

## The z-model

### Parametrization

The z-model is an implementation of the “classical” way to define the “random effect” part of a mixed model, through

$$\eta = \dots + Zz$$

where  $Z$  is a  $n \times m$  matrix and  $z$  a vector of length  $m$  representing zero-mean “random effects”. The z-model is defined as the augmented model

$$\tilde{z} = \begin{pmatrix} v \\ z \end{pmatrix}$$

where  $v \sim \mathcal{N}_n(Zz, \kappa I)$ , where  $\kappa$  is a high fixed precision, and where the precision matrix for  $z$  is  $\tau C$  where  $C > 0$  is a  $m \times m$  (fixed) matrix.

### Hyperparameters

The precision parameter of the z-model is represented as

$$\theta = \log(\tau)$$

and prior is assigned to  $\theta$

### Specification

The z-model is specified inside the `f()` function as

```
f(<whatever>, model="z", Z = <Z>, Cmatrix = <Cmat>, hyper = <hyper>,  
precision = <precision>)
```

where the `Z`-matrix argument defines the  $Z$  matrix and is required. The `Cmatrix` defines the  $C$  matrix and if not given, taken to the the diagonal matrix with dimension  $m$ . The `precision` parameter defines the value of  $\kappa$ .

If  $Z$  is a  $n \times m$  matrix then the  $C$  matrix must be  $m \times m$  matrix, and  $\tilde{z}$  has length  $n + m$ . The  $n$  first terms of  $\tilde{z}$  is then  $v$  and the last  $m$  terms of  $\tilde{z}$  is then  $z$ .

### Hyperparameter spesification and default values

**hyper**

**theta**

**name** log precision

**short.name** prec

**initial** 4

**fixed** FALSE

**prior** loggamma

**param** 1 5e-05

**to.theta** function(x) log(x)

**from.theta** function(x) exp(x)

**constr** FALSE

**nrow.ncol** FALSE

**augmented** FALSE

**aug.factor** 1

**aug.constr**

**n.div.by**

**n.required** TRUE

**set.default.values** TRUE

**pdf** z.pdf

**Example**

**Notes**