Vision and Perception

Lecture 2: Image pyramids



References

Basic reading:

Szeliski textbook, Sections 3.4, 3.5

Additional reading:

The original Laplacian pyramid paper

• Burt and Adelson, "The Laplacian Pyramid as a Compact Image Code," IEEE ToC 1983.

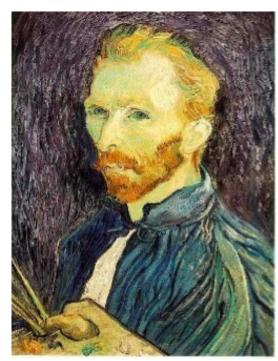
Overview of today's lecture

- Image downsampling
- Aliasing
- Gaussian image pyramid
- Laplacian image pyramid

Image downsampling



Naïve image downsampling



Throw away half the rows and columns

delete even rows delete even columns



delete even rows delete even columns



1/8

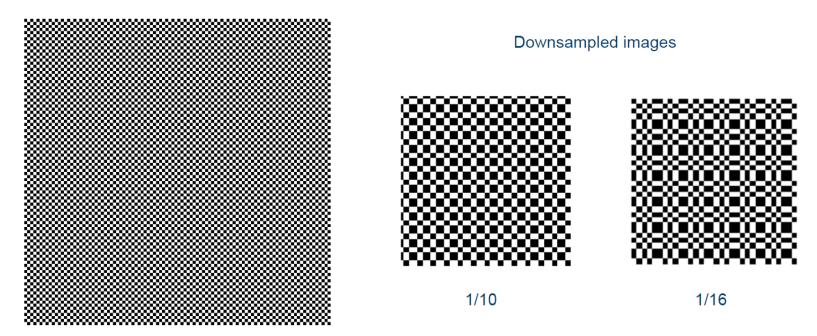
1/4

Naïve image downsampling



What is the 1/8 image so pixelated (and do you know what this effect is called)?

Spatial undersampling

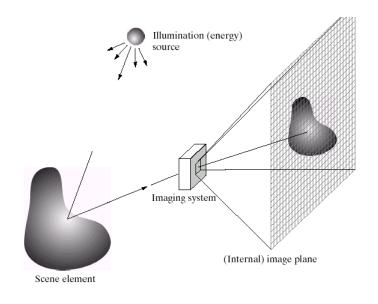


Checkerboard with 10 x 10 pixel squares

Aliasing

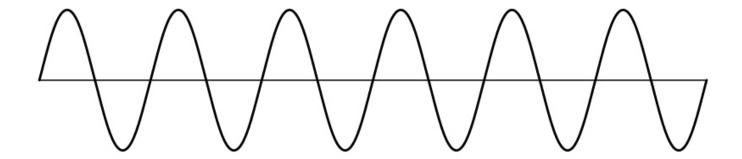
Reminder





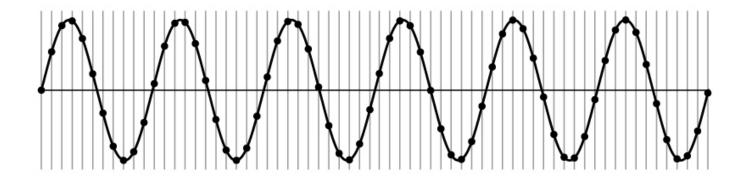
Images are a discrete, or sampled, representation of a continuous world

Very simple example: a sine wave

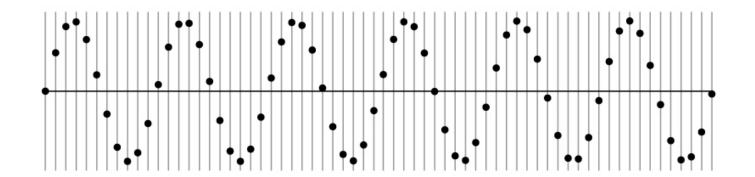


How would you discretize this signal?

Very simple example: a sine wave



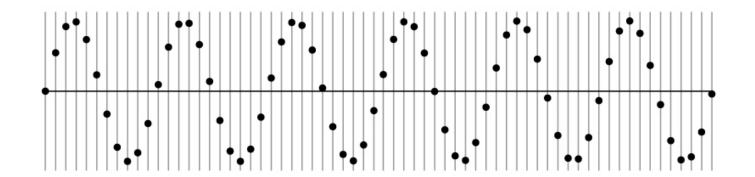
Very simple example: a sine wave



How many samples should I take?

Can I take as *many* samples as I want?

Very simple example: a sine wave

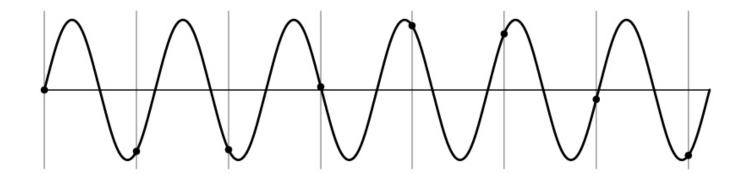


How many samples should I take?

Can I take as *few* samples as I want?

Undersampling

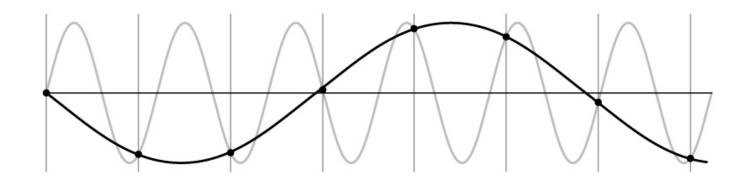
Very simple example: a sine wave



Unsurprising effect: information is lost.

Undersampling

Very simple example: a sine wave

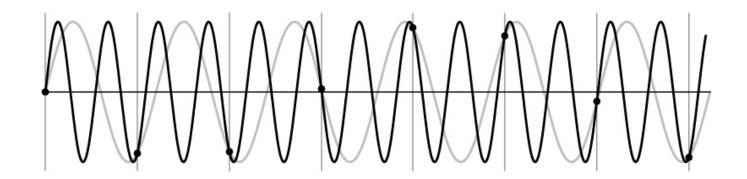


Unsurprising effect: information is lost.

Surprising effect: can confuse the signal with one of *lower* frequency.

Undersampling

Very simple example: a sine wave



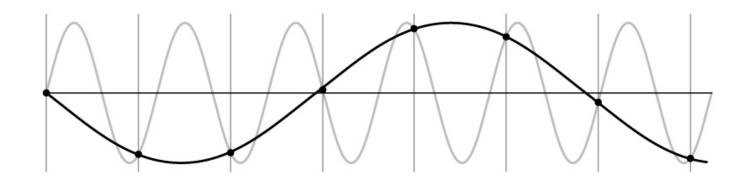
Unsurprising effect: information is lost.

Surprising effect: can confuse the signal with one of *lower* frequency.

Note: we could always confuse the signal with one of *higher* frequency.

Aliasing

Term for: Undersampling can disguise a signal as one of a lower frequency

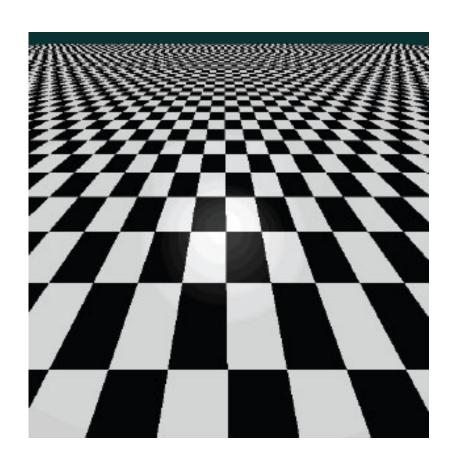


Unsurprising effect: information is lost.

Surprising effect: can confuse the signal with one of *lower* frequency.

Note: we could always confuse the signal with one of *higher* frequency.

Aliasing in textures



Aliasing in photographs

This is also known as "moire"







Anti-aliasing

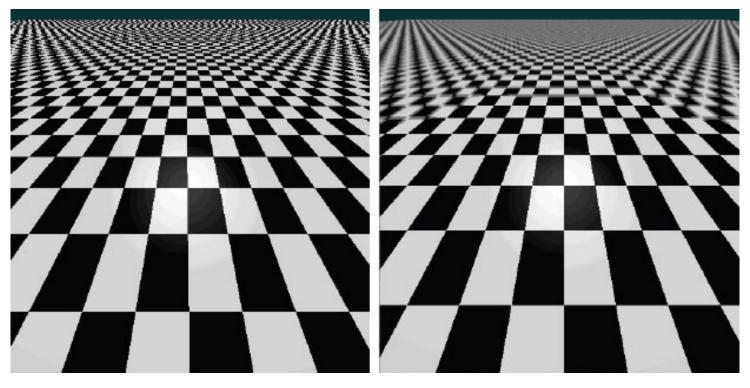
How would you deal with aliasing?

Anti-aliasing

How would you deal with aliasing?

Approach 1: Oversample the signal

Anti-aliasing in textures



aliasing artifacts

anti-aliasing by oversampling

Anti-aliasing

How would you deal with aliasing?

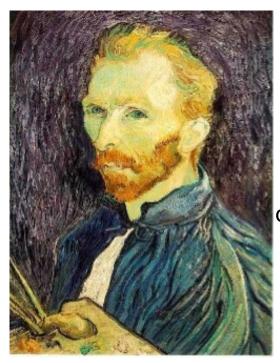
Approach 1: Oversample the signal

Approach 2: Smooth the signal

- Remove some of the detail effects that cause aliasing.
- Lose information, but better than aliasing artifacts.

How would you smooth a signal?

Better image downsampling



Apply a smoothing filter first, then throw away half the rows and columns

Gaussian filter
delete even rows
delete even columns



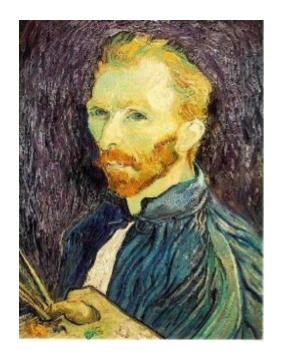
Gaussian filter delete even rows delete even columns

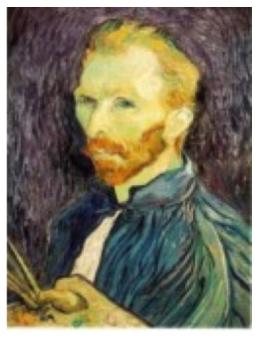


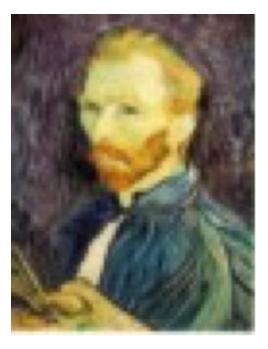
1/8

1/4

Better image downsampling





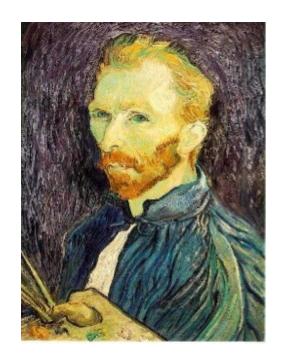


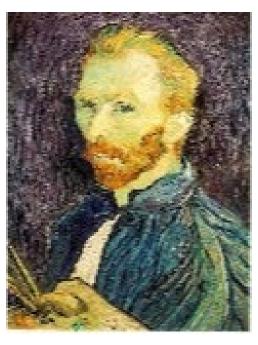
1/2

1/4 (2x zoom)

1/8 (4x zoom)

Naïve image downsampling







1/2

1/4 (2x zoom)

1/8 (4x zoom)

Anti-aliasing

Question 1: How much smoothing do I need to do to avoid aliasing?

Question 2: How many samples do I need to take to avoid aliasing?

Answer to both: Enough to reach the Nyquist limit 2*fmax.

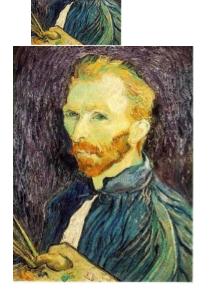
- The reason all of this matters for images is that through application of the <u>Fourier Series</u>, any signal of finite length can be represented as a sum of sinusoids.
- This means that even if a picture has no discernable wave pattern, it can still be represented as a sequence of sinusoids of different frequencies.
- The highest frequency that can be represented in the image is half the Nyquist rate (sampling frequency).

We'll see what this means soon.

Gaussian image pyramid

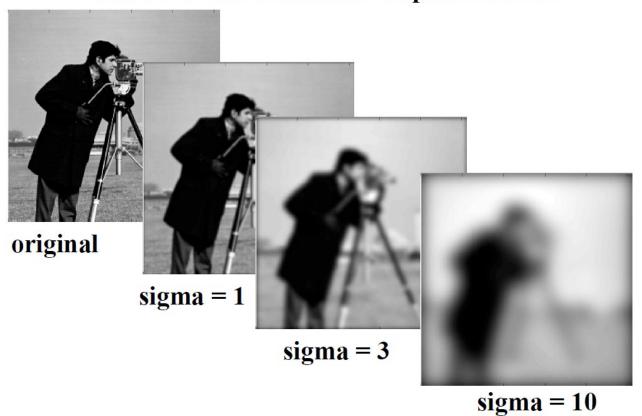
Gaussian image pyramid

The name of this sequence of subsampled images





Idea for Today: Form a Multi-Resolution Representation



Pyramid representation

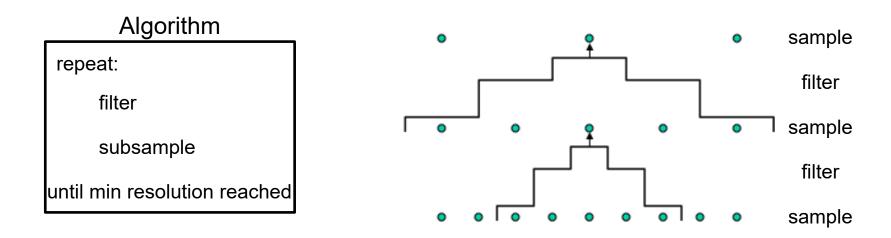
Because a large amount of smoothing limits the frequency of features in the image, we do not need to keep all the pixels around!

Strategy: progressively reduce the number of pixels as we smooth more and more. Leads to a "pyramid" representation if we subsample at each level.

Synthesis: Smooth image with a Gaussian and downsample. Repeat.

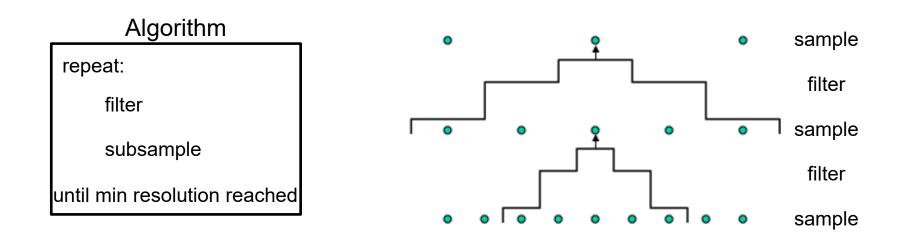
• Gaussian is used because it is self-reproducing (enables incremental smoothing).

Constructing a Gaussian pyramid



Question: How much bigger than the original image is the whole pyramid?

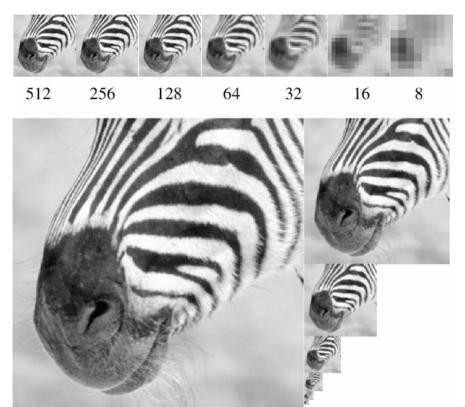
Constructing a Gaussian pyramid



Question: How much bigger than the original image is the whole pyramid?

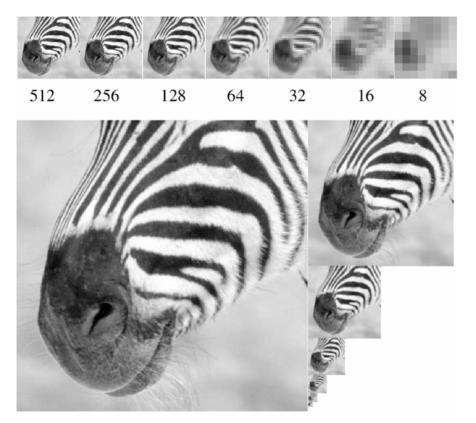
Answer: Just 4/3 times the size of the original image!

Some properties of the Gaussian pyramid



What happens to the details of the image?

Some properties of the Gaussian pyramid

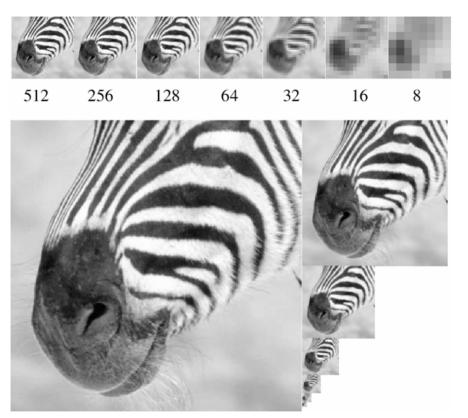


What happens to the details of the image?

 They get smoothed out as we move to higher levels.

What is preserved at the higher levels?

Some properties of the Gaussian pyramid



What happens to the details of the image?

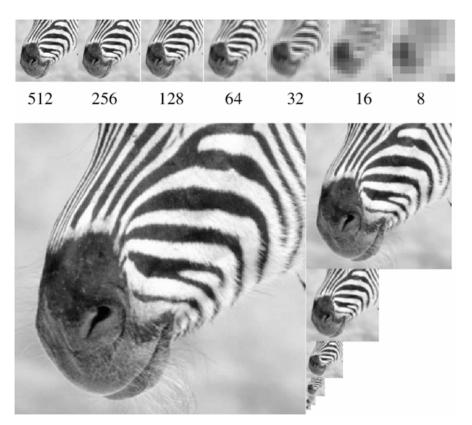
 They get smoothed out as we move to higher levels.

What is preserved at the higher levels?

 Mostly large uniform regions in the original image.

How would you reconstruct the original image from the image at the upper level?

Some properties of the Gaussian pyramid



What happens to the details of the image?

 They get smoothed out as we move to higher levels.

What is preserved at the higher levels?

 Mostly large uniform regions in the original image.

How would you reconstruct the original image from the image at the upper level?

That's not possible.

Blurring is lossy



What does the residual look like?

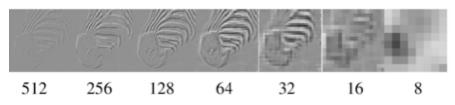
Blurring is lossy



Can we make a pyramid that is lossless?

Laplacian image pyramid

Laplacian image pyramid

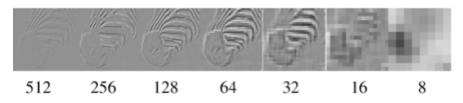


At each level, retain the residuals instead of the blurred images themselves.



Can we reconstruct the original image using the pyramid?

Laplacian image pyramid



At each level, retain the residuals instead of the blurred images themselves.



Can we reconstruct the original image using the pyramid?

Yes we can!

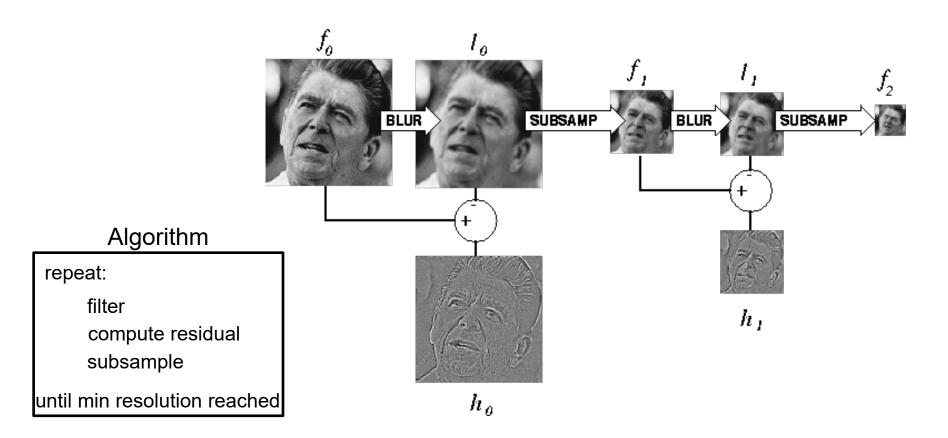
What do we need to store to be able to reconstruct the original image?

Let's start by looking at just one level

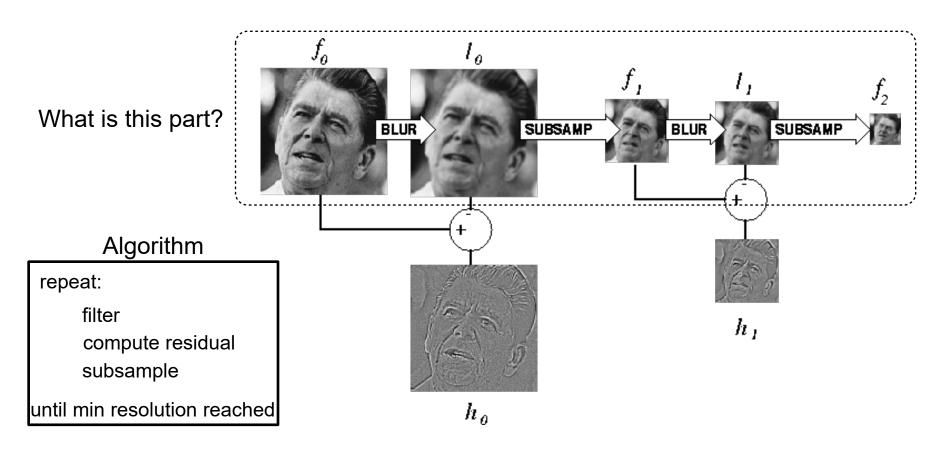


Does this mean we need to store both residuals and the blurred copies of the original?

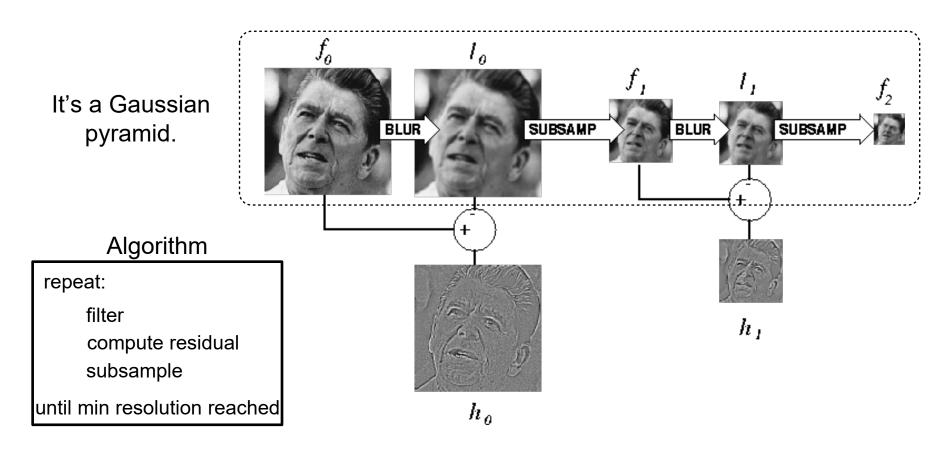
Constructing a Laplacian pyramid



Constructing a Laplacian pyramid



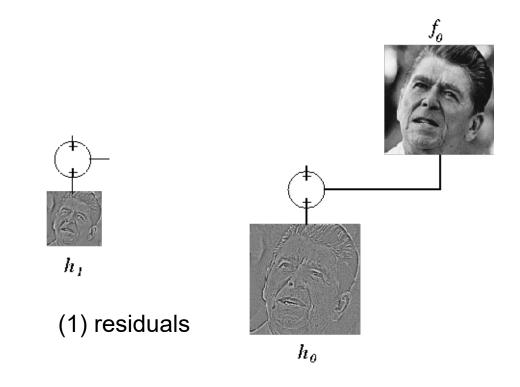
Constructing a Laplacian pyramid



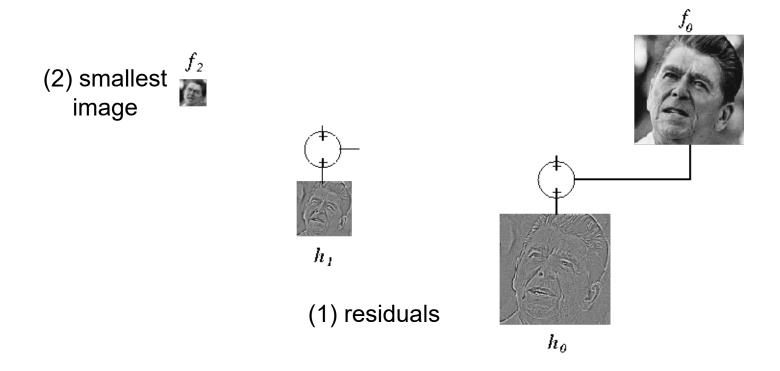
What do we need to construct the original image?



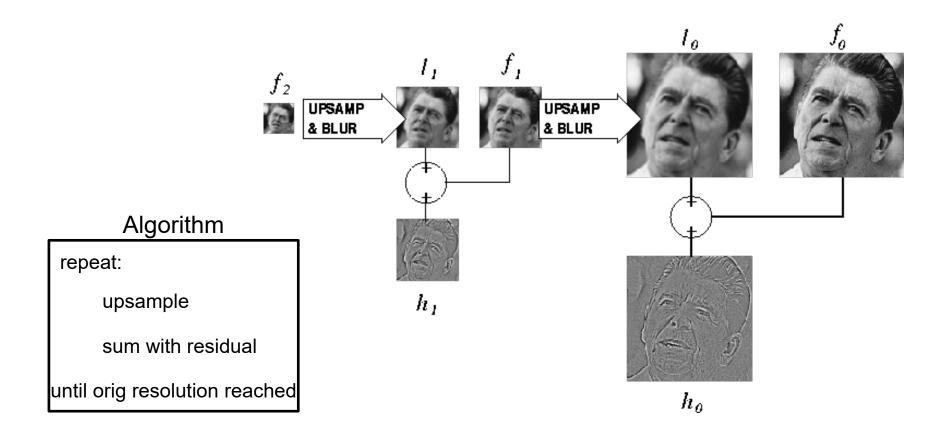
What do we need to construct the original image?



What do we need to construct the original image?



Reconstructing the original image



Gaussian vs Laplacian Pyramid



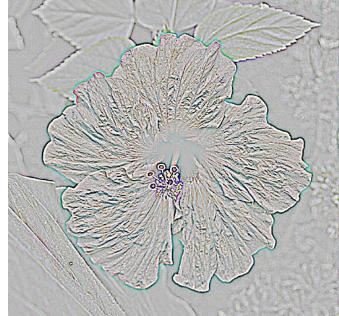






Shown in opposite order for space.





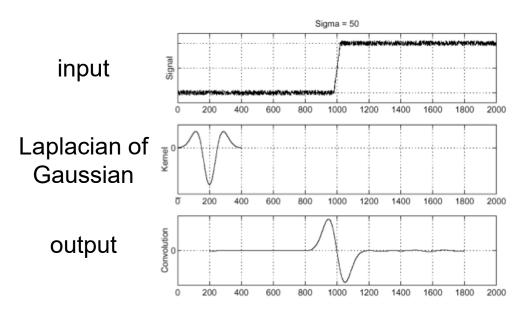




Why is it called a Laplacian pyramid?

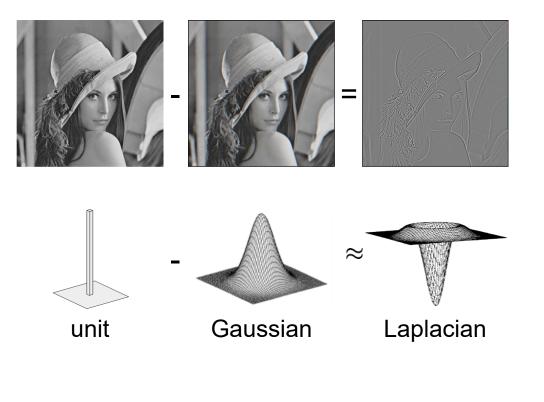
Reminder: Laplacian of Gaussian (LoG) filter

As with derivative, we can combine Laplace filtering with Gaussian filtering

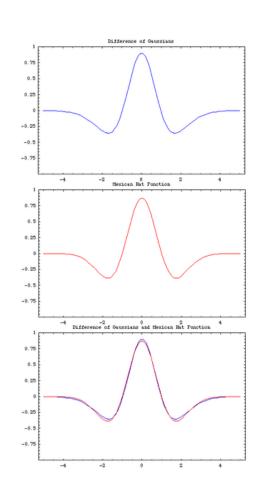


"zero crossings" at edges

Why is it called a Laplacian pyramid?



Difference of Gaussians approximates the Laplacian



What are image pyramids used for?

image compression







image blending

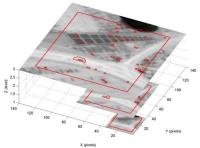
multi-scale detection



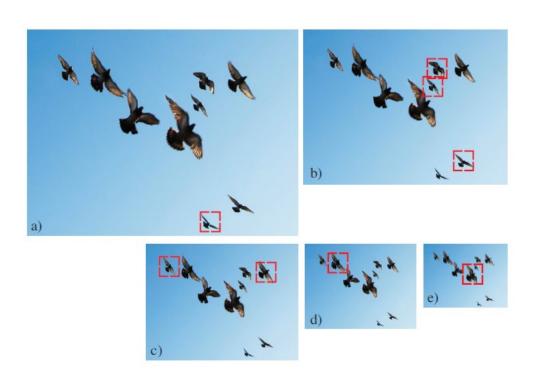


denoising

multi-scale registration



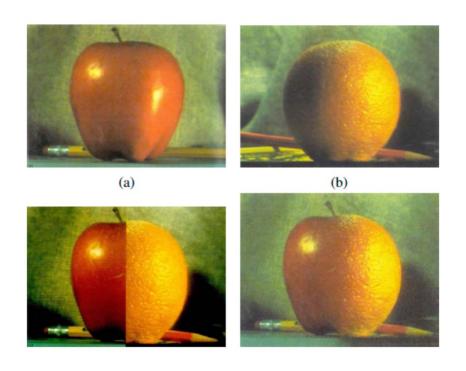
Multi-scale image analysis



- Multiscale image pyramid.
 Each image is 25% smaller than the previous one.
 - The red box indicates the size of a template used for detecting flying birds.
 - As the size of the template is fixed, it will only be able to detect the birds that tightly t inside the box.

 Birds that are smaller or larger will not be detected within a single scale.
 - By running the same template across many levels in this pyramid, different birds instances are detected at different scales.

Image blending



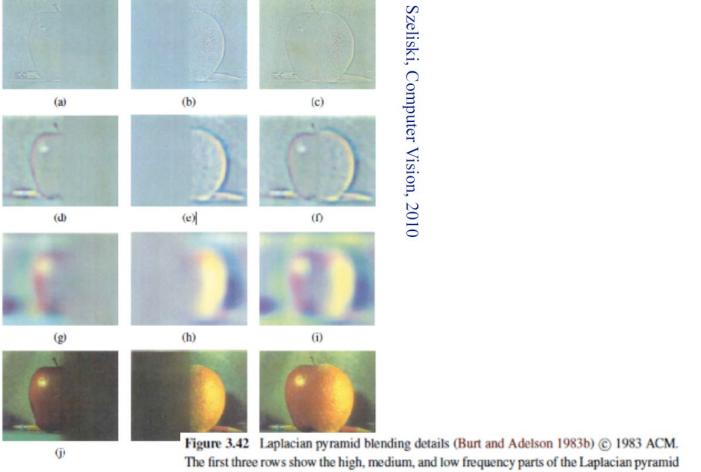
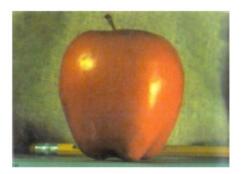


Figure 3.42 Laplacian pyramid blending details (Burt and Adelson 1983b) © 1983 ACM. The first three rows show the high, medium, and low frequency parts of the Laplacian pyramid (taken from levels 0, 2, and 4). The left and middle columns show the original apple and orange images weighted by the smooth interpolation functions, while the right column shows the averaged contributions.

Image blending





- · Build Laplacian pyramid for both images: LA, LB
- Build Gaussian pyramid for mask: G
- Build a combined Laplacian pyramid: L(j) = G(j) LA(j) + (1-G(j)) LB(j)
- Collapse L to obtain the blended image



Aude Oliva, Antonio Torralba, and Philippe G. Schyns. 2006. Hybrid images. ACM Trans. Graph. 25, 3 (July 2006), 527-532.

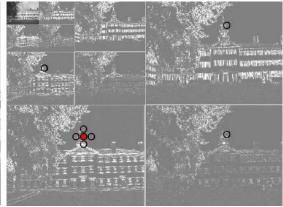
Other types of pyramids

Steerable pyramid: At each level keep multiple versions, one for each direction.



Wavelets: Huge area in image processing





Acknowledgement: some slides and material from Bernt Schiele, Mario Fritz, Michael Black, Bill Freeman, Fei-Fei, Justin Johnson, Serena Yeung, R. Szelisky, Fabio Galasso, Ioannis Gkioulekas