



Epidemiological models - macro level model

Modelling and Simulation

Abramov Mikhail (xabram00)
Pavel Yablouski (xyadlo00)

Brno University of Technologies
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Contents

1	Introduction	2
1.1	Contributors	2
1.2	Model validation	2
2	Topic analysis	2
2.1	Approaches	3
2.2	Sources	3
3	Concept model	3
4	Experiment	5
5	Conclusion	5

1 Introduction

The first aim is to determine the possibilities for determining the value of the effectiveness of various restrictive measures taken by the government of the Czech Republic for the period from September 1, 2020 till the last day of the project - December 7, 2020.

The second aim is to create a predictive model for determining the number of persons who have illness in the same time, persons who have been ill or otherwise have immunity

Used model contains different scenarios of quarantine precautions (using different types of lockdown). Based on simulations of this scenarios, influence of particular scenario is shown. As an experiment, theoretical scenarios from the article and current lockdown type in Czech Republic are analyzed.

1.1 Contributors

This project is solved by team of two students: Abramov Mikhail and Pavel Yadlouski.

1.2 Model validation

Results of theoretical scenarios simulation are compared with reference results from the article. The article by itself was subjected to critical analysis and minor formulas adjustments. Experiment with lockdown type in Czech Republic is compared with reality:)

2 Topic analysis

The necessary information to research this topic was found in scientific articles from IRCACS-International Research Center for Applied Complexity Sciences in Colombia written by Danny Ibarra-Vega^[1]

As epidemic situation in the world become worth with time, there is need to take appropriate precautions based on mathematical models and simulation. One of the base mathematical model for simulation of expansion of the epidemic is SIR model. SIR¹ model is one of the simplest compartment methods.

¹https://en.wikipedia.org/wiki/Compartmental_models_in_epidemiology

This method compares three values:

1. **S** – the number of susceptible individuals
2. **I** – the number of infectious individuals.
3. **R** – the number of removed (and immune) or deceased individuals

2.1 Approaches

For more complex view of system behavior, a mathematical model has been adopted with the Systems Dynamics(SD) methodology². The core of this methodology is that SD models solve the problem of simultaneity (mutual causation) by updating all variables in small time increments with positive and negative feedbacks and time delays structuring the interactions and control.

Used SD model extends basic SIR model with separating the number of recovered and deceased individuals into two variables and addition of auxiliary and state variables that represent hospital capacity, contacts, contacts with infected. As a result, there is a model of 4 stock variables (3).

2.2 Sources

Article with the mathematical model [1] for implementation is found in VUT online library³

3 Concept model

In the model, we proceed from the assumption that immunity is stable and guarantees the absence of recurrent disease for the duration of research period.

²https://en.wikipedia.org/wiki/System_dynamics

³<https://www-sciencedirect-com.ezproxy.lib.vutbr.cz>

Following diagram taken from the reference article.

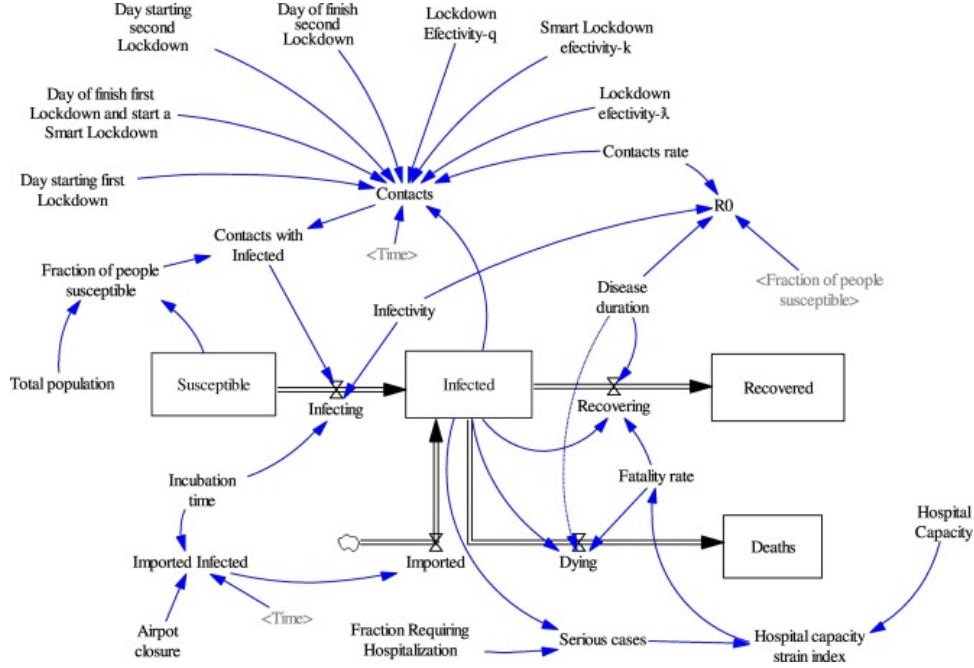


Figure 1: Stock and flows diagram [1]

It shows how each stock (susceptible, infectious, removed, deaths) variable is connected and influenced by other stock and auxiliary variable. Auxiliary variables are constructed from bibliographic references or some estimated, as shown in the

Mathematical equations:

$$\frac{dS}{dt} = -\frac{\beta C i}{it}$$

$$\frac{dI}{dt} = \frac{\beta C}{it} - \frac{I}{Dd} * (1 - Fr)$$

$$\frac{dR}{dt} = \frac{I}{Dd} * (1 - Fr)$$

$$\frac{dD}{dt} = \frac{I}{Dd} * (Fr)$$

4 Experiment

[[TODO Misha napishy suda]]

5 Conclusion

[[TODO Co se naucili]]

[[TODO Doporuceni]]

[[TODO Experiment with other country]]

References

- [1] D. Ibarra-Vega. Lockdown, one, two, none, or smart. modeling containing covid-19 infection. a conceptual model. *Science of The Total Environment*, 730:138917, 2020.