

Information and Database Management Systems I

(CIS 4301 UF Online)

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Homework 4

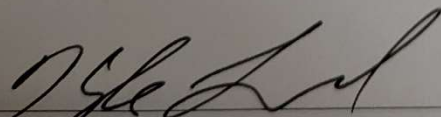
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Instructions: Please provide your answers to the questions of the following pages in Word or handwritten on separate sheets of paper. Mark clearly to which question each answer belongs. Then convert or scan your work into PDF (the latter by using either a scanner or a suitable scanner app on your smartphone). Note that *only the PDF format* is allowed and that your submission must be a *single PDF file*. Finally, upload your PDF file into *Gradescope* and follow the instructions there. In order to enable the graders to fast find the solutions to your questions, it is important that you correctly specify the location of your answer for each question in Gradescope, as it is described there. Otherwise, 0.25 points will be deducted for each answer.

Note: All homework assignments are designed for a period of two, three, or even four weeks (see course deadline sheet). This means they cannot be solved in two or three hours but require a considerable amount of time and effort. Therefore, the first recommendation is to start with them as soon as they are posted. The second recommendation is to distribute the work on a homework assignment over the entire available period. The third recommendation is to submit the homework solutions *on time before the deadline*.

Pledge (Must be signed¹ according to the UF Honor Code):

On my honor, I have neither given nor received unauthorized aid in doing this assignment.



Student signature

¹ Each student is obliged to print out this page, fill in the requested information in a handwritten and readable manner, make the *handwritten signature*, scan this page into PDF, and put this page as the first page of the PDF submission.

Question 1

A) $F = \{A \rightarrow BC, B \rightarrow D, D \rightarrow E, C \rightarrow A\}$

1) Augmentation: $\{B \rightarrow D\} \rightarrow \{BC \rightarrow CD\}$

Augmentation: $\{D \rightarrow E\} \rightarrow \{CD \rightarrow CE\}$

Augmentation: $\{C \rightarrow A\} \rightarrow \{CE \rightarrow AE\}$

Transitivity: $BC \rightarrow CD \rightarrow CE \rightarrow AE$

$BC \rightarrow AE$

2) Decomposition: $\{A \rightarrow BC\} \rightarrow \{A \rightarrow B\}$

Transitivity: $\{B \rightarrow D\} \rightarrow \{A \rightarrow D\}$

Transitivity: $\{D \rightarrow E\} \rightarrow \{A \rightarrow E\}$

Union: $\{A \rightarrow D\} + \{A \rightarrow E\} \rightarrow \{A \rightarrow ED\}$

$A \rightarrow ED$

3) Unable to be logically implied. The only FD with C on the right-hand side requires A, and the only FD with A on the right-hand side requires C. We require either A or C in the left-hand side of the provided FD.

B) $F = \{A \rightarrow BC, CD \rightarrow E, E \rightarrow F, B \rightarrow D\}$

1) Candidate Key

Augmentation: $\{A \rightarrow BC\} \rightarrow \{AC \rightarrow BC\}$

Trivial: $\{A \rightarrow A\} \rightarrow \{AC \rightarrow ABC\}$

Augmentation: $\{B \rightarrow D\} \rightarrow \{AC \rightarrow ABCD\}$

Augmentation: $\{D \rightarrow E\} \rightarrow \{AC \rightarrow ABCDE\}$

Augmentation: $\{E \rightarrow F\} \rightarrow \{AC \rightarrow ABCDEF\}$

2) Candidate Key

Augmentation: $\{A \rightarrow BC\} \rightarrow \{AD \rightarrow BCD\}$

Trivial: $\{A \rightarrow A\} \rightarrow \{AC \rightarrow ABCD\}$

Augmentation: $\{D \rightarrow E\} \rightarrow \{AC \rightarrow ABCDE\}$

Augmentation: $\{E \rightarrow F\} \rightarrow \{AC \rightarrow ABCDEF\}$

3) Candidate Key

Augmentation: $\{A \rightarrow BC\} \rightarrow \{A \rightarrow BC\}$

Trivial: $\{A \rightarrow A\} \rightarrow \{A \rightarrow ABC\}$

Augmentation: $\{B \rightarrow D\} \rightarrow \{A \rightarrow ABCD\}$

Augmentation: $\{D \rightarrow E\} \rightarrow \{A \rightarrow ABCDE\}$

Augmentation: $\{E \rightarrow F\} \rightarrow \{A \rightarrow ABCDEF\}$

C) $F = \{A \rightarrow B, AB \rightarrow C, CD \rightarrow E, E \rightarrow FG\}$

1) $A \rightarrow C$

Start: $A \rightarrow B$

Augmentation: $\{A \rightarrow A\} \rightarrow \{A \rightarrow AB\}$

Transitivity: $\{A \rightarrow AB\} + \{AB \rightarrow C\} \rightarrow \{A \rightarrow C\}$

2) $CD \rightarrow FG$

Transitivity: $\{CD \rightarrow E\} + \{E \rightarrow FG\} \rightarrow \{CD \rightarrow FG\}$

3) $AD \rightarrow E$

Start: $A \rightarrow B$

Augmentation: $\{A \rightarrow A\} \rightarrow \{A \rightarrow AB\}$

Transitivity: $\{A \rightarrow AB\} + \{AB \rightarrow C\} \rightarrow \{A \rightarrow C\}$

Augmentation: $\{A \rightarrow C\} \rightarrow \{AD \rightarrow CD\}$

Transitivity: $\{AD \rightarrow CD\} + \{CD \rightarrow E\} \rightarrow \{AD \rightarrow E\}$

4) $AD \rightarrow FG$

Transitivity: $\{AD \rightarrow E\} + \{E \rightarrow FG\} \rightarrow \{AD \rightarrow FG\}$

5) $AD \rightarrow ABCDEFG$

Augmentation: $\{A \rightarrow B\} \rightarrow \{AD \rightarrow ABD\}$

Augmentation: $\{AB \rightarrow C\} \rightarrow \{AD \rightarrow ABCD\}$

Augmentation: $\{CD \rightarrow E\} \rightarrow \{AD \rightarrow ABCDE\}$

Augmentation: $\{E \rightarrow FG\} \rightarrow \{AD \rightarrow ABCDEFG\}$

Question 2

A) $R(W, X, Y, Z)$; $F = \{X \rightarrow Y, YZ \rightarrow W, W \rightarrow Z\}$; $G = \{X \rightarrow YZ, Y \rightarrow W, W \rightarrow Z, Z \rightarrow Y\}$

Attribute closure for F.

$\{ \}^+ = \{ \}$

$\{W\}^+ = \{W, Z\}$

$\{X\}^+ = \{X, Y\}$

$\{Y\}^+ = \{Y\}$

$\{Z\}^+ = \{Z\}$

$\{W, X\}^+ = \{W, X, Y, Z\}$

$\{W, Y\}^+ = \{W, Y, Z\}$

$\{W, Z\}^+ = \{W, Z\}$

$\{X, Y\}^+ = \{X, Y\}$

$\{X, Z\}^+ = \{X, Z, Y, W\}$

$\{Y, Z\}^+ = \{Y, Z, W\}$

$\{W, X, Y\}^+ = \{W, X, Y, Z\}$

$\{W, X, Z\}^+ = \{W, X, Z, Y\}$

$\{W, Y, Z\}^+ = \{W, Y, Z\}$

$\{X, Y, Z\}^+ = \{X, Y, Z, W\}$

$\{W, X, Y, Z\}^+ = \{W, X, Y, Z\}$

Attribute closure for G.

$\{ \}^+ = \{ \}$

$\{W\}^+ = \{W, Z, Y\}$

$\{X\}^+ = \{X, Y, Z, W\}$

$\{Y\}^+ = \{Y, W, Z\}$

$\{Z\}^+ = \{Z, Y, W\}$

$\{W, X\}^+ = \{W, X, Y, Z\}$

$\{W, Y\}^+ = \{W, Y, Z\}$

$\{W, Z\}^+ = \{W, Z, Y\}$

$\{X, Y\}^+ = \{X, Y, Z, W\}$

$\{X, Z\}^+ = \{X, Z, Y, W\}$

$\{Y, Z\}^+ = \{Y, Z, W\}$

$\{W, X, Y\}^+ = \{W, X, Y, Z\}$

$\{W, X, Z\}^+ = \{W, X, Z, Y\}$

$\{W, Y, Z\}^+ = \{W, Y, Z\}$

$\{X, Y, Z\}^+ = \{X, Y, Z, W\}$

$\{W, X, Y, Z\}^+ = \{W, X, Y, Z\}$

- 1) The attribute closures for functional dependencies F and G are shown above, and the set of functional dependencies for G is larger than that for F. As an example, X is a candidate key for G, but the first candidate keys for F require two attributes (either {W, X} or {X, Z}).
- 2) To adjust F^+ to be equivalent to G^+ we can modify the FD $YZ \rightarrow W$ to just be $Y \rightarrow W$, and add an additional FD $Z \rightarrow Y$. In this configuration, the attributes W, Y, and Z form circular dependencies, where as long as we have one of the attributes, we can always reach the others. In order to match G^+ , we also need to have X connect into this dependency cycle. We could use any FD in the form $X \rightarrow \text{attribute}$, but F already has $X \rightarrow Y$, so there was no need to change it.

B) $R(V, W, X, Y, Z)$; $F = \{W \rightarrow V, X \rightarrow Y, XW \rightarrow Z, YZ \rightarrow XW\}$

1)

YZ:

Start with $YZ \rightarrow XW$

Augment with $W \rightarrow V$

$YZ \rightarrow VWX$

XY:

Nowhere to go from here

W:

Start with $W \rightarrow V$

Nowhere to go from here

2) YZ is a candidate key. Adding the reflexivity rule to the work above, we get $YZ \rightarrow VWXYZ$.

C) $R(A, B, C, D, E, F)$; $F = \{AB \rightarrow C, CD \rightarrow E, E \rightarrow F, B \rightarrow D\}$

$\{ \}^+ = \{ \}$

$\{A\}^+ = \{A\}$

$A \rightarrow A$

$\{B\}^+ = \{B, D\}$

$B \rightarrow B, B \rightarrow D$

$\{C\}^+ = \{C\}$

$C \rightarrow C$

$\{D\}^+ = \{D\}$

$D \rightarrow D$

$\{E\}^+ = \{E, F\}$

$E \rightarrow E, E \rightarrow F$

$\{F\}^+ = \{F\}$

$F \rightarrow F$

$\{A, B\}^+ = \{A, B, C, D, E, F\}$

$AB \rightarrow AB, B \rightarrow D, AB \rightarrow C, CD \rightarrow E, E \rightarrow F$

$\{A, C\}^+ = \{A, C\}$

$AC \rightarrow AC$

$\{A, D\}^+ = \{A, D\}$

$AD \rightarrow AD$

$\{A, E\}^+ = \{A, E, F\}$

$AE \rightarrow AE, E \rightarrow F$
 $\{A, F\}^+ = \{A, F\}$
 $AF \rightarrow AF$
 $\{B, C\}^+ = \{B, C, D, E, F\}$
 $BC \rightarrow BC, B \rightarrow D, CD \rightarrow E, E \rightarrow F$
 $\{B, D\}^+ = \{B, D\}$
 $BD \rightarrow BD$
 $\{B, E\}^+ = \{B, E, F, D\}$
 $BE \rightarrow BE, B \rightarrow D, E \rightarrow F$
 $\{B, F\}^+ = \{B, F, D\}$
 $BF \rightarrow BF, B \rightarrow D$
 $\{C, D\}^+ = \{C, D, E, F\}$
 $CD \rightarrow CD, CD \rightarrow E, E \rightarrow F$
 $\{C, E\}^+ = \{C, E, F\}$
 $CE \rightarrow CE, E \rightarrow F$
 $\{C, F\}^+ = \{C, F\}$
 $CF \rightarrow CF$
 $\{D, E\}^+ = \{D, E, F\}$
 $DE \rightarrow DE, E \rightarrow F$
 $\{D, F\}^+ = \{D, F\}$
 $DF \rightarrow DF$
 $\{E, F\}^+ = \{E, F\}$
 $EF \rightarrow EF$
 $\{A, B, C\}^+ = \{A, B, C, D, E, F\}$
 See $\{AB\}^+$
 $\{A, B, D\}^+ = \{A, B, D, C, E, F\}$
 See $\{AB\}^+$
 $\{A, B, E\}^+ = \{A, B, E, C, F, D\}$
 See $\{AB\}^+$
 $\{A, B, F\}^+ = \{A, B, F, C, D, E\}$
 See $\{AB\}^+$
 $\{A, C, D\}^+ = \{A, C, D, E, F\}$
 $ACD \rightarrow ACD, CD \rightarrow E, E \rightarrow F$
 $\{A, C, E\}^+ = \{A, C, E, F\}$
 $ACE \rightarrow ACE, E \rightarrow F$
 $\{A, C, F\}^+ = \{A, C, F\}$
 $ACF \rightarrow ACF$
 $\{A, D, E\}^+ = \{A, D, E, F\}$
 $ADE \rightarrow ADE, E \rightarrow F$
 $\{A, D, F\}^+ = \{A, D, F\}$
 $ADF \rightarrow ADF$
 $\{A, E, F\}^+ = \{A, E, F\}$
 $AEF \rightarrow AEF$
 $\{B, C, D\}^+ = \{B, C, D, E, F\}$
 See $\{BC\}^+$
 $\{B, C, E\}^+ = \{B, C, E, F, D\}$
 See $\{BC\}^+$
 $\{B, C, F\}^+ = \{B, C, F, D, E\}$

See {BC}+
 {B,D,E}+={B,D,E,F}
 BDE->BDE, E->F
 {B,D,F}+={B,D,F}
 BDF->BDF
 {B,E,F}+={B,E,F,D}
 BEF->BEF, B->D
 {C,D,E}+={C,D,E,F}
 CDE->CDE, E->F
 {C,D,F}+={C,D,F,E}
 CDF->CDF, CD->E
 {C,E,F}+={C,E,F}
 CEF->CEF
 {D,E,F}+={D,E,F}
 DEF->DEF
 {A,B,C,D}+={A,B,C,D,E,F}
 See {AB}+
 {A,B,C,E}+={A,B,C,E,F,D}
 See {AB}+
 {A,B,C,F}+={A,B,C,F,D,E}
 See {AB}+
 {A,B,D,E}+={A,B,D,E,C,F}
 See {AB}+
 {A,B,D,F}+={A,B,D,F,C,E}
 See {AB}+
 {A,B,E,F}+={A,B,E,F,C,D}
 See {AB}+
 {A,C,D,E}+={A,C,D,E,F}
 ACDE->ACDE, E->F
 {A,C,D,F}+={A,C,D,F,E}
 ACDF->ACDF, CD->E
 {A,C,E,F}+={A,C,E,F}
 ACEF->ACEF
 {A,D,E,F}+={A,D,E,F}
 ADEF->ADEF
 {B,C,D,E}+={B,C,D,E,F}
 BCDE->BCDE, E->F
 {B,C,D,F}+={B,C,D,F,E}
 BCDF->BCDF, CD->E
 {B,C,E,F}+={B,C,E,F,D}
 BCEF->BCEF, B->D
 {B,D,E,F}+={B,D,E,F}
 BDEF->BDEF
 {C,D,E,F}+={C,D,E,F}
 CDEF->CDEF
 {A,B,C,D,E}+={A,B,C,D,E,F}
 See {AB}+
 {A,B,C,D,F}+={A,B,C,D,F,E}

See {AB}+
 $\{A,B,C,E,F\}^+ = \{A,B,C,E,F,D\}$
 See {AB}+
 $\{A,B,D,E,F\}^+ = \{A,B,D,E,F,C\}$
 See {AB}+
 $\{A,C,D,E,F\}^+ = \{A,C,D,E,F\}$
 $ACDEF \rightarrow ACDEF$
 $\{B,C,D,E,F\}^+ = \{B,C,D,E,F\}$
 $BCDEF \rightarrow BCDEF$
 $\{A,B,C,D,E,F\}^+ = \{A,B,C,D,E,F\}$
 See {AB}+

Question 3

Step 1

$F_c = \{AB \rightarrow C, C \rightarrow A, BC \rightarrow D, ACD \rightarrow B, D \rightarrow EG, BE \rightarrow C, CG \rightarrow BD, CE \rightarrow G\}$

Step 2

Check $AB \rightarrow C$: neither A nor B can be removed
 Check $BC \rightarrow D$: neither B nor C can be removed
 Check $ACD \rightarrow B$: None can be removed
 Check $BE \rightarrow C$: neither B nor E can be removed
 Check $CG \rightarrow BD$: neither C nor G can be removed
 Check $CE \rightarrow G$: neither C nor E can be removed

$F_c = \{AB \rightarrow C, C \rightarrow A, BC \rightarrow D, ACD \rightarrow B, D \rightarrow EG, BE \rightarrow C, CG \rightarrow BD, CE \rightarrow G\}$

Step 3

Check $AB \rightarrow C$: C cannot be removed
 Check $C \rightarrow A$: A cannot be removed
 Check $BC \rightarrow D$: D cannot be removed
Check $ACD \rightarrow B$: B can be removed
 Check $D \rightarrow EG$: neither E nor G can be removed
 Check $BE \rightarrow C$: C cannot be removed
Check $CG \rightarrow BD$: D can be removed
 Check $CE \rightarrow G$: cannot be removed

$F_c = \{AB \rightarrow C, C \rightarrow A, BC \rightarrow D, ACD \rightarrow \emptyset, D \rightarrow EG, BE \rightarrow C, CG \rightarrow B, CE \rightarrow G\}$

Step 4: Remove $ACD \rightarrow \emptyset$

$F_c = \{AB \rightarrow C, C \rightarrow A, BC \rightarrow D, D \rightarrow EG, BE \rightarrow C, CG \rightarrow B, CE \rightarrow G\}$

Step 5A:

Minimal Cover = $\{AB \rightarrow C, C \rightarrow A, BC \rightarrow D, D \rightarrow E, D \rightarrow G, BE \rightarrow C, CG \rightarrow B, CE \rightarrow G\}$

Question 4

A)

(1) $? = X_A < Y_A$. That is, the lexicographical ordering is based on the alphabetical ordering of the attribute name

(2) $? = X_A == Y_A$ AND $D_A == D_A$. That is, two attributes are equal if and only if both the attribute names are equal, and the domains are the same.

B) $\forall X = \{B_1, B_2, \dots, B_m\} \subseteq R : \{B_1 < B_2 < \dots < B_m\}$

Basically this requires that all attributes being considered must be listed in lexicographical order.

C) $X <_{AS} Y \Leftrightarrow$ one of the following is true:

a) $k < l$ (if X has fewer attributes than Y , it is considered less than Y)

b) $k = l$ and $B_i == C_i$ for all $i < j$ and $B_j < C_j$ for some j between $1-k$ (order by the first attribute that is different between the sets)

D)

```
candidate_keys = []
```

```
for subset1 in all possible attribute subsets:
```

```
    Check if closure of the subset equals the relation R:
```

```
        is_minimal = True
```

```
        If yes:
```

```
            For subset2 in all possible attribute subsets of subset1:
```

```
                If subset2 != subset1 and closure(subset2) == R:
```

```
                    is_minimal = False
```

```
                    Break
```

```
        If is_minimal: candidate_keys.append(subset1)
```

```
Return candidate_keys.sort(key= <AS)          # Sort candidate keys using <AS
```

E)

```
left_side_attributes = set()
```

```
right_side_attributes = set()
```

```
for (X, Y) in F:
```

```
    left_side_attributes.update(X)
```

```
    right_side_attributes.update(Y)
```

```
# Step 1
```

```
attributes_neither_side = set(R) - (left_side_attributes U right_side_attributes)
```

```
# Step 2
```

```
attributes_left_only = left_side_attributes - right_side_attributes
```

```
# Step 3
```

```
attributes_right_only = right_side_attributes - left_side_attributes
```

```
# Step 4
```

```
step4_attributes = attributes_neither_side U attributes_left_only
```

```
# Step 5
```

```
if closure(step4_attributes) == R:
```

```
    return [step4_attributes]
```

```
# Step 6
```

```
step6_attributes = set(R) - (attributes_right_only U step4_attributes)
```



```
# Step 7
candidate_keys = []
for comb in combinations of step6_attributes:
    if closure(step4_attributes U comb) == R:
        candidate_keys.append(combined_attributes)

return candidate_keys
```