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In[230]:= S = e^(-i * x * pi) (e^(i * k * pi) - e^(-i * k * pi)) ^ -1 *
      {{e^(i * k * pi) e^(-i * x * pi) - e^(-i * k * pi) e^(i * x * pi)},
      e^(-i * k * pi) e^(-i * x * pi) - e^(-i * k * pi) e^(i * x * pi)},
      {e^(i * k * pi) e^(-i * x * pi) - e^(i * k * pi) e^(i * x * pi),
      e^(-i * k * pi) e^(-i * x * pi) - e^(i * k * pi) e^(i * x * pi)}}

Psi[x_] = k * e^(-i * x * pi) * {e^(i * k * x), e^(-i * k * x)}
Phi[x_] = k * e^(i * x * pi) * {e^(i * k * x), e^(-i * k * x)}

PPsi[x_] = k * e^(-i * x * pi) * {e^(i * k * x), -e^(-i * k * x)}
PPhi[x_] = k * e^(i * x * pi) * {e^(i * k * x), -e^(-i * k * x)}

PPsi[0].{Cp1, Cm1} + PPhi[0].S.{Cp1, Cm1}
PPsi[pi].{Cp0, Cm0} + PPhi[pi].S.{Cp0, Cm0} - i * alpha * Psi[pi].{Cp0, Cm0}

PPsi[0].{Cp1, Cm1} + PPhi[0].S.{Cp1, Cm1} ==
  PPsi[pi].{Cp0, Cm0} + PPhi[pi].S.{Cp0, Cm0} - i * alpha * Psi[pi].{Cp0, Cm0}

Psi[pi].{Cp0, Cm0} == Psi[0].{Cp1, Cm1}
Solve[Psi[pi].{Cp0, Cm0} == Psi[0].{Cp1, Cm1} &&
  PPsi[0].{Cp1, Cm1} + PPhi[0].S.{Cp1, Cm1} ==
  PPsi[pi].{Cp0, Cm0} + PPhi[pi].S.{Cp0, Cm0} - i * alpha * Psi[pi].{Cp0, Cm0}, {Cp1, Cm1}]

(*S[k,x].{x,y}==(*{a,b}*)
Solve[%,{x,y}]*

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$$\text{Out[230]} = \left\{ \left\{ \frac{e^{-i\pi x} (e^{ik\pi - i\pi x} - e^{-ik\pi + i\pi x})}{-e^{-ik\pi} + e^{ik\pi}}, \frac{e^{-i\pi x} (e^{-ik\pi - i\pi x} - e^{-ik\pi + i\pi x})}{-e^{-ik\pi} + e^{ik\pi}} \right\}, \left\{ \frac{e^{-i\pi x} (e^{ik\pi - i\pi x} - e^{ik\pi + i\pi x})}{-e^{-ik\pi} + e^{ik\pi}}, \frac{e^{-i\pi x} (e^{-ik\pi - i\pi x} - e^{ik\pi + i\pi x})}{-e^{-ik\pi} + e^{ik\pi}} \right\} \right\}$$

$$\text{Out[231]} = \{e^{ikx - ix\pi} k, e^{-ikx - ix\pi} k\}$$

$$\text{Out[232]} = \{e^{ikx + ix\pi} k, e^{-ikx + ix\pi} k\}$$

$$\text{Out[233]} = \{e^{ikx - ix\pi} k, -e^{-ikx - ix\pi} k\}$$

$$\text{Out[234]} = \{e^{ikx + ix\pi} k, -e^{-ikx + ix\pi} k\}$$

$$\text{Out[235]} = -Cm1 k + Cp1 k + Cm1 \left(\frac{e^{-i\pi x} (e^{-ik\pi - i\pi x} - e^{-ik\pi + i\pi x}) k}{-e^{-ik\pi} + e^{ik\pi}} - \frac{e^{-i\pi x} (e^{-ik\pi - i\pi x} - e^{ik\pi + i\pi x}) k}{-e^{-ik\pi} + e^{ik\pi}} \right) +$$

$$Cp1 \left(\frac{e^{-i\pi x} (e^{ik\pi - i\pi x} - e^{-ik\pi + i\pi x}) k}{-e^{-ik\pi} + e^{ik\pi}} - \frac{e^{-i\pi x} (e^{ik\pi - i\pi x} - e^{ik\pi + i\pi x}) k}{-e^{-ik\pi} + e^{ik\pi}} \right)$$

$$\text{Out[236]} = -\text{Cm0 } e^{-i k \pi - i \pi \Phi} k + \text{Cp0 } e^{i k \pi - i \pi \Phi} k +$$

$$\text{Cm0} \left(\frac{e^{i k \pi} (e^{-i k \pi - i \pi \Phi} - e^{-i k \pi + i \pi \Phi}) k}{-e^{-i k \pi} + e^{i k \pi}} - \frac{e^{-i k \pi} (e^{-i k \pi - i \pi \Phi} - e^{i k \pi + i \pi \Phi}) k}{-e^{-i k \pi} + e^{i k \pi}} \right) +$$

$$\text{Cp0} \left(\frac{e^{i k \pi} (e^{i k \pi - i \pi \Phi} - e^{-i k \pi + i \pi \Phi}) k}{-e^{-i k \pi} + e^{i k \pi}} - \frac{e^{-i k \pi} (e^{i k \pi - i \pi \Phi} - e^{i k \pi + i \pi \Phi}) k}{-e^{-i k \pi} + e^{i k \pi}} \right) -$$

$$i \left(\text{Cm0 } e^{-i k \pi - i \pi \Phi} k + \text{Cp0 } e^{i k \pi - i \pi \Phi} k \right) \alpha$$

$$\text{Out[237]} = -\text{Cm1 } k + \text{Cp1 } k + \text{Cm1} \left(\frac{e^{-i \pi \Phi} (e^{-i k \pi - i \pi \Phi} - e^{-i k \pi + i \pi \Phi}) k}{-e^{-i k \pi} + e^{i k \pi}} - \frac{e^{-i \pi \Phi} (e^{-i k \pi - i \pi \Phi} - e^{i k \pi + i \pi \Phi}) k}{-e^{-i k \pi} + e^{i k \pi}} \right) +$$

$$\text{Cp1} \left(\frac{e^{-i \pi \Phi} (e^{i k \pi - i \pi \Phi} - e^{-i k \pi + i \pi \Phi}) k}{-e^{-i k \pi} + e^{i k \pi}} - \frac{e^{-i \pi \Phi} (e^{i k \pi - i \pi \Phi} - e^{i k \pi + i \pi \Phi}) k}{-e^{-i k \pi} + e^{i k \pi}} \right) == -\text{Cm0 } e^{-i k \pi - i \pi \Phi} k +$$

$$\text{Cp0 } e^{i k \pi - i \pi \Phi} k + \text{Cm0} \left(\frac{e^{i k \pi} (e^{-i k \pi - i \pi \Phi} - e^{-i k \pi + i \pi \Phi}) k}{-e^{-i k \pi} + e^{i k \pi}} - \frac{e^{-i k \pi} (e^{-i k \pi - i \pi \Phi} - e^{i k \pi + i \pi \Phi}) k}{-e^{-i k \pi} + e^{i k \pi}} \right) +$$

$$\text{Cp0} \left(\frac{e^{i k \pi} (e^{i k \pi - i \pi \Phi} - e^{-i k \pi + i \pi \Phi}) k}{-e^{-i k \pi} + e^{i k \pi}} - \frac{e^{-i k \pi} (e^{i k \pi - i \pi \Phi} - e^{i k \pi + i \pi \Phi}) k}{-e^{-i k \pi} + e^{i k \pi}} \right) -$$

$$i \left(\text{Cm0 } e^{-i k \pi - i \pi \Phi} k + \text{Cp0 } e^{i k \pi - i \pi \Phi} k \right) \alpha$$

$$\text{Out[238]} = \text{Cm0 } e^{-i k \pi - i \pi \Phi} k + \text{Cp0 } e^{i k \pi - i \pi \Phi} k == \text{Cm1 } k + \text{Cp1 } k$$

$$\text{Out[239]} = \left\{ \left\{ \text{Cp1} \rightarrow -\frac{1}{2} e^{-i k \pi - i \pi \Phi} \left(-2 \text{Cp0 } e^{2 i k \pi} + \text{Cm0 } i \alpha + \text{Cp0 } e^{2 i k \pi} i \alpha \right), \right. \right.$$

$$\left. \left. \text{Cm1} \rightarrow \frac{1}{2} e^{-i k \pi - i \pi \Phi} \left(2 \text{Cm0} + \text{Cm0 } i \alpha + \text{Cp0 } e^{2 i k \pi} i \alpha \right) \right\} \right\}$$