

# Bym model for spatial effects

## Parametrization

This model is simply a union of the besag model  $u$  and a iid model  $v$ , so that

$$x = \begin{pmatrix} v + u \\ u \end{pmatrix}$$

Note that the length of  $x$  is  $2n$  if the length of  $u$  (and  $v$ ) is  $n$ . The benefite is that this allows to get the posterior marginals of the sum of the spatial and iid model; otherwise it offers no advantages.

## Hyperparameters

The hyperparameters are the precision  $\tau_1$  of the iid model ( $v$ ) and the precision  $\tau_2$  of the besag model ( $u$ ). The precision parameters are represented as

$$\theta = (\theta_1, \theta_2) = (\log \tau_1, \log \tau_2)$$

and the prior is defined on  $\theta$ .

## Specification

The bym model is specified inside the `f()` function as

```
f(<whatever>, model="bym", graph=<graph>,  
  hyper=<hyper>, adjust.for.con.comp = TRUE,  
  scale.model = FALSE)
```

The neighbourhood structure of  $\mathbf{x}$  is passed to the program through the `graph` argument.

The option `adjust.for.con.comp` adjust the model if the graph has more than one connected component, and this adjustment can be disabled setting this option to `FALSE`. This means that `constr=TRUE` is interpreted as a sum-to-zero constraint on *each* connected component and the `rankdef` parameter is set accordingly.

The logical option `scale.model` determine if the besag-model-part of the model  $u$  should be scaled to have an average variance (the diagonal of the generalized inverse) equal to 1. This makes prior spesification much easier. Default is `FALSE` so that the model is not scaled.

## Hyperparameter spesification and default values

### hyper

#### theta1

```
hyperid 10001  
name log unstructured precision  
short.name prec.unstruct  
prior loggamma  
param 1 5e-04  
initial 4  
fixed FALSE  
to.theta function(x) log(x)  
from.theta function(x) exp(x)
```

#### theta2

```

hyperid 10002
name log spatial precision
short.name prec.spatial
prior loggamma
param 1 5e-04
initial 4
fixed FALSE
to.theta function(x) log(x)
from.theta function(x) exp(x)

constr TRUE

nrow.ncol FALSE

augmented TRUE

aug.factor 2

aug.constr 2

n.div.by

n.required TRUE

set.default.values TRUE

pdf bym

```

## Example

For examples of application of this model see the **Bym** example in Volume I.

## Notes

The term  $\frac{1}{2} \log(|R|^*)$  of the normalisation constant is not computed, hence you need to add this part to the log marginal likelihood estimate, if you need it. Here  $R$  is the precision matrix with a unit precision parameter for the Besag part of the model.