## **Tutorial Week 3**

## **Trigonometry revision**

1. Sketch the graphs of  $\sin \theta$  and  $\cos \theta$ , and extend the following table of trigonometric values to  $\theta = 2\pi$ :

	0	π/6	π/4	π/3	π/2
sin	0	1/2	1/√2	$\sqrt{3}/2$	1
cos	1	$\sqrt{3}$ / 2	$1/\sqrt{2}$	1/2	0
tan	0	1/√3	1	$\sqrt{3}$	*

2. Write down the value of  $\theta$  for each of the following pairs of sines and cosines, and state the quadrant in which each lies:

(i) 
$$\cos \theta = 1/\sqrt{2}$$
,  $\sin \theta = -1/\sqrt{2}$  (ii)  $\cos \theta = -1/\sqrt{2}$ ,  $\sin \theta = 1/\sqrt{2}$ 

(iii) 
$$\cos \theta = -1/\sqrt{2}$$
,  $\sin \theta = -1/\sqrt{2}$  (iv)  $\cos \theta = \sqrt{3}/2$ ,  $\sin \theta = 1/2$ 

(v) 
$$\cos \theta = \sqrt{3} / 2$$
,  $\sin \theta = -1/2$  (vi)  $\cos \theta = -\sqrt{3} / 2$ ,  $\sin \theta = -1/2$ .

3. Show that  $tan(\pi / 12) = 2 - \sqrt{3}$ .

4. Show that 
$$\cos\left(\theta + \frac{\pi}{3}\right) + \sin\left(\theta + \frac{\pi}{6}\right) = \cos\theta$$
.

5. Solve the equation  $\cos 2x - 5\cos x = 2$  in the interval  $0 \le x \le 2\pi$ .

6. Show that 
$$2\cot\left(\frac{x}{2}\right)\left(1-\cos^2\left(\frac{x}{2}\right)\right) = \sin x$$
.

7. Show that  $\cos 3\theta = 4\cos^3 \theta - 3\cos \theta$ .