

Sigmoidal effect of a covariate

Parametrization

This model implements a non-linear effect of a positive covariate x as a part of the linear predictor. It comes in two variants, *sigmoidal*

$$\beta \frac{x^k}{x^k + a^k} \quad \text{or} \quad \beta \frac{z}{z + 1}$$

with $z = (x/a)^k$, $x \geq 0$, $k > 0$ and $a > 0$, and the *reverse-sigmoidal*

$$\beta \frac{a^k}{x^k + a^k} \quad \text{or} \quad \beta \frac{1}{z + 1}.$$

Here, a is the halflife parameter, k the shape-parameter and β the scaling.

Hyperparameters

This model has three hyperparameters, the scaling β , halflife a and shape k ,

$$\theta_1 = \beta \quad \theta_2 = \log(a) \quad \theta_3 = \log(k)$$

and the priors are given for θ_1, θ_2 and θ_3 .

Specification

```
f(x, model="sigm",    hyper = ..., precision = <precision>)
f(x, model="revsigm", hyper = ..., precision = <precision>)
```

where `precision` is the precision for the tiny noise used to implement this as a latent model.

Hyperparameter specification and default values

hyper

theta1

```
hyperid 38001
name beta
short.name b
initial 1
fixed FALSE
prior normal
param 1 10
to.theta function(x) x
from.theta function(x) x
```

theta2

```
hyperid 38002
name loghalflife
short.name halflife
initial 3
fixed FALSE
```

```

    prior loggamma
    param 3 1
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
  theta3
    hyperid 38003
    name logshape
    short.name shape
    initial 0
    fixed FALSE
    prior loggamma
    param 10 10
    to.theta function(x) log(x)
    from.theta function(x) exp(x)

  constr FALSE

  nrow.ncol FALSE

  augmented FALSE

  aug.factor 1

  aug.constr

  n.div.by

  n.required FALSE

  set.default.values FALSE

  status experimental

  pdf sigm

```

Example

```

sigm = function(x, halflife, shape = 1)
{
  xx = (x/halflife)^shape
  return (xx/(1.0+xx))
}
revsigm = function(x, halflife, shape = 1)
{
  xx = (x/halflife)^shape
  return (1.0/(1.0+xx))
}

n = 1000
lambda = 10
s=0.01
x = rpois(n, lambda = lambda)
halflife = lambda

```

```
shape = 2
```

```
y = sigm(x, halflife, shape) + rnorm(n, sd = s)
r = inla(y ~ -1 + f(x, model="sigm"),
        data = data.frame(y, x),
        family = "gaussian",
        control.family = list(
            hyper = list(
                prec = list(
                    initial = log(1/s^2),
                    fixed = TRUE))))
summary(r)
```

```
y = revsigm(x, halflife, shape) + rnorm(n, sd = s)
r = inla(y ~ -1 + f(x, model="revsigm"),
        data = data.frame(y, x),
        family = "gaussian",
        control.family = list(
            hyper = list(
                prec = list(
                    initial = log(1/s^2),
                    fixed = TRUE))))
summary(r)
```

Notes

None