

# The Berkson Measurement Error (MEB) model

## Parametrization

This is an implementation of the Berkson measurement error model for a fixed effect. The observed covariate is  $w$  but it is  $x$  that goes into the linear predictor

$$\eta = \dots + \beta x + \dots ,$$

where  $x = w + u$ ,  $u$  is Gaussian with precision  $\tau_u \times s$ , and  $s$  is a vector of fixed scalings.

## Hyperparameters

This model has 2 hyperparameters,  $\theta = (\theta_1, \theta_2)$ . The hyperparameter specification is as follows:

$$\theta_1 = \beta$$

and the prior is defined on  $\theta_1$ ,

$$\theta_2 = \log(\tau_u)$$

and the prior is defined on  $\theta_2$ .

## Specification

The MEB is specified inside the `f()` function as

```
f(w, [<weights>], model="meb", hyper = <hyper>, scale = <s>)
```

Here, `w` are the observed covariates, and the fixed scaling of the observational precision is given in argument `scale`. If the argument `scale` is not given, then  $s$  is set to 1.

Note that only the unique values of `w` are used, so if two or more elements of `w` are *identical*, then they refer to the *same* element in the covariate  $x$ .

## Hyperparameter specification and default values

### hyper

#### theta1

```
name    beta
short.name  b
prior    gaussian
param    1 0.001
initial  1
fixed    FALSE
to.theta function(x) x
from.theta function(x) x
```

#### theta2

```
name    prec.obs
short.name  prec
prior    loggamma
param    1 1e-04
initial  6.90775527898214
fixed    FALSE
```

```

    to.theta function(x) log(x)
    from.theta function(x) exp(x)

constr FALSE

nrow.ncol FALSE

augmented FALSE

aug.factor 1

aug.constr

n.div.by

n.required FALSE

set.default.values FALSE

status experimental

pdf meb

```

## Example

```

n = 100
beta = 2
w = rnorm(n)
prec.u = 1
prec.y = 1
s = runif(n,min=0,max=1)
x = w + rnorm(n, sd = 1/sqrt(s*prec.u))
y = 1 + beta*x + rnorm(n, sd = 1/sqrt(prec.y))

## prior parameters
prior.beta = c(0, 0.0001)
prior.prec.u = c(10, 9/prec.u)
prior.prec.y = c(10, 9/prec.y)

formula = y ~ f(w,model="meb", scale=s,
               hyper = list(
                 beta = list(
                   param = prior.beta,
                   fixed = FALSE
                 ),
                 prec.obs = list(
                   param = prior.prec.u,
                   fixed = FALSE
                 )
               )
)

r = inla(formula, data = data.frame(y, w, s),
         family = "gaussian",

```

```

control.family = list(
  hyper = list(
    prec = list(param = prior.prec.y,
                 fixed = FALSE
                )
          )
)

```

## Notes

- INLA provide the posterior of  $\nu = \beta x$  and NOT  $x$ . The results comes in the order given by the sorted (from low to high) values of  $\mathbf{x}$  and the field ID gives the mapping.