

SEMESTER-II

Practical-1

Basic of R software.

- (i) R is a software for data analysis and statistical computing.
- (ii) It is a software by which effective data handling and outcome storage is possible.
- (iii) It is capable of graphical display.
- (iv) It's a free software.

Problems.

$$\begin{aligned} & 2^2 + 1 - 51 + 4 \times 5 + 6/5 \\ \Rightarrow & 2^2 + \text{abs}(-5) + 4 \times 5 + 6/5 \\ = & 30.2 \end{aligned}$$

$$\begin{aligned} & x = 20 \\ & y = 2x \\ & z = x + y, \sqrt{z} \\ \Rightarrow & x = 20 \\ & y = 2 \times 20 \\ & z = x + y \\ & \text{sqrt}(z) \\ = & 7.74 \end{aligned}$$

$$\begin{aligned} & x = 10 \\ & y = 15 \\ & z = 5 \\ 1) & x + y + z \\ 2) & xyz \end{aligned}$$

EGO

- c) \sqrt{xyz}
d) round of \sqrt{xyz}

$$\Rightarrow \begin{aligned}x &= 10 \\y &= 15 \\z &= 5 \\a &= 10 * 15 * 5 \\b &= \sqrt{a}\end{aligned}$$

round (a).

A vector in R software is denoted by
the syntax c.

- 1) $c(2, 3, 5, 7)^2$
 $a = c(2, 3, 5, 7)^2$
4 9 25 49
- 2) $c(2, 3, 5, 7)^1 c(2, 3)$
4 27 25 343
- 3) $c(2, 3, 5, 7, 9, 11)^1 c(2, 3)$
4 27 25 343 81 1331
- 4) $c(1, 2, 3, 4, 5, 6)^1 c(2, 3, 4)$
1 8 81 16 125 1296
- 5) $c(2, 3, 5, 6)^1 3$
6 9 15 18

$$6) \Rightarrow C(2, 4, 6, 8) * C(-2, -3, -5, -7)$$

$$[1] \quad -4 \quad -12 \quad -30 \quad -56$$

034

$$7) \Rightarrow x = C(2, 4, 6, 8)$$

$$x \neq 10$$

$$[1] \quad 12 \quad 14 \quad 16 \quad 18$$

$$8) \Rightarrow C(2, 4, 6, 8) + C(-2, -3, -1, 0)$$

$$[1] \quad 0 \quad 1 \quad 5 \quad 8$$

\rightarrow sum product

8) Find the sum, product, sqrt of the following sum and product for the following vali

$$(4, 9, 2, 5, 7, 8, 3, 6, 15, 12, 10, 9, 8, 13, 14)$$

$$a = C(4, 9, \dots)$$

$$y = \text{sum}(a)$$

$$z = \text{Prod}(a)$$

$$\cancel{y^{10.5}}$$

$$[1] \quad 125$$

$$\cancel{z}$$

$$[1] \quad 5$$

$$\cancel{y^{10.5}}$$

$$[1] \quad 11.18034$$

Adding of Matrix

$x = \text{matrix}(\text{row}=3, \text{ncol}=3, c(4, 5, 6, 7, 8, 9, 4, 0, 2))$
 $y = \text{matrix}(\text{row}=3, \text{ncol}=3, c(8, 4, 5, 11, 12, 8, 9, 7, 4))$

$$\begin{bmatrix} x \\ [1,] \end{bmatrix} \begin{bmatrix} [1] & [2] & [3] \\ 4 & 7 & 1 \\ 5 & 8 & 0 \\ 6 & 9 & 2 \end{bmatrix}$$

$$\begin{bmatrix} x+y \\ [1,] \end{bmatrix} \begin{bmatrix} [1] & [2] & [3] \\ 10 & 18 & 13 \\ 9 & 20 & 7 \\ 11 & 17 & 6 \end{bmatrix}$$

$$\begin{bmatrix} y \\ [1,] \end{bmatrix} \begin{bmatrix} [1] & [2] & [3] \\ 6 & 11 & 9 \\ 4 & 12 & 7 \\ 5 & 8 & 4 \end{bmatrix}$$

$$\begin{bmatrix} x^*y \\ [1,] \end{bmatrix} \begin{bmatrix} [1] & [2] & [3] \\ 24 & 77 & 36 \\ 20 & 96 & 0 \\ 30 & 72 & 8 \end{bmatrix}$$

$$\begin{bmatrix} x^*2 \\ [1,] \end{bmatrix} \begin{bmatrix} [1] & [2] & [3] \\ 8 & 14 & 8 \\ 10 & 16 & 0 \\ 12 & 18 & 4 \end{bmatrix}$$

$$\begin{array}{r} A \rightarrow \\ \hline 2 \cdot 12 \cdot 9 \end{array}$$

$$\begin{bmatrix} y^*2 \\ [1,] \end{bmatrix} \begin{bmatrix} [1] & [2] & [3] \\ 12 & 22 & 18 \\ 8 & 24 & 14 \\ 10 & 16 & 8 \end{bmatrix}$$

Ran 2^0.5

[1] 2925682

Q13) Find the sum, product, max, min, values of
 $c(2, 8, 9, 11, 10, 7, 6)^2$

$x = c(2, 8, \dots)^2$

[1] 4 64 81 121 100 49 36

sum(x)

[1] 455

prod(x)

[1] 44 25 9 2748400

max(x)

[1] 121

min(x)

[1] 4.

Q Matrix

$x \leftarrow \text{matrix}(\text{nrow} = 3, \text{ncol} = 4, c(2, 6, 7, 8, 9, 4, 5, 10, 1,$

1)

	[1,1]	[1,2]	[1,3]	[1,4]
[1,1]	2	8	5	1
[2,1]	6	9	0	4
[3,1]	7	4	2	5

$$n=10, P=0.6, q=0.4$$

036

$dbinom(7, 10, 0.6)$

[1] 0.2149908

$dbinom(4, 10, 0.6)$

[1] 0.1114769.

$pbinom(4, 10, 0.6)$

[1] 0.1662386

$1 - Pbinom(6, 10, 0.6)$

[1] 0.3822806

$dbinom(2, 10, 0.6)$

[1] 0.0001048576

$dbinom(10, 10, 0.6)$

[1] 0.006046618

2) Suppose there are 12 mcq's in an English question paper. Each question has $\frac{1}{5}$ answers and only 1 is correct. Find the probability.

(i) 4 correct answers

(ii) Almost 4 correct answers

(iii) At least 3 correct answers

→ $n=12, P=1/5$

(i) $P(X=4)$

→ $dbinom(4, 12, 1/5)$

[1] 0.13287

(ii) $Pbinom(4, 12, 1/5)$

[1] 0.927

(iii) $1 - Pbinom(2, 12, 1/5)$

[1] 0.4416

3) Find the complete binomial distribution where $a=5, b=0.1$

→ $dbinom(0, 5, 0.1)$

[1] 0.59049

PRACTICAL - 2 Binomial Distribution

n = Total no of trials

p = P(success)

q = P(failure)

x :

$$P(x) = {}^n C_x p^x q^{n-x}; \quad x=0, 1, \dots$$

$$E(x) = np$$

$$V(x) = npq$$

$d\text{binom}(x, n, p)$ $n \neq p$ $p\text{binom}(x, n, p)$	$P(x)$ $E(x)$
--	------------------

Problems .

- 1) Toss a coin 10 times with probability (heads = 0.6)
let X be the number of heads.
- 1) Find the probability of ① 7 heads , ② 4 heads
 - ③ Atmost 4 heads , ④ at least 6 heads
 - ⑤ no head ⑥ All heads
- Also find expectation and variance .

> dbinom(1, 5, 0.1)

[1] 0.328

> dbinom(2, 5, 0.1)

[1] 0.0729

> dbinom(3, 5, 0.1)

[1] 0.0081

> dbinom(4, 5, 0.1)

[1] 0.00045

> dbinom(5, 5, 0.1)

[1] 1e-05

4) Find the probability of exactly 10 success out of 100 trials with $p = 0.1$

→ pbinom(100, 10, 0.1)

[1] 1

5) X follows binomial distribution with $n=12$ & $p=0.25$

Find (i) $P(X \leq 5)$ (ii) $P(X > 7)$ (iii) $P(5 \leq X \leq 7)$

> pbinom(5, 12, 0.25)

[1] 0.94755

> 1 - pbinom(7, 12, 0.25)

[1] 0.0027

> pbinom(6, 12, 0.25)

[1] 0.985

6) There are 10 members in a committee. Probability of any member attending a meeting is 0.9. What is the probability that members are attending the meeting?

> pbinom(7, 10, 0.9)

[1] 0.070190

- 7) A salesman making a sale to a customer on a typical day has 20% probability to meet 30 customers. What is the minimum no. of sales he will make with 88% probability?
- $\Rightarrow > \text{dbinom}$
 $[1] 9$

- 8) For $n = 10$, $p = 0.6$. Find the binomial probability of that & plot the graphs of pmf & cdf.

$> n = 10$
 $> p = 0.6$
 $> x = 0:n$
 $> bp = \text{dbinom}(x, n, p)$
 $> d = \text{data.frame,}$
 $(\text{"x.values"} = x, \text{"Probability"} = bp)$
 $> d$

	<u>x.values</u>	Probability
1	0	0.00104
2	1	0.0015
3	2	0.0010
4	3	0.42467
5	4	0.11147

580

6
7
8
9
10
11

5
6
7
8
9
10

0.2000
0.250822
0.21499
0.12093
0.04031
0.00604

Q1. check w

i)

x	
$P(x)$	0

condi

si

2)

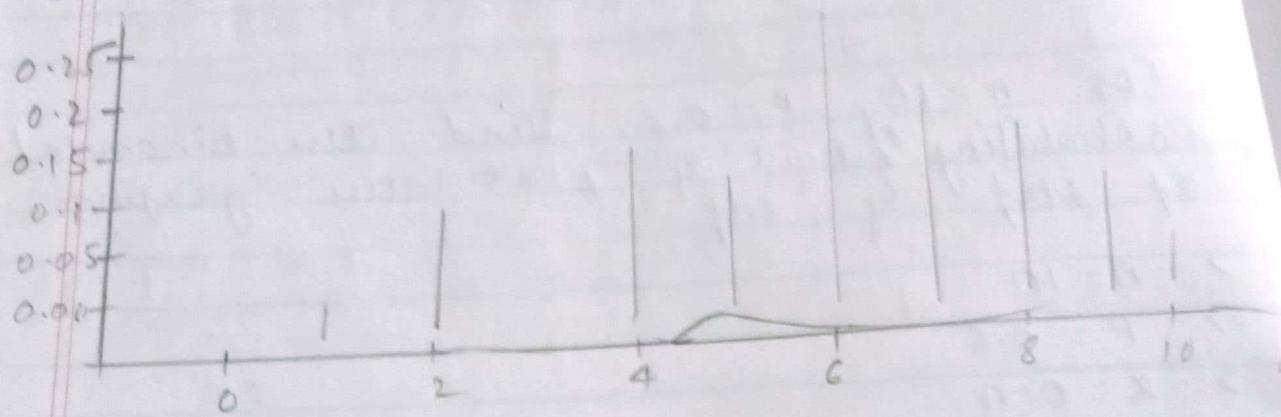
x	
$P(x)$	

> Px
>

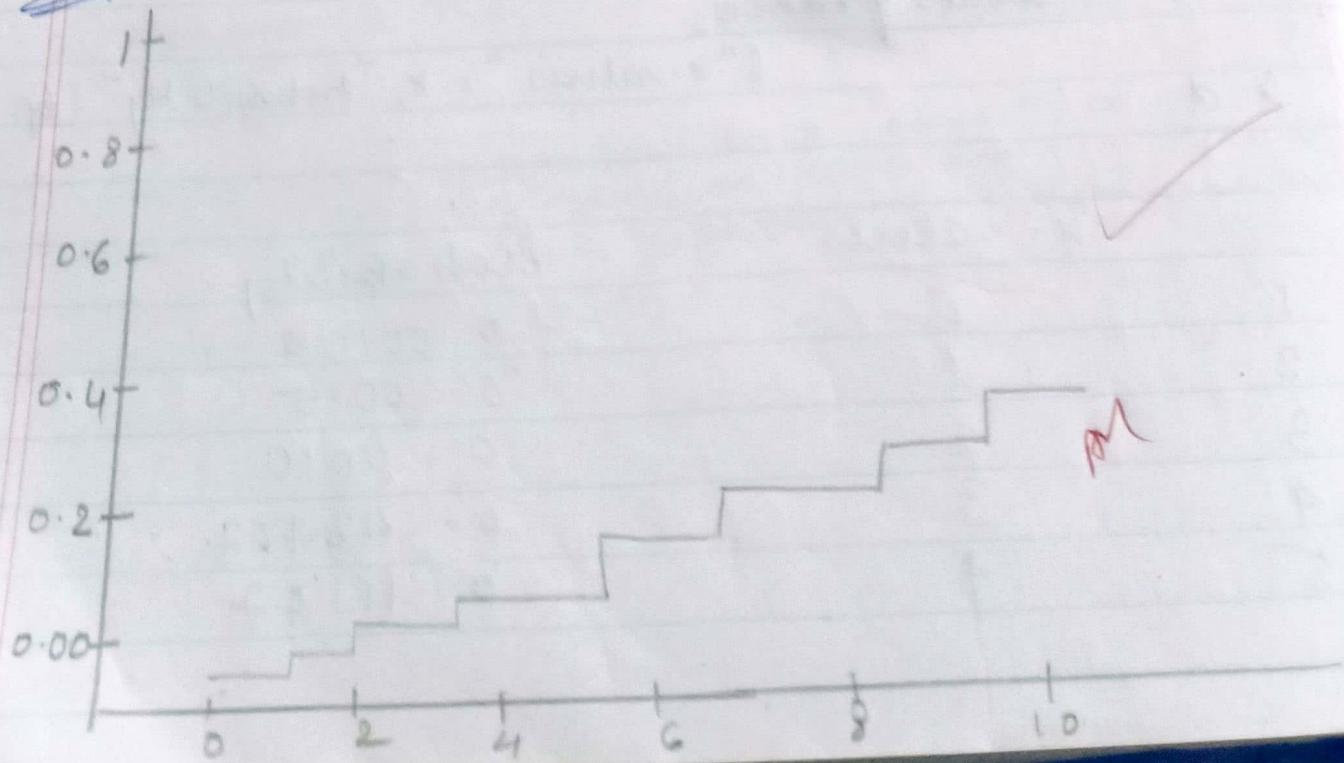
[1]

2

pmt



cdf



Q2. Following is a pmf of (x)

x_i	1	2	3	4	5
$P(x)$	0.1	0.15	0.2	0.3	0.25

Find mean & variance.

x_i	$P(x)$	$xP(x)$	$x^2 P(x)$
1	0.1	0.1	0.1
2	0.125	0.3	0.6
3	0.2	0.6	1.8
4	0.3	1.2	4.8
5	0.25	1.25	6.25

$$\sum x P(x) = 3.45 \quad \sum x^2 P(x) = 13.55$$

$$\text{Mean} = E(x) = \sum x P(x) = 3.45$$

$$\begin{aligned}\text{Var} &= V(x) = \sum x^2 P(x) - [\sum x P(x)]^2 \\ &= 13.55 - (3.45)^2 \\ &= 1.6475\end{aligned}$$

Using R

> $x = \text{seq}(1, 5, 1)$

Prob = c(0.1, 0.15, 0.2, 0.3, 0.25)

a = x * prob

sum(a)

sum(b)

mean = sum(a)

mean

[1] 3.45

b = (x^2) * prob

var = sum(b) - mean^2

var

[1] 1.6475

PRACTICAL - 3

038

Q1. check the following are pmf or not.

x	1	2	3	4	5
$P(x)$	0.2	0.5	-0.5	0.5	0.4

condition for it is 1) $0 \leq P(x) \leq 1$

$$2) \sum_{x_i} P(x_i) = 1$$

since, it doesn't satisfy the given condition
 \therefore It is not a pmf.

x	10	20	30	40	50
$P(x)$	0.3	0.2	0.3	0.1	0.1

$$> \text{Prob} = C(0.3, 0.2, 0.1, 0.1)$$

$$> \text{sum (Prob)}$$

[1] 1

Hence it is satisfying both the condition.

\therefore It is a pmf.

x	0	1	2	3	4
$P(x)$	0.4	0.2	0.3	0.2	0.1

$$> \text{Prob} = C(0.4, 0.2, 0.3, 0.2, 0.1)$$

$$> \text{sum (Prob)}$$

[1] 1.2

Hence it is not satisfying the condition

It is not a pmf.

Find mean and variance of X .

x	5	10	15	20	25
$p(x)$	0.1	0.3	0.2	0.25	0.15

Using R

$$x = \text{seq}(5, 25, 5)$$

$$\text{Prob} = c(0.1, 0.3, 0.2, 0.25, 0.15)$$

$$a = x^* \text{Prob}$$

$$\text{mean} = \text{sum}(a)$$

mean

$$[1] 15.25$$

$$b = (x^2)^* \text{Prob}$$

$$\text{Var} = \text{sum}(b) - \text{mean}^2$$

Var

$$[1] 38.6875$$

Q4) i) Find Gdf of the following pmf and draw the graph of cdf

x	1	2	3	4
$p(x)$	0.4	0.3	0.2	0.1

$$a = \text{seq}(1, 4, 1)$$

$$\text{Prob} = c(0.4, 0.3, 0.2, 0.1)$$

$$a = \text{cumsum}(\text{Prob})$$

a

$$[1] 0.4, 0.7, 0.9, 1.0$$

880

$$F(x) = \begin{cases} 0 & \text{if } x < 0 \\ 0.4 & \text{if } 0 \leq x < 2 \\ 0.7 & \text{if } 2 \leq x < 3 \\ 0.9 & \text{if } 3 \leq x < 4 \\ 1.0 & \text{if } x \geq 4 \end{cases}$$

> plot (x, F(x), "S")

x		0		2		4		6		8	
F(x)		0.2		0.3		0.9		0.2		0.1	

> x = seq(0, 8, 2)

$$\text{Prob} = c(0.2, 0.3, 0.2, 0.2, 0.1)$$

a = cumsum(Prob)

-a

[1] 0.2 0.5 0.7 0.9 1.0

$$f(x) = \begin{cases} 0 & \text{if } x < 0 \\ 0.2 & \text{if } 0 \leq x < 2 \\ 0.5 & \text{if } 2 \leq x < 4 \\ 0.7 & \text{if } 4 \leq x < 6 \\ 0.9 & \text{if } 6 \leq x < 8 \\ 1.0 & \text{if } x \geq 8 \end{cases}$$

> plot (x, f(x), "S")

PRACTICAL - 04

$$P(X=x) = \binom{n}{x} p^x q^{n-x}$$

given
 $n=8, p=0.6, q=0.4$

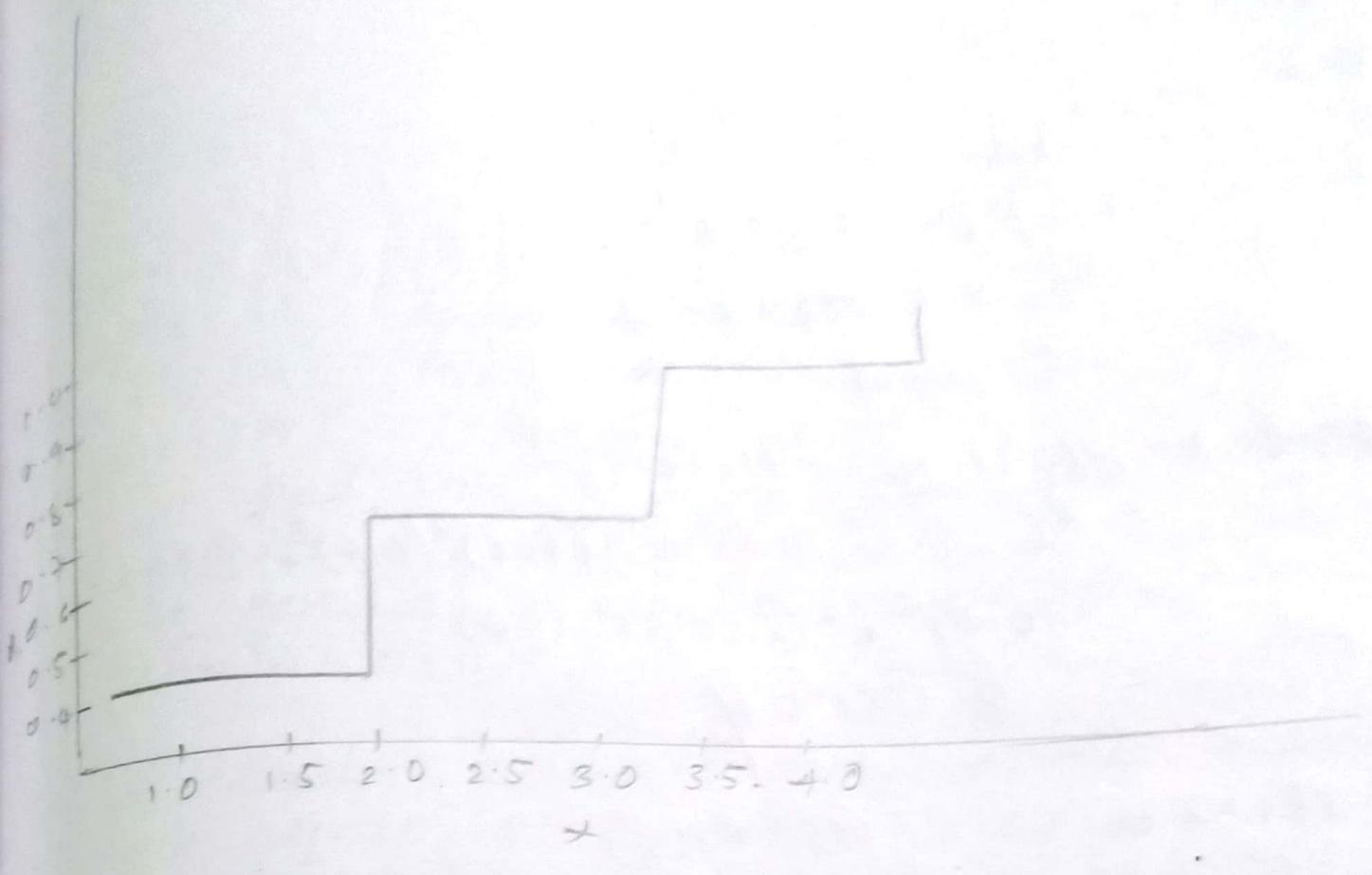
$$\begin{aligned} 1. P(X=7) &= \binom{8}{7} (0.6)^7 (0.4) \\ &= {}^8C_7 \times 0.2799 \times 0.4 \\ &= 0.08957 \end{aligned}$$

$$\begin{aligned} 2. P(X \leq 3) &= P(0) + P(1) + P(2) + P(3) \\ &= {}^8C_0 (0.6)^0 (0.4)^8 + {}^8C_1 (0.6)^1 (0.4)^7 + {}^8C_2 (0.6)^2 \\ &= (0.4)^0 + {}^8C_3 (0.6)^2 (0.4)^3 \\ &= 0.1736704 \end{aligned}$$

$$\begin{aligned} 3. P(X=2 \text{ or } 3) &= P(2) + P(3) \\ &= 0.04128768 + 0.12386304 \\ &= 0.161515012 \end{aligned}$$

M

040



PRACTICAL - 05
Normal distribution

$$x \sim N(\mu, \sigma^2)$$

$$p(x = x) = dnorm(x, \mu, \sigma)$$

$$p(x \leq x) = pnorm(x, \mu, \sigma)$$

$$p(x > x) = 1 - pnorm(x, \mu, \sigma)$$

To find the value of K , so that $p(x \leq K) = P$
 $qnorm(P, \mu, \sigma)$

To generate a random sample of size n ,
 $rnorm(n, \mu, \sigma)$

A random variable x follows normal distribution
 with $\mu = 10$, $\sigma = 2$, find:

$$\begin{aligned} i) \quad & p(x \leq 7) & ii) \quad & p(x > 12) & iii) \quad & p(5 \leq x \leq 12) \\ iv) \quad & p(x < K) = 0.4 \end{aligned}$$

$$> p1 = pnorm(7, 10, 2)$$

$$> p1$$

$$[1] 0.0668072$$

$$> p2 = 1 - pnorm(12, 10, 2)$$

$$> p2$$

$$[1] 0.1586553$$

$$> p3 = pnorm(12, 10, 2) - pnorm(5, 10, 2)$$

$$> p3$$

$$[1] 0.8351351$$

$$> k = qnorm(0.4, 10, 2)$$

$$> k$$

$$[1] 9.493306$$

110

Q2. $X \sim N(100, 36)$

- (i) $P(X \leq 110)$ (ii) $P(X \geq 105)$ (iii) $P(X \leq 92)$
(iv) $P(95 \leq X \leq 110)$ (v) $P(X < k) = 0.9$

> a = pnorm(110, 100, 6)

> a

[1] 0.9522090

> b = 1 - pnorm(105, 100, 6)

> b

[1] 0.2023284

> c = pnorm(92, 100, 6)

> c

[1] ~~0.09121122~~ 0.09121122

> d = pnorm(108, 100, 6) - pnorm(95, 100, 6)

> d

[1] 0.7498813

> k = qnorm(0.9, 100, 6)

> k

[1] 107.6893

Q3 generate 10 random samples & find sample
mean, median, variance & S.D

042

> x = rnorm(10, 10, 3)

> x

[1] 13.937393 12.040522 11.512806 9.774476
5.884007 8.433805 15.813018 14.174675
6.495235 9.305191

> mu = mean(x)

[1] 10.73711

> mc = median(x)

[1] 10.64364

> n = 10

[1] 10

> var = (n-1) * var(x)/n

> var

[1] 9.995247

> sd = sqrt(var)

> sd

[1] 3.161526

Q4 Plot the standard curve

> x = seq(-3, 3, by = 0.1)

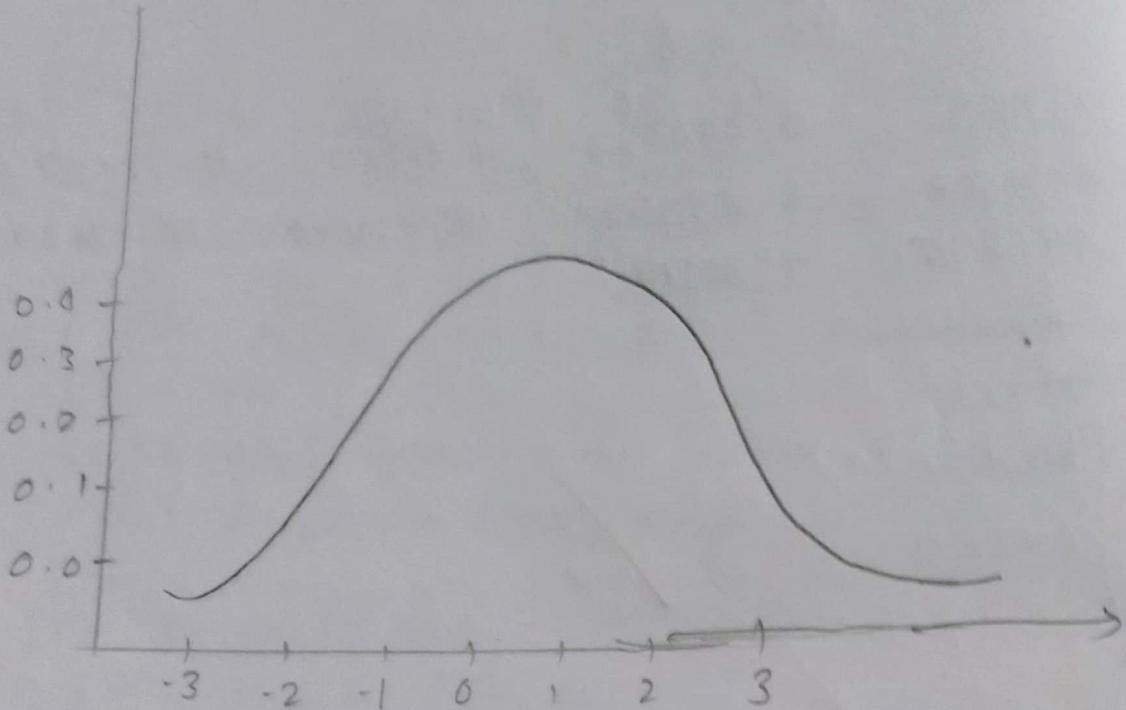
> x

> y = dnorm(x)

> y

> plot(x, y, xlab = "x values", ylab = "probabilities")
main = "standard normal curve")

540



Q5. $X \sim N(50, 100)$

Find : (i) $P(X \leq 60)$ (ii) $P(X > 65)$ (iii) $P(45 \leq X \leq 60)$

> $\text{Pnorm}(60, 50, 10)$

[1] 0.8413447

> $\text{Pnorm}(60, 50, 10) - \text{Pnorm}(45, 50, 10)$

[1] 0.5328072

> 1 - $\text{Pnorm}(65, 50, 10)$

[1] 0.0668072

PM

PRACTICAL NO: 6
Z & T distribution

1) Test the hypothesis ; $H_0 : \mu = 20$ against $H_1 : \mu \neq 20$
 A sample of size 400 is selected by the
 sample mean is 20.2 & the standard deviation
 is 2.25. Test at 5% level of significance
 > $m_0 = 20$; $m_x = 20.2$; $s_d = 2.25$; $n = 400$
 > m_0 ; m_x ; s_d ; n

[1] 20
 [1] 20.2
 [1] 2.25
 [1] 400

$$> z_{cal} = (m_x - m_0) / (s_d / \sqrt{n})$$

> z_{cal}
 [1] 1.777778

> Let "Z calculated is =" z_{cal}
 $z_{calculated} = 1.777778 >$

> Pvalue = $2 * (1 - pnorm(\text{abs}(z_{cal})))$

> Pvalue

[1] 0.0754

Since the value is greater than 0.05 we
 accept the value of μ .

2) We want to test the hypothesis $H_0 : \mu = 250$
 against $H_1 : \mu \neq 250$. A sample of size
 100 has a mean of 275 & S.D is 50
 Test the hypothesis at 5% level of significance

> $m_0 = 250$; $m_x = 275$; $sd = 30$; $n = 100$

> m_0 ; m_x ; sd ; n

[1] 250

[1] 275

[1] 30

[1] 100

> $z_{cal} = (m_x - m_0) / (sd / \sqrt{n})$

> z_{cal}

[1] 8.3333

> ~~* Cat ("Calculated is =", zcal)~~

~~Calculated is = 8.3333 >~~

> Pvalue = $2^* (1 - \text{pnorm}(\text{abs}(z_{cal})))$

> Pvalue

[1] 0

We reject H_0 :
4

3] We want to test the hypothesis ~~at~~ $H_0: p =$ against $H_1: p \neq 0.2$ (P = Population proportion)
A sample of 400 is selected and the sample proportion is calculated 0.125. Test the hypothesis at 1%.

> $p = 0.2$

> $Q = 1 - p$ [1] 0.8

> ~~p~~ $p = 0.125$

> $n = 400$

$$z_{\text{cal}} = (p - \hat{p}) / (\text{sgt}(p * q/n))$$

044

$$z_{\text{cal}} = 3.75$$

- [1] In a big city 325 men out of 600 men were found to be self-employed thus this information supports the conclusion that half of the men in the city are self-employed? ($P = 0.5$)

$$\hat{p} = 325/600$$

$$\hat{p}$$

$$[1] 0.541667$$

$$\hat{n} = 600$$

$$\hat{q} = 1 - \hat{p}$$

$$Q$$

$$[1] 0.5$$

$$z_{\text{cal}} = (p - \hat{p}) / (\text{sgt}(p * \hat{q}/n))$$

$$z_{\text{cal}}$$

$$[1] 2.041241$$

$$p\text{value} = 2 * (1 - \text{Prnorm}(\text{abs}(z_{\text{cal}})))$$

$$p\text{value}$$

$$[1] 0.04122683$$

- 0.2
4) Test the hypothesis $H_0: \mu = 50$ against $H_1: \mu \neq 50$

a sample of 30 is collected

47, 45, 49, 45, 48, 46, 45, 49, 45, 40, 47,
50, 49, 52, 44, 45, 48, 46, 45, 49, 45, 40, 47,
55, 54, 46, 58, 47, 44, 59, 60, 61, 41, 52,
44, 55, 56, 46, 45, 48, 49

110
 > $s = c(50, 49, 52, 44, 45, 48, 46, 45, 49, 45, 46, 48, 46, 44, 49, 50, 51, 52, 53, 54, 46, 58, 49, 44, 59, 60, 61, 41, 52, 49, 46, 45, 48, 49)$
 > s
 [1] ~~44~~ 44
 > length(s)
 [1] 30
 > mu = mean(s)
 > mx
 [1] 49.3333
 > sd = sd(s)
 > cd
 [1] 5.658886
 > mo = 50
 > var = (n-1) * var(s) / length(s)
 > var
 [1] 639 - 3923
 3) > n = length(s)
 > n
 [1] 30
 > zcal = (mo - mx) / sd / (sqrt(n))
 > zcal
 [1] 0.02150885
 > pvalue = 2 * (1 - pnorm(abs(zcal)))
 > pvalue
 [1] 0.9828397

RM
 2021-20

PRACTICAL NO : 07
Large sample test.

- 1) two random samples drawn from 2 populations with size 1000, 2000 are respectively. Test the hypothesis that the 2 population means are equal or not at 5% level of significance. The sample means are 67 and 68. respectively.
- $$H_0: \mu_1 = \mu_2 \quad \text{against } H_1: \mu_1 \neq \mu_2$$

> $n_1 = 1000$
 > $n_2 = 2000$
 > $m\bar{x}_1 = 67$
 > $m\bar{x}_2 = 68$
 > $sd_1 = 2$
 > $sd_2 = 3$
 > $z_{cal} = (\bar{x}_1 - \bar{x}_2) / \sqrt{(sd_1^2/n_1 + sd_2^2/n_2)}$

> cat ("2 calculated is =", zcal)
 > z calculated is = -10.84652.

> pval = 2 * (1 - pnorm(abs(zcal)))

> pval

[1] 0

$\therefore pval < 0.05$, we reject $H_0: \mu_1 = \mu_2$

Q) A study at noise level in two hospitals is demonstrated. following data is calculated first sample is

$$\Rightarrow n_1 = 84$$

$$> n_2 = 84$$

$$> \bar{x}_1 = 61.7$$

$$> \bar{x}_2 = 59.2$$

$$> s_1 = 7.9$$

$$> s_2 = 7.8$$

$$> z_{cal} = (\bar{x}_1 - \bar{x}_2) / \sqrt{(\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2})}$$

$$[1] 1.131111$$

$$> pvalue = 2 * (1 - pnorm(abs(z_{cal})))$$

$$> pvalue$$

$$[1] 0.2580$$

∴ p-value is > 0.01 , we accept the $H_0: \mu_1 = \mu_2$

Q3) from each of the 2 population of oranges
 the following samples are collected
 the proportion of bad oranges are equal or not
 whether
 sample size = 250
 no. of bad oranges = 44 2) sample size = 200
 no. of bad oranges = 30

$H_0: P_1 = P_2$ against $H_1: P_1 \neq P_2$

$$\geq n_1 = 250$$

$$\geq n_2 = 200$$

$$\geq P_1 = 44/250$$

$$\geq P_2 = 30/200$$

$$\geq P = (n_1 * P_1 + n_2 * P_2) / (n_1 + n_2)$$

$$\geq P$$

$$[1] 0.1644$$

$$\geq q = 1 - P$$

$$\geq Z_{\text{cal}} = (P_1 - P_2) / \sqrt{P * q * (1/n_1 + 1/n_2)}$$

$$[1] 0.7343$$

$$\geq \text{Pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(Z_{\text{cal}})))$$

$$\geq \text{Pvalue}$$

$$[1] 0.4590$$

$\therefore \text{Pvalue} > 0.05$, we accept $H_0: P_1 = P_2$

Q4). Random Sample of 400 males & 600 females
 where as need whether they want a ATM
 nearly. 200 males & 340 females were in favour
 of proposal, test the hypothesis that the
 proportion of males & females favouring proposal
 are equal or not at 5%.

320
→ $H_0: P_1 = P_2$ against $H_1: P_1 \neq P_2$

> $n_1 = 400$

> $n_2 = 600$

> $P_1 = 200/400$

> $P_2 = 340/600$

=> $P = (n_1 * P_1 + n_2 * P_2) / (n_1 + n_2)$

> P

[1] 0.59

> $q = 1 - P$

> $z_{\text{cal}} = (P_1 - P_2) / \sqrt{P * q * (1/n_1 + 1/n_2)}$

> z_{cal}

[1] -1.7247

> $P\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$

[1] 2.303922e-06

∴ $P\text{value} < 0.05$, we reject $H_0: P_1 = P_2$.

Q5. Following are the two independent samples from the 2 population test. equally bc of 2 population mean at 5% level of significance

$$x_1 = 74, 77, 74, 75, 79, 70, 82, 72, 75, 78, 77, 76, 70.$$

$$x_2 = 72, 76, 74, 70, 70, 78, 70, 72, 75, 79, 75, 78, 72, 74, 80.$$

1) $y_1 = 4.1, 4.7, 7.7, 7.4, \dots$, $y_2 = 4.1, 4.7, 7.7, 7.4, \dots$
 2) $n_1 = \text{length}(y_1)$
 3) $m\bar{x}_1 = \text{mean}(y_1)$
 4) variance = $(n_1 - 1) * \text{var}(y_1) / n_1$,
 5) variance
 [1] 0.4508
 6) $sd^2 = \text{sqrt}(\text{variance})$
 7) sd^1
 [1] 0.6714
 8) $y_2 = 7.2, 7.6, 7.4, \dots$
 9) $n_2 = \text{length}(y_2)$
 10) $m\bar{x}_2 = \text{mean}(y_2)$
 11) var = $(n_2 + 1) * \text{var}(y_2) / n_2$
 [1] 0.6168
 12) $sd^2 = \text{sqrt}(\text{var})$
 [1] 0.7850
 13) $t_{\text{cal}} = (m\bar{x}_1 - m\bar{x}_2) / \text{sqrt}((sd^1)^2 / n_1 + (sd^2)^2 / n_2)$
 14) t_{cal}
 [1] 1.5151
 15) cat("t calculated is : ", tcal)
 [1] t calculated is 1.5151

580

PRACTICAL NO: 08
small sample test

- 1) The random sample of 15 observations are given by 80, 100, 110, 105, 122, 70, 120, 110, 101, 88, 85, 89, 107, 125. Do this data support the assumption that population mean is 100
 $H_0: \mu_1 = \mu_2$

> $x = c(80, 100, 110, \dots, 125)$

> x

> $t.test(x)$

one sample t-test

data: x
 $t = 24.029$, $df = 14$, p-value = $8.819e-13$

alternative hypothesis: true mean is not equal to 0

95 percent confidence interval:

91.3775 109.28892

sample estimates:

mean of x

100.3333

Since p-value is less than 0.05 the value of $H_0: \mu_1$ is rejected.

- 2) Two groups of 10 students score the following marks

group 1 - 18, 22, 21, 17, 20, 17, 23, 20, 22, 21
group 2 - 16, 20, 14, 21, 20, 18, 13, 15, 17, 21

Test with hypothesis that there is no significant difference between the two at 1% level of significance.

$H_0 = \mu_1 = \mu_2$
grp A = C (18, 22, ...)
grp B = C (16, 20, ...)

> t-test (grp A, grp B)

welch two sample t-test

data: grp A and grp B

$t = 2.2573$, $df = 16.376$, p-value = 0.03798

alternative hypothesis: true difference in means is not equal to 0

95 percent confidence interval:

0.1628205 5.0371795

sample estimates:

mean of X mean of Y

20.1

∴ p-value is greater than 0.05 it is accepted.

3) Two types of medicine are used on 5 and 7 patients for reducing their weight.

The decrease in the weight after using medicine given below.

$$\underline{H_0: \mu_1 = \mu_2}$$

A = 10, 12, 13, 11, 14

B = 8, 9, 12, 14, 15, 10, 9

Is there a significant difference in effect of the medicine.

80
 $H_0: \mu_1 = \mu_2$
 $\Rightarrow \begin{cases} x = CC[10, 12, \dots] \\ y = CC[8, 9, \dots] \end{cases}$
 $\Rightarrow \begin{cases} x \\ [1] \end{cases} = 10, 12, \dots$
 $\Rightarrow \begin{cases} y \\ [1] \end{cases} = 8, 9, \dots$
 $\Rightarrow t.test(x, y)$
 Welch two sample t-test

data : x and y
 $t = 0.80884, df = 9.7594, p\text{-value} = 0.4406$
 alternative hypothesis : true difference in means
 is not equal to 0.
 $-1.78117, 3.78117$
 sample estimates:
 mean of x and y
 $12, 11$
 since p-value is greater than 0.05 we
 accept the value.

- 2) The weight reducing diet program is conducted and the observations are noted by 10 participants test whether the program is effective or not

data before - 120, 125, 115, 130, 123, 119, 122, 127, 118

after - 101, 114, 107, 120, 115, 112, 112, 120, 119

Q10

$$H_0: \mu_1 = \mu_2$$

⑧
 > a = c(60, ...),
 > b = c(64, ...)
 > t.test(a, b)

welch two sample t-test

data: a ~ b

t = -0.6303, df = 13.836, p-value = 0.5382

alternative hypothesis: true difference in mean is not equal to 0

95 percent confidence interval:

-15.422359 8.422359

mean of X mean of Y
80.0 83.5

Since p-value is greater than 0.05

H_0 : There is no significant difference against H_1 : the diet program reduce weight
 $H_0: \mu_1 = \mu_2$.

- ? d. before = G (120, 125 ...)
- ? d. after = C (111, 114 ...)
- ? t-test (d. before, d. after, paired = T, alternative = "less")

Paired t-test.

data: d. before and d. after

$t = 9.0711$, $df = 9$, p-value = 1

alternative hypothesis: true difference in mean is less than 0

95 percent confidence interval:

- Inf 9.616654

sample estimates:

mean of the differences.

8.

since p-value is greater than 0.05 we accept the value

5) Sample A = 68, 67, 75, 76, 82, 84, 88, 90,
 \checkmark 92

B = 64, 66, 74, 78, 82, 85, 87, 92, 93, 95
 \checkmark 97

Test the population means are equal or not

$H_0: \mu_1 = \mu_2$

- Q) The following are marks before & after ⁰⁵⁰
 test the program is effective or not.
- before = 71, 72, 74, 69, 70, 74, 76, 70, 73, 75
 after = 74, 77, 74, 73, 79, 76, 82, 72, 75, 71
- H₀: $\mu_1 = \mu_2$
- > before = c(71, ...)
 > after = c(74, ...)
 > t.test(before, after, paired = T, alternative = "greater")
- Paired t-test:

data : before & after

t = -4.4691, df = 9, P-value = 0.9992

alternative hypothesis : true difference in means is greater than 0.

95 percent confidence interval :

-5.076639

sample estimates. ^{int}

mean of the differences

-3.6

∴ p-value is greater than 0.05 we accept the value.

AM
67.62 20

B - 64, 66, 74, 82, 85, 87, 92, 95, 93, 97.
 Test whether the variance at 5% level population has the same level of significance.

$$\begin{aligned} n &= 100 \\ \bar{x} &= 52 \\ m_0 &= 55 \\ s_d &= 7 \end{aligned}$$

$$z_{\text{cal}} = (\bar{x} - m_0) / (s_d / (\sqrt{n}))$$

> z_{cal}

$$[1] \quad z_{\text{cal}} = -4.285714$$

$$> \text{Pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

> Pvalue

$$[1] \quad 1.82153e-05$$

\therefore Pvalue is less than 0.05 we reject the null hypothesis $H_0: \mu_1 = \mu_2$.

Q.

$$\Rightarrow P = 0.5$$

$$\Rightarrow p = 350/700$$

$\Rightarrow p =$

$$[1] \quad 0.5$$

$$\Rightarrow n = 700$$

$$\Rightarrow q = 1 - p$$

$$\Rightarrow q$$

$$[1] \quad 0.5$$

PRACTICAL - NO-9.

large & small number sample test

- Q1. The arithmetic mean of sample of 100 items from a large population is 52 if a standard deviation is 7. test the hypothesis that the population mean is 55 against the alternative population mean is more than 55 at 5% level of significance.
- Q2. In big city 350 out of 100 males are found to be smokers thus this information supports the exactly half of the males in the city are smokers? Test at 1%. LOS
- Q3. 1000 articles from a factory A are found to have 2% defectives. 1500 article from a second factory B are found to have 1% defective. Test that 5% level of significance that the two factory similar or not.
- Q4. A sample of size 400 was drawn by a sample mean 99 test at 5% LOS that the sample comes from the population with mean 100 variance 64?
- Q5. The flower stems are selected by the heights are found to be (cm) 63, 63, 68, 69, 71, 71, 72. Test the hypothesis that mean weight is 66 or not at the 1% of significance.
- Q6. Two random sample were drawn from two normal populations and their values are A - 66, 67, 75, 76, 82, 84, 88, 90, 92 -

B - 64, 66,
Test w/
variance

$$\begin{aligned} n &= 100 \\ mx &= 5 \\ mo &= \\ sd &= \\ zcal &= \\ &> zcal \\ [1] & \\ &> P \\ &> P \\ &> P \\ [1] & \end{aligned}$$

$$\begin{aligned} g. & \\ \Rightarrow & P \\ &> P \\ &> P \\ &> P \\ &> P \end{aligned}$$

```

> p = 0.5
> zcal = (p - P) / (sqrt(p * q / n))
> zcal
[1] 0
> pval = 2 * (1 - pnorm(abs(zcal)))
> pval
[1] 1
∴ pvalue > 0.05 we accept the value.

```

3.

\Rightarrow

```

> n1 = 1000
> n2 = 1500
> p1 = 0.02
> p2 = 0.01

```

$$\Rightarrow \bar{q} = 1 - \bar{p}$$

```

> p = (n1 * p1 + n2 * p2) / (n1 + n2)

```

$$\Rightarrow \bar{p}$$

```
[1] 0.014
```

$$\Rightarrow \bar{q} = 1 - \bar{p}$$

$$\Rightarrow \bar{q}$$

$$\Rightarrow 0.986$$

$$> zcal = (p1 - p2) / sqrt(p * q * (1/n1 + 1/n2))$$

\Rightarrow

```

> zcal

```

```
[1] 2.084842
```

$$> pvalue = 2 * (1 - pnorm(abs(zcal)))$$

\Rightarrow

```

> pvalue

```

```
[1] 0.03708364
```

\therefore Value is less than 0.05 we reject the value

$$H_0 : \mu_1 = \mu_2$$

1. \Rightarrow

```

> n = ?
> mx = ?
> mo = ?
> var = ?
> sd = ?
> sd = ?
[1] 8
> zca
> zca
[1] -
> pva
> pva
[1] 0

```

```

> n = 100
> mx = 99
> mo = 100
> var = 64
> sd = sqrt(var)
> sd
[1] 8

```

```

> zcal = (mx - mo) / (sd / sqrt(n))
> zcal
[1] -2.5

```

```

> Pvalue = 2 * (1 - pnorm(abs(zcal)))
> Pvalue

```

[1] 0.01241933
~~Pvalue < 0.05 we reject null hypothesis.~~

5.
> x = c(63, 63, 68, 69, 71, 71, 72)

```

> x
[1] 63 63 68 69 71 71 72
> t.test(x)

```

one sample t-test

data : v

t = 47.94, df = 6, Pvalue = 5.52e-09

alternative hypothesis: true mean is equal to
0 as present confidence interval:

64.6647 71.622092

sample size tested:

mean of x

68.14286

520

∴ P-value is less than 0.01. we reject $H_0 : \sigma^2 = \sigma_0^2$

Q6.

H_0 : population is same

σ_1^2 = variance in population

$> \bar{x} = \text{mean(Data)}$

$> \bar{y} = \text{mean(Data)}$

$> F = \frac{\bar{x}}{\bar{y}}$ var, test(\bar{x}, \bar{y})

$> F$

F test to compare 2 variance.

data = \bar{x} & \bar{y}

$F = 0.70687$, num df = 8, denom df = 10, p-value = 0.6359

solution alternative hypothesis: true ratio of variance is not equal to 1.

75 percent confidence interval:

0.1833

3.036039

sample estimates:

ratio of variances

0.70687

∴ P-value is greater than 0.05: we accept $H_0 : \sigma^2 = \sigma_0^2$ i.e. the population have some variance.

PRACTICAL - 10

Anova and chi-square test
 Use the following data to test whether the cleanliness of home & cleanliness of the child independent or not.

	clean	dirty
clean	70	50
fairly clean	80	20
dirty	35	45

H_0 : CC & CH

$x = \{20, 80, 35, 50, 20, 45\}$

$m = 3$ (rows)

$n = 2$ (columns)

$y = \text{matrix}(x, \text{row} = m, \text{ncol} = n)$

y

	[, 1]	[, 2]
[1,]	70	50
[2,]	80	20
[3,]	35	45

$PV = \text{chisq.test}(y)$

PV

Pearson's Chi - squared test

data : y

$\chi^2 = 25.646, df = 2, p\text{-value} = 2.698e^{-4}$

i. P-value

H₀: vaccination is better than 0.05 we expect except
H₁: varieties are independent

b. perform ANOVA for our data.

A

B

C

D

observations

50, 52

53, 55, 53

56, 58, 57, 56

52, 51, 54, 55

, H₀: The means of the varieties are equal

> $\bar{x}_1 = \text{mean}(50, 52)$

> $\bar{x}_2 = \text{mean}(53, \dots)$

> $\bar{x}_3 = \text{mean}(56, \dots)$

> $\bar{x}_4 = \text{mean}(52, \dots)$

> d = stack(list(b1 = x1, b2 = x2, b3 = x3, b4 = x4))

> one way.test(values ~ vrid, data = d, var.equal = T)

data : values and vrid

F = 11.735, numdf = 3, denom df = 9, pvalue = 0.00123

> anova = aov(values ~ vrid, data = d)

> anova

Call:

aov(formula = values ~ vrid, data = d)

terms :

sum of squares	vrid	Residuals
71.06416	18.10667	

Deg. of freedom	3	9

If p-value is less than 0.05 we reject.

$$H_0: CC \text{ & } CF$$

- Q2. Use the following data to find association of a particular disease on independence.

	DEF	Not DEF
Vaccination	20	80
Given		
Not given	25	35

$\Rightarrow H_0: \text{Vaccination and disease are independent}$

$$> x = c(20, 25, 80, 35)$$

$$> m = 2$$

$$> n = 2$$

> y: matrix (nrow=m, ncol=2)

> y

	[1,1]	[1,2]
[1,]	20	30
[2,]	25	35

> p = chisq.test(y)

> p

Pearson's Chi-squared test with Yates' continuity

data: y

X-squared = 5, df = 1, p-value = 0.024

Residual standard error: 1.42074
estimated effects maybe unbalanced

Since pvalue is less than 0.05

H_0 : The means of the varieties are equal

Q4. The following data gives the life of 4 brands

Type	Observation
A	20, 23, 18, 17, 18, 22, 24
B	19, 15, 17, 20, 16, 17
C	21, 19, 22, 17, 20
D	15, 14, 16, 18, 14

Test the hypothesis that the average life for the four brand are same

$\rightarrow H_0$: Avg life of 4 brands are same.

$$> x_1 = c(20, 23, 18, 17, 18, 22, 24)$$

$$x_2 = c(19, 15, 17, 20, 16, 17)$$

$$x_3 = c(21, 19, 22, 17, 20)$$

$$x_4 = c(15, 14, 16, 18, 14)$$

$$d = \text{stack}(\text{list}(b_1 = x_1, b_2 = x_2, b_3 = x_3, b_4 = x_4))$$

> names(d)

> one way. test (values ~ind, data = d, var ~qval,
one way analysis of means)

data: values ~ind

P = 0.8445, numdf = 3, denomdf = 20, P value:
0.00234

? anova = aov (values ~ ind, data = d)

? anova

(all)

? aov (formula = values ~ ind, data = d)

same!

	ind	Residuals
Sum of squares	91.4381	89.0619
Deg. of freedom	3	20

Residual standards dev: 2.110236.

estimated effects may be unbalanced

∴ the p-value is less than 0.05, we reject

? One thousand students of a college are graded according to their IQ and the economic condition of their home. Check that is there any association between IQ and their economic condition of their home.

		high	low
EC	Med	330	200
	low	240	160

PRACTICAL NO: 11

Non-parametric test

056

Following are amounts of sulphuric oxide emitted by industries in 20 days to test hypothesis that population median is 21.5 to test observations -

17, 15, 20, 29, 19, 18, 22, 25, 27, 9
24, 20, 17, 6, 24, 14, 15, 23, 20, 26

H0: population median is 21.5

> x = c(17, 15, ...)

> x median = 21.5

> sp = length(x[x > med])

> SP

[1] 9

> sn = length(x[x < med])

[1] 11

> n = sp + sn

> n

[1] 20

> pv = pbinom(sp, n, 0.5)

> PV

[1] 0.4119015

∴ pvalue > 0.05 we accept H0.

→ H_0 : EC & IQ are independent
 $x = c(460, 330, 240, 140, 200, 160)$

> $m = 3$

> $n = 2$

> $y = \text{matrix}(x, \text{ncol} = m, \text{nrow} = n)$

> y

	[,1]	[,2]
[1,]	460	140
[2,]	330	200
[3,]	240	160

> $\text{pr} = \text{chisq.test}(y)$

> pr Pearson's chi-squared test

data : y

$X^2 = 39.726$, df = 2, p-value = 2.364e-05

∴ p-value is less than 0.05, we reject

H_0 : EC & IQ are independent

PM

Q30

Q3. Following are the 10 observations

612, 619, 631, 628, 643, 640, 655, 64,
670, 663

Apply sign test to test hypothesis that
population median is 625 against alternative
it is greater than 625 at 10% level.

H_0 : population median is 625

> $x = c(612, 619, 631, 628, 643, 640, 655, 64, 670, 663)$

> x
[1] 625

> $sp = \text{length}(x[x > m])$

> sp

[1] 8

> $sn = \text{length}(x[x < m])$

[1] 2

> $n = sp + sn$

[1] 10

> $pvalue = \text{pbinom}(sp, n, 0.5)$

> $pvalue$

[1] 0.9892578

$\therefore pvalue > 0.01$, we accept H_0 .

The 10 observations are -

36, 22, 21, 30, 24, 25, 20, 27, 20, 18

Using sign test, test hypothesis is 25
against alternative is less than 25 at $5\% \text{ level}$

H_0 : population median is 25

$\geq k = 6$

$m = 25$

m^*

[D] 25

$\geq sp = \text{length } (\{x | x > m\})$

[D] 3

$sp = \text{length } (\{x | x < m\})$

[I] 96

$n = sp + sn$

[I] 9

$\geq pr = \text{binom}(sn, n, 0.5)$

p^v

[I] 1

$\therefore p\text{value} > 0.05$, we accept H_0

520.

Q4.

Following are measurements -

63, 65, 60, 89, 61, 71, 58, 57, 69, 62, 63,
72, 65

Using wilcoxon signed rank test ^{test} that population median is 60 against alternative it is greater than 60 at 5% LOS.

H_0 : population median is 60

$> X = \{63, 65, 60, \dots\}$

$>$ wilcox. test (X , alt = "greater", $m = 60$)

wilcoxon signed rank test with
Continuity correction

Q5. Observations

use - wilcoxon signed rank test the hypo
that pop. median is less than 20.

058

15, 19, 25, 24, 20, 21, 32, 28, 12, 25

- > H_0 : population median is 20.
> $x = ((15, 17, 25 \dots))$

> wilcox. test (x, alt = "less", mu = 20)

wilcoxon signed rank test with continuity
correction

data : x

v = 48.5, p-value = 0.9282

alternative hypothesis: True location is less than 20.

- Q6. 20, 25, 27, 30, 18 wilcoxon signed rank test the
hypothesis at population median is 25 against
the alternative population median is not equal to
25 at 5%. LOS -

⇒ H_0 : population median is 25

> $x = ((20, 25 \dots))$

> wilcox. test (x, alt = "two.sided", mu = 25)

wilcoxon signed rank test with continuity
correction

data : x

v = 3.5, pvalue = 0.71

act hypo: true location is not equal to 25

∴ P-value > 0.05 ∴ we accept H_0 .

∴ we accept H_0 .