# Generic3 model

# Parametrization

The generic3 model implements the following precision matrix

$$\mathbf{Q} = \tau_{\text{common}} \sum_{i=1}^{m} \tau_i \mathbf{R}_i, \qquad 1 < m \le 10, \tag{1}$$

where each  $R_i \geq 0$ , and  $\tau_i$  is the specific precision parameter and  $\tau_{\text{common}}$  is a shared one.

# Hyperparameters

The hyperparameters are defined as

$$\theta_i = \log(\tau_i), \qquad i = 1, 10$$

and

$$\theta_{11} = \log(\tau_{\text{common}})$$

and priors are assigned to  $(\theta_1, \theta_2, \ldots)$ .

# Specification

The generic3 model is specified inside the f() function as

```
f(<whatever>, model="generic3", Cmatrix = <list.of.Cmat>, hyper = <hyper>)
```

where cf.Cmat> a list of length m (maximum 10) of  $R_i$ -matrices. By default,  $\theta_j$  for  $j = m+1,\ldots,11$  is set to fixed (this includes  $\tau_{\text{common}}$ ).

### Hyperparameter spesification and default values

### hyper

```
theta1
```

name log precision1

short.name prec1

initial 4

fixed FALSE

prior loggamma

**param** 1 5e-05

to.theta function(x) log(x)

from.theta function(x) exp(x)

### theta2

name log precision2

short.name prec2

initial 4

fixed FALSE

prior loggamma

**param** 1 5e-05

to.theta function(x) log(x)

```
from.theta function(x) exp(x)
theta3
    name log precision3
    short.name prec3
    initial 4
    fixed FALSE
    prior loggamma
    param 1 5e-05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
theta4
    name log precision4
    short.name prec4
    initial 4
    fixed FALSE
    prior loggamma
    param 1 5e-05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
theta5
    name log precision5
    short.name prec5
    initial 4
    fixed FALSE
    prior loggamma
    param 1 5e-05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
theta6
    name log precision6
    short.name prec6
    initial 4
    fixed FALSE
    prior loggamma
    param 1 5e-05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
theta7
    name log precision7
    short.name prec7
    initial 4
    fixed FALSE
    prior loggamma
    param 1 5e-05
```

```
to.theta function(x) log(x)
         from.theta function(x) exp(x)
    theta8
         name log precision8
         short.name prec8
        initial 4
         fixed FALSE
         prior loggamma
         param 1 5e-05
         to.theta function(x) log(x)
         from.theta function(x) exp(x)
    theta9
         name log precision9
         short.name prec9
         initial 4
        fixed FALSE
         prior loggamma
         param 1 5e-05
         to.theta function(x) log(x)
         from.theta function(x) exp(x)
    theta10
         name log precision10
        short.name prec10
        initial 4
         fixed FALSE
         prior loggamma
         param 1 5e-05
         to.theta function(x) log(x)
         from.theta function(x) exp(x)
    theta11
         name log precision common
         short.name prec.common
        initial 0
         fixed TRUE
         prior loggamma
         param 1 5e-05
         to.theta function(x) log(x)
         from.theta function(x) exp(x)
constr FALSE
nrow.ncol FALSE
augmented FALSE
aug.factor 1
```

```
aug.constr
n.div.by
n.required TRUE
set.default.values TRUE
status experimental
pdf generic3
Example
make.sm = function(n, prob = 0.1)
    A = matrix(runif(n*n), n, n)
    Patt = matrix(runif(n*n), n, n)
    Patt[Patt > prob] = 0
    A = A * Patt
    diag(A) = runif(n)
    A = A %*% t(A)
    A = A / \max(\operatorname{diag}(A))
    return (inla.as.sparse(A))
}
nsim = 100
n = 5
m = 3
Cmat = list()
Q = inla.as.sparse(matrix(0, n, n))
for(i in 1:m) {
    Cmat[[i]] = make.sm(n)
    Q = Q + i*Cmat[[i]]
}
yy = inla.qsample(nsim, Q)
y = c(yy)
idx = rep(1:n, nsim)
r = rep(1:nsim, each = n)
r = inla(y ~ -1 +
    f(idx, model="generic3",
      Cmatrix = Cmat, replicate = r,
      hyper = list(
          prec1 = list(initial = log(1)),
          prec2 = list(initial = log(2)),
          prec3 = list(initial = log(3))),
    data = list(y=y, Cmat=Cmat, r=r),
    verbose=TRUE,
    control.family = list(
        hyper = list(
            prec = list(
                initial = 10,
                fixed = TRUE))))
summary(r)
```

Notes