# Proportional odds model

### **Parametrisation**

The proportional odds model, is for discrete observations

$$y \in \{1, 2, \dots, K\}, \qquad K > 1,$$

defined via the cumulative distribution function

$$F(k) = \text{Prob}(y \le k) = \frac{\exp(\gamma_k)}{1 + \exp(\gamma_k)}$$

where

$$\gamma_k = \alpha_k - \eta.$$

 $\{\alpha_k\}$  is here increasing sequence of K-1 cut-off points, and  $\eta$  is the linear predictor,

$$\alpha_0 = -\infty < \alpha_1 < \alpha_2 < \ldots < \alpha_{K-1} < \alpha_K = 1$$

The likelihood for an observation is then

$$Prob(y = k) = F(k) - F(k-1).$$

#### **Link-function**

There is no option here.

## Hyperparameters

The hyperparameters are  $\theta_1, \ldots, \theta_{K-1}$ , where

$$\alpha_1 = \theta_1$$
,

and

$$\alpha_k = \alpha_{k-1} + \exp(\theta_k) = \theta_1 + \sum_{j=2}^k \exp(\theta_j)$$

for k = 2, ..., K - 1.

## **Specification**

- family = pom
- Required arguments: y (observations)

Number of classes, K is determined as the maximum of the observations. Empty classes are not allowed.

## Example

In the following example we estimate the parameters in a simulated example with Poisson responses.

## POM example

### Notes