# LogNormal

#### Parametrisation

The LogNormal has density

$$f(y) = \frac{1}{y\sqrt{2\pi}}\sqrt{\tau}\exp\left(-\frac{1}{2}\tau(\log y - \mu)^2\right), \quad y > 0$$

where

 $\tau > 0$  is the precision parameter,

 $\mu$  is the mean parameter.

#### **Link-function**

The parameter  $\mu$  is linked to the linear predictor as:

$$\eta = \mu$$

## Hyperparameters

The  $\tau$  parameter is represented as

$$\theta = \log \tau$$

and the prior is defined on  $\theta$ .

# Specification

- family = lognormal for regression models and family = lognormalsurv for survival models.
- Required arguments: y Given in a format by using inla.surv() function for family = lognormal.surv

#### Hyperparameter spesification and default values

#### lognormal

```
theta
hyperid 77101
name log precision
short.name prec
initial 4
fixed FALSE
prior loggamma
param 1 5e-05
to.theta function(x) log(x)
from.theta function(x) exp(x)
survival FALSE
discrete FALSE
link default identity
pdf lognormal
```

### lognormalsurv

```
hyper
theta
hyperid 78001
name log precision
short.name prec
initial 2
fixed FALSE
prior loggamma
param 1 5e-05
to.theta function(x) log(x)
from.theta function(x) exp(x)
survival TRUE
discrete FALSE
link default identity
pdf lognormal
```

## Example

In the following example we estimate the parameters in a simulated case

```
## these should give the same results
n = 300
x = runif(n)
eta = 1+x
y = exp(rnorm(n, mean = eta, sd = 1))
data = list(y=y, event=rep(1, n), x=x)
formula = inla.surv(y, event) ~ 1 + x
r=inla(formula, family ="lognormalsurv", data=data)
summary(r)

data = data.frame(y, x)
formula = y ~ 1 + x
r=inla(formula, family ="lognormal", data=data)
summary(r)
```

#### Notes

• lognormalsurv can be used for right censored, left censored, interval censored data. A general framework to represent time is given by inla.surv. If the observed times y are large/huge, then this can cause numerical overflow, and if you encounter this problem, try to scale the observatios, like time = time / max(time).