# Student-t model for Stochastic volatility

#### Parametrization

The Student-t likelihood for stochastic volatility models is defined as:

$$\pi(y|\eta) = \sigma\epsilon$$

where

$$\epsilon \sim T_{\nu}$$

and  $T_{\nu}$  is a Student-t distribution with  $\nu$  degrees of freedom standardised to that is has mean 0 and variance 1 for any value of  $\nu$ .

#### **Link-function**

The squared scale parameter  $\sigma$  is linked to the linear predictor  $\eta$  as:

$$\sigma^2 = \exp(\eta)$$

## Hyperparameters

The degrees of freedom  $\nu$  is represented as

$$\theta = \log(\nu - 2)$$

and the prior is defined on  $\theta$ 

### **Specification**

- family = stochvol.t
- Required argument: y.

### Hyperparameter spesification and default values

#### hyper

#### theta

name log degrees of freedom

short.name dof

initial 4

fixed FALSE

prior loggamma

**param** 1 0.5

to.theta function(x) log(x-2)

from.theta function(x) 2+exp(x)

survival FALSE

discrete FALSE

link default log

**pdf** stochvolt

## Example

In the following example we specify the likelihood for the stochastic volatility model to be Student-t

```
n=1000
x = 0.1 * arima.sim(n = n, model = list(ar = 0.9))
y=exp(x/2)*rt(n,df=6)
time=1:n
data=data.frame(y,time)

formula=y~f(time, model="ar1")+1
result=inla(formula,family="stochvol.t",data=data)
## sometimes we need to add
## control.inla = list(cmin = 1e-2)
## to make it converge
hyper=inla.hyperpar(result)
```

#### Notes

None