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Robotics 2 (SS 2019)

Exercise Sheet 5

Presentation during exercises in calendar week 25

The code can only be compiled and run on the CIP Pool! Don't forget to run "source .bashrc" after logging in.

In this sheet we solve different Boundary Value Problems (BVP) using the Multi Shooting Implementation Muscod II. A skeleton file is provided. You need to define your problem in the source file (SRC/bvpXX.cc) and the DAT file (DAT/bvpXX.dat). Build your files in the build directory and run the code using:

moscod "name_of_DAT_file"

Exercise 5.1 – Single Shooting Solve the following ODE for different boundary conditions:

$$\ddot{x} + x = 0 \to \begin{bmatrix} \dot{x} \\ \dot{v} \end{bmatrix} = \begin{bmatrix} v \\ -x \end{bmatrix} \tag{1}$$

Boundary Condition 1:

$$x(0) = 0$$
$$x(\frac{3\pi}{2}) = 1$$

Boundary Condition 2:

$$x(0) = 0$$
$$x(\pi) = 0$$

Boundary Condition 3:

$$x(0) = 0$$
$$x(\pi) = 1$$

What is the general solution to the ODE? What do you expect for the different boundary conditions? What does the optimization code return?

Exercise 5.2 – Multiple Shooting Solve the following ODE for different boundary conditions:

$$\begin{bmatrix} \dot{x} \\ \dot{v} \end{bmatrix} = \begin{bmatrix} v \\ \lambda_1 \cdot \sinh(\lambda_1 \cdot x) \end{bmatrix}$$
 (2)

Boundary Condition:

$$x(0) = 0$$
$$x(1) = 1$$

Vary the λ_1 parameter in the range of 1 to 20. How does the function change? Is Muscod always able to solve the BVP? How do you need to adjust your DAT file?