

Binomial

Parametrisation

The Binomial distribution is

$$\text{Prob}(y) = \binom{n}{y} p^y (1-p)^{n-y}$$

for responses $y = 0, 1, 2, \dots, n$, where

n : number of trials.

p : probability of success in each trial.

Link-function

The mean and variance of y are given as

$$\mu = np \quad \text{and} \quad \sigma^2 = np(1-p)$$

and the probability p is linked to the linear predictor by

$$p(\eta) = \frac{\exp(\eta)}{1 + \exp(\eta)}$$

Hyperparameters

None.

Specification

- family = `binomial`
- Required arguments: y and n (keyword `Ntrials`)

Example

In the following example we estimate the parameters in a simulated example with binomial responses.

```
n=100
a = 1
b = 1
z = rnorm(n)
eta = a + b*z
Ntrials = sample(c(1,5,10,15), size=n, replace=TRUE)
prob = exp(eta)/(1 + exp(eta))
y = rbinom(n, size=Ntrials, prob = prob)

data = list(y=y,z=z)
formula = y ~ 1+z
result = inla(formula, family = "binomial", data = data, Ntrials=Ntrials)
summary(result)
```

Notes

If the response is a **factor** it must be converted to $\{0, 1\}$ before calling `inla()`, as this conversion is not done automatic (as for example in `glm()`).