Student-t with strata

Parametrization

This model is an extention to the Student-t, where different strata have their own precisions but the degrees-of-freedom parameter is common.

The Student-t likelihood is defined so that

$$\sqrt{w \ \tau_s}(y-\eta) \sim T_{\nu}$$

for continuous response y where

 au_s : is the precision parameter, depending on the stratum s

w: is a fixed weight w > 0

 η : is the linear predictor

 T_{ν} : is a standardized Student-t with ν degrees of freedom such that its variace is 1 for any value of ν , common for all strata.

Link-function

Identity

Hyperparameters

This likelihood $N_s + 1$ hyperparameters

$$\theta_1 = \log(\nu - 2)$$

$$\theta_2 = \log(\tau_1)$$

$$\theta_3 = \log(\tau_2)$$

$$etc....$$

$$\theta_{N_s+1} = \log(\tau_{N_s})$$

where N_s is the number of strata defined. The current implementation limits N_s to 10, but this is easy to fix if needed. The prior is defined on $\theta = (\theta_1, \theta_2, ...)$.

Specification

- family = tstrata
- Required argument: y and w (keyword weights, default to 1), and inla()-argument "strata" which is either a integer vector with elements $1, 2, ..., N_s$, or factor for which the levels defines the strata.

Hyperparameter spesification and default values

hyper

theta1

hyperid 101001

name log degrees of freedom

```
short.name dof
    initial 4
    fixed FALSE
    prior loggamma
    param 1 0.01
    to.theta function(x) log(x-5)
    from.theta function(x) 5+exp(x)
theta2
    hyperid 101002
    name log precision1
    short.name prec1
    initial 2
    fixed FALSE
    prior loggamma
    param 1 5e-05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
theta3
    hyperid 101003
    name log precision2
    short.name prec2
    initial 2
    fixed FALSE
    prior loggamma
    param 1 5e-05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
theta4
    hyperid 101004
    name log precision3
    short.name prec3
    initial 2
    fixed FALSE
    prior loggamma
    param 1 5e-05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
theta5
    hyperid 101005
    name log precision4
    short.name prec4
    initial 2
    fixed FALSE
    prior loggamma
```

```
param 1 5e-05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
theta6
    hyperid 101006
    name log precision5
    short.name prec5
    initial 2
    fixed FALSE
    prior loggamma
    param 1 5e-05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
theta7
    hyperid 101007
    name log precision6
    short.name prec6
    initial 2
    fixed FALSE
    prior loggamma
    param 1 5e-05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
theta8
    hyperid 101008
    name log precision7
    short.name prec7
    initial 2
    fixed FALSE
    prior loggamma
    param 1 5e-05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
theta9
    hyperid 101009
    name log precision8
    short.name prec8
    initial 2
    fixed FALSE
    prior loggamma
    param 1 5e-05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
theta10
```

```
hyperid 101010
         name log precision9
         short.name prec9
         initial 2
         fixed FALSE
         prior loggamma
         param 1 5e-05
         to.theta function(x) log(x)
         from.theta function(x) exp(x)
     theta11
         hyperid 101011
         name log precision10
         short.name prec10
         initial 2
         fixed FALSE
         prior loggamma
         param 1 5e-05
         to.theta function(x) log(x)
         {\bf from.theta} \ {\tt function(x)} \ {\tt exp(x)}
survival FALSE
discrete FALSE
link default identity
\mathbf{pdf} tstrata
Example
Notes
```

None