Practice 9

COMP9021, Term 3, 2019

1 Word ladders

Write a program word_ladder.py that computes all transformations of a word_word_1 into a word_word_2, consisting of sequences of words of minimal length, starting with word_1, ending in word_2, and such that two consecutive words in the sequence differ by at most one letter. All words have to occur in a dictionary with name dictionary.txt, stored in the working directory.

It is convenient and effective to first create a dictionary whose keys are all words in the dictionary with one letter replaced by a "slot", the value for a given key being the list of words that match the key with the "slot" being replaced by an appropriate letter. From this dictionary, one can then build a dictionary with words as keys, and as value for a given key the list of words that differ in only one letter from the key.

The program implements a function word_ladder(word_1, word_2) that returns the list of all solutions, a solution being as previously described.

Next is a possible interaction.

['TRAIN', 'GRAIN',

'GROIN',

'GROWN',

'CROWN',

'CROWS',

'CROPS',

```
$ python3
>>> from word ladder import *
>>> for ladder in word ladder('cold', 'warm'): print(ladder)
['COLD', 'CORD', 'WORD', 'WORM', 'WARM']
['COLD', 'CORD', 'WORD', 'WARD', 'WARM']
['COLD', 'CORD', 'CARD', 'WARD', 'WARM']
>>> for ladder in word_ladder('three', 'seven'): print(ladder)
['THREE', 'THREW', 'SHREW', 'SHRED', 'SIRED', 'SITED', 'SATED', 'SAVED', 'SAVER', 'SEVER', 'SEVER']
>>> for ladder in word_ladder('train', 'bikes'): print(ladder)
['TRAIN', 'BRAIN',
                  'BRAWN', 'BROWN',
                                   'BROWS'.
                                                            'COOPS'.
                                                                             'CORES'.
                                                                                                       'BAKES'.
Γ'TRATN'
         BRATN :
                  'BRAWN'
                          , BBUMN :
                                   , BBUMS,
                                            CRUMS,
                                                    'CBUDS'
                                                            'COOPS'
                                                                     CORPS
                                                                             'CORES'
                                                                                      COKES
                                                                                              PUKES
                                                                                                       PIKES
                                                                                                               'RTKES'
                                                                                                                BIKES,
                                                            'COOPS
                                                                                               CAKES
['TRAIN'
         'BRAIN
                  'BRAWN'
                           BROWN
                                   BROWS
                                            'CROWS
                                                    'CROPS'
                                                                     CORPS
                                                                              CORES
                                                                                      'CARES
                                                                                                       'BAKES
                                                                                                        BAKES
L'ALTN'
         'RRATN
                  'RRAWN
                          ' BROWN :
                                   'RROWS
                                            CROWS:
                                                    CROPS ?
                                                            'COUDS:
                                                                     CORPS
                                                                             CORES
                                                                                      RORES
                                                                                              'BARES
                                                                                                       BAKES
                                                                                                               'BTKES'
['TRAIN'
                                            CROWS
                                                                                               POKES
                                                                                                                BIKES
         BRAIN
                  BRAWN
                           BROWN
                                   BROWS
                                                    CROPS
                                                             COOPS
                                                                     CORPS
                                                                              CORES
                                                                                      PORES
                                                                                                       PIKES
 TRAIN
                                   CROWN
                                            CROWS
                                                                                                        BAKES
Γ'TRAIN'.
         'BRAIN'
                  'BRAWN'
                          'BROWN
                                   'CROWN
                                            'CROWS
                                                    'CROPS'
                                                            'COOPS
                                                                     CORPS'
                                                                             CORES
                                                                                      COKES
                                                                                              POKES
                                                                                                       PIKES
                                                                                                               'BIKES'
                                                                                                                BIKES
['TRAIN
          BRAIN
                  BRAWN
                           BROWN
                                   CROWN
                                            CROWS
                                                    CROPS
                                                             COOPS
                                                                     CORPS
                                                                              CORES
                                                                                      CARES
                                                                                               CAKES
                                                                                                       BAKES
rann'
                                                                     CORPS
         BRATN
                  BRAWN
                           BROWN
                                   CROWN
                                            CROWS
                                                    CROPS
                                                            'COOPS
                                                                              CORES
                                                                                      CARES
                                                                                               BARES
                                                                                                       BAKES
Γ'TRAIN'.
         'BRAIN'
                  'BRAWN'
                          'BROWN'
                                   'CROWN'
                                            'CROWS
                                                    'CROPS'
                                                            'COOPS
                                                                     'CORPS'
                                                                             'CORES
                                                                                      BORES
                                                                                              'BARES
                                                                                                       BAKES
                                                                                                               'BIKES'
['TRAIN'
          BRATN
                  BRAWN
                           BROWN
                                   CROWN
                                            CROWS
                                                    CROPS
                                                             COOPS
                                                                     CORPS
                                                                              CORES
                                                                                      PORES
                                                                                               POKES
                                                                                                       PIKES
                                                                                                                BIKES
Γ'TRATN'
         CRATN
                  CROTN
                           , GROWN
                                   CROWS
                                            CROWS
                                                            COOPS
                                                                     CORPS
                                                                              CORES
                                                                                      COKES
                                                                                              CAKES
                                                                                                       BAKES
                                                    CRUDS
                                                                                                                'BIKES'
['TRAIN'
         'GRAIN
                  'GROIN'
                          'GROWN'
                                   'GROWS
                                            'CROWS
                                                    'CROPS'
                                                            'COOPS
                                                                     'CORPS
                                                                             'CORES
                                                                                      COKES
                                                                                              'POKES
                                                                                                       PIKES
                                                                                                               'BIKES'
['TRAIN
                                                                             CORES
Γ'TRATN'
         GRATN
                  'GROTN'
                          GROWN :
                                   GROWS
                                            'CROWS
                                                    CROPS ?
                                                            COOPS
                                                                     CORPS
                                                                             CORES
                                                                                      CARES
                                                                                              BARES
                                                                                                       BAKES
                                                                                                               'BTKES'
                                                                                              BARES
['TRAIN'
         'GRAIN
                  'GROIN'
                          'GROWN'
                                   'GROWS
                                            'CROWS
                                                    'CROPS'
                                                            'COOPS
                                                                     'CORPS
                                                                             'CORES
                                                                                      BORES
                                                                                                       BAKES
                                                                                                               'BIKES'
['TRAIN'
         'GRAIN
                          'GROWN
                                   GROWS
                                            CROWS
                                                    CROPS
                                                            'COOPS
                                                                     CORPS
                                                                             CORES
                                                                                      PORES
                                                                                              POKES
                                                                                                       PIKES
                                                                                                               'BIKES'
Γ'TRATN'.
         'GRATN'
                  'GROIN'
                          'GROWN
                                   CROWN :
                                            'CROWS
                                                    'CROPS'
                                                            'COOPS
                                                                     CORPS
                                                                             CORES
                                                                                      COKES
                                                                                              CAKES
                                                                                                       BAKES
                                                                                                               'BIKES'
['TRAIN',
         GRATN
                  GROTN
                          GROWN :
                                                            COOPS,
                                                                     CORPS
                                                                              CORES
                                                                                      COKES
                                                                                              POKES
                                                                                                       PIKES
                                                                                                               'BTKES'
                                   CROWN
                                            CROWS
                                                    CROPS ?
['TRAIN',
                  'GROIN'
                          'GROWN
                                   'CROWN'
                                            'CROWS
                                                    'CROPS'
                                                            'COOPS'
                                                                     'CORPS'
                                                                             CORES
                                                                                      CARES
                                                                                                       BAKES
```

'CORPS'

'CORES'.

'CARES'.

'BARES',

'BAKES',

'BIKES']

'COOPS'.

```
['TRAIN', 'GRAIN', 'GROIN', 'GROWN', 'CROWN', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'BORES', 'BAKES', 'BAKES', 'BIKES']
['TRAIN', 'GRAIN', 'GROIN', 'GROWN', 'CROWN', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'PORES', 'POKES', 'PIKES', 'BIKES']
['TRAIN', 'DRAIN', 'DRAWN', 'DROWN', 'CROWN', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'COKES', 'CAKES', 'BAKES', 'BIKES']
                                                                            'CROWS', 'CROPS', 'COOPS', 'CORPS',
                                                                                                                                                                     'POKES',
                                                                                                                                                                                                    'BIKES']
['TRAIN', 'DRAIN', 'DRAWN', 'DROWN',
                                                             'CROWN',
                                                                                                                                        'CORES', 'COKES',
                                                                                                                                                                                     'PIKES',
['TRAIN', 'DRAIN', 'DRAWN', 'DROWN',
                                                             'CROWN',
                                                                             'CROWS',
                                                                                           'CROPS',
                                                                                                          'COOPS', 'CORPS',
                                                                                                                                        'CORES'
                                                                                                                                                       'CARES',
                                                                                                                                                                      'CAKES'
                                                                                                                                                                                     'BAKES',
                                                                                                                                                                                                    'BIKES']
 ['TRAIN', 'DRAIN', 'DRAWN',
                                              'DROWN',
                                                             'CROWN',
                                                                            'CROWS',
                                                                                           'CROPS',
                                                                                                          'COOPS',
                                                                                                                         'CORPS',
                                                                                                                                        'CORES',
                                                                                                                                                       'CARES',
                                                                                                                                                                      'BARES'
                                                                                                                                                                                     'BAKES',
                                                                                                                                                                                                    'BIKES']
                                                             'CROWN',
['TRAIN', 'DRAIN', 'DRAWN', 'DROWN', ['TRAIN', 'DRAIN', 'DRAWN', 'DROWN',
                                                                            'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'BORES', 'CROWS', 'CROPS', 'COOPS', 'COOPS', 'CORPS', 'CORES', 'PORES',
                                                                                                                                                                     'BARES',
                                                                                                                                                                                    'BAKES', 'BIKES']
'PIKES', 'BIKES']
                                                              'CROWN',
                                                                                                                                                                      'POKES'
['TRAIN', 'DRAIN', 'DRAWS', 'DRAWS', 'BRAGS', 'BRATS', 'BEATS', 'BESTS', 'BUSTS', 'BUSES', 'BASES', 'BAKES', 'BIKES']
['TRAIN', 'DRAIN', 'DRAWN', 'DRAWS', 'DRAGS', 'BRAGS', 'BRATS', 'BEATS', 'BELTS', 'BELLS', 'BALLS', 'BALLS', 'BAKES', 'BIKES']
```

2 The Word Search puzzle

The Word Search puzzle consists of a grid of letters and a number of words, that have to be read horizontally, vertically or diagonally, in either direction. Write a program word_search.py that defines a class WordSearch with the following properties.

- To create a WordSearch object, the name of a file has to be provided. This file is meant to store a number of lines all with the same number of uppercase letters, those lines possibly containing spaces anywhere, and the file possibly containing extra blank lines.
- __str__() is implemented.
- It has a method number_of_solutions() to display the number of solutions for each word length for which a solution exists.
- It has a method locate_word_in_grid() that takes a word as argument; it returns None if the word cannot be read in the grid, and otherwise returns the x and y coordinates of an occurrence of the first letter of the word in the grid and the direction to follow (N, NE, E, SE, S, SW, W or NW) to read the whole word from that point onwards. Coordinates start from 0, with the x-axis pointing East, and the y-axis pointing South.
- It has a method locate_words_in_grid() that takes any number of words as arguments, and returns a dictionary who keys are those words and whose values are None or the triple returned by locate_word_in_grid() when called with that word as argument.
- It has a method display_word_in_grid() that takes a word as argument and in case the word can be read from the grid, prints out the grid with all characters being displayed in lowercase, except for those that make up word, displayed in uppercase.

Here is a possible interaction.

```
DAO ELD LOG GBMNE
ITDCMEAINRUTS L
CLUUEICGGGOLII
KMUIMUIDIRIALE
EURTUNGSTENBYH
LILSLTTULRUOEI
CMATETIURDRCRU
IDSCAMAGNESIUM
MAMPDMUINATII
PCNPLATINUMDLL
HZEMANGANESEI
MGITINRUNORITC
MGITINRUNORITC
MGITINRUNORITC
MGRIANAMERCURYN
UOTCCREPPOCEER
```

```
$ python3
 >>> from word_search import *
>>> import pprint
>>> ws = WordSearch('word_search_1.txt')
 >>> print(ws)
 N D A O E L D L O G B M N E
 ITDCMEAINRUTSL
 CLUUEICGGGOLII
 KMUIMUIDIRIALT
 EURTUNGSTENBVH
L I L S L T T U L R U O E I
C M A T E T I U R D R C R U
 IDSCAMAGNESIUM
 \begin{smallmatrix} M&A&M&P&D&M&U&I&N&A&T&I&T&I\\ P&C&N&P&L&A&T&I&N&U&M&D&L&L \end{smallmatrix} 
 HZEMANGANESEIG
 MGITINRUNORITC
 RIANNAMERCURYN
U O T C C R E P P O C E E R
>>> metal = 'PLATINUM'
>>> print(f'{metal}: ws.locate_word_in_grid(metal)')
 PLATINUM: (3, 9, 'E')
 >>> metal = 'SODIUM'
 >>> print(f'{metal}: ws.locate_word_in_grid(metal)')
 SODIUM: None
SODIUM: None
>>> metals = ('PLATINUM', 'COPPER', 'MERCURY', 'TUNGSTEN', 'MAGNESIUM', 'ZINC', 'MANGANESE',
... 'TITANIUM', 'TIN', 'IRON', 'LITHIUM', 'CADMIUM', 'GOLD', 'COBALT', 'SILVER',
... 'NICKEL', 'LEAD', 'IRIDIUM', 'URANIUM', 'SODIUM')
>>> located_metals = ws.locate_words_in_grid(*metals)
... 'NICKEL', 'LEAD', 'IRIDIUN', '
>>> located_metals = ws.locate_wor
>>> pprint.pprint(located_metals)
{'CADMIUN': (1, 9, 'N'),
'COBPALT': (11, 6, 'N'),
'GODID': (9, 0, 'W'),
'IRIDIUM': (10, 3, 'W'),
'IRIDIUM': (10, 3, 'W'),
'LEAD': (4, 5, 'S'),
'LITHIUM': (13, 1, 'S'),
'MAGNESIUM': (5, 7, 'E'),
'MANGANESE': (3, 10, 'E'),
'MERCURY': (6, 12, 'E'),
'PLATINUM': (12, 1, 'S'),
'SILVER': (12, 1, 'S'),
'SILVER': (12, 1, 'S'),
'TITANIUM': (12, 8, 'W'),
'TITANIUM': (12, 8, 'W'),
'TITANIUM': (12, 8, 'W'),
'UNGSTEN': (3, 4, 'E'),
'URANIUM': None,
  'URANIUM': None,
'ZINC': (1, 10, 'SE')}
 >>> for metal in metals:
 ... print(metal, end = ':\n')
             ws.display_word_in_grid(metal)
            print()
 DI ATTNIIM ·
ndaoeldlogbmne
itdcmeainrutsl
cluueicgggolii
kmuimuidirialt
 eurtungstenbvh
 lilslttulruoei
 cmatetiurdrcru
 idscamagnesium
mampdmuinatiti
pcnPLATINUMdll
 hzemanganeseig
m g i t i n r u n o r i t c
r i a n n a m e r c u r y n
\verb"uotccreppoceer"
 COPPER:
ndaoeldlogbmne
itdcmeainrutsl
cluueicgggolii
kmuimuidirialt
eurtungstenbvh
lilslttulruoei
cmatetiurdrcru
 idscamagnesium
 mampdmuinatiti
 pcnplatinumdll
 hzemanganeseig
mgitinrunoritc
riannamercuryn
 uotccREPPOCeer
\tt n d a o e l d l o g b m n e
itdcmeainrutsl
cluueicgggolii
```

```
k m u i m u i d i r i a l t
e u r t u n g s t e n b v h
l i l s l t t u l r u o e i
c m a t e t i u r d r c r u
i d s c a m a g n e s i u m
m a m p d m u i n a t i t i
p c n p l a t i n u m d l l
h z e m a n g a n e s e i g
m g i t i n r u n o r i t c
r i a n n a M E R C U R Y n
u o t c c r e p p o c e e r
```

TUNGSTEN:

ndaoeldlogbmne
itdcmeainrutsl
cluueicgggolii
kmuimuidirialt
eurTUNGSTENbvh
lilslttulruoei
cmatetiurdrcru
idscamagnesium
mampdmuinatiti
pcnplatinumdll
hzemanganeseig
mgitinrunoritc
riannamercuryn
uotccreppoceer

MAGNESTUM:

n d a o e l d l o g b m n e i t d c m e a i n r u t s l c l u u e i c g g g o l i i k m u i m u i d i r i a l t e u r t u n g s t e n b v h l i l s l t t u l r u o e i c m a t e t i u r d r c r u i d s c a M A G N E S I U M m a m p d m u i n a t i t i p c n p l a t i n u m d l l h z e m a n g a n e s e i g m g i t i n r u n o r i t c r i a n n a m e r c u r y n u o t c c r e p p o c e e r

ZINC:

ndaoeldlogbmne
itdcmeainrutsl
cluueicgggolii
kmuimuidirialt
eurtungstenbvh
lilslttulruoei
cmatetiurdrcru
idscamagnesium
mampdmuinatiti
pcnplatinumdll
hZemanganeseig
mgItinrunoritc
riaNnamercuryn
uotcCreppoceer

MANGANESE:

ndaoeldlogbmne
itdcmeainrutsl
cluueicgggolii
kmuimuidirialt
eurtungstenbvh
lilslttulruoei
cmatetiurdrcru
idscamagnesium
mampdmuinatiti
pcnplatinumdll
tzeMANGANESEig
mgitinrunoritc
riannamercuryn
uotccreppoceer

TITANIUM:

ndaoeldlogbmne
itdcmeainrutsl
cluueicgggolii
kmuimuidirialt
eurtungstenbvh
lilslttulruoei
cmatetiurdrcru
idscamagnesium
mampdMUINATITi
pcnplatinumdll
zemanganeseig
mgitinrunoritc
riannamercuryn
uotccreppoceer

```
TIN:

ndaoeldlogbmne
itdcmeainrutsl
cluueicgggolii
kmuimuidirialt
eurtungstenbvh
lilslttulruoei
cmatetiurdrcru
idscamagNesium
mampdmuInatiti
pcnplaTinumdll
hzemanganeseig
mgitinrunoritc
riannamercury
uotccreppoceer

IRON:
```

ndaoeldorutschrift nu tcsl
cluueicgggolii
kmuimuidirialt
eurtungstenbvh
lilsltulruoei
cmatetiurdrcru
idscamagnesium
mampdmuinatiti
pcnplatinumdll
hzemanganeseig
mgitinruNORItc
riannamercuryn
uotccreppoceer

LITHIUM:

ndaoeldoruts L
cluweicgggoliI
kmuimuidirialT
eurtungstenbvH
lilsltulruoeI
cmatetiurdrcrU
idscamagnesiuM
mampdmuinatiti
pcnplatinumdll
hzemanganeseig
mgitinrunoritc
riannamercuryn
uotccreppoceer

CADMIUM:

ndaoeldlogbmne
itdcmeainrutsl
cluueicgggolii
kMuimuidirialt
eUrtungstenbvh
lIlslttulruoei
cMatetiurdrcru
iDscamagnesium
mAmpdmuinatiti
pCnplatinumdll
hzemanganeseig
mgitinrunoritc
riannamercuryn
uotccreppoceer

GOLD:

n d a o e l D L O G b m n e i t d c m e a i n r u t s l c l u u e i c g g g o l i i k m u i m u i d i r i a l t e u r t u n g s t e n b v h l i l s l t t u l r u o e i c m a t e t i u r d r c r u i d s c a m a g n e s i u m m a m p d m u i n a t i t i p c n p l a t i n u m d l l h z e m a n g a n e s e i g m g i t i n r u n o r i t c r u o t c r r e p p o c e e r

COBALT:

ndaoeldlogbmne
itdcmeainruTsl
cluueicgggoLii
kmuimuidiriAlt
eurtungstenBvh
lilslttulruOei
cmatetiurdrCru
idscamagnesium
mampdmuinatiti
pcnplatinumdll
hzemanganeseig

m g i t i n r u n o r i t c r i a n n a m e r c u r y n u o t c c r e p p o c e e r

SILVER:

ndaoeldlogbmne
itdcmeainrutSl
cluueicgggolli
kmuimuidiriaLt
eurtungstenbVh
lilslttulruoEi
cmatetiurdrcRu
idscamagnesium
mampdmuinatiti
pcnplatinumdll
hzemanganeseig
mgitinrunoritc
riannamercuryn
uotccreppoceer

NICKEL:

Ndaoeldlogbmne
Itdcmeainrutsl
Cluueicgggolii
Kmuimuidirialt
Eurtungstenbvh
Lilslttulruoei
cmatetiurdrcru
idscamagnesium
mampdmuinatiti
pcnplatinumdll
hzemanganeseig
mgitinrunoritc
runtannamercury
nuotccreppoceer

LEAD:

ndaoeldlogbmne
itdcmeainrutsl
cluueicgggolii
kmuimuidirialt
eurtungstenbvh
lilsLttulruoei
cmatEtiurdrcru
idscAmagnesium
mampDmuinatiti
pcnplatinumdll
hzemanganeseig
mgitinrunoritc
riannamercuryn
uotccreppoceer

IRIDIUM:

INDIDIN:

ndaoeldlogbmne

itdcmeainrutsl

cluueicgggolii

kmui MUIDIRIalt

eurtungstenbvh

lilslttulruoei

cmatetiurdrcru

idscamagnesium

mampdmuinatiti

pcnplatinumdll

hzemanganeseig

mgitinrunoritc

riannamercuryn

uotccreppoceer

URANIUM:

SODTUM:

3 Possible subtractions yielding a given sum

Write a program subtractions.py that takes as input an iterable L of nonnegative integers and an integer N, and displays all ways of inserting minus signs and parentheses in L, resulting in an expression that evaluates to N. For this question we make use of eval().

Next is a possible interaction.

```
$ python3
>>> from subtractions import *
>>> subtractions((1, 2, 3, 4, 5), 1)
1 - ((2 - 3) - (4 - 5))
(1 - ((2 - 3) - 4)) - 5
>>> subtractions((1, 2, 3, 4, 5), 2)
>>> subtractions((1, 2, 3, 4, 5), 3)
1 - (2 - (3 - (4 - 5)))
1 - ((2 - (3 - 4)) - 5)
(1 - (2 - 3)) - (4 - 5)
>>> subtractions((1, 2, 3, 4, 5), 4)
>>> subtractions((1, 2, 3, 4, 5), 5)
(1 - 2) - ((3 - 4) - 5)
>>> subtractions((1, 3, 2, 5, 11, 9, 10, 8, 4, 7, 6), 40)
1 - ((((3 - 2) - 5) - 11) - (9 - ((((10 - 8) - 4) - 7) - 6)))
1 - (((((((3-2)-5)-11)-9)-10)-(8-(4-(7-6))))
1 - ((((((3-2)-5)-11)-9)-10)-((8-(4-7))-6))
1 - ((((((((3-2)-5)-11)-9)-10)-(8-4))-(7-6))
1 - (((((3-2)-5)-11)-(9-(((10-8)-4)-7)))-6)
1 - (((((((3-2)-5)-11)-(9-((10-8)-4)))-7)-6)
1 - ((((((((3-2)-5)-11)-(9-(10-8)))-4)-7)-6)
1 - (((((((((3-2)-5)-11)-(9-10))-8)-4)-7)-6)
(1-3)-((((2-5)-11)-9)-(10-(((8-4)-7)-6)))
(1-3)-(((((2-5)-11)-9)-(10-((8-4)-7)))-6)
(1-3)-((((((2-5)-11)-9)-(10-(8-4)))-7)-6)
(1-3)-(((((((2-5)-11)-9)-(10-8))-4)-7)-6)
(1 - ((((3 - 2) - 5) - 11) - 9)) - ((((10 - 8) - 4) - 7) - 6)
((1-3)-(((2-5)-11)-9)-10))-(((8-4)-7)-6)
(1 - ((((((3 - 2) - 5) - 11) - 9) - 10) - 8)) - (4 - (7 - 6))
(1 - ((((((3 - 2) - 5) - 11) - 9) - 10) - (8 - (4 - 7)))) - 6
(1 - ((((((((3 - 2) - 5) - 11) - 9) - 10) - (8 - 4)) - 7)) - 6
((1 - ((((((3 - 2) - 5) - 11) - 9) - 10) - 8)) - (4 - 7)) - 6
```

4 Voting systems (optional)

Find out (e.g., in Wikipedia) about these voting systems: (a) one round method, (b) two round method, (c) elimination method, (d) De Borda count, and (e) De Condorcet count.

The elimination method works as follows. One adds up the tallies of all candidates who rank 1st and eliminate the candidate(s) who get the minimal number of votes (as ranked 1st candidates). For a given ordering, the candidates who remain and were ranked after the eliminated candidate(s) see their ranking go up so that the ordering is preserved, and rankings range from 1 up to the number of candidates that remain (for instance, if to start with, there are 5 candidates, A, B, C, D and E who are ranked 1, 2, 3, 4 and 5, respectively, and if B and D are eliminated because they get the least number of votes as 1st candidates across all rankings, then for that particular ranking, A remains ranked 1st, C becomes ranked 2nd, and E becomes ranked third). The process is repeated until there is only one candidate left, or all candidates that remain get exactly the same number of votes as preferred candidates.

Then design a program election.py that defines a class Election, with objects of this class created from Excel files of the kind provided as examples, to which the methods

```
one_round_winners(),two_round_winners(),elimination_winner(),de_borda_winners(), and
```

de_condorcet_winners()

can be applied. Also, the <u>__str__()</u> method is implemented so as to display in textual form the election results recorded in the Excel file.

Next is a possible interaction.

```
$ python3
>>> from election import *
>>> election = Election('election_1.xlsx')
>>> print(election)
Number of votes Albert Emily
                                  Oscar
                                          Maria
                                                   Max
                                            2
     3273
                   1
                           5
                                    4
                                                    3
     2182
                   5
                                                    2
     1818
                   5
                           2
                                    1
                                                    3
     1636
                   5
                           4
                                    2
                                                    3
                                            1
      727
                   5
                           2
                                    4
                                            3
                                                    1
      364
                   5
                           4
                                    2
                                            3
                                                    1
>>> election.one_round_winners()
The winner is Albert.
>>> election.two_round_winners()
The winner is Emily.
>>> election.elimination_winners()
The winner is Oscar.
>>> election.de_borda_winners()
The winner is Maria.
>>> election.de_condorcet_winners()
The winner is Max.
>>> election = Election('election_2.xlsx')
Number of votes Albert Emily
                                 Oscar
                                          Maria
                                                   Max
     1000
                   1
                           2
                                    3
                                            4
                                                    5
>>> election.one_round_winners()
The winner is Albert.
>>> election.two_round_winners()
The winner is Albert.
>>> election.elimination_winners()
The winner is Max.
>>> election.de_borda_winners()
The winner is Albert.
>>> election.de_condorcet_winners()
The winner is Albert.
```

```
>>> election = Election('election_3.xlsx')
>>> print(election)
Number of votes Albert
     1000
     1000
                   1
     1000
                   1
     1000
                   1
     1000
     1000
>>> election.one_round_winners()
All candidates are winners.
>>> election.two_round_winners()
All candidates are winners.
>>> election.elimination_winners()
All candidates are winners.
>>> election.de_borda_winners()
All candidates are winners.
>>> election.de_condorcet_winners()
All candidates are winners.
>>> election = Election('election_4.xlsx')
>>> print(election)
Number of votes Albert Emily
                                 Oscar
     1000
                   1
                           2
                                   3
                   2
                                   3
     1000
>>> election.one_round_winners()
The winners are Albert and Emily.
>>> election.two_round_winners()
The winners are Albert and Emily.
>>> election.elimination_winners()
The winner is Oscar.
>>> election.de_borda_winners()
The winners are Albert and Emily.
>>> election.de_condorcet_winners()
The winners are Albert and Emily.
```

```
>>> election = Election('election_5.xlsx')
>>> print(election)
Number of votes Albert Emily
                                  Oscar
                                          Maria
     1000
                   1
                                    3
                                            4
                   2
     1000
                           3
                                    1
                                            4
     1000
                   3
                           1
                                            4
>>> election.one round winners()
The winners are Albert, Emily and Oscar.
>>> election.two_round_winners()
The winners are Albert, Emily and Oscar.
>>> election.elimination_winners()
The winner is Maria.
>>> election.de_borda_winners()
The winners are Albert, Emily and Oscar.
>>> election.de_condorcet_winners()
There is no winner.
>>> election = Election('election_6.xlsx')
>>> print(election)
Number of votes Albert Emily
                                  Oscar
     1000
                   1
                           2
                                    3
                   2
                                    3
     1000
                           1
      250
                   2
                           3
                                    1
      250
                   3
>>> election.one_round_winners()
The winners are Albert and Emily.
>>> election.two_round_winners()
The winners are Albert and Emily.
>>> election.elimination_winners()
The winners are Albert and Emily.
>>> election.de_borda_winners()
The winners are Albert and Emily.
>>> election.de_condorcet_winners()
The winners are Albert and Emily.
```

5 Context free grammars (advanced, optional)

A context free grammar is a set of production rules of the form

```
symbol_0 ---> symbol_1 ... symbol_n
```

where symbol_0, ..., symbol_n are either terminal or nonterminal symbols, with symbol_0 being necessarily nonterminal. A symbol is a nonterminal symbol iff it is denoted by a word built from underscores or uppercase letters. A special nonterminal symbol is called the *start symbol*. The language *generated* by the grammar is the set of sequences of terminal symbols obtained by replacing a nonterminal symbol by the sequence on the right hand side of a rule having that nonterminal symbol on the left hand side, starting with the start symbol. For instance, the following, where EXPRESSION is the start symbol, is a context free grammar for a set of arithmetic expressions.

```
EXPRESSION --> EXPRESSION TERM_OPERATOR TERM

EXPRESSION --> TERM

TERM --> TERM FACTOR_OPERATOR FACTOR

TERM --> FACTOR

FACTOR --> NUMBER

FACTOR --> (EXPRESSION)

NUMBER --> DIGIT NUMBER

NUMBER --> DIGIT

DIGIT --> 0

...

DIGIT --> 9

TERM_OPERATOR --> +

TERM_OPERATOR --> +

FACTOR_OPERATOR --> *

FACTOR_OPERATOR --> /
```

Moreover, blank characters (spaces or tabs) can be inserted anywhere except inside a number. For instance, (2 + 3) * (10 - 2) - 12 * (1000 + 15) is an arithmetic expression generated by the grammar.

Note that operators associate to the left. The grammar is *unambiguous*, in the sense that every expression generated by the grammar has a unique evaluation.

Write down a program <code>context_free_grammar.py</code> that implements a function <code>evaluate()</code> which takes a string representing an expression as an argument, checks whether the expression can be generated by the grammar, and in case the answer is yes, returns the value of the expression, provided that no division by 0 is attempted; otherwise, the function returns <code>None</code>.

Next is a possible interaction.

```
$ python3
>>> from context_free_grammar import *
>>> evaluate('100')
100
>>> evaluate('(100)')
100
>>> evaluate('1 - 20 + 300')
>>> evaluate('((((((1))-((20))+((300)))))')
281
>>> evaluate('20 * 4 / 5')
16.0
>>> evaluate('((((((20))*((4))/((5)))))')
>>> evaluate('1 + 20 * 30 - 400 / 500')
>>> evaluate('1 + (20*30-400) / 500')
1.4
>>> evaluate('1+(20 / 30 * 400)- 500')
-232.3333333333333
>>> evaluate('1 + 2 * (3+4*5) / (6*7-8/9)')
2.1189189189189186
>>> evaluate('100)')
>>> evaluate('100 + ')
>>> evaluate('100 + -3')
>>> evaluate('100 # 50')
>>> evaluate('100 / 0')
```

Before you tackle the exercise, find out about recursive descent parsers. To easily tokenise the string, check out the findall() function from the re module.