# Poisson

### Parametrisation

The Poisson distribution is

$$Prob(y) = \frac{\lambda^y}{y!} \exp(-\lambda)$$

for responses  $y = 0, 1, 2, \ldots$ , where

 $\lambda$ : the expected value.

#### **Link-function**

The mean and variance of y are given as

$$\mu = \lambda$$
 and  $\sigma^2 = \lambda$ 

and the mean is linked to the linear predictor by

$$\lambda(\eta) = E \exp(\eta)$$

where E > 0 is a known constant (or  $\log(E)$  is the offset of  $\eta$ ).

## Hyperparameters

None.

# **Specification**

- family = poisson
- $\bullet$  Required arguments: y and E

## Example

In the following example we estimate the parameters in a simulated example with Poisson responses.

```
n=100
a = 1
b = 1
z = rnorm(n)
eta = a + b*z
E = sample(1:10, n, replace=TRUE)
lambda = E*exp(eta)
y = rpois(n, lambda = lambda)

data = list(y=y,z=z)
formula = y ~ 1+z
result = inla(formula, family = "poisson", data = data, E=E)
summary(result)
```

### Notes

This likelihood also accept E = 0 and in this case  $\log(E)$  is defined to be 0. Non-integer values of  $y \ge 0$  is accepted although the normalising constant of the likelihood is then wrong (but its a constant only).