

THE UNIVERSITY OF ZAMBIA
SCHOOL OF HUMANITIES AND SOCIAL SCIENCES
ECONOMICS DEPARTMENT
ECN 2115 TUTORIAL SHEET 1

1. You are given a firm that wishes to maximize profits (Π). The total revenue function of the firm is; $R = 4000Q - 33Q^2$. The total cost function is $C = 2Q^3 - 3Q^2 + 400Q + 5000$. Find the optimum quantity that maximises profits.

2. We have three goods X_1 , X_2 and X_3 . We have in the market place, the price of $P_1 = K10$, the price of good X_1 ; $P_2 = K2$, the price of good X_2 ; and $P_3 = K4$, the price of good X_3 . The consumer has $K100$ to spend on these items. The consumer must spread the expenditure of these three items such as to maximize utility. We are given the consumer's utility function as follows: $U = U(X_1, X_2, X_3) = 5 \log X_1 + 3 \log X_2 + 2 \log X_3$.
a) Derive the consumer's budget constraint. b) Solve for the optimal bundle (X_1, X_2, X_3)

3. You are given an objective function $f(X, Y) = 4X^2 + 3XY + 6Y^2$ and the constraint on the function in the form of $X + Y = 56$. Optimize $f(X, Y)$ subject to the constraint.

4. Suppose the market demand curve for a product is given by $Q_d = 1000 - 10P$ and the
 - a) market supply curve is given by $Q_s = -50 + 25P$.
 - b) a. What are the equilibrium price and quantity?
 - c) b. What is the Inverse Form of the demand curve?
 - d) c. At the market equilibrium, what is the price elasticity of demand?
 - e) d. Suppose the price in this market is \$25. What is the amount of excess demand?

5. Suppose demand for good A is given by $Q_A^d = 500 - 10P_A + 2P_B + 0.70I$ where P_A is the price of good A, P_B is the price of some other good B, and I is income. Assume that P_A is currently \$10, P_B is currently \$5, and I is currently \$100.
 - a. What is the elasticity of demand for good A with respect to the price of good A at the current situation?
 - b. What is the cross-price elasticity of the demand for good A with respect to the price of good B at the current situation?
 - c. What is the income elasticity of demand for good A at the current situation?

5. Consider the utility function $U(x, y) = 3x^2 + 5y$ with $MU_x = 6x$ and $MU_y = 5$.
- Is the assumption that “more is better” satisfied for both goods?
 - What is the $MRS_{x,y}$ for this utility function?
 - Is the $MRS_{x,y}$ diminishing, constant, or increasing as the consumer substitutes x for y along an indifference curve?
 - Will the indifference curves corresponding to this utility function be convex, concave, or straight lines?

Explain.

6. Consider two goods, A and B. For each of the following scenarios, develop the utility function $U(A, B)$ that matches the given information.

- The consumer believes that good A and B are perfect substitutes with one unit of A equivalent to four units of B.
- The consumer believes that good A and B are perfect compliments and always uses three unites of B for every unit of A.

7. Linda consumes two goods, X and Y. Her utility function is $U = XY$. Initially, $P_x = \$18$ and $P_y = \$2$. Linda's income is \$288. Then the price of X falls to \$8. [The following questions ask you to calculate a mathematical example of the income and substitution effects of a price decrease for good X.]

- a) Complete the following table.

Basket	X	Y	$U = XY$	$\frac{MU_x}{MU_y} = \frac{P_x}{P_y}$	Expenditure $P_x X + P_y Y$
A					
B	12	48			
C					

- The movement from point A to point B illustrates which effect, the income effect or the substitution effect? Explain.
- The movement from point B to point C illustrates which effect, the income effect or the substitution effect? Explain.
- Is good X a normal, inferior, or Giffen good? Explain.