

Exercise 2 Given the following ASP program P:

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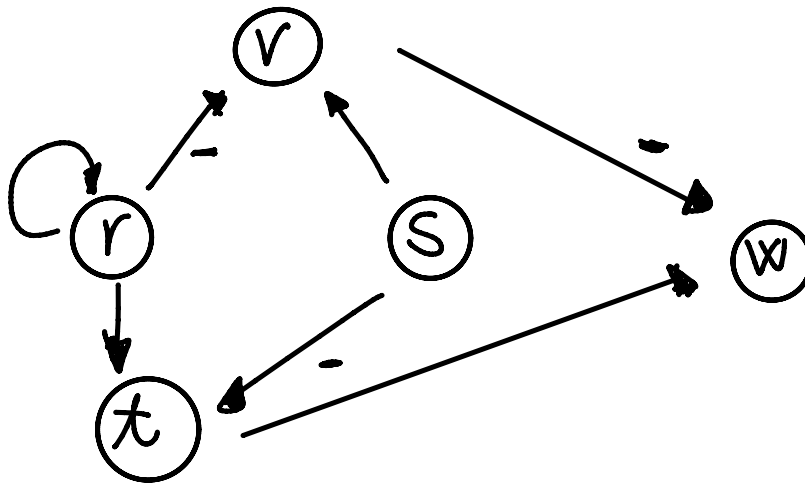
r(x,y) :- g(x,y).
r(x,z) :- g(x,y), r(y,z).
s(x,y) :- g(x,y).
t(x,y) :- r(x,y), not s(x,y).
v(x,y) :- s(x,y), not r(x,y).
w(x,z) :- g(x,y), t(x,y), not v(y,z).
g(a,b). g(b,c). g(d,e). g(e,f).
    
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- tell whether P is stratified;
- compute the answer sets of P.

a)

IDB = {r/2, s/2, t/2, v/2, w/2}

EDB = {g/2}



P is stratified

b)

$S_1 = \{r, s\}$

$S_2 = \{t, v\}$

$S_3 = \{w\}$

$MM0 = EDB(P) = \{g(a,b), g(b,c), g(d,e), g(e,f)\}$

$P(S1) = \{$

$r(x,y) :- g(x,y).$

$r(x,z) :- g(x,y), r(y,z).$

$s(x,y) :- g(x,y).$

$\}$

$I = MM0$

$I' = Tp(I) = \{r(a,b), r(b,c), r(d,e), r(e,f), s(a,b), s(b,c), s(d,e), s(e,f)\}$

$\Delta I = \{\Delta r(a,b), \Delta r(b,c), \Delta r(d,e), \Delta r(e,f),$

$\Delta s(a,b), \Delta s(b,c), \Delta s(d,e), \Delta s(e,f)\}$

$\Delta P = \{$

$\Delta r(x,z) :- g(x,y), \Delta r(y,z).$

$\}$

1-iteration

$I = I \cup \{r(a,b), r(b,c), r(d,e), r(e,f), s(a,b), s(b,c), s(d,e), s(e,f)\}$

$\Delta I = \{\Delta r(a,b), \Delta r(b,c), \Delta r(d,e), \Delta r(e,f), \Delta s(a,b), \Delta s(b,c), \Delta s(d,e), \Delta s(e,f)\}$

$\Delta I = \{\Delta r(a,c), \Delta r(d,f)\}$

2-iteration

$I = I \cup \{r(a,c), r(d,f)\}$

$\Delta I = \{\Delta r(a,c), \Delta r(d,f)\}$

$\Delta I = \{\}$

$MM1 = MM0 \cup \{r(a,b), r(b,c), r(d,e), r(e,f), r(a,c), r(d,f),$
 $s(a,b), s(b,c), s(d,e), s(e,f)\}$

$P(S2) = \{$

$t(x,y) :- r(x,y), \text{not } s(x,y).$

$v(x,y) :- s(x,y), \text{not } r(x,y).$

$\}$

$MM2 = MM1 \cup \{t(a,c), t(d,f)\}$

$P(S3) = \{$
 $w(x,y) :- g(x,y), t(x,y), \text{ not } v(y,z).$
 $\}$

$MM3 = MM2 \cup \{\}$

$MM(P) = \{g(a,b), g(b,c), g(d,e), g(e,f),$
 $r(a,b), r(b,c), r(d,e), r(e,f), r(a,c), r(d,f),$
 $s(a,b), s(b,c), s(d,e), s(e,f),$
 $t(a,c), t(d,f)\}$