

Answer to the question no. 1

	1	2	3	4	5	6
1	(1, 1) ✓	(1, 2) ✓	(1, 3) ✓	(1, 4) ✓	(1, 5) ✓	(1, 6) ✓
2	(2, 1) ✓	(2, 2) ✓	(2, 3) ✓	(2, 4) ✓	(2, 5) ✓	(2, 6) ✓
3	(3, 1) ✓	(3, 2) ✓	(3, 3) ✓	(3, 4) ✓	(3, 5) ✓	(3, 6) ✓
4	(4, 1) ✓	(4, 2) ✓	(4, 3) ✓	(4, 4) ✓	(4, 5) ✓	(4, 6) ✓

Total number of trials ~~for~~ = 24

The possible values of x are the numbers 2 through 12. $x = 2$ is the event and $x = 2, \dots$

total events are 11.

x	2	3	4	5	6	7	8	9	10
$P(x)$	$\frac{1}{24}$	$\frac{2}{24}$	$\frac{3}{24}$	$\frac{4}{24}$	$\frac{4}{24}$	$\frac{4}{24}$	$\frac{3}{24}$	$\frac{2}{24}$	$\frac{1}{24}$

The table is the probability distribution.

Answer to the question no: 2

Total number of trials for throwing
a Four & a Six sided die's are 24.

[From (1)]

Therefore, the number of trials to expect

a total 26 is, $46 - 24 = 22 + 1 = 23$

(1,1) (1,1) (1,1) (1,1) (1,1) (1,1) (1,1) (1,1)
(1,1) (1,1) (1,1) (1,1) (1,1) (1,1) (1,1) (1,1)
(1,1) (1,1) (1,1) (1,1) (1,1) (1,1) (1,1)

= 23 trials for the worst case

Ans

Answer to the question no: 3

The event $(7 \geq x \geq 5)$ is the union of mutually exclusive events $X=7, X=6$

& $X=5$ Thus,

$$P(7 \geq x \geq 5) = P(7) + P(6) + P(5)$$

$$= \frac{4}{24} + \frac{4}{24} + \frac{4}{24}$$

$$= 0.5$$

Ans

Answer to the question no: 4

If receiving 2 from exactly one of the two die is success then the probability is,

$$\frac{9}{24} = 0.375$$

$$n = 8, r = 3 \text{ so } p = 0.375$$

~~$${}^nC_r \cdot (1-p)^{n-r} \cdot (1)$$~~

$${}^nC_r (1-p)^{n-r} \cdot (p)^r$$

$$= {}^8C_3 (1-0.375)^{8-3} \cdot (0.375)^3$$

$$= 56 \times 0.0954 \times 0.05273$$

$$= 0.28170$$

Ans

Answer to the question no: 5

We know, $E(x) = \sum_{k=-\infty}^{\infty} k P(x=k)$

We know, $P(x) = E(x)/V(x)$

$E(x)$ = number of events

$V(x)$ = total number of trials = 3 Ans

$$0.1K = E(x)/3$$

$$\therefore E(x) = 0.3K$$

Ans

Answer to the question no. 6
We know,

$$P(Y) = E(Y)/V(Y)$$

$E(Y)$ = number of events

$V(Y)$ = Total number of trials

$$\therefore P(Y) = \frac{1}{3} \\ = 0.333$$

Therefore, the probability of Richard catching a ball thrown to him is 0.333 Ans

Answer to the question no. 7

First,

3 numbers are divisible by both 7 & 9

and they are $\{63, 126, 189\}$

Second,

There are, $\frac{200}{7-3} = 25$ numbers that are divisible by 7 only.

Third, There are, $\frac{200}{9-3} = 19$ numbers that are divisible by 9 only.

Therefore, there are $25 + 19 = 44$ ^{Ans}
numbers in the set that are divisible
by either 7 or 9 but not both.
Ans

Answer to the question no: 8

First, there are $\frac{200}{3} = 66$ numbers
that are divisible by 3.

Second, $\frac{200}{4} = 50$ numbers that are
divisible by 4 ~~and~~

Third, $\frac{200}{12} = 16$ numbers that are divisible
by 12.

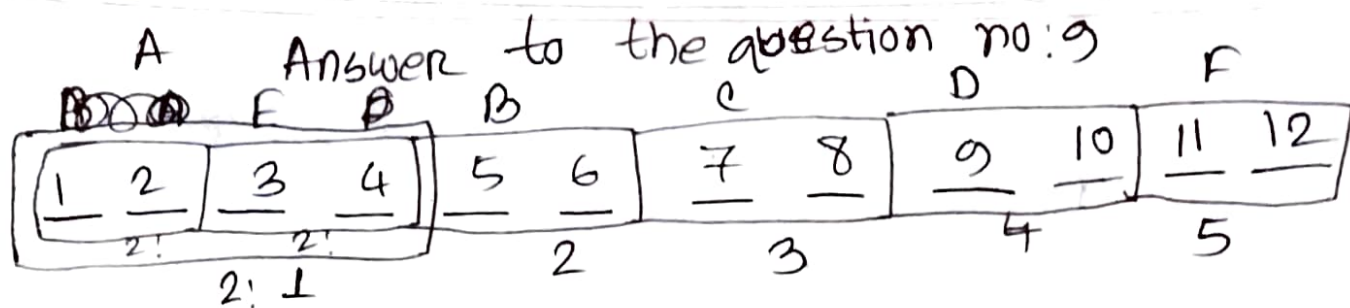
Also, $66 + 50 + 16 = 116 - 16 = 100$,

there are 100 numbers that are

divisible by 3 or 4 or 12.

Lastly, $200 - 100 = 100$ numbers that
are not divisible by 3, 4 or 12.

Ans: 100



$$5! \times 2! \times 2! \times 2! = 192 \text{ ways. } \underline{\text{Ans}}$$

Answer to the question no: 10

Given, $E(X) = 8$ let, X be the random variable
 $E(Y) = 26$ distribution with, $a=1$,
 $P(X)$ $b=6$ & $n = b - a + 1 = 6$

So, Mean, $\frac{(a+b)}{2} = \frac{7}{2}$ and for the second,

$$\frac{n^2-1}{12} + \frac{a+b}{4} = \frac{91}{6}$$

Now, $E(X) = E(U_1 + U_2 + U_3)$
 $= E(U_1) + E(U_2) + E(U_3)$
 $= 2\frac{1}{2}$

for the sum,

$$E(x) = E(x_1^2) + E(x_2^2) + E(x_3^2)$$

$$= 3 \times \frac{31}{6}$$

$$= \frac{31}{2}$$

$$= 45.5 \quad \underline{\text{Ans}}$$

Answer to the question no: 11

Brac University Building lift stops on the top & the ground floor without any call and if the lift is going up it will go up first and then receive going down call

The probability will be $\frac{10}{11}$ Ans

as there are 10 floors below

Answer to the question no: 12

Tamim's best friend (B) wants to beat in between Tamim (T) & other friend (O), they can seat in ABO, OBA 2 ways.
and for 8 friends there can be.

$$2 \times 6! = 1440 \text{ ways.}$$

Ans

Answer to the question no: 13

Given, $P(\text{Infected}) = 8\%$

$$P(\text{Not Infected}) = (100 - 8)\% = 92\%$$

$$P(\text{Positive \& Infected}) = 95\%$$

$$P(\text{Negative \& Infected}) = (100 - 95)\% = 5\%$$

$$P(\text{Positive \& Not infected}) = 3\%$$

$$P(\text{Negative \& Not infected}) = (100 - 3)\% = 97\%$$

$$P(\text{Not Infected \& Negative}) = \frac{P(\text{Negative \& Not Infected}) \cdot P(\text{Not Infected})}{P(\text{Negative \& Not Infected}) \cdot P(\text{Not Infected}) + P(\text{Negative \& Infected}) \cdot P(\text{Infected})}$$

$$= \frac{(97 \times 92)\%}{97 \times 92 + 5 \times 8}$$

$$= \left(\frac{(97 \times 92)}{(97 \times 92) + (5 \times 8)} \right)\%$$

$$= 1.05\% \quad \underline{\text{Ans}}$$

Answer to the question no: 14

$$\left(5u + \frac{3}{y} + \frac{4}{u} + \frac{5}{7}y\right)^8$$

$$= \cancel{8C_0} (5u)^8 \cdot \left(\frac{3}{y}\right)$$

$$= \left(5u + \frac{4}{u} + \frac{3}{y} + \frac{5}{7}y\right)^8$$

$$= \left(\frac{20u+4}{u} + \frac{21+5y^2}{7y}\right)^8$$

$$= {}^8C_0 \left(\frac{20u+4}{u}\right)^8 \cdot \left(\frac{21+5y^2}{7y}\right)^0 + {}^8C_1 \left(\frac{20u+4}{u}\right)^7 \left(\frac{21+5y^2}{7y}\right)^1$$

$$+ {}^8C_2 \left(\frac{20u+4}{u}\right)^6 \left(\frac{21+5y^2}{7y}\right)^2 + {}^8C_3 \left(\frac{20u+4}{u}\right)^5 \left(\frac{21+5y^2}{7y}\right)^3$$

$$+ {}^8C_4 \left(\frac{20u+4}{u}\right)^4 \left(\frac{21+5y^2}{7y}\right)^4 + {}^8C_5 \left(\frac{20u+4}{u}\right)^3 \left(\frac{21+5y^2}{7y}\right)^5$$

$$+ {}^8C_6 \left(\frac{20u+4}{u}\right)^2 \left(\frac{21+5y^2}{7y}\right)^6 + {}^8C_7 \left(\frac{20u+4}{u}\right)^1 \left(\frac{21+5y^2}{7y}\right)^7$$

$$+ {}^8C_8 \left(\frac{20u+4}{u}\right)^0 \left(\frac{21+5y^2}{7y}\right)^8$$

Answer to the question no: 15

There are $4C_2 = 6$ games within each
of eight groups

Altogether, $6 \times 8 = 48$ games
Ans