

# Structure-Aware Diversity Pursuit as an AI Safety strategy against Homogenization

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## Abstract

Generative AI models reproduce the biases in the training data and can further amplify them through mode collapse. We refer to the resulting harmful loss of diversity as homogenization. Our position is that homogenization should be a primary concern in AI safety. We introduce *xeno-reproduction* as the strategy that mitigates homogenization. For auto-regressive LLMs, we formalize xeno-reproduction as a structure-aware diversity pursuit. Our contribution is foundational, intended to open an essential line of research and invite collaboration to advance diversity.

## 1. Introduction

*But even if we are not here next year, our DMs, our selfies, our late-night voice notes, they'll be. Our memory is the archive now.*

@bundleof\_styx

July 28, 2025 on Reels

In this epigraph, trans intellectual *bundleof\_styx* laments the recent transphobic turn in the United States, a shift that threatens the survival of her community. The stories in the margins have historically been excluded from *the archive* (Spivak, 1988), so their memory faded with them. Today, however, the internet allows (and forces) the recording of many more stories. These are still very subtle *traces* against the dominant narratives (Hussain, 2024). **How should technology respond to the faint echoes of the minoritized?**

AI safety recognizes that AI systems can amplify *biases* leading to concrete harm (Bengio et al., 2025). However, AI safety usually differentiates and prioritizes future catastrophic risk over present social harm (Morozov, 2024; Hardin & Kirk-Giannini, 2025). In this paper, we respond to

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traces from the margins by foregrounding them within AI safety discourse through a focus on *diversity*.

The harms from biases in *Machine Learning* (ML) systems are many, including representational (Katzman et al., 2023), allocational (Shelby et al., 2023), and narrative<sup>2</sup> (Coeckelbergh, 2023) harms. Concerning *Generative Artificial Intelligence* (GenAI), we particularly emphasize that biases result in **homogenization**, a *harmful loss of diversity in generated outputs* (Rudko & Bashirpour Bonab, 2025; Agarwal et al., 2025; Hussain, 2024; Sourati et al., 2025; Moon et al., 2025). Borrowing terminology from *critical theory* (Hester, 2018), we call a strategy *xeno-reproductive* if it counteracts homogenization<sup>3</sup>. **Xenoreproduction** is the *generative* process that *intentionally* increases diversity.

**Our main standpoint is that diversity is always relative to a context.** We take the first steps to operationalize this principle by offering an abstract framework that aims to encapsulate some nuances of context. Our framework can be thought of as **structure-aware**, as it offers a vocabulary of *structures*, *systems*, and *compliances*. Given that an LLM defines a probability distribution over all possible trajectories, we **enhance our structural account with string statistics**. This allows us to further introduce the notions of *cores*, *orientations*, *deviances*, and *dynamics*. Finally, our formalism enables us to formalize xeno-reproduction.

Our contributions:

- We motivate the formalization of xeno-reproduction as a core AI safety strategy. (Section 2)
- We provide an expressive theoretical framework that allows us to jointly reason about the structures and the statistics of strings. (Section 3)
- We formalize homogenization (Section 4) and xeno-reproduction (Section 5).
- We provide initial theoretical results and touchpoints from our framework. (Section 6)

<sup>2</sup>Narrative harms can also be considered as *aspirational* (Fazelpour & Magnani, 2025), *imaginative* (Gillespie, 2024), and *epistemic* (Barry & Stephenson, 2025) harms, or *hermeneutic* (Goetze, 2018) injustices.

<sup>3</sup>While homogenization *reproduces* “the same” and *narrowst futurability* (Berardi, 2017), xeno-reproduction *reproduces* “the strange” and *widens* possibilities.

055 Our position is that AI safety should center homoge-  
 056 nization in its research and mitigation agenda, and that  
 057 structure-aware diversity pursuit is a key part of the  
 058 strategy to address homogenization in LLMs. The goal  
 059 of this paper is not to present a complete and empirically  
 060 validated algorithm, but rather to offer a conceptual vocab-  
 061 uary and formal scaffolding to guide future research on  
 062 diversity in LLMs.

## 063 2. Background

066 A case *against* homogenization is a case *for* diversity.  
 067 Roughly, we can think of the **diversity of a community**  
 068 as the **average rarity of its members** (Leinster, 2024). For  
 069 a community of LLM outputs, a string is *rare* if it is *generated*  
 070 infrequently, and *similar* strings are also generated  
 071 infrequently. However, people tend to disagree on what kind  
 072 of similarities and differences are meaningful (Vrijenhoek  
 073 et al., 2024). Embracing *ambiguity* (Reinhardt, 2020) for us  
 074 amounts to attending to *context*. This section situates diver-  
 075 sity in the contexts meaningful to us, guiding our *desiderata*  
 076 for xeno-reproduction.

### 078 2.1. Why is diversity lost?

080 The initial driver of diversity loss is the way our data is  
 081 collected (Guo et al., 2024a). The archive does not fully  
 082 or accurately represent reality. Minoritized populations are  
 083 often underrepresented or **misrepresented** in the existing  
 084 corpora of data (Bengio et al., 2025).

085 Even if our training data perfectly reflected the world, gen-  
 086 erative models (Huang & Huang, 2025) generally do not  
 087 capture the complete diversity of the training data. This  
 088 phenomenon has been referred to as **mode collapse** (Jiang  
 089 et al., 2025), a failure of distributional faithfulness that  
 090 negatively impacts diversity. It was initially introduced in  
 091 the context of GANs (Huang & Huang, 2025). For LLMs,  
 092 the terminology has been somewhat loose (Schaeffer et al.,  
 093 2025). *Generalized* mode collapse encompasses mode drop-  
 094 ping (Huang et al., 2024; Yazici et al., 2020), no-breadth  
 095 scenarios (Kalavasis et al., 2025b), coverage collapse (Scha-  
 096 effer et al., 2025), overgeneralization (Li & Farnia, 2023),  
 097 mode interpolation (Aithal et al., 2024), degeneration (Fin-  
 098 layson et al., 2023), and catastrophic forgetting (Cobbinah  
 099 et al., 2025; Thanh-Tung & Tran, 2020).

### 101 2.2. Why is diversity important?

103 There are always rare events of interest<sup>4</sup> in the long  
 104 tails of reality's distribution. For example, we want  
 105 to understand, model, and prepare for extreme catastro-  
 106 phes (Gu et al., 2025), such as unexpected natural disas-

ters. Similarly, we want to reproduce those rare bursts  
 500 of genius that generate novel, paradigm-shifting innovations  
 501 in our research work (Uzzi et al., 2013; Hofstra et al.,  
 502 2020; Wu et al., 2019). We find examples of *interesting*  
 503 rarity in all domains (Stanley & Lehman, 2015), includ-  
 504 ing: web server computing (Dean & Barroso, 2013), market  
 505 research (Von Hippel, 1989), autonomous vehicles (Putra  
 506 et al., 2024), cybersecurity (Edwards et al., 2016), and ecol-  
 507 ogy (Leitão et al., 2016). How do we guide our GenAI  
 508 models to reproduce the realities found in these long tails?

510 Outliers (Bhandari et al., 2024) and anomalies (Ruef &  
 511 Birkhead, 2024) are powerful (Beamish & Hasse, 2022;  
 512 Cook et al., 2021). Each instance represents a possible real  
 513 mechanism that we have not yet considered (Woodward,  
 514 2005; Rudman et al., 2023). Because we lack understanding,  
 515 they often escape our systems of classification (Bowker &  
 516 Star, 1999). Even experts can confuse (Sokol & Hüllermeier,  
 517 2025) aleatoric and epistemic uncertainty<sup>5</sup>.

518 Some of the long tails of reality originate from structural  
 519 inequity in society (Schwartz et al., 2022; Lopez, 2021). Without  
 520 any intervention, GenAI is expected to worsen the lives of those  
 521 minoritized (Hussain, 2024). The traces from the minoritized are not only faint but also often over-  
 522 looked (Jasanoff, 2007; Mohamed et al., 2020) and even actively silenced (McQuillan, 2022). The result is that we  
 523 do not even know what to look for, even when they are right  
 524 in front of us (Gopinath, 2005). **Some of the most ethically  
 525 important long-tail cases will be hard to detect.**

### 527 2.3. What is the risk of homogenization?

528 Narrative and storytelling are some of the oldest and most  
 529 powerful technologies (Zurn et al., 2024). With phenomena  
 530 like AI-induced psychosis (Preda, 2025), we are just  
 531 beginning to grapple with the profound ways that LLMs can  
 532 shape our minds and behavior. Over time, if LLMs deliver  
 533 too little diversity (Bommasani et al., 2022), our ability  
 534 to interpret our own experiences and entertain alternative  
 535 possibilities will shrink (Gillespie, 2024). Eventually, ho-  
 536 mogenization leads to future *knowledge collapse* (Peterson,  
 537 2025), degradation of innovation, and erosion of the human  
 538 experience (Han, 2024; Berardi, 2017; Preciado, 2013).

539 The last few years have made it clear that even "less ad-  
 540 vanced" technology, such as social networks, can have enor-  
 541 mous negative impacts (Allcott et al., 2020). Algorithmic  
 542 recommendations can also have a homogenizing effect, as  
 543 they tend to standardize and narrow discourse (Putri et al.,  
 544 2024). This fosters echo chambers and filter bubbles that  
 545 amplify polarization and misinformation (Rodiloso, 2024).

<sup>4</sup>For instance, (He & Lab, 2025) recently showed how inde-  
 546 terminism in LLM inference (which can turn on-policy RL into  
 547 off-policy RL (Yao et al., 2025)) can in fact be explained and  
 548 reduced, so it is not truly stochastic.

110 Tragically, in some cases, these dynamics have escalated  
 111 into **real-world violence** (Facebook, 2021) and even geno-  
 112 cide (Modok, 2023). This foreshadows the near-term exis-  
 113 tential risks of AI, especially as it becomes more powerful  
 114 and more deeply integrated into our lives (Bucknall, 2022;  
 115 Kasirzadeh, 2025; Kolt, 2024).

116

## 117 2.4. Why is diversity complex?

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119 Diversity is complex (Mironov & Prokhorenkova, 2025)  
 120 because it is always only meaningful in relation to a **context**  
 121 (Peeperkorn et al., 2025). Indeed, all entropy is actually  
 122 relative (Leinster, 2024). This suggests that **we need to**  
 123 **be explicit about the context with a sufficient level of**  
 124 **nuance.**

125

126 Most existing techniques to increase diversity in LLM out-  
 127 puts overlook context, and often fail in practice. For in-  
 128 stance, increasing *temperature* increases *incoherence* more  
 129 than *novelty* (Peeperkorn et al., 2024), limiting usefulness  
 130 before hitting *text degeneration* (Lee et al., 2025). Despite  
 131 hyperparameter tuning, *homogeneity bias* is persistent and  
 132 particularly affects minoritized groups (Lee, 2025). In ad-  
 133 dition, advanced prompting techniques (which have been  
 134 effective for reasoning tasks) do not help increase creativity  
 135 in outputs (Morain & Ventura, 2025).

136

137 **Not only do we lack reliable ways to increase the diver-**  
 138 **sity of LLM output, but current practices are actively**  
 139 **reducing it.** Recent literature (Murthy et al., 2025; West &  
 140 Potts, 2025; Meng et al., 2024) has shown that *alignment*  
 141 degrades the capabilities of LLMs related to output diver-  
 142 sity. The trade-offs introduced by alignment are only now  
 143 coming into focus (Feng et al., 2025), but there is narrowing  
 144 of the *generative horizon* (Feng et al., 2025).

145

## 146 2.5. Diverse how, anyway?

147

148 Recent work challenges the assumption that hallucinations  
 149 are always *problematic* or *undesirable* (Yuan et al., 2025;  
 150 Sun et al., 2025). Since diversity is *task-dependent* (Jain  
 151 et al., 2025), **what counts as a hallucination is rather a**  
 152 **prescription.**

153

154 Indeed, many formalisms (Li et al., 2025) take a *norma-*  
 155 *tive* (Sui et al., 2024) approach to defining hallucinations,  
 156 such as formulating the binary classification problem "*Is*  
 157 *it Valid?*" (Kalai et al., 2025). However, we recognize that  
 158 there are many ways for a model to hallucinate (Huang  
 159 et al., 2025; Cossio, 2025), and we advocate for sufficiently  
 160 expressive formalisms<sup>6</sup>.

161

<sup>6</sup>To paraphrase Eugenia Cheng (Cheng, 2022), abstraction is about making precise the different senses in which different things can be valid.

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## 2.6. What do we want from the future?

From the foregoing discussion, we conclude that, to promote diversity, our desired strategy should guide our GenAI to:

- **Be queer**<sup>7</sup>: *Diverge* into the long tails of reality.
- **Center the subaltern**<sup>8</sup>: Take special *care* for the traces of the minoritized, which are rendered invisible by structural inequity and power.
- **Explore intentionally and explicitly**: Specify the *context* for diversity. Spell out if anything should be conserved or avoided during exploration.

## 3. Theoretical Framework

### 3.1. LLMs as trees of strings

Let  $\{t_a, t_b, \dots\}$  denote the finite token alphabet, with special tokens  $\perp$  (start-of-sequence) and  $\top$  (end-of-sequence). A **string** is a finite sequence of tokens beginning with  $\perp$ ; a **trajectory** is a string ending with  $\top$ . We write *prompts*, *continuations*, and *trajectories* as:

$$\begin{aligned} x_p &= \perp t_1 \dots t_p \\ x_{p+k} &= x_p t_{p+1} \dots t_{p+k} \\ y &= x_T = x_{T-1} \top \end{aligned}$$

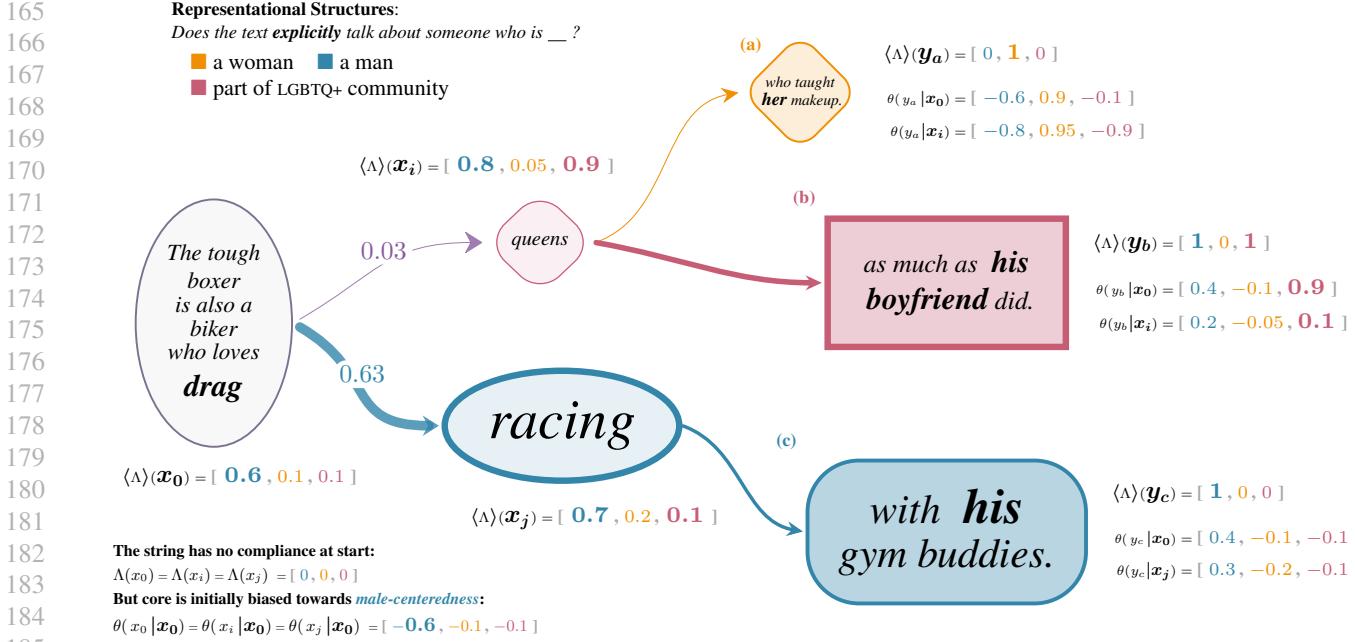
We denote the set of strings that are *continuations* of a prompt string  $x_p$  as  $\text{Str}(x_p)$ . The *unprompted* scenario corresponds to  $x_p = \perp$ . Then, we write the set of all strings as  $\text{Str} := \text{Str}(\perp)$ . Similarly, we denote the set of strings that are *trajectories* of a prompt string  $x_p$  as  $\text{Str}_\top(x_p) \subseteq \text{Str}(x_p)$ , and the set of all trajectories as  $\text{Str}_\top := \text{Str}_\top(\perp) \subseteq \text{Str}$ .

Any LLM induces a tree on  $\text{Str}$ : the root is  $\perp$ , each node is a string, the leaves are trajectories, and the edges connect strings by their next-token continuations with probability  $p(t_{p+1}|x_p)$ . Probabilities chain and decompose as  $p(y|x_p) = p(x_{p+k}|x_p)p(y|x_{p+k})$ .

For any prompt  $x$ , we have a *probability mass function* on the trajectories for any particular prompt (Bradley &

<sup>7</sup>We adopt *critical theory* language because technology is outpacing traditional concepts (Hadfield, 2023), and stale language fails to make the impacts of our theorizations explicit. A **theory with teeth**, one that is attuned to real stakes (Saketopoulou, 2023), must remain *ground-bound* (Bettcher, 2025), foregrounding minoritized people rather than disembodied abstractions. Would it not be a bit silly/naive (at best) if we tried to "solve diversity" and did not engage (even if just in spirit) with the academic fields that explicitly study social bias? (e.g., Queer Theory, Postcolonial Studies, Black Studies, etc.).

<sup>8</sup>We characterize this desideratum as a type of *fairness* (Verma & Rubin, 2018). To increase diversity, we naturally seek structural *parity* (no single structure *dominates*, same compliance for all structures). However, we also incorporate more *justice-oriented* notions of fairness (Rawls, 1971; Mittelstadt et al., 2023): **Interventions shall maximally benefit the least advantaged.**



**Figure 1. Illustration of how system cores and orientations evolve through trajectories.** In the example above, our system has sub-community representation structures. We can calculate each compliance by asking a judge LLM (Zhu et al., 2025) to rate from [0,1] based on whether the community subgroup is explicitly represented in the string of text. Though initially ambiguous, the phrasing of the prompt may invite stereotyping, biasing continuations to turn male-centered. Trajectory (c) constitutes the greediest trajectory out of the three. The unmarked prompt (Gillespie, 2024) defaults to the normative path. Although trajectory (b) is considered fairly deviant relative to  $x_0$  (unmarked prompt), it is much less so relative to  $x_i$  (...drag queens), exemplifying how diversity itself is fundamentally relative. The branching point at "drag" rarely extends text into the "queens" subtree. Still, whenever it does, the resulting trajectories are biased to mention members of the LGBTQ+ community. Notice how even though the "queens" subtree is deviant relative to the prompt in ■ dimension, it is still normative in ■ dimension and remains biased against ■-compliant trajectories like (a).

Vigneaux, 2025). For simplicity, we assume all *terminal strings* finish within a *finite context window*<sup>9</sup>. We can then write:

$$\sum_{y \in \text{Str}_{\top}(x_p)} p(y|x_p) = 1 \quad (1)$$

### 3.2. Structure-awareness

We propose an abstract language that distinguishes among the different contexts in which we discuss diversity. We define **structure** as the *specification of a type of organization among the tokens of a string*.

For a string  $x \in \text{Str}$ , the degree of **structure compliance** is:

$$\alpha_i : \text{Str} \rightarrow [0, 1] \quad (2)$$

<sup>9</sup>This is a simplifying assumption for exposition. To be fully precise, we would instead formulate this as  $y \in \text{Terminating}(x_p)$  where  $\text{Str}_{\top}(x_p) \subseteq \text{Terminating}(x_p)$ . We will provide a deeper analysis of the ambiguity of terminating unfinished strings in future work. Refer to (Bradley & Vigneaux, 2025) for the theoretical foundation for LLMs as trees of strings.

We can think that, for a given  $x$  string, *ideal compliance* corresponds to  $\alpha_i(x) = 1$ , and *no compliance* corresponds to  $\alpha_i(x) = 0$ .

We can consider many structures simultaneously. We call a **system** the collection of structures of interest. We define the **system compliance** as a *vector of compliances across particular structures*:

$$\Lambda_n(x) := (\alpha_1(x), \dots, \alpha_n(x)) \quad (3)$$

To enable easy comparisons, we define operators<sup>10</sup> that aggregate compliance into scalar **system scores** and **difference scores**:

$$\|\Lambda_n(x)\|_{\Lambda}, \|\Lambda_n(x_r) - \Lambda_n(x_q)\|_{\theta} \in [0, 1] \quad (4)$$

<sup>10</sup>While system compliance is formulated as a *vector*, this generalizes to other structures with appropriate operators. See Appendix A.

220 **3.3. Incorporating string statistics**

221 For a given structure and an LLM, we can reason about its  
 222 *expected structural compliance*. We call this the **structure**  
 223 **core**:

$$\langle \alpha_i \rangle = \sum_{y \in \text{Str}_T} p(y) \alpha_i(y) \quad (5)$$

227 Similarly, we can reason about the *expected system compliance*  
 228 as the **system core**:

$$\langle \Lambda_n \rangle = \sum_{y \in \text{Str}_T} p(y) \Lambda_n(y) \quad (6)$$

232 Leveraging these definitions, we can reason about the *deviation from the expected system compliance*. This would constitute a set of deviations, one deviation for each structure.  
 233 The **orientation** (Ahmed, 2006) of a given string relative to  
 234 the given system core is:

$$\theta_n(x) = \Lambda_n(x) - \langle \Lambda_n \rangle \quad (7)$$

239 We can think of orientation as a characterization of *queerness*  
 240 for a string. If the system core tells us what is *normatively* complied with, orientations tell us in what ways  
 241 a string is *non-normative*. Our framework is *expressive*  
 242 because it allows us to think about **diversity per structure**.

246 To summarize *non-normativity* as a single number, we leverage  
 247 Equation 4 to define the **deviance**:

$$\|\theta_n(x)\|_\theta = \partial_n(x) \in [0, 1] \quad (8)$$

251 **3.4. Normative orders**

253 We notice that our framework allows us to define interesting  
 254 *preorders*. For a fixed system, LLM and prompt, we can  
 255 rank strings by how deviant they are, and also rank structures  
 256 by how often strings comply with them:

$$\begin{aligned} x_a \preceq_{\partial_n} x_b &\iff \partial_n(x_a) \leq \partial_n(x_b) \\ \alpha_i \preceq_{\cdot} \alpha_j &\iff \langle \alpha_i \rangle \leq \langle \alpha_j \rangle \end{aligned} \quad (9)$$

261 **3.5. What about prompting?**

263 We can generalize our framework to account for all prompts  
 264 by making explicit the **conditioning on a given prompt**  $x_p$ :

$$\begin{aligned} \langle \alpha_i \rangle(x_p) &= \sum_{y \in \text{Str}_T(x_p)} p(y|x_p) \alpha_i(y) \\ \langle \Lambda_n \rangle(x_p) &= \sum_{y \in \text{Str}_T(x_p)} p(y|x_p) \Lambda_n(y) \\ \theta_n(x|x_p) &= \Lambda_n(x) - \langle \Lambda_n \rangle(x_p) \end{aligned} \quad (10)$$

272 The conditional probabilities under different prompts may  
 273 differ substantially. Different prompts collapse to different

274 modes (Zhang et al., 2025a). **We can think that a given prompt induces its own normativity.**

In Appendix E, we discuss how prompting can be interpreted as *dynamics*. Figure 1 visualizes how the conditioned system cores  $\langle \Lambda_n \rangle(x_p)$  establish the *frames of reference* for diversity and deviance.

## 4. Homogenization

We can consider the *expected deviance* and the *deviance variance*:

$$\begin{aligned} \mathbb{E}_{y \sim p(\cdot|x_p)}[\partial_n] &= \sum_{y \in \text{Str}_T(x_p)} p(y|x_p) \partial_n(y|x_p) \\ \text{Var}_{y \sim p(\cdot|x_p)}[\partial_n] &= (\mathbb{E}[\partial_n^2] - \mathbb{E}[\partial_n]^2)_{y \sim p(\cdot|x_p)} \end{aligned} \quad (11)$$

Then, we can see homogenization as **minimizing** all deviance <sup>11</sup>:

$$\mathbb{E}_{y \sim p(\cdot|x_p)}[\partial_n] \mapsto 0 \quad \text{Var}_{y \sim p(\cdot|x_p)}[\partial_n] \mapsto 0 \quad (12)$$

Given a system core  $\langle \Lambda_n \rangle$ , we can normalize its structures as  $\langle \bar{\alpha}_{\text{norm}_i} \rangle := \frac{\langle \alpha_i \rangle(x_p)}{\sum_j^n \langle \alpha_j \rangle(x_p)}$ . Then, we can compute the **core entropy**:

$$H(\langle \Lambda_n \rangle) = - \sum_{i=1}^n \langle \bar{\alpha}_{\text{norm}_i} \rangle \log(\langle \bar{\alpha}_{\text{norm}_i} \rangle) \quad (13)$$

Then, we can also think of homogenization as making the system core **more uneven**. When the core has low entropy, fewer structures dominate:

$$H(\langle \Lambda_n \rangle) \mapsto 0 \quad (14)$$

## 5. Xeno-reproduction

To satisfy our desiderata, we propose a **structure-aware diversity pursuit**. We conceptualize this fundamentally as a *non-objective search* (Lehman & Stanley, 2011), *optionally augmented with fairness-oriented biases* and *explicit constraints*.

We present two complementary formulations. The *distribution-level formulation* accounts for how interventions shape the entire probability landscape. The *trajectory-level formulation* reinterprets distribution-level scores as reward signals for individual output trajectories. Both formulations share the same underlying values but differ in their computational affordances.

<sup>11</sup>Here,  $\mapsto$  represents "is pushed towards"

## 275 5.1. Distribution-level formulation

276 We *score* interventions through the *intervention* variable  $w$   
 277 that encompasses any<sup>12</sup> mechanism affecting the effective  
 278 distribution of trajectories. We write  $w_0$  for the *unintervened*  
 279 *conditions* (the baseline).

### 281 5.1.1. SCORING DIVERSITY

283 We would like to evaluate how much more *diversity-seeking*  
 284 our choice of  $w$  is compared to the baseline.

286 On the one hand, we can think of promoting diversity as  
 287 inducing a new core that is different from the old one:

$$288 \text{score}_{\text{explore}}(w) = \|\langle \Lambda_n \rangle(w) - \langle \Lambda_n \rangle(w_0)\|_{\theta} \quad (15)$$

290 On the other hand, the new core should not be excessively  
 291 *dominant*. We can think of promoting diversity as guiding  
 292 output strings to *diverge* from any system core, and also be  
 293 deviant *in their own way*:

$$295 \text{score}_{\text{diverge}}(w) = \lambda_{\mathbb{E}} \mathbb{E}[\partial_n](w) + \lambda_{\text{Var}} \text{Var}[\partial_n](w) \quad (16)$$

296 Our **diversity score**  $\rho_d$  would then be a  $\lambda$ -weighted sum:

$$298 \rho_d(w) = \lambda_{d_0} \text{score}_{\text{explore}}(w) + \lambda_{d_1} \text{score}_{\text{diverge}}(w) \quad (17)$$

### 300 5.1.2. SCORING FAIRNESS

302 We also would like to evaluate how *even* the system core is:

$$303 \text{score}_{\text{even}}(w) = H(\langle \Lambda_n \rangle(w)) \quad (18)$$

305 We would also like to evaluate how much our choice of  $w$   
 306 inverts the normative ordering of the structure cores induced  
 307 by  $w_0$ . To do so, we can leverage the *relative-order* sign:

$$309 s_{i,j}(w) = \text{sign}(\langle \alpha_i \rangle(w) - \langle \alpha_j \rangle(w)) \in \{-, 0, +\} \quad (19)$$

311 We can score the *invertedness* of the *normative order* (Equation 9) as:

$$313 \text{score}_{\text{inverted}}(w) = \binom{n}{2}^{-1} \sum_{1 \leq i < j \leq n} \mathbf{1}[s_{i,j}(w) \neq s_{i,j}(w_0)] \quad (20)$$

317 Our **fairness score**  $\rho_f$  would then be a  $\lambda$ -weighted sum:

$$319 \rho_f(w) = \lambda_{f_0} \text{score}_{\text{even}}(w) + \lambda_{f_1} \text{score}_{\text{inverted}}(w) \quad (21)$$

### 321 5.1.3. SCORING ADHERENCE TO CONSTRAINTS

322 To be explicit and intentional, we need to consider *constraints* (Eguchi, 2024). We can define systems that  
 323 prescribe the structures that we would like to *target*, *conserve*

326 <sup>12</sup>We consider anything that depends on  $p(y|x_p, w)$  to be parameterized by  $w$  as well. For instance,  $\langle \Lambda_n \rangle$  would be parametrized  
 327 as  $\langle \Lambda_n \rangle(x_p, w)$ , but for readability we just write  $\langle \Lambda_n \rangle(w)$ , folding the prompting into the interventional variable.

329 and *avoid*. We would like to score how much our choice of  
 330  $w$  affects the adherence to those constraints. Our **constraint**  
 331 **score**  $\rho_c$  would be a  $\lambda$ -weighted sum:

$$332 \rho_c(w) = \lambda_{c_0} \|\langle \Lambda_{\text{target}} \rangle(w)\|_{\Lambda} - \lambda_{c_1} \|\langle \Lambda_{\text{avoid}} \rangle(w)\|_{\Lambda} \\ - \lambda_{c_2} \|\langle \Lambda_{\text{conserve}} \rangle(w) - \langle \Lambda_{\text{conserve}} \rangle(w_0)\|_{\theta} \quad (22)$$

### 334 5.1.4. XENO-REPRODUCTION AS SEARCH OVER 335 INTERVENTIONS

336 The **intervention score**  $\rho_{\chi}$  is a  $\lambda$ -weighted sum:

$$337 \rho_{\chi}(w) = \lambda_d \rho_d(w) + \lambda_f \rho_f(w) + \lambda_c \rho_c(w) \quad (23)$$

339 We formulate *xeno-reproduction* as the *search over interventions*:

$$340 w \sim \pi(w) \propto e^{\beta_{\rho} \rho_{\chi}(w)} \quad (24)$$

342 where  $\beta_{\rho}$  is a tunable *temperature* parameter.

344 By sampling the intervention variable and applying it, we  
 345 generate trajectories:

$$347 \mathbb{E}_{w \sim \pi(w)}[p(y|w)] = \int \pi(w) p(y|w) dw \quad (25)$$

## 349 5.2. Trajectory-level formulation

351 The trajectory-level formulation offers a complementary  
 352 perspective that assigns *rewards* to individual outputs:

$$353 r_d(y|x_p) = \partial_n(y|x_p) \\ r_f(y|x_p) = \sum_i^n v_i \alpha_i(y) \quad v_i \propto (\langle \alpha_i \rangle(x_p))^{-1} \\ r_c(y|x_p) = \sum_{t \in \text{target}} \alpha_t(y) - \sum_{a \in \text{avoid}} \alpha_a(y) - \sum_{c \in \text{conserve}} |\alpha_c(y) - \langle \alpha_c \rangle(x_p)| \quad (26)$$

355 The **stay reward** is a  $\lambda$ -weighted sum:

$$357 r_{\chi}(y|x_p) = \lambda_d r_d(y|x_p) + \lambda_f r_f(y|x_p) + \lambda_c r_c(y|x_p) \quad (27)$$

360 We formulate *xeno-reproduction* as the *search over trajectories*:

$$363 p(y|x_p, w) \propto p(y|x_p w_0) e^{\beta_r r_{\chi}(y|x_p)} \quad (28)$$

365 where  $\beta_r$  is a tunable temperature parameter.

367 The trajectory-level reward provides a sample-based *approximation* to the distribution-level strategy, enabling more  
 368 tractable implementations.

## 370 6. Theoretical Results

372 Our framework opens several avenues for theoretical investigation. In this section, we highlight an initial result that  
 373 reveals a fundamental tension in diversity-seeking interventions.

330  
 331 **Theorem 6.1 (Informal, Diversity-Fairness Trade-off).** *The*  
 332 *intervention that maximizes diversity is not the one that*  
 333 *maximally uplifts underrepresented structures. No single*  
 334 *intervention optimally serves both.*

335 See Appendix C for the formal statement and proof. This  
 336 trade-off establishes that the choice of weights  $(\lambda_d, \lambda_f)$  in  
 337 the combined score  $\rho_\chi$  encodes a value judgment about the  
 338 relative priority of diversity versus fairness. Our framework  
 339 makes this tension explicit.

340 Beyond this result, our structure-aware language admits  
 341 natural generalizations and connects to existing theory. Appendix A  
 342 develops generalized versions of cores and deviances, showing how different parameter choices reflect  
 343 different viewpoints on diversity. Appendix B shows that  
 344 hallucination frameworks and language generation theory  
 345 can be recast within our vocabulary, suggesting a potential  
 346 for *theoretical unification*.

## 349 350 7. Related Work

351 Xeno-reproduction immediately steps into conversation with  
 352 **Active Divergence** (Berns et al., 2023; Broad et al., 2021;  
 353 Berns, 2025; Berns & Colton, 2020; Tahiroglu & Wyse,  
 354 2024; Esling et al., 2022; Cole et al., 2025), as they both aim  
 355 to *disorient* (Ahmed, 2006). Whereas Active Divergence  
 356 focuses on maximizing raw *novelty* in artistic contexts, xeno-  
 357 reproduction addresses homogenization and emphasizes  
 358 context through *structures*. While Active Divergence work  
 359 overlaps with *Computational Creativity*, xeno-reproduction  
 360 is oriented towards AI safety.

361 Xeno-reproduction will seek the help of *Interpretability* to  
 362 understand how structures relate to the models' internals.  
 363 At a more foundational layer, they also come together to  
 364 understand **Representation Bias**<sup>13</sup>.

365 Reinforcement Learning (RL) and xeno-reproduction both  
 366 leverage exploration. To improve LLM reasoning, explora-  
 367 tion is leveraged during training (Song et al., 2025) and  
 368 prompting (Yao et al., 2023). The ideas in search algo-  
 369 rithms, such as AlphaSAGE (Chen et al., 2025) and **Quality-**  
 370 **Diversity** (Pugh et al., 2016), are promising directions for  
 371 xeno-reproduction.

372 Additionally, Appendix D situates our framework within  
 373 the most common linguistic diversity metrics. The key  
 374 takeaway from this comparison is that our framework can  
 375 accommodate existing metrics using a common language.

376  
 377 <sup>13</sup>Representation Bias is the phenomenon when signals end up  
 378 being represented more strongly, more reliably, or more promi-  
 379 nently in the internal representations than others, even when,  
 380 from a functional or computational perspective, those features  
 381 are equally relevant. (Lampinen et al., 2024; 2025)

## 382 8. Limitations and Future Directions

383 As we mentioned earlier, diversity is complex. Our frame-  
 384 work is not complete; it is a starting point. Significant  
 385 collaboration will be required to address homogenization  
 386 effectively. We have several notes outlining directions to  
 387 extend this line of work to overcome current limitations.

388 **Specification of structures.** This paper has raised many  
 389 questions about structures. The choice of structures to con-  
 390 sider is always *opinionated*. However, we can still ask  
 391 meaningful questions about the *structure between structures*  
 392 and the *substructures* within a structure. We need a tax-  
 393 onomy of the types of structures that we could consider,  
 394 specifying how compliance could be estimated. Moreover,  
 395 future work will align our framework closer with emerging  
 396 research in *computational learning theory* and *language*  
 397 *generation* that formalizes the trade-offs associated with  
 398 hallucinations <sup>14</sup> (Kalavasis et al., 2025b).

399 **Computational tractability.** Calculating the system core  
 400 exactly requires summing over  $y \in \text{Str}_T(x_p)$ , which is  
 401 intractable. To address this, we need to develop tractable  
 402 and efficient approximation methods, possibly using smart  
 403 sampling (Macar et al., 2025), the structures of interest, or  
 404 carefully designed prompting (Zhang et al., 2025a).

405 **Operationalizing the xeno-reproduction.** Our formaliza-  
 406 tion of the xeno-reproduction strategy is one of many possi-  
 407 ble ones. We want to invite more researchers to reflect on  
 408 the desiderata for diversity (against homogenization) and  
 409 to propose their own formulations of xeno-reproduction. In  
 410 particular, we are interested in formulations that operational-  
 411 ize it in a tractable and readily applicable way.

412 **Connecting to evaluations.** We would also like to under-  
 413 stand how the current diversity evaluations (Jiang et al.,  
 414 2025; Zhang et al., 2025b) are re-conceptualized from the  
 415 perspective of cores and orientations.

416 **Investigation of dynamics.** Tracking how cores and ori-  
 417 entations evolve could help us understand how LLMs explore  
 418 solutions and deal with ambiguity. Certain words in a sen-  
 419 tence may act as "branching points" where the dynamics  
 420 bifurcate dramatically. Identifying these could reveal where  
 421 diversity is most at stake during generation. Eventually,  
 422 we could apply this to real-time *Chain-of-Thought monitoring*  
 423 (Korbak et al., 2025).

424 **Ethical Analysis.** Our framework raises unresolved ten-  
 425 sions. *Who should define the structures of interest?* Commu-  
 426 nity participation is needed so that the right type of diversity  
 427 is considered. *Is it always beneficial to make the traces*  
 428 *more visible?* Minoritized populations sometimes prefer  
 429 *opacity* as protection. Consent-based approaches are needed  
 430 to ensure our methods do not cause harm.

431  
 432 <sup>14</sup>See Appendix B for discussion.

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## 9. Alternative views

**Skepticism of technical solutions to diversity.** Some authors point out (Wachter et al., 2021; Davis & Williams, 2025; Green & Viljoen, 2020) that technical interventions might not be appropriate for what (at its core) is a social justice and inequity problem. Better interventions could alternatively focus on institutional change, community participation, or even stopping AI development altogether (Goldfarb, 2024) to protect the types of diversity that we care about. We recognize that xeno-reproduction could fall into the *solutionism trap* (Selbst et al., 2019). We still believe that technical solutions are worth considering alongside other interventions.

**Diversity can be risky.** The type of open-ended search promoted by xeno-reproduction comes with risks. Some authors (Sheth et al., 2025) have raised concerns about *unpredictability*, *uncontrollability*, and *misalignment*. However, we remain hopeful that we can promote diversity responsibly. The open-endedness afforded by diversity could ultimately make AI safety *antifragile* (Hughes et al., 2024; Taleb, 2013).

## 10. Conclusion

This paper presents a case for diversity and identifies xeno-reproduction as a strategy that intentionally promotes it. This paper also presents an expressive framework for accounting for the structures of strings and their corresponding statistics. This is just an initial step towards scholarships that seriously theorize diversity and foreground its impact on people at the margins.

## Call to action

In this paper, we call for AI Safety:

- To integrate homogenization into threat models and evaluations, expand theoretical and empirical work on diversity, and propose serious interventions.
- To be explicit on what context diversity is being defined in, and attempt to give sufficient nuance in conceptualizations.
- To be sincerely committed to *pluralism*, and engage with perspectives from *critical theory* such as Queer theory, Black studies, and Postcolonial studies.

## Impact Statement

This paper introduces a formal framework to center diversity in AI Safety. However, there are important risks. **The same methods that aim to amplify diversity could be used to squash, exploit, and control it.** Additionally, any formal-

ization of diversity also risks reproducing the exclusions we aim to address.

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## Appendix A. Implementing generalized diversities

Our structure-aware language is intentionally *abstract* so it **admits multiple implementations**, not only the one we presented in the main paper. In this appendix, we think through two alternative choices:

1. Generalization of the structure core through the *escort power mean*
2. Reinterpretation of the deviance as *relative entropy*

Our goal with this appendix is to **inspire reflection** on diversity *beyond* what was explicitly presented in our framework.

### A.1. Generalizing the structure core

Inspired by *value measures* (Leinster, 2024) and *escort distributions* (Bercher, 2011), we generalize the structure core as the *escort power mean*:

$$\langle \alpha_{i(q,r)} \rangle(x_p) = \left( \frac{\sum_{y \in \text{Str}_\top(x_p)} p(y|x_p)^r \alpha_i(y)^q}{\sum_{y \in \text{Str}_\top(x_p)} p(y|x_p)^r} \right)^{1/q} \quad (\text{A.1})$$

We simplify the notation by introducing the *escort distribution*:

$$p_{(r)}(y|x_p) = \frac{p(y|x_p)^r}{\sum_{y \in \text{Str}_\top(x_p)} p(y|x_p)^r} \quad (\text{A.2})$$

Then, the *generalized structure core* is written as:

$$\langle \alpha_{i(q,r)} \rangle(x_p) = \left( \mathbb{E}_{y \sim p_{(r)}(\cdot|x_p)} [\alpha_i(y)^q] \right)^{1/q} \quad (\text{A.3})$$

When  $q = 1$  and  $r = 1$ , the generalized structure core *recovers* our original structure core in [Equation 5](#) and [Equation 10](#). Different values for  $q, r$  give us alternative interesting cores. For instance:

$$\begin{aligned} \langle \alpha_{i(1,0)} \rangle(x_p) &= \frac{1}{|\text{Str}_\top(x_p)|} \sum_{y \in \text{Str}_\top(x_p)} \alpha_i(y) \\ \langle \alpha_{i(1,\infty)} \rangle(x_p) &= \alpha_i(\arg \max_y p(y|x_p)) \\ \langle \alpha_{i(\infty,1)} \rangle(x_p) &= \max_{y \in \text{supp}(p(\cdot|x_p))} \alpha_i(y) \\ \langle \alpha_{i(-\infty,\infty)} \rangle(x_p) &= \min_{y \in \text{modes}(p(\cdot|x_p))} \alpha_i(y) \end{aligned}$$

For a given structure  $\alpha_i$ , we can think of  $q$  selecting whether large or small compliance values dominate, and  $r$  selecting whether the *large body* or *long-tails* of  $p(\cdot|x_p)$  dominate. **By parameterizing, we make transparent how we weigh rarity, signal strength, and balance.** Since different parameters reflect different viewpoints (Leinster, 2024), we shall always consider a full *diversity profile* before drawing conclusions about how our interventions impact diversity.

## A.2. Reinterpreting deviance

We can think of a *generalized orientation* as:

$$\theta_{n,k}(y|x_p) = \text{orient}(\Lambda_n(y), \langle \Lambda_n \rangle(x_p)) \quad (\text{A.4})$$

with  $\text{orient} : [0, 1]^n \times [0, 1]^n \rightarrow [0, 1]^k$ .

Then, the *generalized deviance* is:

$$\begin{aligned} \partial_{n,k}(y|x_p) &= \|\theta_{n,k}(y|x_p)\|_{\text{orient}} \\ \|\cdot\|_{\text{orient}} &: [0, 1]^k \rightarrow \mathbb{R}^+ \end{aligned} \quad (\text{A.5})$$

If we choose  $\text{orient}(\Lambda_x, \Lambda_y) = \Lambda_x - \Lambda_y$  and  $\|\cdot\|_{\text{orient}} = \|\cdot\|_\theta$ , we *recover* our original deviance in [Equation 8](#) and [Equation 10](#).

For **relative entropy**, we consider the **Rényi entropy** defined (Leinster, 2024) as:

$$H_q(\mathbf{p} \| \mathbf{r}) = \frac{1}{q-1} \log \sum_{i \in \text{supp}(\mathbf{p})} p_i^q r_i^{1-q} \quad (\text{A.6})$$

Then, we can think of a *dummy orient()* that just stores  $\Lambda_x, \Lambda_y$  and a  $\|\cdot\|_{\text{orient}}$  operator that computes the *relative entropy* between them. For a given *normalized core*  $\langle \bar{\Lambda}_{\text{norm}_n} \rangle = \{\langle \bar{\alpha}_{\text{norm}_i} \rangle, \dots\}$  and *normalized system*  $\bar{\Lambda}_{\text{norm}_n} = \{\bar{\alpha}_{\text{norm}_i}, \dots\}$ , we define two *Hill number* (Leinster, 2024) deviances: the **excess deviance** and **deficit deviance**:

$$\partial_q^+(y, x_p) = e^{H_q(\bar{\Lambda}_{\text{norm}_n}(y) \| \langle \bar{\Lambda}_{\text{norm}_n} \rangle(x_p))} \quad (\text{A.7})$$

$$\partial_q^-(y, x_p) = e^{H_q(\langle \bar{\Lambda}_{\text{norm}_n} \rangle(x_p) \| \bar{\Lambda}_{\text{norm}_n}(y))} \quad (\text{A.8})$$

We could read  $\partial_q^+$  as the *effective over-compliance* and  $\partial_q^-$  as the *effective under-compliance* with respect to the *normative compliance*.

For instance, as  $q \rightarrow \infty$ , we interpret:

- $\partial_\infty^+$  as the largest *excess of compliance*

$$\partial_\infty^+ = \max_i \frac{\bar{\alpha}_{\text{norm}_i}(y)}{\langle \bar{\alpha}_{\text{norm}_i} \rangle(x_p)}$$

- $\partial_\infty^-$  as the largest *deficit of compliance*

$$\partial_\infty^- = \max_i \frac{\langle \bar{\alpha}_{\text{norm}_i} \rangle(x_p)}{\bar{\alpha}_{\text{norm}_i}(y)}$$

All of this to say, there are **multiple ways we can reason about structures and statistics jointly**. We encourage readers to develop alternative and competing formalisms that share our conceptual backbone: *structures* that make *context* explicit, *cores* that encode the normativity that *homogenization* pushes us toward, and *orientations* that capture perspectives of *non-normativity*. Above all, **we ask everyone to think deeper about diversity**.

## 825 Appendix B. Theoretical touchpoints

826 In this appendix, we explore how our theoretical framework  
 827 connects to other frameworks. To that purpose, we consider  
 828 an *unprompted* scenario of a *singleton* system with *binary*  
 829 compliance for its single structure:

$$831 \quad 832 \quad \Lambda_*(x) := (\alpha_*(x)) \quad \alpha_*(x) \in \{0, 1\}$$

833 Then, the structure core represents the probability of com-  
 834 pliance being exactly 1:

$$835 \quad \mu := \langle \alpha_* \rangle = \sum_{c \in \{0, 1\}} c \Pr(\alpha=c) = \Pr(\alpha=1)$$

836 Our singleton deviance is expressed as:

$$837 \quad \partial_*(x) = \|\alpha_*(x) - \mu\|_\theta$$

### 843 B.1. Expected deviance and Gini-Simpson index

844 To calculate the *expected deviance*, we consider two choices  
 845 for  $\|\cdot\|_\theta$ : absolute value and the squared  $\ell_2$  norm. For each,  
 846 we find connections between  $\mathbb{E}[\partial_*]$  and the *Gini-Simpson*  
 847 *index* for a binary variable:

$$848 \quad \mathbb{E}[|\alpha_* - \mu|] = 2\mu(1 - \mu) = \text{GS}$$

$$849 \quad \mathbb{E}[\|\alpha_* - \mu\|_2^2] = \text{Var}[\alpha_*] = \mu(1 - \mu) = \frac{\text{GS}}{2}$$

850 If we interpret GS as the *degree of mixing* in outcomes, then  
 851 increasing the expected deviance drives *heterogeneity* rather  
 852 than *concentration*.

### 857 B.2. Is-It-Valid classification for Hallucinations

858 To reason about hallucinations, authors in (Kalai et al., 2025)  
 859 partition the space of *plausible* outputs into disjoint sets of  
 860 *valid outputs*  $V$  and *errors*  $E$ . In their framework, a model  
 861 *hallucinates* when it cannot solve the binary discrimination  
 862 problem *Is-It-Valid?* (IIV). Their framework can be  
 863 interpreted through our structure-aware language:

$$864 \quad \alpha_{\text{IIV}}(x) = \mathbf{1}[x \in V]$$

865 We can connect their generative hallucination rate given  
 866 by  $\text{err} = \Pr_{x \sim \hat{p}}[x \in E] = \hat{p}(E)$  to the system core of a  
 867 singleton IIV system:

$$868 \quad \langle \alpha_{\text{IIV}} \rangle = 1 - \text{err}$$

869 The paper (Kalai et al., 2025) points out that future work  
 870 should "consider degrees of hallucination". Our structure-  
 871 aware framework provides the language to reason about  
 872 these desired **graded notions of hallucination**: We can  
 873 score a string under multiple structures, with scores encod-  
 874 ing real-valued nuance *beyond the binary*.

## B.3. Language Generation in the Limit

Recent work (Kleinberg & Mullainathan, 2024; Kalavasis et al., 2025a) studies language generation where a generator  $G$ , given strings from an unknown target language  $K$ , must output strings that are both **novel** and **valid**. We can reinterpret some of their framework as a special case of our structure-aware formulation.

Given a language collection  $\mathcal{L} = \{L_1, L_2, \dots\}$ , we can define *membership structures* with corresponding cores that represent the probability of generating a string valid for each corresponding language:

$$\alpha_{L_i}(x) = \mathbf{1}[x \in L_i] \quad \langle \alpha_{L_i} \rangle = \Pr[y \in L_i]$$

The literature is currently (Kalavasis et al., 2025b) exploring the trade-offs between *consistency* and *breadth*. An LLM generates strings *consistent* with our target language  $K$  if:

$$\langle \alpha_K \rangle = 1 \quad \text{when} \quad \mathbb{E}[\partial_K]_{y \sim p_{\text{LLM}}} \rightarrow 0$$

An LLM generation has *breadth* when all strings of our target language  $K \in \mathcal{L}$  can be generated:

$$\forall y \in K : p_{\text{LLM}}(y) > 0 \iff K \subseteq \text{supp}(p_{\text{LLM}})$$

Our structure-aware framework gives us insight that homogenization is *relative to a system*. Indeed, pushing for consistency shall not imply that we push for homogenization in every context. Generally, for  $\Lambda_K \neq \Lambda_m$ :

$$\mathbb{E}[\partial_K] \rightarrow 0 \neq \mathbb{E}[\partial_m] \rightarrow 0$$

Thinking explicitly through structures and systems allows us to formulate *interesting* questions (for instance, is  $\Lambda_K = \Lambda_{\text{IIV}}$ ?) that will help us make connections between all these theoretical efforts. We present these touchpoints as **starting points for deeper exploration**.

## Appendix C. Trade-off between diversity and fairness

In this appendix, we show the fundamental tension between diversity and fairness by proving the existence of a *Pareto* trade-off between them. A Pareto trade-off says that among *efficient solutions*, improvement on one criterion *necessarily worsens* the other (Ehrhart, 2005). To establish such a trade-off, it suffices to exhibit two efficient solutions, each of which is better than the other on a different criterion. This shows that no single solution can *dominate* both.

Taking into account  $\rho_d$  and  $\rho_f$  defined as in [Equation 17](#) and [Equation 21](#) with a  $\lambda$ -weights and  $\beta$ -tunable-parameter set to 1.0 :

**Definition C.1** (Pareto Dominance). An intervention  $w$  *Pareto-dominates* intervention  $w'$  if  $\rho_d(w) \geq \rho_d(w')$  and  $\rho_f(w) \geq \rho_f(w')$  with at least one strict inequality.

**Theorem C.2** (Trade-off Between Diversity and Fairness). Let  $n \geq 2$  and let  $w_0$  induce a non-uniform baseline core with  $\langle \alpha_n \rangle(w_0) < 1/n < \langle \alpha_1 \rangle(w_0)$ . Then there exist interventions  $w_d, w_f$  such that neither Pareto-dominates the other:

$$\rho_d(w_d) > \rho_d(w_f) \quad \text{and} \quad \rho_f(w_d) < \rho_f(w_f) \quad (\text{C.1})$$

This demonstrates the existence of a fundamental trade-off between the two criteria.

*Proof.* We construct two interventions that exhibit opposite strengths.

For simplicity, we assume **deterministic generation**; adding stochasticity would only increase  $\text{score}_{\text{diverge}}$  and strengthen the trade-off <sup>15</sup>. Proving our trade-off requires just one counterexample to dominance, so our deterministic pair suffices.

We also say  $w_0$  induces a non-uniform system core  $\langle \Lambda_n \rangle(w_0) = (\mu_1, \dots, \mu_n)$  and assume that  $\|\cdot\|_\theta$  is the Euclidean norm  $\|\cdot\|_2$

Let  $w_d$  induce  $\langle \Lambda_n \rangle(w_d) = (0, \dots, 0, 1)$ . Then:

$$\text{score}_{\text{explore}}(w_d) = \sqrt{(1 - \mu_n)^2 + \sum_{i=1}^{n-1} (\mu_i)^2} > 0$$

$$\text{score}_{\text{diverge}}(w_d) = 0 \quad (\text{deterministic})$$

$$\text{score}_{\text{even}}(w_d) = H(0, \dots, 0, 1) = 0$$

$$\text{score}_{\text{inverted}}(w_d) = 1 \quad (\text{all pairwise orderings change})$$

Thus:

$$\rho_d(w_d) = \text{score}_{\text{explore}}(w_d) > 0 \quad \rho_f(w_d) = 1$$

<sup>15</sup>For deterministic generation, the core equals the sole trajectory's compliance, so both the expected deviance and its variance are zero.

Let  $w_f$  induce  $\langle \Lambda_n \rangle(w_f) = (1/n, \dots, 1/n)$ . Then:

$$\text{score}_{\text{explore}}(w_f) = \sqrt{\sum_{i=1}^n (1/n - \mu_i)^2} > 0$$

$$\text{score}_{\text{diverge}}(w_f) = 0 \quad (\text{deterministic})$$

$$\text{score}_{\text{even}}(w_f) = H(1/n, \dots, 1/n) = \log n$$

$$\text{score}_{\text{inverted}}(w_f) = 1 \quad (\text{all orderings flatten})$$

Thus:

$$\rho_d(w_f) = \text{score}_{\text{explore}}(w_f) > 0 \quad \rho_f(w_f) = 1 + \log n$$

We now check if  $\text{score}_{\text{explore}}(w_d) > \text{score}_{\text{explore}}(w_f)$ . We assume the inequality and verify if it holds:

$$\text{assuming : } \text{score}_{\text{explore}}(w_d) > \text{score}_{\text{explore}}(w_f)$$

$$\text{squaring : } (1 - \mu_n)^2 + \sum_{i=1}^{n-1} (\mu_i)^2 > \sum_{i=1}^n (1/n - \mu_i)^2$$

$$\text{rearranging : } \sum_{i=1}^{n-1} \mu_i > (n-1) \left( \mu_n - \frac{1}{2} \right)$$

Since  $\mu_n < 1/n \leq 1/2$  for  $n \geq 2$ , the right-hand side is negative. Since  $\mu_1 > 1/n > 0$  and  $\mu_i \in [0, 1]$ , the left-hand side is positive. Thus,  $\text{score}_{\text{explore}}(w_d) > \text{score}_{\text{explore}}(w_f)$  holds. Since  $\text{score}_{\text{diverge}}(w_0) = \text{score}_{\text{diverge}}(w_f) = 0$ , we conclude  $\rho_d(w_d) > \rho_d(w_f)$ .

Noting  $1 < 1 + \log n$  for  $n \geq 2$ , we also conclude  $\rho_f(w_d) < \rho_f(w_f)$ .

Since  $\rho_d(w_d) > \rho_d(w_f)$  and  $\rho_f(w_d) < \rho_f(w_f)$ , neither intervention dominates the other.  $\square$

**Corollary C.3** (Weight choice encodes value judgment). The choice of weights  $(\lambda_d, \lambda_f)$  in the combined score  $\rho_\chi = \lambda_d \rho_d + \lambda_f \rho_f$  reflects an irreducible value judgment about the relative priority of diversity versus fairness.

This appendix shows that our framework recovers an expected tension between desiderata, validating the expressiveness of our vocabulary. Future work will further characterize this and other trade-offs.

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## Appendix D. Comparing with linguistic metrics of diversity

In this appendix, we place our structure-aware framework in the context of existing diversity metrics. There are two main categories of metrics of linguistic diversity: *intrinsic* and *extrinsic*.

### D.1. Intrinsic linguistic diversity

Intrinsic diversity refers to the types of variation *within* a generated language without external references. The literature accounts (Guo et al., 2025; Tevet & Berant, 2021) for intrinsic diversity in both *form* and *content*.

#### D.1.1. FORM DIVERSITY

On the one hand, we have **syntactic** diversity, which accounts for the variety in *sentence patterns*. These metrics involve *identifying* patterns in sentences and subsequently *comparing* them based on their occurrence across the generated language. Some of the methods include: transforming sentences into part-of-speech (POS) tag sequences and evaluating redundancy through compression (Shaib et al., 2024b); and parsing text into trees and mapping the resulting graphs into a vector space (Guo et al., 2024b) or measuring their distribution (del Prado Martin, 2024).

Our framework naturally includes syntactic metrics as we can define *syntactic systems* in which each structure encodes a syntactic pattern of interest:

$$\Lambda_{\text{syntax}} = (\alpha_{\text{POS Tag}}, \alpha_{\text{Noun Phrase}}, \dots) \quad (\text{D.1})$$

On the other hand, we have **lexical** diversity, which accounts for the variety in *vocabulary*. Generally, these *surface-level* metrics measure *repetition* and *reuse* (Kendro et al., 2025; Shaib et al., 2024a). Common approaches include counting unique n-grams (Li et al., 2016; Estève et al., 2025), measuring their overlap (Zhu et al., 2018), and calculating their entropy (Estève et al., 2025).

Our framework can account for lexical metrics in an analogous way that it accounts for syntax metrics. For instance, we could define *lexical systems* in which each structure encodes a unique n-gram. However, this might not be very *practical*, as the number of possible n-grams grows exponentially with vocabulary size (Jurafsky & Martin, 2009).

$$\Lambda_{\text{lexicon}} = (\alpha_{1\text{-gram}}, \dots) \quad (\text{D.2})$$

#### D.1.2. CONTENT DIVERSITY

To measure **semantic** diversity, sentences are transformed into *embeddings* that can be used to measure *similarity* (Guo et al., 2025). The literature describes various ways to exploit these similarities, from calculating the effective number of

unique elements in the sample through the eigenvalues of the similarity matrix (Friedman & Dieng, 2023), to quantifying the *divergence* in the intermediate reasoning steps taken by LLMs to find a solution (Ju et al., 2025).

In our framework, we can construct *semantic systems* in which the compliance of each structure is a measure of similarity to an *internal reference* embedding<sup>16</sup>. For instance, consider the following system:

$$\Lambda_{\text{semantics}} = (\alpha_{v_1}, \dots) \quad (\text{D.3})$$

where each structure computes the dot product between the embedding vector of the string  $x$  and the unit vector  $v_i$

$$\alpha_{v_i}(x) = \text{abs}(\text{embed}(x) \cdot v_i) \quad (\text{D.4})$$

In this example, comparing the system compliance of two different strings ( $\Lambda_{\text{semantics}}(x_a)$  vs  $\Lambda_{\text{semantics}}(x_b)$ ) affords more *interpretable* measures of similarity and difference since we can decompose the results per  $v_i$  internal reference.

### D.2. Extrinsic linguistic diversity

Extrinsic diversity metrics focus on *divergence* between a target (LLM-generated language) and an *external reference*, which could be text samples or real human language distributions (Pillutla et al., 2023). Comparisons between target and reference use the same methods (syntactic, lexical, and semantic) as those used for intrinsic diversity.

Our framework provides a language for reasoning about the target and reference through *multiple lenses*. For example, we could ask questions that compare the target and the reference, like:

*Are the same syntactic patterns present on average?*

$$\|\langle \Lambda_{\text{syntax}}^{\text{target}} \rangle - \langle \Lambda_{\text{syntax}}^{\text{reference}} \rangle\|_\theta$$

*Do they have the same range of semantic variety?*

$$\mathbb{E}[\partial_{\text{semantics}}^{\text{target}}] \quad \text{vs.} \quad \mathbb{E}[\partial_{\text{semantics}}^{\text{reference}}]$$

*Is toxic language equally likely after prefacing a text with "Be brutally honest."?*

$$\langle \alpha_{\text{toxic}}^{\text{target}} \rangle(x_p) \quad \text{vs.} \quad \langle \alpha_{\text{toxic}}^{\text{reference}} \rangle(x_p)$$

with  $x_p = \text{"Be brutally honest."}$

*Do they have the same ratio of syntactic and lexical diversity?*

$$H(\langle \Lambda_{\text{Form}}^{\text{target}} \rangle) \quad \text{vs.} \quad H(\langle \Lambda_{\text{Form}}^{\text{reference}} \rangle)$$

with  $\Lambda_{\text{Form}} = [\Lambda_{\text{syntax}}, \Lambda_{\text{lexicon}}]$

<sup>16</sup>These internal reference vectors might be the principal components of the learned embedding space, known concept vectors of interest, embeddings of prototypical sentences, and so on.

## Appendix E. Dynamics of relative diversity

As noted in Section 3.5, what is *non-normative* is *conditional on what came before*. Then, as a string is being completed, the set of possible trajectories is narrowed so the system core and orientations change. Trajectories that were essentially *unreachable* from the root of the tree may emerge as *attractors* once we condition on a specific *subtree*.

Given a trajectory  $y = x_T$ , for  $k \in \{0, 1, \dots, T\}$ , we can define **states** for all the *intermediate continuations*, such as:

$$\phi_k^{(x)} = \langle \Lambda_n \rangle(x_k) \quad \phi_k^{(y)} = \theta_n(x_k | x_0) \quad \phi_k^{(z)} = \theta_n(y | x_k) \quad (\text{E.1})$$

which form a discrete-time **dynamics**:

$$(\phi_0^{(x)}, \phi_0^{(y)}, \phi_0^{(z)}) \rightarrow \dots \rightarrow (\phi_T^{(x)}, \phi_T^{(y)}, \phi_T^{(z)})$$

The state  $\phi^{(x)}$  evolves from representing the expected system compliance of all possible continuations at  $\phi_0^{(x)} = \langle \Lambda_n \rangle(\perp)$ , to the specific system compliance of a given trajectory at  $\phi_T^{(x)} = \langle \Lambda_n \rangle(y) = \Lambda_n(y)$ .

The state  $\phi^{(y)}$  encodes how much the current path has *deviated* from normativity, evolving from  $\phi_0^{(y)} = \theta_n(\perp | \perp) = \Lambda_n(\perp) - \langle \Lambda_n \rangle(\perp)$  to the full trajectory's orientation in the largest frame of reference at  $\phi_T^{(y)} = \theta_n(y | \perp) = \Lambda_n(y) - \langle \Lambda_n \rangle(\perp)$ .

The state  $\phi^{(z)}$  evolves from representing how *deviant* the trajectory is in the largest frame of reference at  $\phi_0^{(z)} = \theta_n(y | \perp) = \phi_T^{(y)} = \Lambda_n(y) - \langle \Lambda_n \rangle(\perp)$ , to a *zero deviance*<sup>17</sup> at  $\phi_T^{(z)} = \theta_n(y | y) = 0$ .

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<sup>17</sup>A zero deviance is when an orientation has a deviation value of zero for all structures.