## **NMix**

### Parametrisation

The N-Mixture distribution is a Poisson mixture of the Binomials, as

$$Prob(y) = \sum_{n=y}^{\infty} {n \choose y} p^n (1-p)^{n-y} \times \frac{\lambda^n}{n!} \exp(-\lambda)$$

for responses y = 0, 1, 2, ..., n, where n is Poisson number of trials, and p is probability of success. Replicated reponses  $y_1, y_2, ..., y_r$ , are iid from the Binomial, given (a common) n from the Poisson,

$$\operatorname{Prob}(y_1, \dots, y_r) = \sum_{n=\max\{y_1, \dots, y_r\}}^{\infty} \left\{ \prod_{i=1}^r \binom{n}{y_i} p^n (1-p)^{n-y_i} \right\} \times \frac{\lambda^n}{n!} \exp(-\lambda)$$

### **Link-function**

The probability p is linked to the linear predictor by

$$p(\eta) = \frac{\exp(\eta)}{1 + \exp(\eta)}$$

for the default logit link, while  $\lambda$  depends on fixed covariates

$$\log(\lambda) = \sum_{j=1}^{m} \beta_j x_j$$

with one vector of covariates for each observation. m can be maximum 10 and minimum 1.

## Hyperparameters

The parameters  $\theta_1 = \beta_1, \theta_2 = \beta_2, \dots, \theta_m = \beta_m$ .

#### Hyperparameter spesification and default values

### hyper

#### theta1

**hyperid** 101101

name beta1

short.name beta1

initial 2.30258509299405

fixed FALSE

**prior** normal

**param** 0 0.5

to.theta function(x) x

from.theta function(x) x

## theta2

**hyperid** 101102

name beta2

short.name beta2

```
initial 0
    fixed FALSE
    prior normal
    param 01
    to.theta function(x) x
    from.theta function(x) x
theta3
    hyperid 101103
    name beta3
    short.name beta3
    initial 0
    fixed FALSE
    prior normal
    param 01
    to.theta function(x) x
    from.theta function(x) x
theta4
    hyperid 101104
    name beta4
    short.name beta4
    initial 0
    fixed FALSE
    prior normal
    param 01
    to.theta function(x) x
    from.theta function(x) x
theta5
    hyperid 101105
    name beta5
    short.name beta5
    initial 0
    fixed FALSE
    prior normal
    param 0 1
    to.theta function(x) x
    from.theta function(x) x
theta6
    hyperid 101106
    name beta6
    short.name beta6
    initial 0
    fixed FALSE
    prior normal
    param 0 1
```

```
to.theta function(x) x
    from.theta function(x) x
theta7
    hyperid 101107
    name beta7
    short.name beta7
    initial 0
    fixed FALSE
    prior normal
    param 01
    to.theta function(x) x
    from.theta function(x) x
theta8
    hyperid 101108
    name beta8
    short.name beta8
    initial 0
    fixed FALSE
    prior normal
    param 01
    to.theta function(x) x
    from.theta function(x) x
theta9
    hyperid 101109
    name beta9
    short.name beta9
    initial 0
    fixed FALSE
    prior normal
    param 0 1
    to.theta function(x) x
    from.theta function(x) x
theta10
    hyperid 101110
    name beta10
    short.name beta10
    initial 0
    fixed FALSE
    prior normal
    param 0 1
    to.theta function(x) x
    from.theta function(x) x
```

status experimental

```
survival FALSE
```

discrete TRUE

link default logit probit

pdf nmix

# Specification

- family = nmix
- Required arguments: the response Y and covariates X as inla.mdata(Y, X [, additional.covariates])

The response is a matrix where each row are replicates, where responses that are NA's are ignored. The covariates is one or many vectors, matrices or data frames. Each row of the covariates  $(x_{i1}, x_{i2}, \ldots, x_{im})$  defines the covariates used for the *i*'th response(s) (the *i*'th row of Y). Note that  $\beta_{m+1}, \ldots, \beta_{10}$  are fixed to zero.

# Example

In the following example we estimate the parameters in a simulated example with replications.

```
nrep = 5
n = 50
y = matrix(NA, n, nrep)
x = c()
xx = c()
intercept = 1
for(i in 1:n) {
    local.x = runif(1) - 0.5
    lambda = exp(2 + local.x)
    N = rpois(1, lambda)
    local.xx = runif(1) - 0.5
    eta = intercept + local.xx
    p = \exp(eta)/(\exp(eta) + 1)
    nr = sample(1:nrep, 1)
    y[i, 1:nr] = rbinom(nr, size = N, prob = p)
    x = c(x, local.x)
    xx = c(xx, local.xx)
}
Y = inla.mdata(y, 1, x)
r = inla(Y ~1 + xx,
         data = list(Y=Y, xx=xx),
         family = "nmix",
         control.fixed = list(prec.intercept=1, prec=1))
```

# Notes