

Knowledge Representation and Semantic Technologies

# **Ontologies and OWL**

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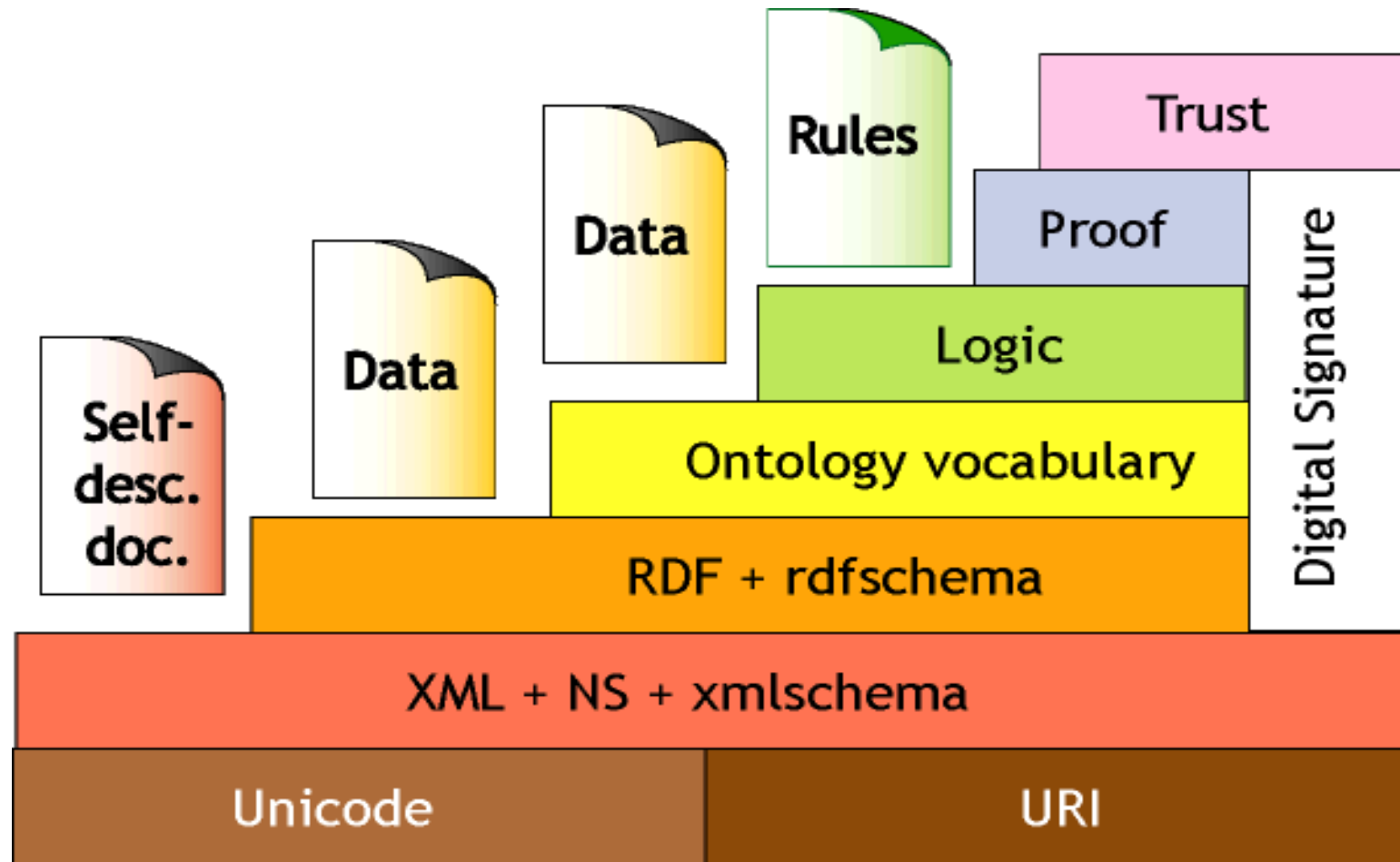
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# The Semantic Web Tower

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# Ontology in computer science

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- ontology = **shared conceptualization** of a domain of interest (Gruber, 1993)
- shared vocabulary (set of terms)
  - ⇒ simple (shallow) ontology
- (complex) relationships between terms
  - ⇒ deep ontology
- AI view:
  - ontology = logical theory (knowledge base)
- DB view:
  - ontology = conceptual data model

# Structure of an ontology

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- Terms = names for important concepts in the domain
  - **Elephant** is a concept whose members are a kind of animal
  - **Herbivore** is a concept whose members are exactly those animals who eat only plants or parts of plants
  - **Adult\_Elephant** is a concept whose members are exactly those elephants whose age is greater than 20 years
- Relationships between terms = background knowledge/constraints on the domain
  - **Adult\_Elephants** weigh at least 2,000 kg
  - All **Elephants** are either **African\_Elephants** or **Indian\_Elephants**
  - No individual can be both a **Herbivore** and a **Carnivore**

# Ontology languages

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Kinds of potential ontology languages:

- Graphical notations
- Logic-based languages
- Object-oriented languages
- Web schema languages

# Ontology languages

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- Graphical notations:
  - Semantic networks
  - Topic Maps
  - UML
  - RDF

# Ontology languages

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- Logic based languages:
  - Description Logics
  - Rules (e.g., RuleML, Logic Programming/Prolog)
  - First Order Logic (e.g., KIF)
  - Conceptual graphs
  - (Syntactically) higher order logics (e.g., LBase)
  - Non-classical logics (e.g., F-logic, Non-Monotonic Logics, Modal Logics)

# Obect-oriented languages

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many languages use object-oriented models based on:

- **Objects/Instances/Individuals**
  - Elements of the domain of discourse
  - Equivalent to constants in FOL
- **Types/Classes/Concepts**
  - Sets of objects sharing certain characteristics
  - Equivalent to unary predicates in FOL
- **Relations/Properties/Roles**
  - Sets of pairs (tuples) of objects
  - Equivalent to binary predicates in FOL



# Web schema languages

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- Existing Web languages extended to facilitate content description
  - XML → XML Schema (XMLS)
  - RDF → RDF Schema (RDFS)
- XMLS *not* an ontology language
  - Changes format of DTDs (document schemas) to be XML
  - Adds an extensible type hierarchy
    - Integers, Strings, etc.
    - Can define sub-types, e.g., positive integers
- RDFS *is* recognizable as an ontology language
  - Classes and properties
  - Sub/super-classes (and properties)
  - Range and domain (of properties)

# Limitations of RDFS

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- RDFS **too weak** to describe resources in sufficient detail
  - No **localised range and domain** constraints
    - Can't say that the range of `hasChild` is `person` when applied to persons and `elephant` when applied to elephants
  - No **existence/cardinality** constraints
    - Can't say that all *instances* of `person` have a mother that is also a person, or that persons have exactly 2 parents
  - No **transitive, inverse or symmetrical** properties
    - Can't say that `isPartOf` is a transitive property, that `hasPart` is the inverse of `isPartOf` or that `touches` is symmetrical
  - ...

# Web ontology language requirements

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Desirable features identified for Web Ontology Language:

- Extends existing Web standards (XML, RDF, RDFS)
- Easy to understand and use (should be based on familiar KR idioms)
- Formally specified
- Of “adequate” expressive power
- Possible to provide automated reasoning support

Two languages developed to satisfy above requirements: DAML and OIL

The OWL language (based on DAML+OIL) became a W3C recommendation in 2004

# OWL

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- OWL = Web Ontology Language
- the OWL family is constituted by 3 different languages (with different expressive power):
  - OWL Full
    - union of OWL syntax and RDF
  - OWL-DL
    - “DL fragment” of OWL Full
  - OWL-Lite
    - “easier to implement” subset of OWL DL

# OWL

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- OWL standards and technology:
  - first version of OWL standardized in 2004
  - reasoning techniques and tools are recent
  - “optimization” of reasoning not fully explored
  - 2009: W3C standardization of **OWL 2**

# OWL class constructors

Constructor	DL Syntax	Example	Modal Syntax
intersectionOf	$C_1 \sqcap \dots \sqcap C_n$	Human $\sqcap$ Male	$C_1 \wedge \dots \wedge C_n$
unionOf	$C_1 \sqcup \dots \sqcup C_n$	Doctor $\sqcup$ Lawyer	$C_1 \vee \dots \vee C_n$
complementOf	$\neg C$	$\neg$ Male	$\neg C$
oneOf	$\{x_1\} \sqcup \dots \sqcup \{x_n\}$	{john} $\sqcup$ {mary}	$x_1 \vee \dots \vee x_n$
allValuesFrom	$\forall P.C$	$\forall$ hasChild.Doctor	$[P]C$
someValuesFrom	$\exists P.C$	$\exists$ hasChild.Lawyer	$\langle P \rangle C$
maxCardinality	$\leq_n P$	$\leq 1$ hasChild	$[P]_{n+1}$
minCardinality	$\geq_n P$	$\geq 2$ hasChild	$\langle P \rangle_n$

- XMLS **datatypes** as well as classes in  $\forall P.C$  and  $\exists P.C$ 
  - E.g.,  $\exists$ hasAge.nonNegativeInteger
- Arbitrarily complex **nesting** of constructors
  - E.g., Person  $\sqcap \forall$ hasChild.Doctor  $\sqcup \exists$ hasChild.Doctor

# OWL axioms

Axiom	DL Syntax	Example
subClassOf	$C_1 \sqsubseteq C_2$	Human $\sqsubseteq$ Animal $\sqcap$ Biped
equivalentClass	$C_1 \equiv C_2$	Man $\equiv$ Human $\sqcap$ Male
disjointWith	$C_1 \sqsubseteq \neg C_2$	Male $\sqsubseteq \neg$ Female
sameIndividualAs	$\{x_1\} \equiv \{x_2\}$	{President_Bush} $\equiv$ {G_W_Bush}
differentFrom	$\{x_1\} \sqsubseteq \neg\{x_2\}$	{john} $\sqsubseteq \neg$ {peter}
subPropertyOf	$P_1 \sqsubseteq P_2$	hasDaughter $\sqsubseteq$ hasChild
equivalentProperty	$P_1 \equiv P_2$	cost $\equiv$ price
inverseOf	$P_1 \equiv P_2^-$	hasChild $\equiv$ hasParent <sup>-</sup>
transitiveProperty	$P^+ \sqsubseteq P$	ancestor <sup>+</sup> $\sqsubseteq$ ancestor
functionalProperty	$\top \sqsubseteq \leq 1P$	$\top \sqsubseteq \leq 1$ hasMother
inverseFunctionalProperty	$\top \sqsubseteq \leq 1P^-$	$\top \sqsubseteq \leq 1$ hasSSN <sup>-</sup>

Axioms (mostly) reducible to inclusion ( $\sqsubseteq$ )

$C \equiv D$  iff both  $C \sqsubseteq D$  and  $D \sqsubseteq C$

# XML syntax for OWL

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E.g., concept  $\text{Person} \sqcap \forall \text{hasChild}.\text{Doctor} \sqcup \exists \text{hasChild}.\text{Doctor}$ :

```
<owl:Class>
  <owl:intersectionOf rdf:parseType=" collection">
    <owl:Class rdf:about="#Person"/>
    <owl:Restriction>
      <owl:onProperty rdf:resource="#hasChild"/>
      <owl:toClass>
        <owl:unionOf rdf:parseType=" collection">
          <owl:Class rdf:about="#Doctor"/>
          <owl:Restriction>
            <owl:onProperty rdf:resource="#hasChild"/>
            <owl:hasClass rdf:resource="#Doctor"/>
          </owl:Restriction>
        </owl:unionOf>
      </owl:toClass>
    </owl:Restriction>
  </owl:intersectionOf>
</owl:Class>
```



# OWL functional and RDF syntax

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- In the next slides, we introduce the **functional** and **RDF** syntax of OWL (OWL 2)
- Functional syntax:
  - Functional-style syntax for OWL statements
  - E.g.: `DisjointClasses(C1 C2)`
- RDF syntax:
  - Expresses every OWL statement as a set of RDF triples
  - E.g.: `C1 owl:disjointWith C2.`

# Abbreviations

Letters	Meaning	Letters	Meaning	Letters	Meaning	Letters	Meaning
C	class expression	CN	class name	D	data range	DN	datatype name
P	object property expression	PN	object property name	R	data property	A	annotation property
a	individual	aN	individual name	_:a	anonymous individual (a blank node label)	v	literal
n	non-negative integer	f	facet	ON	ontology name	U	IRI
s	IRI or anonymous individual	t	IRI, anonymous individual, or literal	p	prefix name	_:x	blank node
(a <sub>1</sub> ... a <sub>n</sub> )	RDF list						

# Declarations

Language Feature	Functional Syntax	RDF Syntax
class	Declaration( Class( CN ) )	CN rdf:type owl:Class.
datatype	Declaration( Datatype( DN ) )	DN rdf:type rdfs:Datatype.
object property	Declaration( ObjectProperty( PN ) )	PN rdf:type owl:ObjectProperty.
data property	Declaration( DataProperty( R ) )	R rdf:type owl:DatatypeProperty.
annotation property	Declaration( AnnotationProperty( A ) )	A rdf:type owl:AnnotationProperty.
named individual	Declaration( NamedIndividual( aN ) )	aN rdf:type owl:NamedIndividual.

# Boolean operators and enumeration

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Language Feature	Functional Syntax	RDF Syntax
intersection	ObjectIntersectionOf( $C_1 \dots C_n$ )	<code>_:x rdf:type owl:Class. _:x owl:intersectionOf ( <math>C_1 \dots C_n</math> ).</code>
union	ObjectUnionOf( $C_1 \dots C_n$ )	<code>_:x rdf:type owl:Class. _:x owl:unionOf ( <math>C_1 \dots C_n</math> ).</code>
complement	ObjectComplementOf( $C$ )	<code>_:x rdf:type owl:Class. _:x owl:complementOf <math>C</math>.</code>
enumeration	ObjectOneOf( $a_1 \dots a_n$ )	<code>_:x rdf:type owl:Class. _:x owl:oneOf ( <math>a_1 \dots a_n</math> ).</code>

# Object property restrictions

Language Feature	Functional Syntax	RDF Syntax
universal	ObjectAllValuesFrom(P C)	<code>_:x rdf:type owl:Restriction. _:x owl:onProperty P. _:x owl:allValuesFrom C</code>
existential	ObjectSomeValuesFrom(P C)	<code>_:x rdf:type owl:Restriction. _:x owl:onProperty P. _:x owl:someValuesFrom C</code>
individual value	ObjectHasValue(P a)	<code>_:x rdf:type owl:Restriction. _:x owl:onProperty P. _:x owl:hasValue a.</code>
local reflexivity	ObjectHasSelf(P)	<code>_:x rdf:type owl:Restriction. _:x owl:onProperty P. _:x owl:hasSelf "true"^^xsd:boolean.</code>
exact cardinality	ObjectExactCardinality(n P)	<code>_:x rdf:type owl:Restriction. _:x owl:onProperty P. _:x owl:cardinality n.</code>
qualified exact cardinality	ObjectExactCardinality(n P C)	<code>_:x rdf:type owl:Restriction. _:x owl:onProperty P. _:x owl:qualifiedCardinality n. _:x owl:onClass C.</code>

# Object property restrictions (contd.)

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Language Feature	Functional Syntax	RDF Syntax
maximum cardinality	ObjectMaxCardinality(n P)	<code>_:x rdf:type owl:Restriction. _:x owl:onProperty P. _:x owl:maxCardinality n.</code>
qualified maximum cardinality	ObjectMaxCardinality(n P C)	<code>_:x rdf:type owl:Restriction. _:x owl:onProperty P. _:x owl:maxQualifiedCardinality n. _:x owl:onClass C.</code>
minimum cardinality	ObjectMinCardinality(n P)	<code>_:x rdf:type owl:Restriction. _:x owl:onProperty P. _:x owl:minCardinality n.</code>
qualified minimum cardinality	ObjectMinCardinality(n P C)	<code>_:x rdf:type owl:Restriction. _:x owl:onProperty P. _:x owl:minQualifiedCardinality n. _:x owl:onClass C.</code>

# Data property restrictions

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Language Feature	Functional Syntax	RDF Syntax
universal	DataAllValuesFrom(R D)	<code>_:x rdf:type owl:Restriction.</code> <code>_:x owl:onProperty R.</code> <code>_:x owl:allValuesFrom D.</code>
existential	DataSomeValuesFrom(R D)	<code>_:x rdf:type owl:Restriction.</code> <code>_:x owl:onProperty R.</code> <code>_:x owl:someValuesFrom D.</code>
literal value	DataHasValue(R v)	<code>_:x rdf:type owl:Restriction.</code> <code>_:x owl:onProperty R.</code> <code>_:x owl:hasValue v.</code>
exact cardinality	DataExactCardinality(n R)	<code>_:x rdf:type owl:Restriction.</code> <code>_:x owl:onProperty R.</code> <code>_:x owl:cardinality n.</code>
qualified exact cardinality	DataExactCardinality(n R D)	<code>_:x rdf:type owl:Restriction.</code> <code>_:x owl:onProperty R.</code> <code>_:x owl:qualifiedCardinality n.</code> <code>_:x owl:onClass D.</code>

# Data property restrictions (contd.)

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Language Feature	Functional Syntax	RDF Syntax
maximum cardinality	DataMaxCardinality(n R)	<code>_:x rdf:type owl:Restriction.</code> <code>_:x owl:onProperty R.</code> <code>_:x owl:maxCardinality n.</code>
qualified maximum cardinality	DataMaxCardinality(n R D)	<code>_:x rdf:type owl:Restriction.</code> <code>_:x owl:onProperty R.</code> <code>_:x owl:maxQualifiedCardinality n.</code> <code>_:x owl:onClass D.</code>
minimum cardinality	DataMinCardinality(n R)	<code>_:x rdf:type owl:Restriction.</code> <code>_:x owl:onProperty R.</code> <code>_:x owl:minCardinality n.</code>
qualified minimum cardinality	DataMinCardinality(n R D)	<code>_:x rdf:type owl:Restriction.</code> <code>_:x owl:onProperty R.</code> <code>_:x owl:minQualifiedCardinality n.</code> <code>_:x owl:onClass D.</code>



# Object and data property expressions

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Language Feature	Functional Syntax	RDF Syntax
named object property	PN	PN
universal object property	owl:topObjectProperty	owl:topObjectProperty
empty object property	owl:bottomObjectProperty	owl:bottomObjectProperty
inverse property	ObjectInverseOf(PN)	_:x owl:inverseOf PN

Language Feature	Functional Syntax	RDF Syntax
named data property	R	R
universal data property	owl:topDataProperty	owl:topDataProperty
empty data property	owl:bottomDataProperty	owl:bottomDataProperty

# Class axioms

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Language Feature	Functional Syntax	RDF Syntax
subclass	SubClassOf( $C_1$ $C_2$ )	$C_1$ rdfs:subClassOf $C_2$ .
equivalent classes	EquivalentClasses( $C_1 \dots C_n$ )	$C_j$ owl:equivalentClass $C_{j+1}$ . $j=1 \dots n-1$
disjoint classes	DisjointClasses( $C_1$ $C_2$ )	$C_1$ owl:disjointWith $C_2$ .
pairwise disjoint classes	DisjointClasses( $C_1 \dots C_n$ )	$\_ :x$ rdf:type owl:AllDisjointClasses. $\_ :x$ owl:members ( $C_1 \dots C_n$ ).
disjoint union	DisjointUnionOf( $CN$ $C_1 \dots C_n$ )	$CN$ owl:disjointUnionOf ( $C_1 \dots C_n$ ).

# Object property axioms

Language Feature	Functional Syntax	RDF Syntax
subproperty	SubObjectPropertyOf( $P_1 P_2$ )	$P_1$ rdfs:subPropertyOf $P_2$ .
property chain inclusion	SubObjectPropertyOf(ObjectPropertyChain( $P_1 \dots P_n$ ) $P$ )	$P$ owl:propertyChainAxiom ( $P_1 \dots P_n$ ).
property domain	ObjectPropertyDomain( $P C$ )	$P$ rdfs:domain $C$ .
property range	ObjectPropertyRange( $P C$ )	$P$ rdfs:range $C$ .
equivalent properties	EquivalentObjectProperties( $P_1 \dots P_n$ )	$P_j$ owl:equivalentProperty $P_{j+1}$ , $j=1 \dots n-1$
disjoint properties	DisjointObjectProperties( $P_1 P_2$ )	$P_1$ owl:propertyDisjointWith $P_2$ .
pairwise disjoint properties	DisjointObjectProperties( $P_1 \dots P_n$ )	$\_ :x$ rdf:type owl:AllDisjointProperties. $\_ :x$ owl:members ( $P_1 \dots P_n$ ).
inverse properties	InverseObjectProperties( $P_1 P_2$ )	$P_1$ owl:inverseOf $P_2$ .
functional property	FunctionalObjectProperty( $P$ )	$P$ rdf:type owl:FunctionalProperty.
inverse functional property	InverseFunctionalObjectProperty( $P$ )	$P$ rdf:type owl:InverseFunctionalProperty.

# Object property axioms (contd.)

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Language Feature	Functional Syntax	RDF Syntax
reflexive property	ReflexiveObjectProperty(P)	P rdf:type owl:ReflexiveProperty.
irreflexive property	IrreflexiveObjectProperty(P)	P rdf:type owl:IrreflexiveProperty.
symmetric property	SymmetricObjectProperty(P)	P rdf:type owl:SymmetricProperty.
asymmetric property	AsymmetricObjectProperty(P)	P rdf:type owl:AsymmetricProperty.
transitive property	TransitiveObjectProperty(P)	P rdf:type owl:TransitiveProperty.

# Data property axioms

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Language Feature	Functional Syntax	RDF Syntax
subproperty	$\text{SubDataPropertyOf}(R_1 R_2)$	$R_1 \text{ rdfs:subPropertyOf } R_2.$
property domain	$\text{DataPropertyDomain}(R C)$	$R \text{ rdfs:domain } C.$
property range	$\text{DataPropertyRange}(R D)$	$R \text{ rdfs:range } D.$
equivalent properties	$\text{EquivalentDataProperties}(R_1 \dots R_n)$	$R_j \text{ owl:equivalentProperty } R_{j+1}.$ $j=1 \dots n-1$
disjoint properties	$\text{DisjointDataProperties}(R_1 R_2)$	$R_1 \text{ owl:propertyDisjointWith } R_2.$
pairwise disjoint properties	$\text{DisjointDataProperties}(R_1 \dots R_n)$	$\_x \text{ rdf:type}$ $\text{owl:AllDisjointProperties}.$ $\_x \text{ owl:members } ( R_1 \dots R_n ).$
functional property	$\text{FunctionalDataProperty}(R)$	$R \text{ rdf:type owl:FunctionalProperty}.$

# Assertions (ABox statements)

Language Feature	Functional Syntax	RDF Syntax
individual equality	SameIndividual( $a_1 \dots a_n$ )	$a_j$ owl:sameAs $a_{j+1}$ . $j=1 \dots n-1$
individual inequality	DifferentIndividuals( $a_1 \ a_2$ )	$a_1$ owl:differentFrom $a_2$ .
pairwise individual inequality	DifferentIndividuals( $a_1 \dots a_n$ )	$\_x$ rdf:type owl:AllDifferent. $\_x$ owl:members ( $a_1 \dots a_n$ ).
class assertion	ClassAssertion( $C \ a$ )	$a$ rdf:type $C$ .
positive object property assertion	ObjectPropertyAssertion( $PN \ a_1 \ a_2$ )	$a_1$ $PN \ a_2$ .
positive data property assertion	DataPropertyAssertion( $R \ a \ v$ )	$a \ R \ v$ .
negative object property assertion	NegativeObjectPropertyAssertion( $P \ a_1 \ a_2$ )	$\_x$ rdf:type owl:NegativePropertyAssertion. $\_x$ owl:sourceIndividual $a_1$ . $\_x$ owl:assertionProperty $P$ . $\_x$ owl:targetIndividual $a_2$ .
negative data property assertion	NegativeDataPropertyAssertion( $R \ a \ v$ )	$\_x$ rdf:type owl:NegativePropertyAssertion. $\_x$ owl:sourceIndividual $a$ . $\_x$ owl:assertionProperty $R$ . $\_x$ owl:targetValue $v$ .

# XML Schema datatypes in OWL

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- OWL supports **XML Schema** primitive datatypes
  - E.g., integer, real, string, ...
- Strict **separation** between “object” classes and datatypes
  - Disjoint interpretation domain  $\Delta_D$  for datatypes
    - For a datavalue  $d$ ,  $d^{\mathcal{I}} \subseteq \Delta_D$
    - And  $\Delta_D \cap \Delta^{\mathcal{I}} = \emptyset$
  - Disjoint “object” and datatype properties
    - For a datatype property  $P$ ,  $P^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \times \Delta_D$
    - For object property  $S$  and datatype property  $P$ ,  $S^{\mathcal{I}} \cap P^{\mathcal{I}} = \emptyset$
- Equivalent to the “ $(D_n)$ ” in  $\mathcal{SHOIN}(D_n)$

# OWL DL semantics

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- Mapping OWL to equivalent DL ( $\mathcal{SHOIN}(\mathbf{D}_n)$ ):
  - Facilitates provision of reasoning services (using DL systems)
  - Provides **well defined semantics**
- DL semantics defined by **interpretations**:  $\mathcal{I} = (\Delta^{\mathcal{I}}, \cdot^{\mathcal{I}})$ , where
  - $\Delta^{\mathcal{I}}$  is the **domain** (a non-empty set)
  - $\cdot^{\mathcal{I}}$  is an **interpretation function** that maps:
    - **Concept** (class) name  $A \rightarrow$  subset  $A^{\mathcal{I}}$  of  $\Delta^{\mathcal{I}}$
    - **Role** (property) name  $R \rightarrow$  binary relation  $R^{\mathcal{I}}$  over  $\Delta^{\mathcal{I}}$
    - **Individual** name  $i \rightarrow i^{\mathcal{I}}$  element of  $\Delta^{\mathcal{I}}$



# OWL DL ontologies are DL knowledge bases

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- An OWL ontology maps to a DL Knowledge Base

$$\mathcal{K} = \langle \mathcal{T}, \mathcal{A} \rangle$$

- $\mathcal{T}(\text{Tbox})$  is a set of axioms of the form:

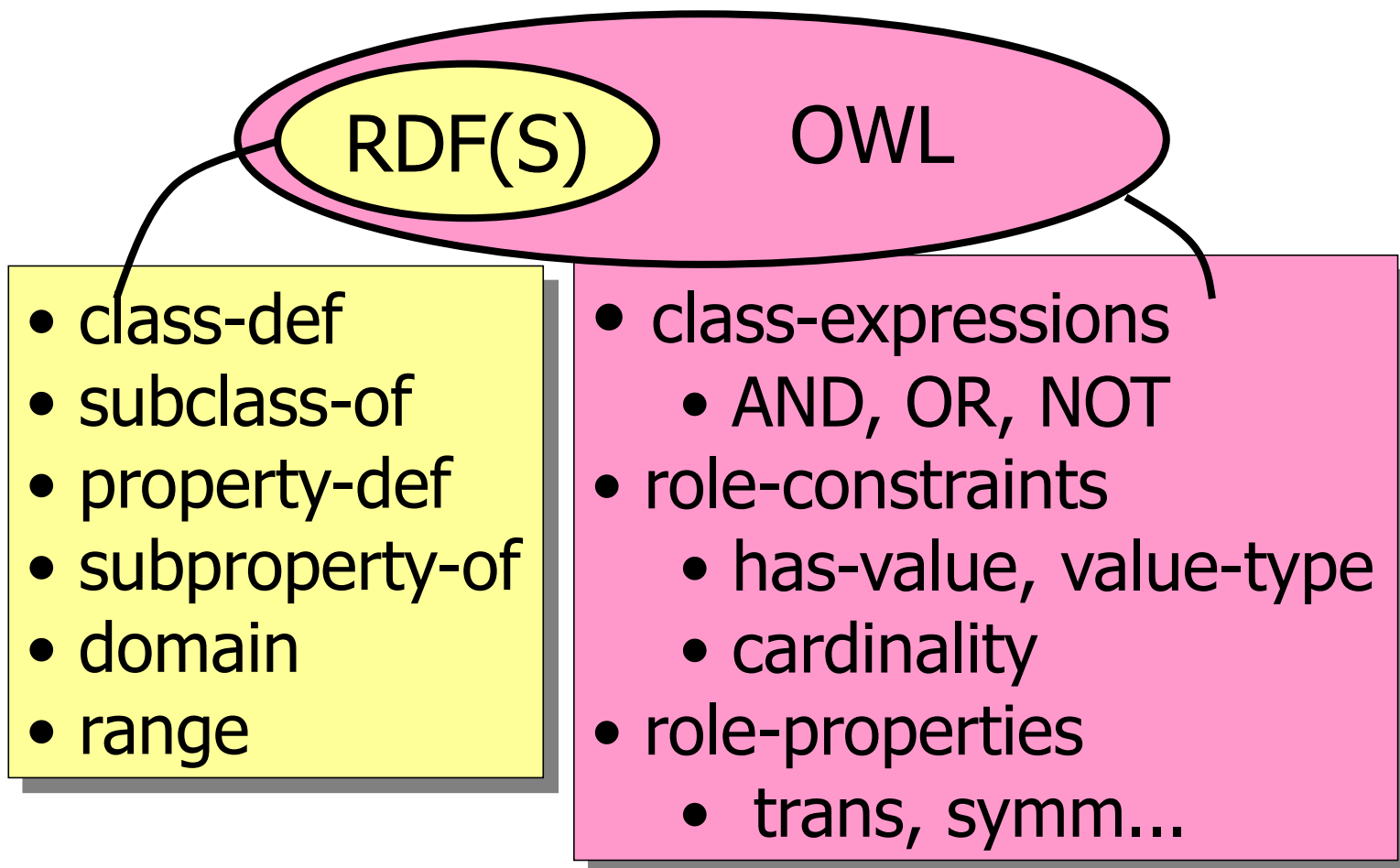
- $C \sqsubseteq D$  (concept inclusion)
- $C \equiv D$  (concept equivalence)
- $R \sqsubseteq S$  (role inclusion)
- $R \equiv S$  (role equivalence)
- $R^+ \sqsubseteq R$  (role transitivity)

- $\mathcal{A}(\text{Abox})$  is a set of axioms of the form

- $x \in D$  (concept instantiation)
- $\langle x, y \rangle \in R$  (role instantiation)

# OWL vs. RDFS

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# OWL vs. First-Order Logic

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- in general, DLs correspond to decidable subclasses of first-order logic (FOL)
- DL KB = first-order theory
- OWL Full is NOT a FOL fragment!
  - reasoning in OWL Full is undecidable
- OWL-DL and OWL-Lite are decidable fragments of FOL

# OWL vs. First-Order Logic

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let  $\mathcal{K} = \langle \mathcal{T}, \mathcal{A} \rangle$  be an ontology about persons where:

- $\mathcal{T}$  contains the following inclusion assertions:

**MALE  $\sqsubseteq$  PERSON**

**FEMALE  $\sqsubseteq$  PERSON**

**MALE  $\sqsubseteq \neg$  FEMALE**

**PERSON  $\sqsubseteq \exists \text{Father}^- . \text{MALE}$**

- $\mathcal{A}$  contains the following instance assertions:

**MALE(Bob)**

**PERSON (Mary)**

**PERSON(Paul)**

# OWL vs. First-Order Logic

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- $\mathcal{T}$  corresponds to the following FOL sentences:

$\forall x. \text{MALE}(x) \rightarrow \text{PERSON}(x)$

$\forall x. \text{FEMALE}(x) \rightarrow \text{PERSON}(x)$

$\forall x. \text{MALE}(x) \rightarrow \neg \text{FEMALE}(x)$

$\forall x. \text{PERSON}(x) \rightarrow \exists y. \text{Father}(y,x) \text{ and } \text{MALE}(y)$

- $\mathcal{A}$  corresponds to the following FOL ground atoms:

$\text{MALE}(\text{Bob})$

$\text{PERSON}(\text{Mary})$

$\text{PERSON}(\text{Paul})$

# Inference tasks in OWL

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- Ontology consistency (corresponds to KB consistency in DL)
- Concept/role consistency (same as DL)
- Concept/role subsumption and equivalence (same as DL)
- Instance checking (same as DL)
- ...

# Inference tasks

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- OWL-DL ontology = first-order logical theory
- verifying the formal properties of the ontology corresponds to **reasoning** over a first-order theory

# Inference tasks

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- OWL-DL ontology = first-order logical theory
- verifying the formal properties of the ontology corresponds to **reasoning** over a first-order theory
- main reasoning tasks over ontologies:
  - consistency of the ontology
  - concept (and role) consistency
  - concept (and role) subsumption
  - instance checking
  - instance retrieval
  - query answering



# Consistency of the ontology

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- Is the ontology  $K=(T,A)$  consistent (non-self-contradictory)?
- i.e., is there at least a model for  $K$ ?
- intensional + extensional reasoning task
- fundamental formal property:
- inconsistent ontology  $\Rightarrow$  there is a semantic problem in  $K$ !
- $K$  must be repaired

# Consistency of the ontology

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Example TBox:

$\text{MALE} \sqsubseteq \text{PERSON}$

$\text{FEMALE} \sqsubseteq \text{PERSON}$

$\text{MALE} \sqsubseteq \neg \text{FEMALE}$

$\text{PERSON} \sqsubseteq \exists \text{hasFather.MALE}$

$\text{PERSON} \sqsubseteq \exists \text{hasMother.FEMALE}$

$\text{hasMother} \sqsubseteq \text{hasParent}$

$\text{hasFather} \sqsubseteq \text{hasParent}$

$\exists \text{hasParent.BLACK-EYES} \sqsubseteq \text{BLACK-EYES}$

# Consistency of the ontology

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Example ABox:

MALE(Bob)

MALE(Paul)

FEMALE(Ann)

hasFather(Ann,Paul)

hasMother(Paul,Mary)

BLACK-EYES(Mary)

$\neg$  BLACK-EYES(Ann)

$\Rightarrow$  TBox + ABox **inconsistent** (Ann should have black eyes)

# Concept consistency

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- is a concept definition  $C$  consistent in a TBox  $T$ ?
- i.e., is there a model of  $T$  in which  $C$  has a non-empty extension?
- intensional (schema) reasoning task
- detects a fundamental modeling problem in  $T$ :
  - if a concept is not consistent, then it can never be populated!

# Concept subsumption

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- is a concept C subsumed by another concept D in T?
- i.e., is the extension of C contained in the extension of D in every model of T?
- intensional (schema) reasoning task
- allows to do classification of concepts (i.e., to construct the concept ISA hierarchy)

# Instance checking

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- is an individual  $a$  a member of concept  $C$  in  $K$ ?
- i.e., is the fact  $C(a)$  satisfied by every interpretation of  $K$ ?
- intensional + extensional reasoning task
- basic “instance-level query” (tell me if object  $a$  is in class  $C$ )

# Instance retrieval

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- find all members of concept  $C$  in  $K$
- i.e., compute all individuals  $a$  such that  $C(a)$  is satisfied by every interpretation of  $K$
- intensional + extensional reasoning task
- (slight) generalization of instance checking

# Query answering

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- compute the answers to a **query**  $q$  in  $K$  (expressed in some query language)
- i.e., compute all tuples of individuals  $t$  such that  $q(t)$  is entailed by  $K$  ( $= q(t)$  is satisfied by every interpretation of  $K$ )
- extensional + extensional reasoning task
- generalization of instance checking and instance retrieval
- e.g.: database queries (SQL-like) over ontologies (or SPARQL-like queries)



# Queries over ontologies

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classes of queries over DL ontologies considered:

- **conjunctive queries** = subclass of SQL queries
  - correspond to select-project-join queries
- **unions of conjunctive queries**
  - correspond to select-project-join-union queries
- **more expressive queries** (e.g., epistemic queries)
- **SPARQL queries**
  - restrictions/extensions of SPARQL

# SPARQL 1.1

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- SPARQL 1.1 is the W3C standard query language over OWL ontologies (released in 2013)
- SPARQL 1.1 has different associated **entailment regimes** that define the semantics of queries over different datasets (RDF models, RDFS+RDF graphs, OWL ontologies)
- the semantics of SPARQL queries for OWL is defined by two entailment regimes for SPARQL:
  - **OWL 2 RDF-based semantics** entailment regime
  - **OWL 2 direct semantics** entailment regime (corresponds to DL semantics)

# Computational aspects of reasoning

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- reasoning in OWL-DL is decidable (and the complexity is characterized)
- however: high computational complexity (EXPTIME)
- (optimized) reasoning algorithms developed
- OWL-DL reasoning tools implemented

# Current OWL technology

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two kinds of tools:

- OWL editors (“environments”)
- OWL reasoners

# OWL editors

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- allow for visualizing/browsing/editing OWL ontologies
- able to connect to an external OWL reasoner  
=> OWL “environments”
- main current tools:
  - Protege
  - SWOOP
  - OWLed2

# OWL reasoning tools

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two categories:

- OWL-DL reasoners, e.g.:
  - Hermit
  - Pellet
  - Konclude
  - Racer, RacerPro
  - Fact++
- reasoners for “tractable fragments” of OWL-DL, e.g.:
  - ELK (OWL 2 EL)
  - Mastro, Ontop (OWL 2 QL)
  - RDFox (OWL 2 RL)

# OWL-DL reasoning tools

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- all tools support “standard” reasoning tasks, i.e.:
  - consistency of the ontology
  - concept consistency
  - concept subsumption and classification
  - instance checking and retrieval
  - query answering (SPARQL)

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