

NMixNB

Parametrisation

The N-MixtureNB distribution is a negative Binomial mixture of the Binomials, as

$$\text{Prob}(y) = \sum_{n=y}^{\infty} \binom{n}{y} p^n (1-p)^{n-y} \times \frac{\Gamma(n+\delta)}{\Gamma(\delta)n!} q^\delta (1-q)^n$$

for responses $y = 0, 1, 2, \dots, n$, where n is Poisson number of trials, and p is probability of success. For δ and q , see below. Replicated reponses y_1, y_2, \dots, y_r , are iid from the Binomial with the same p , conditioned on the same n from the negative Binomial,

$$\text{Prob}(y_1, \dots, y_r) = \sum_{n=\max\{y_1, \dots, y_r\}}^{\infty} \left\{ \prod_{i=1}^r \binom{n}{y_i} p^n (1-p)^{n-y_i} \right\} \times \frac{\Gamma(n+\delta)}{\Gamma(\delta)n!} q^\delta (1-q)^n$$

The negative binomial is parameterized in terms of the mean λ and overdispersion $1/\delta$, where $q = \delta/(\delta + \mu)$; see the R documentation `?dnbinom` for this parameterisation (where $\delta = \text{size}$).

Link-function

The probability p is linked to the linear predictor by

$$p(\eta) = \frac{\exp(\eta)}{1 + \exp(\eta)}$$

for the default logit link, while λ depends on fixed covariates

$$\log(\lambda) = \sum_{j=1}^m \beta_j x_j$$

with one vector of covariates for each observation. m can be maximum 10 and minimum 1.

Hyperparameters

The parameters $\theta_1 = \beta_1, \theta_2 = \beta_2, \dots, \theta_m = \beta_m$, and overdispersion $\theta_{11} = \log(1/\delta)$.

Hyperparameter spesification and default values

doc NegBinomial-Poisson mixture

hyper

theta1

hyperid 101121

name beta1

short.name beta1

initial 2.30258509299405

fixed FALSE

prior normal

param 0 0.5

to.theta function(x) x

from.theta function(x) x

theta2
hyperid 101122
name beta2
short.name beta2
initial 0
fixed FALSE
prior normal
param 0 1
to.theta function(x) x
from.theta function(x) x

theta3
hyperid 101123
name beta3
short.name beta3
initial 0
fixed FALSE
prior normal
param 0 1
to.theta function(x) x
from.theta function(x) x

theta4
hyperid 101124
name beta4
short.name beta4
initial 0
fixed FALSE
prior normal
param 0 1
to.theta function(x) x
from.theta function(x) x

theta5
hyperid 101125
name beta5
short.name beta5
initial 0
fixed FALSE
prior normal
param 0 1
to.theta function(x) x
from.theta function(x) x

theta6
hyperid 101126
name beta6
short.name beta6

```

    initial 0
    fixed FALSE
    prior normal
    param 0 1
    to.theta function(x) x
    from.theta function(x) x
theta7
    hyperid 101127
    name beta7
    short.name beta7
    initial 0
    fixed FALSE
    prior normal
    param 0 1
    to.theta function(x) x
    from.theta function(x) x
theta8
    hyperid 101128
    name beta8
    short.name beta8
    initial 0
    fixed FALSE
    prior normal
    param 0 1
    to.theta function(x) x
    from.theta function(x) x
theta9
    hyperid 101129
    name beta9
    short.name beta9
    initial 0
    fixed FALSE
    prior normal
    param 0 1
    to.theta function(x) x
    from.theta function(x) x
theta10
    hyperid 101130
    name beta10
    short.name beta10
    initial 0
    fixed FALSE
    prior normal
    param 0 1

```

```

    to.theta function(x) x
    from.theta function(x) x
theta11
    hyperid 101131
    name overdispersion
    short.name overdispersion
    initial 0
    fixed FALSE
    prior pc.gamma
    param 7
    to.theta function(x) log(x)
    from.theta function(x) exp(x)

```

status experimental

survival FALSE

discrete TRUE

link default logit probit

pdf nmixnb

Specification

- family = nmixnb
- Required arguments: the response Y and covariates X as `inla.mdata(Y, X [, additional.covariates])`

The response is a matrix where each row are replicates, where responses that are `NA`'s are ignored. The covariates is one or many vectors, matrices or data.frames. Each row of the covariates $(x_{i1}, x_{i2}, \dots, x_{im})$ defines the covariates used for the i 'th response(s) (the i 'th row of Y). Note that $\beta_{m+1}, \dots, \beta_{10}$ are fixed to zero.

Example

In the following example we estimate the parameters in a simulated example with replications.

```

nrep.max = 5
n = 50
y = matrix(NA, n, nrep.max)
x = c()
xx = c()
size = 3
overdispersion = 1/size
intercept = 1

for(i in 1:n) {
  local.x = runif(1) - 0.5
  lambda = exp(2 + local.x)
  N = rnbinom(1, mu=lambda, size=size)

```

```

local.xx = runif(1) - 0.5
eta = intercept + local.xx
p = exp(eta)/(exp(eta) + 1)
## sample the number of replications
nr = sample(1:nrep.max, 1)
## and sample these. note that 'y' is initialized with NA's,
## so if nr < nrep.max, then
## y[i,(nr+1):nrep.max] would be NA.
y[i, 1:nr]= rbinom(nr, size = N, prob = p)
x = c(x, local.x)
xx = c(xx, local.xx)
}

Y = inla.mdata(y, 1, x)
r = inla(Y ~ 1 + xx,
        data = list(Y=Y, xx=xx),
        family = "nmixnb",
        control.fixed = list(prec.intercept=1, prec=1))

```

Notes