Besag model for spatial effects

Parametrization

The besag model for random vector $\mathbf{x} = (x_1, \ldots, x_n)$ is defined as

$$x_i | x_j, i \neq j, \tau \sim \mathcal{N}(\frac{1}{n_i} \sum_{i \sim j} x_j, \frac{1}{n_i \tau}) \tag{1}$$

where n_i is the number of neighbours of node i, $i \sim j$ indicates that the two nodes i and j are neighbours.

Hyperparameters

The precision parameter τ is represented as

$$\theta_1 = \log \tau$$

and the prior is defined on θ_1.

Specification

The besag model is specified inside the `f()` function as

```
 f(<whatever>,model="besag",graph=<graph>,
   hyper=<hyper>, adjust.for.con.comp = TRUE)
```

The neighbourhood structure of $\mathbf{x}$ is passed to the program through the `graph` argument.

If the option `adjust.for.con.comp=TRUE` then the model is adjusted if the graph has more than one connected compoment. This adjustment can be disabled setting this option to `FALSE`. If `adjust.for.con.comp=TRUE` then `constr=TRUE` is interpreted as a sum-to-zero constraint on *each* connected component in the graph and the `rankdef` parameter is set to the number of connected components.

Hyperparameter spesification and default values

hyper

> **theta**
>> **name** log precision
>> **short.name** prec
>> **prior** loggamma
>> **param** 1 5e-05
>> **initial** 4
>> **fixed** FALSE
>> **to.theta** function(x) log(x)
>> **from.theta** function(x) exp(x)

constr TRUE

nrow.ncol FALSE

augmented FALSE

aug.factor 1

aug.constr

n.div.by

n.required TRUE

set.default.values TRUE

pdf besag

Example

For examples of application of this model see the `Bym`, `Munich`, `Zambia` or `Scotland` examples in Volume I.

Notes

The besag model intrinsic with rankdef 1.