

qPoisson

Parametrisation

The Poisson distribution is

$$\text{Prob}(y) = \frac{\lambda^y}{y!} \exp(-\lambda)$$

for responses $y = 0, 1, 2, \dots$, where

λ : the expected value.

Link-function

The mean and variance of y are given as

$$\mu = \lambda \quad \text{and} \quad \sigma^2 = \lambda$$

and the mean is linked to the linear predictor by

$$\lambda(\eta) = E q_\alpha$$

where $E > 0$ is a known constant (or $\log(E)$ is an offset), and q_α is the α quantile of the continuous Poisson distribution.

Hyperparameters

None.

Specification

- family = qpoisson
- Required arguments: y , E and α (given as `control.family = list(quantile = α)`).

Hyperparameter specification and default values

hyper

survival FALSE

discrete TRUE

link default log

pdf qpoisson

Example

In the following example we estimate the parameters in a simulated example with Poisson responses.

```
n=100
a = 1
b = 1
z = rnorm(n)
eta = a + b*z
E = sample(1:10, n, replace=TRUE)
lambda = E*exp(eta)
```

```
y = rpois(n, lambda = lambda)

data = list(y=y,z=z)
formula = y ~ 1+z
result = inla(formula, family = "poisson", data = data, E=E)
summary(result)
```

Notes