T/2$  gives from (7)

$$\boxed{\frac{V_r}{V_p} \approx \frac{T}{2\tau}} \quad (\tau \gg T) \quad (3.33), (13)$$

Lastly, it can be shown that the  $i_D|_{\max}$  for the full-cycle peak rectifier:

$$i_D|_{\max} \approx \frac{V_p}{R} \left( 1 + 2\pi \sqrt{\frac{V_p}{2V_r}} \right) \quad [\text{A}] \quad (3.35), (14)$$

is **approximately one-half** that of the half-cycle peak rectifier when  $V_r \ll V_p$ .