

## Student- $t$

### Parametrization

The Student- $t$  likelihood is defined so that

$$\sqrt{s} \tau (y - \eta) \sim T_\nu$$

for continuous response  $y$  where

$\tau$  : is the precision parameter

$s$  : is a fixed scaling  $s > 0$

$\eta$  : is the linear predictor

$T_\nu$  : is a standardized Student- $t$  with  $\nu$  degrees of freedom such that its variance is 1 for any value of  $\nu$ .

### Link-function

Identity

### Hyperparameters

This likelihood has two hyperparameters

$$\begin{aligned}\theta_1 &= \log(\tau) \\ \theta_2 &= \log(\nu - 2)\end{aligned}$$

and the prior is defined on  $\theta = (\theta_1, \theta_2)$ .

### Specification

- family = T
- Required argument:  $y$  and  $s$  (keyword `scale`, default to 1).

### Hyperparameter specification and default values

**hyper**

**theta1**

```
hyperid 100001
name log precision
short.name prec
initial 0
fixed FALSE
prior loggamma
param 1 5e-05
to.theta function(x) log(x)
from.theta function(x) exp(x)
```

**theta2**

```
hyperid 100002
```

```
name log degrees of freedom
short.name dof
initial 5
fixed FALSE
prior loggamma
param 1 0.5
to.theta function(x) log(x-2)
from.theta function(x) 2+exp(x)
```

**survival** FALSE

**discrete** FALSE

**link** default identity

**pdf** student-t

## Example

```
#simulate data
n=100
phi=0.85
mu=0.5
eta=rep(0,n)
for(i in 2:n)
eta[i]=mu+phi*(eta[i-1]-mu)+rnorm(1)
nu=3
t=rt(n,df=nu)
y=eta+t/(sqrt(nu/(nu-2)))
data=list(y=y,z=seq(1:n))
#define the model and fit
formula=y~f(z,model="ar1")
result=inla(formula,family="T",data=data)
```

## Notes

None