## Student-t with strata

#### Parametrization

This model is an extention to the Student-t, where different strata have their own precisions but the degrees-of-freedom parameter is common.

The Student-t likelihood is defined so that

$$\sqrt{w \ \tau_s}(y-\eta) \sim T_{\nu}$$

for continuous response y where

 $au_s$  : is the precision parameter, depending on the stratum s

w: is a fixed weight w > 0

 $\eta$ : is the linear predictor

 $T_{\nu}$ : is a standardized Student-t with  $\nu$  degrees of freedom such that its variace is 1 for any value of  $\nu$ , common for all strata.

#### **Link-function**

Identity

## Hyperparameters

This likelihood  $N_s + 1$  hyperparameters

$$\theta_1 = \log(\nu - 2)$$

$$\theta_2 = \log(\tau_1)$$

$$\theta_3 = \log(\tau_2)$$

$$etc....$$

$$\theta_{N_s+1} = \log(\tau_{N_s})$$

where  $N_s$  is the number of strata defined. The current implementation limits  $N_s$  to 10, but this is easy to fix if needed. The prior is defined on  $\theta = (\theta_1, \theta_2, ...)$ .

## **Specification**

- family = tstrata
- Required argument: y and w (keyword weights, default to 1), and inla()-argument "strata" which is either a integer vector with elements  $1, 2, ..., N_s$ , or factor for which the levels defines the strata.

### Hyperparameter spesification and default values

doc A stratified version of the Student-t likelihood

hyper

theta1

hyperid 101001

```
name log degrees of freedom
    {f short.name}\ {f dof}
    initial 4
    fixed FALSE
    prior loggamma
    param 1 0.01
    to.theta function(x) log(x-5)
    from.theta function(x) 5+exp(x)
theta2
    hyperid 101002
    name log precision1
    short.name prec1
    initial 2
    fixed FALSE
    prior loggamma
    param 1 5e-05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
theta3
    hyperid 101003
    name log precision2
    short.name prec2
    initial 2
    fixed FALSE
    prior loggamma
    param 1 5e-05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
theta4
    hyperid 101004
    name log precision3
    short.name prec3
    initial 2
    fixed FALSE
    prior loggamma
    param 1 5e-05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
theta5
    hyperid 101005
    name log precision4
    short.name prec4
    initial 2
    fixed FALSE
```

```
prior loggamma
    param 1 5e-05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
theta6
    hyperid 101006
    name log precision5
    short.name prec5
    initial 2
    fixed FALSE
    prior loggamma
    param 1 5e-05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
theta7
    hyperid 101007
    name log precision6
    short.name prec6
    initial 2
    fixed FALSE
    prior loggamma
    param 1 5e-05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
theta8
    hyperid 101008
    name log precision7
    short.name prec7
    initial 2
    fixed FALSE
    prior loggamma
    param 1 5e-05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
theta9
    hyperid 101009
    name log precision8
    short.name prec8
    initial 2
    fixed FALSE
    prior loggamma
    \mathbf{param}\ 1\ 5\mathrm{e}\text{-}05
    to.theta function(x) log(x)
    from.theta function(x) exp(x)
```

## theta10

hyperid 101010
name log precision9
short.name prec9
initial 2
fixed FALSE
prior loggamma
param 1 5e-05
to.theta function(x) log(x)
from.theta function(x) exp(x)

## theta11

hyperid 101011
name log precision10
short.name prec10
initial 2
fixed FALSE
prior loggamma
param 1 5e-05
to.theta function(x) log(x)
from.theta function(x) exp(x)

## survival FALSE

discrete FALSE

link default identity

**pdf** tstrata

# Example

Notes

None