# log1exp effect of a covariate

#### Parametrization

This model implements a non-linear effect of a positive covariate x as a part of the linear predictor,

$$\beta \log (1 + \exp(\alpha - \gamma x))$$

where  $\beta, \alpha, \gamma \in \Re$  and  $x \geq 0$ .

#### Hyperparameters

This model has three hyperparameters, the scaling  $\beta$ , halflife a and shape k,

$$\theta_1 = \beta$$
  $\theta_2 = \alpha$   $\theta_3 = \gamma$ 

and the priors are given for  $\theta_1, \theta_2$  and  $\theta_3$ .

#### **Specification**

```
f(x, model="log1exp", hyper = ..., precision = crecision>)
```

where precision is the precision for the tiny noise used to implement this as a latent model.

#### Hyperparameter specification and default values

doc A nonlinear model of a covariate

## hyper

```
theta1
```

```
hyperid 39011
name beta
```

short.name b

initial 1

fixed FALSE

**prior** normal

param 01

to.theta function(x) x

from.theta function(x) x

### theta2

**hyperid** 39012

name alpha

 $\mathbf{short.name} \ \ \mathbf{a}$ 

initial 0

fixed FALSE

prior normal

param 0 1

to.theta function(x) x

from.theta function(x) x

#### theta3

```
hyperid 39013
         name gamma
         short.name g
         initial 0
         fixed FALSE
         prior normal
         param 01
         to.theta function(x) x
         from.theta function(x) x
constr FALSE
nrow.ncol FALSE
augmented FALSE
aug.factor 1
aug.constr
n.div.by
n.required FALSE
set.default.values FALSE
status experimental
pdf \log 1 exp
Example
log1exp = function(x, beta, alpha, gamma)
{
    return (beta * log(1.0 + exp(alpha - gamma * x)))
}
n = 100
lambda = 2
s=0.1
x = rpois(n, lambda = lambda)
beta = 1
alpha = 0
gamma = .5
y = log1exp(x, beta, alpha, gamma) + rnorm(n, sd = s)
r = inla(y ~-1 + f(x, model="log1exp"),
        data = data.frame(y, x),
        family = "gaussian",
        control.inla = list(h=0.001),
        control.family = list(
                hyper = list(
                        prec = list(
                                initial = log(1/s^2),
```

## fixed = TRUE))))

summary(r)

Notes

None