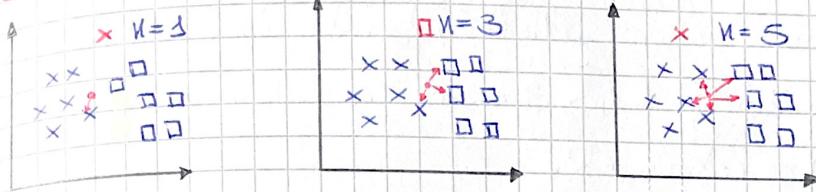


Question 1



In the first and the third case the new instance will be classified as  $x$ , in the second case as  $\square$ .

Question 2

- **Convolutional stage:** in this stage is performed the convolution operation

$$I * K(i, j) = \sum_{m \in S_1} \sum_{n \in S_2} I(m, n) K(i - m, j - n).$$

In this stage are applied two principles:

\* **Sparse connectivity:** each node is not connected to all the nodes of the successive layer but only to the closest.

\* **Parameter sharing:** we force some parameters to have the same value. In this mode we reduce the number of trained parameters.

- **Detector stage:** non-linear activation function (ReLU, Sigmoid).

- **Pooling stage:** we can have max-pooling or average-pooling. In max pooling we compute the max of a rectangular region, in average pooling the average.

Question 3

We want to maximize the data variance after the projection to some direction  $U_1$ :

Projected points:  $U_1^T X_n$ . We want to maximize the projected variance:

$$\max_{U_1} U_1^T S U_1 \text{ St. } U_1^T U_1 = 1 \quad \text{This is equivalent to}$$

$$\max_{U_1} U_1^T S U_1 + \lambda_3 (1 - U_1^T U_1). \quad \text{If we set the derivative to 0:}$$

$$S U_1 = \lambda_3 U_1 \quad U_1 \text{ must be an eigenvector of } S.$$

$U_1^T S U_1 = \lambda_3$  is the variance after the projection.

The variance is maximum if  $U_1$  is the eigenvector corresponding to the largest eigenvalue  $\lambda_3$ . This is called principal component.

### Question 4

We can use a MDP =  $\langle X, A, \delta, r \rangle$  with  $X$  set of states and  $X = \{l_s, r_s\}$  left and right side of the river,  $A$  set of actions with  $A = \{br_1, br_2, br_3\}$  that are the 3 possible actions: traverse bridge 1, 2, 3.  $\delta$  is the transition function of  $X \times A \rightarrow X$  and  $r$  is the reward function  $r: X \times A \rightarrow \mathbb{R}$ .

For this problem we can use Q-Learning:

For each  $x$  we initialize  $\hat{Q}(0)(x, a) \leftarrow 0$

We observe the current state;

for each time  $t = 1 \dots T$

We choose an action and we execute this action;

We collect the reward and we observe the new state;

$$\hat{Q}(t)(n, a) \leftarrow r + \gamma \max_{a' \in A} \hat{Q}(t-1)(n', a')$$

The optimal policy is  $\pi^*(n) = \arg \max_{a \in A} \hat{Q}(t)(n, a)$

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We can use the  $\epsilon$ -greedy policy for balancing exploration and exploitation:

We choose exploration with probability  $\epsilon$  and exploitation with probability  $1 - \epsilon$ .

### Question 5

Given a classification problem with  $K$  classes is possible to compute, using a confusion matrix, how many times an instance of a class  $C_i$  is classified into a class  $C_j$ .

	LOW	MED	HIGH
LOW	20	20	10
MED	5	10	15
HIGH	5	5	40

3). The accuracy is the sum of the elements in the main diagonal divided by the sum of all the elements.

$$\text{accuracy} = \frac{20+10+40}{150} = \frac{70}{150} \approx 50\%$$

### Question 6

1).  $E(\mathbf{N}) = \frac{1}{2} \sum_{n=1}^N (t_n - \mathbf{N}^\top \phi(x_n))$  is the error function.

2).  $\phi_4(x, y) = xy \quad \phi_5(x) = x^2 \Rightarrow y(\underline{x}) = N_1 n_1 + N_2 n_2 + N_3 n_3 + N_4 \phi_4(x_1, x_2) + N_5 \phi_5(x_3)$

3). We can use Sequential learning:  $\hat{\mathbf{w}} \leftarrow \hat{\mathbf{w}} + \eta [t_n - \mathbf{N}^\top \phi(x_n)] \phi(x_n)$