

NMix

Parametrisation

The N-Mixture distribution is a Poisson mixture of the Binomials, as

$$\text{Prob}(y) = \sum_{n=y}^{\infty} \binom{n}{y} p^n (1-p)^{n-y} \times \frac{\lambda^n}{n!} \exp(-\lambda)$$

for responses $y = 0, 1, 2, \dots, n$, where n is Poisson number of trials, and p is probability of success. Replicated reponses y_1, y_2, \dots, y_r , are iid from the Binomial, given (a common) n from the Poisson,

$$\text{Prob}(y_1, \dots, y_r) = \sum_{n=\max\{y_1, \dots, y_r\}}^{\infty} \left\{ \prod_{i=1}^r \binom{n}{y_i} p^n (1-p)^{n-y_i} \right\} \times \frac{\lambda^n}{n!} \exp(-\lambda)$$

Link-function

The probability p is linked to the linear predictor by

$$p(\eta) = \frac{\exp(\eta)}{1 + \exp(\eta)}$$

for the default logit link, while λ depends on fixed covariates

$$\log(\lambda) = \sum_{j=1}^m \beta_j x_j$$

with one vector of covariates for each observation. m can be maximum 10 and minimum 1.

Hyperparameters

The parameters $\theta_1 = \beta_1, \theta_2 = \beta_2, \dots, \theta_m = \beta_m$.

Hyperparameter spesification and default values

doc Binomial-Poisson mixture

hyper

theta1

hyperid 101101

name beta1

short.name beta1

initial 2.30258509299405

fixed FALSE

prior normal

param 0 0.5

to.theta function(x) x

from.theta function(x) x

theta2

hyperid 101102

name beta2

```

    short.name beta2
    initial 0
    fixed FALSE
    prior normal
    param 0 1
    to.theta function(x) x
    from.theta function(x) x
theta3
    hyperid 101103
    name beta3
    short.name beta3
    initial 0
    fixed FALSE
    prior normal
    param 0 1
    to.theta function(x) x
    from.theta function(x) x
theta4
    hyperid 101104
    name beta4
    short.name beta4
    initial 0
    fixed FALSE
    prior normal
    param 0 1
    to.theta function(x) x
    from.theta function(x) x
theta5
    hyperid 101105
    name beta5
    short.name beta5
    initial 0
    fixed FALSE
    prior normal
    param 0 1
    to.theta function(x) x
    from.theta function(x) x
theta6
    hyperid 101106
    name beta6
    short.name beta6
    initial 0
    fixed FALSE
    prior normal

```

```

    param 0 1
    to.theta function(x) x
    from.theta function(x) x
theta7
    hyperid 101107
    name beta7
    short.name beta7
    initial 0
    fixed FALSE
    prior normal
    param 0 1
    to.theta function(x) x
    from.theta function(x) x
theta8
    hyperid 101108
    name beta8
    short.name beta8
    initial 0
    fixed FALSE
    prior normal
    param 0 1
    to.theta function(x) x
    from.theta function(x) x
theta9
    hyperid 101109
    name beta9
    short.name beta9
    initial 0
    fixed FALSE
    prior normal
    param 0 1
    to.theta function(x) x
    from.theta function(x) x
theta10
    hyperid 101110
    name beta10
    short.name beta10
    initial 0
    fixed FALSE
    prior normal
    param 0 1
    to.theta function(x) x
    from.theta function(x) x

```

status experimental

survival FALSE

discrete TRUE

link default logit probit

pdf nmix

Specification

- family = nmix
- Required arguments: the response Y and covariates X as `inla.mdata(Y, X [, additional.covariates])`

The response is a matrix where each row are replicates, where responses that are NA's are ignored. The covariates is one or many vectors, matrices or data.frames. Each row of the covariates $(x_{i1}, x_{i2}, \dots, x_{im})$ defines the covariates used for the i 'th response(s) (the i 'th row of Y). Note that $\beta_{m+1}, \dots, \beta_{10}$ are fixed to zero.

Example

In the following example we estimate the parameters in a simulated example with replications.

```
nrep = 5
n = 50
y = matrix(NA, n, nrep)
x = c()
xx = c()
intercept = 1

for(i in 1:n) {
  local.x = runif(1) - 0.5
  lambda = exp(2 + local.x)
  N = rpois(1, lambda)
  local.xx = runif(1) - 0.5
  eta = intercept + local.xx
  p = exp(eta)/(exp(eta) + 1)
  nr = sample(1:nrep, 1)
  y[i, 1:nr]= rbinom(nr, size = N, prob = p)
  x = c(x, local.x)
  xx = c(xx, local.xx)
}

Y = inla.mdata(y, 1, x)
r = inla(Y ~ 1 + xx,
  data = list(Y=Y, xx=xx),
  family = "nmix",
  control.fixed = list(prec.intercept=1, prec=1))
```

Notes