

# Error Bars of Effective Areas

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09-05-2024

# Effective Area

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$N_{\text{det}}$  is not an integer, more on this below.

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- In practice, then,  $N_{\text{det}}$  is an array of floats.