Gradient Boosting Trees

Applied Machine Learning for Educational Data Science

true

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In Bagged Trees or Random Forests models, the trees are developed independently by taking a random sample of rows and columns from the dataset. The main difference between Gradient Boosting Trees and Bagged Trees or Random Forests is that the trees are developed sequentially and each tree model is built upon the errors of the previous tree models. The sequential process of model building and predictions in gradient boosted trees can be conceptually demonstrated as below.

Sequential Development of Trees from Residuals

Let's try to implement this idea in a toy dataset we use to predict a readability score from the number of sentences.

```
readability_sub <- read.csv('https://raw.githubusercontent.com/uo-datasci-specialization/c4-ml-fall-202
readability_sub[,c('sents','target')]</pre>
```

```
sents target
1 7 -2.58591
2 23 0.45993
3 17 -1.07471
4 7 -1.81700
5 6 -1.81492
```

```
6
      18 -0.94968
7
      10 -0.12103
       4 -2.82201
8
9
       9 -0.74845
10
      28 0.73949
      15 -0.96219
11
12
      10 -2.21515
      10 -1.21845
13
14
       8 -1.89544
15
      19 -0.04101
16
      15 -1.83717
17
       6 -0.18819
18
       6 -0.81739
       7 -1.86308
19
20
      19 -0.41630
```

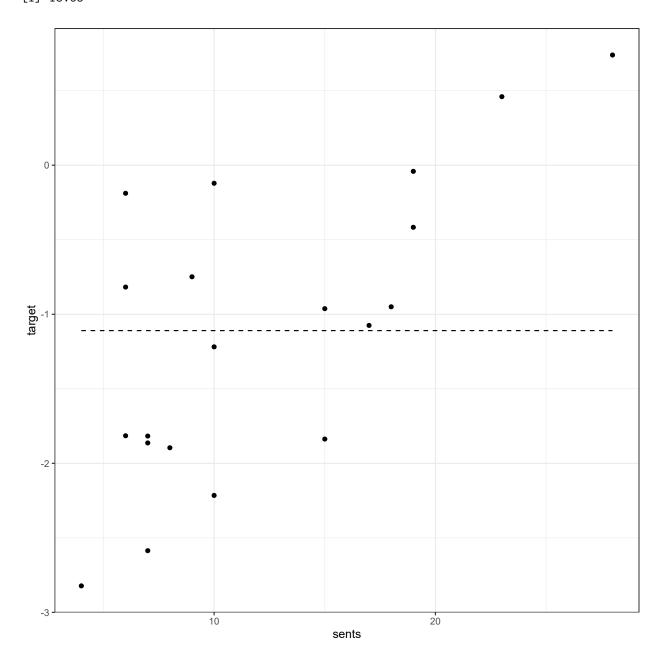
Iteration 0

We first start with a simple model that uses the average target outcome to predict the readability for all observations in this toy dataset. We calculate the predictions and residuals from our first model, and fit a tree model to the residuals using the number of sentences as the predictor.

```
readability_sub$pred1 <- mean(readability_sub$target)
readability_sub$res1 <- readability_sub$target - readability_sub$pred
readability_sub[,c('sents','target','pred1','res1')]</pre>
```

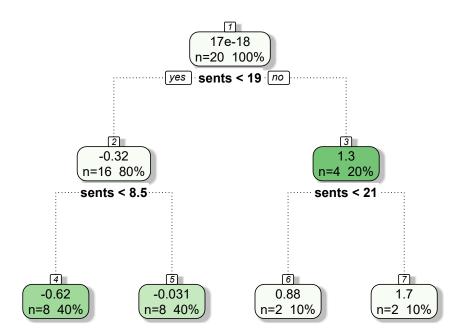
```
sents
           target pred1
                             res1
1
      7 -2.58591 -1.109 -1.47648
2
      23 0.45993 -1.109 1.56936
3
      17 -1.07471 -1.109 0.03473
4
      7 -1.81700 -1.109 -0.70757
5
      6 -1.81492 -1.109 -0.70548
6
     18 -0.94968 -1.109 0.15975
7
     10 -0.12103 -1.109 0.98840
8
      4 -2.82201 -1.109 -1.71257
9
      9 -0.74845 -1.109
                          0.36098
10
      28 0.73949 -1.109 1.84892
11
     15 -0.96219 -1.109 0.14724
12
      10 -2.21515 -1.109 -1.10572
13
      10 -1.21845 -1.109 -0.10902
      8 -1.89544 -1.109 -0.78601
14
15
     19 -0.04101 -1.109 1.06842
      15 -1.83717 -1.109 -0.72773
16
17
      6 -0.18819 -1.109
                         0.92125
18
      6 -0.81739 -1.109 0.29204
      7 -1.86308 -1.109 -0.75364
19
20
      19 -0.41630 -1.109 0.69313
```

```
# SSE at the end of Iteration 0
sum(readability_sub$res1^2)
```



Iteration 1

Now, we fit a tree model to predict the residuals from the number of sentences. Notice that I fix the value of certain parameters while fitting the tree model (e.g., complexity parameter, minsplit, maxdepth).



Let's see the predictions of residuals from Model 1.

predict(model1, readability_sub)

```
3
                                  4
                                           5
                                                    6
                                                              7
-0.61606
         1.70914 -0.03142 -0.61606 -0.61606 -0.03142 -0.03142 -0.61606
                                          13
                                                    14
               10
                        11
                                 12
                                                             15
-0.03142
         1.70914 -0.03142 -0.03142 -0.03142 -0.61606 0.88078 -0.03142
               18
                        19
-0.61606 -0.61606 -0.61606 0.88078
```

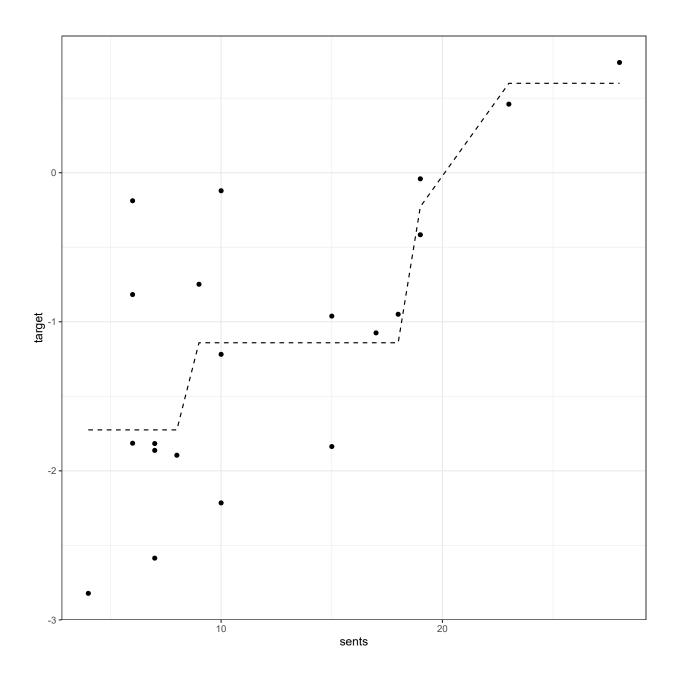
Now, add the predicted residuals from Model 1 to the predictions from Iteration 0 to obtain the new predictions at the end of Iteration 1.

```
readability_sub$pred2 <- readability_sub$pred1 + predict(model1, readability_sub)
readability_sub$res2 <- readability_sub$target - readability_sub$pred2
readability_sub[,c('sents','target','pred1','res1','pred2','res2')]</pre>
```

```
sents
          target pred1
                                   pred2
                                             res2
                            res1
1
      7 -2.58591 -1.109 -1.47648 -1.7255 -0.86042
2
     23 0.45993 -1.109 1.56936 0.5997 -0.13978
3
     17 -1.07471 -1.109 0.03473 -1.1409 0.06615
      7 -1.81700 -1.109 -0.70757 -1.7255 -0.09151
4
5
      6 -1.81492 -1.109 -0.70548 -1.7255 -0.08943
6
     18 -0.94968 -1.109 0.15975 -1.1409 0.19117
7
     10 -0.12103 -1.109 0.98840 -1.1409 1.01982
8
      4 -2.82201 -1.109 -1.71257 -1.7255 -1.09651
9
      9 -0.74845 -1.109 0.36098 -1.1409 0.39240
10
     28 0.73949 -1.109 1.84892 0.5997 0.13978
     15 -0.96219 -1.109 0.14724 -1.1409 0.17866
11
12
     10 -2.21515 -1.109 -1.10572 -1.1409 -1.07430
13
     10 -1.21845 -1.109 -0.10902 -1.1409 -0.07760
14
      8 -1.89544 -1.109 -0.78601 -1.7255 -0.16995
15
     19 -0.04101 -1.109 1.06842 -0.2287 0.18765
16
     15 -1.83717 -1.109 -0.72773 -1.1409 -0.69631
17
      6 -0.18819 -1.109 0.92125 -1.7255 1.53731
18
      6 -0.81739 -1.109 0.29204 -1.7255 0.90810
19
      7 -1.86308 -1.109 -0.75364 -1.7255 -0.13758
20
     19 -0.41630 -1.109 0.69313 -0.2287 -0.18765
```

```
# SSE at the end of Iteration 1
sum(readability_sub$res2^2)
```

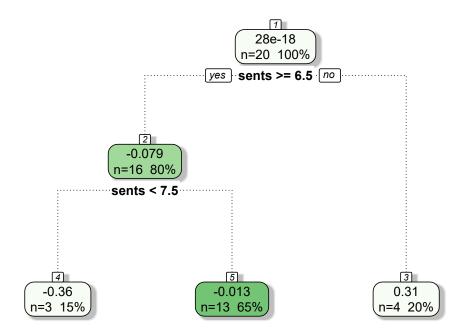
[1] 8.216



Iteration 2

We repeat Iteration 1, but the only difference is that we now fit a tree model again to predict the residuals obtained after the updated predictions at the end of Iteration 1.

fancyRpartPlot(model2,type=2,sub='')



Let's see the predictions of residuals from Model 2.

predict(model2, readability_sub)

Now, add the predicted residuals from Model 2 to the predictions from Iteration 1 to obtain the new predictions at the end of Iteration 2.

```
readability_sub$pred3 <- readability_sub$pred2 + predict(model2, readability_sub)
readability_sub$res3 <- readability_sub$target - readability_sub$pred3

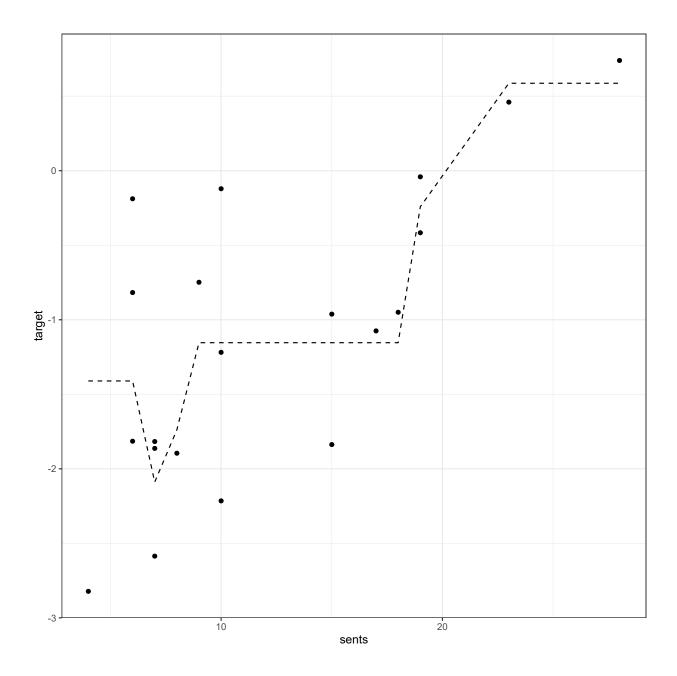
readability_sub[,c('sents','target','pred1','res1','pred2','res2','pred3','res3')]

sents target pred1 res1 pred2 res2 pred3 res3
1 7 -2.58591 -1.109 -1.47648 -1.7255 -0.86042 -2.0887 -0.49725
2 23 0.45993 -1.109 1.56936 0.5997 -0.13978 0.5866 -0.12670</pre>
```

```
17 -1.07471 -1.109 0.03473 -1.1409 0.06615 -1.1539
3
                                                    0.07922
4
      7 -1.81700 -1.109 -0.70757 -1.7255 -0.09151 -2.0887 0.27166
5
      6 -1.81492 -1.109 -0.70548 -1.7255 -0.08943 -1.4106 -0.40429
6
     7
     10 -0.12103 -1.109 0.98840 -1.1409
                                     1.01982 -1.1539 1.03290
8
      4 -2.82201 -1.109 -1.71257 -1.7255 -1.09651 -1.4106 -1.41138
9
      9 -0.74845 -1.109 0.36098 -1.1409
                                    0.39240 -1.1539 0.40547
10
     28 0.73949 -1.109 1.84892 0.5997 0.13978 0.5866 0.15285
     15 -0.96219 -1.109 0.14724 -1.1409 0.17866 -1.1539 0.19174
11
12
     10 -2.21515 -1.109 -1.10572 -1.1409 -1.07430 -1.1539 -1.06122
13
     10 -1.21845 -1.109 -0.10902 -1.1409 -0.07760 -1.1539 -0.06452
14
      8 -1.89544 -1.109 -0.78601 -1.7255 -0.16995 -1.7386 -0.15688
15
     19 -0.04101 -1.109 1.06842 -0.2287
                                     0.18765 -0.2417
                                                    0.20072
16
     15 -1.83717 -1.109 -0.72773 -1.1409 -0.69631 -1.1539 -0.68324
      6 -0.18819 -1.109 0.92125 -1.7255 1.53731 -1.4106 1.22244
17
18
      6 -0.81739 -1.109 0.29204 -1.7255 0.90810 -1.4106 0.59323
19
      7 -1.86308 -1.109 -0.75364 -1.7255 -0.13758 -2.0887 0.22559
20
```

```
# SSE at the end of Iteration 2
sum(readability_sub$res3^2)
```

[1] 7.422



We can keep iterating and add tree models as long as we find a tree model that improves our predictions (minimizing SSE).

A more formal introduction of Gradient Boosting Trees

Let $\mathbf{x}_i = (x_{i1}, x_{i2}, x_{i3}, ..., x_{ij})$ represent a vector of observed values for the i^{th} observation on j predictor variables, and y_i is the value of the target outcome for the i^{th} observation. A gradient boosted tree model is an ensemble of T different tree models sequentially developed and the final prediction of the outcome is obtained by using an additive function as

$$\hat{y_i} = \sum_{t=1}^T f_t(\mathbf{x}_i),$$

where f_t is a tree model obtained at Iteration t from the residuals at Iteration t-1.

The algorithm optimizes an objective function $\mathfrak{L}(\mathbf{y}, \hat{\mathbf{y}})$ in an additive manner. This objective loss function can be defined as sum of squared errors when the outcome is continuous or logistic loss when the outcome is categorical.

The algorithm starts with a constant prediction. For instance, in the above example, we start with the average outcome. Then, a new tree model that minimizes the objective loss function is searched and added at each iteration.

$$\hat{y}_{i}^{(0)} = \bar{y}$$

$$\hat{y}_{i}^{(1)} = \hat{y}_{i}^{(0)} + \alpha f_{1}(\mathbf{x}_{i})$$

$$\hat{y}_{i}^{(2)} = \hat{y}_{i}^{(1)} + \alpha f_{2}(\mathbf{x}_{i})$$

$$\vdots$$

$$\vdots$$

$$\hat{y}_{i}^{(t)} = \hat{y}_{i}^{(t-1)} + \alpha f_{t}(\mathbf{x}_{i})$$

Notice that I added a multiplier, α , while adding our predictions at each iteration. In the above example, we simply fixed this multiplier to 1, $\alpha = 1$, as we added the whole of new prediction to the previous prediction. This is not necessary. We can also choose to add only a fraction of new predictions (e.g., $\alpha = 0.1, 0.05, 0.01, 0.001$) at each iteration. This multiplier in machine learning literature is called **learning rate**. The smaller the learning rate, the more iterations (more tree models) we will need to achieve the same level of performance. So, the number of iterations (number of tree models, T) and the learning rate (α) play in tandem. Both of these parameters are known as the **boosting hyperparameters** and need to be tuned.

Think about choosing a **learning rate** as choosing your speed on a highway and **number of trees** as the time it takes to arrive at your destination. Suppose you are traveling from Eugene to Portland on I-5. If you drive 40 miles/hour, you are less likely to involve in an accident because you are more aware of your surroundings, but it will take 3-4 hours to arrive at your destination. If you are 200 miles/hour, it will only take you an hour to arrive at your destination, assuming you will not have an accident on the way (which is very likely). So, you try to find a speed level that is fast enough to arrive at your destination and also safe enough not to have an accident on your way.

TECHNICAL NOTE

Why do people call it **Gradient** Boosting? It turns out that the updates at each iteration based on the residuals from a previous model is related to the concept of negative gradient (first derivative) of the objective loss function with respect to the predicted values from the previous step.

$$-g_i^t = -\frac{\partial \mathcal{L}(y_i, \hat{y}_i^{t-1})}{\partial \hat{y}_i^{t-1}} = \hat{y}_i^{(t)} - \hat{y}_i^{(t-1)}$$

The general logic of gradient boosting works as

- take a differentiable loss function, $\mathfrak{L}(\mathbf{y}, \hat{\mathbf{y}})$, that summarizes the distance between observed and predicted values,
- start with an initial model to obtain initial predictions, $f_0(\mathbf{x}_i)$,

- iterate until termination:
 - calculate the negative gradients of the loss function with respect to predictions from previous step
 - fit a tree model to the negative gradients
 - update the predictions (with a multiplier, a.k.a learning rate).

Most software use mathematical approximations and computational hocus pocus to do these computations for faster implementation.

Fitting Gradient Boosting Trees using the gbm package

The gradient boosting trees can be fitted using the gbm function from the 'gbm package. The code below tries to replicate our example above using the toy dataset.

```
require(gbm)
              gbm(formula
gbm.model <-</pre>
                                   = target ~ sents,
                  data
                                   = readability_sub,
                                   = 'gaussian',
                  distribution
                                    = 2,
                  n.trees
                  shrinkage
                                    = 1,
                  interaction.depth = 2,
                  n.minobsinnode = 2,
                  bag.fraction
                                    = 0,
                  cv.folds
                                    = 1)
```

Model and Data:

- formula, a description of the outcome and predictive variables in the model using column names
- data, name of the data object to look for the variables in the formula statement
- distribution, a character to specify the type of objective loss function to optimize. 'gaussian' is typically used for continuous outcomes(minimize the squared error) and 'bernoulli' is typically used for the binary outcomes (minimizes the logistic loss)

Hyperparameters:

- n.trees, number of trees to fit (the number of iterations)
- shrinkage, learning rate.
- interaction.depth, the maximum depth of each tree developed at each iteration
- n.minobsinnode, the minimum number of observations in each terminal note of tree models at each iteration

Stochastic Gradient Boosting:

• bag.fraction, the proportion of observations to be randomly selected for developing a new tree at each iteration.

In Gradient Boosting Trees, when we develop a new tree model at each iteration, we use all observations (100% of rows). So, we can set bag.fraction=1 and gbm fits a gradient boosting tree model. On the other hand, adding a random component may sometimes help and yield better performance. You can think about this as an integration of Bagging and Boosting. So, we may want to take a random sample of observations to develop a tree model at each iteration. For instance, if you set bag.fraction=.9, the algorithm will first randomly sample 90% of the observations at each iteration before fitting the new tree model to residuals from the previous step. When bag.fraction is anything lower than 1, this is called Stochastic Gradient Boosting Trees. bag.fraction can also be considered as a hyperparameter to tune by trying different values to find an optimal value, or it can be fixed to a certain number.

Cros validation:

• cv.folds, number of cross-validation folds to perform.

Parallel Processing:

• n.cores, the number of CPU cores to use.

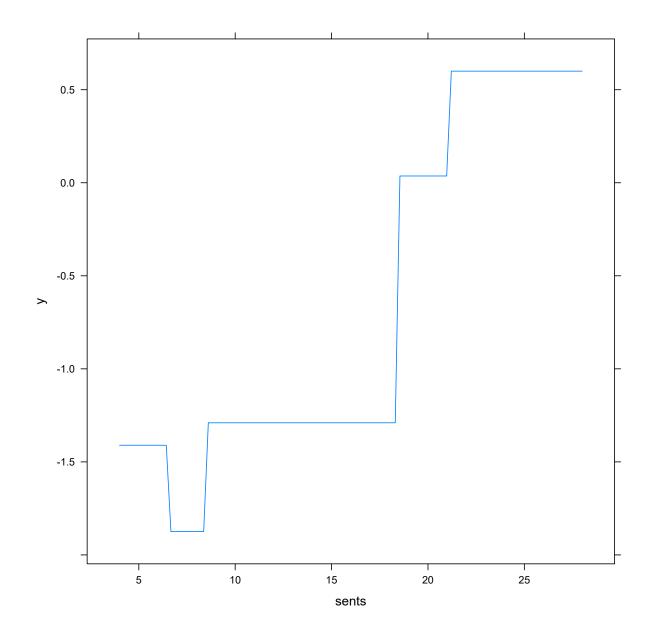
```
# Obtain predictions from the model

predict(gbm.model)

[1] -1.8746  0.5997 -1.2900 -1.8746 -1.4106 -1.2900 -1.2900 -1.4106 -1.2900
[10]  0.5997 -1.2900 -1.2900 -1.8746  0.0364 -1.2900 -1.4106 -1.4106
[19] -1.8746  0.0364

# Plot the final model

plot(gbm.model)
```



Fitting Gradient Boosting Trees using the caret package and Hyperparameter Tuning

The gbm algorithm is available in the caret package. Let's check the hyperparameters available to tune.

```
require(caret)
getModelInfo()$gbm$parameters
```

parameter class label
1 n.trees numeric # Boosting Iterations
2 interaction.depth numeric Max Tree Depth

```
3 shrinkage numeric Shrinkage
4 n.minobsinnode numeric Min. Terminal Node Size
```

The most important four parameters are all available to tune. Note that it is very challenging to find the best combination of values for all these four hyperparameters unless you implement a full grid search which may take a very long time. You may appply a general sub-optimal strategy to tune the hyperparameters step by step either in pairs or one by one. Below is one way to implement such strategy:

- 1. Fix the interaction.depth and n.minobsinnode to a certain value (e.g., interaction.depth = 5, n.minobsinnode = 10),
- 2. Pick a small value of learning rate (shrinkage) such as 0.05 or 0.1,
- 3. Do a grid search and find the optimal number of trees (n.trees) using the fixed values at #1 and #2,
- 4. Fix the n.trees at its optimal value from #3, keep shrinkage same as in #2, and do a two-dimensional grid search for interaction.depth and n.minobsinnode and find the optimal number of depth and minimum observation in a terminal node,
- 5. Fix the interaction.depth and n.minobsinnodeat their optimal values from #4, lower the learning rate and increase the number of trees to see if the model performance can be further improved.
- 6. Fix interaction.depth,n.minobsinnode, shrinkage, and n.trees at their optimal values from previus steps, and do a grid search for bag.fraction.

At the link below you will find an interactive app you can play to understand the dynamics among these hyperparameters and optimize them in toy examples.

http://arogozhnikov.github.io/2016/07/05/gradient boosting playground.html

Predicting Readability Scores Using Gradient Boosting Trees

First, we import and prepare data for modeling. Then, we split the data into training and test pieces.

```
# Import the dataset
readability <- read.csv('https://raw.githubusercontent.com/uo-datasci-specialization/c4-ml-fall-2021/ma
# Remove the variables with more than 80% missingness
require(finalfit)
            <- ff_glimpse(readability)$Continuous</pre>
missing
            <- which(as.numeric(missing_$missing_percent) > 80)
readability <- readability[,-flag_na]</pre>
# Write the recipe
require(recipes)
blueprint_readability <- recipe(x</pre>
                                       = readability,
                                 vars = colnames(readability),
                                 roles = c(rep('predictor',990),'outcome')) %>%
  step_zv(all_numeric()) %>%
  step_nzv(all_numeric()) %>%
  step_impute_mean(all_numeric()) %>%
  step_normalize(all_numeric_predictors()) %>%
  step_corr(all_numeric(),threshold=0.9)
```

```
# Train/Test Split
set.seed(10152021) # for reproducibility

loc     <- sample(1:nrow(readability), round(nrow(readability) * 0.9))
read_tr <- readability[loc, ]
read_te <- readability[-loc, ]</pre>
```

Prepare the data partitions for 10-fold cross validation.

Set the multiple cores for parallel processing.

```
require(doParallel)

ncores <- 10

cl <- makePSOCKcluster(ncores)

registerDoParallel(cl)</pre>
```

Step 1: Tune the number of trees

Now, we will fix the learning rate at 0.1 (shrinkage=0.1), interaction depth at 5 (interaction.depth=5), and minimum number of observations at 10 (n.minobsinnode = 10). We will do a grid search for number of trees from 1 to 1000 (n.trees = 1:1000). Note that I fix the bag fraction at 1 and pass it as an argument in the caret::train function because it is not allowed in the hyperparameter grid.

\$everything

user system elapsed 176.45 1.31 354.86

\$final

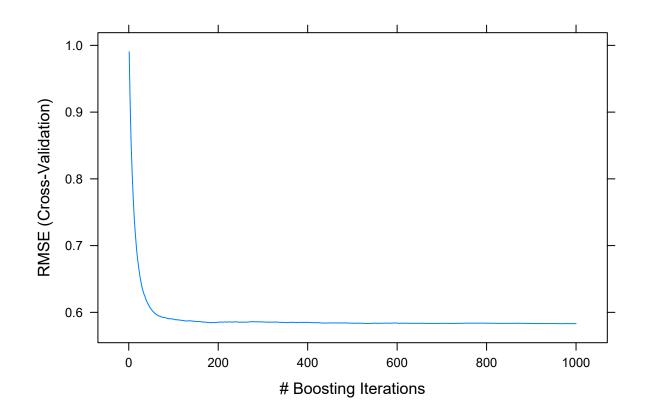
user system elapsed 156.3 0.0 156.3

\$prediction

[1] NA NA NA

This took about 6 minutes to run. We now look at the plot, and how the cross-validated RMSE changes as a function of number of trees.

```
plot(gbm1,type='1')
```



This indicates that there is not much improvement after 200 trees with these settings (this is just eyeballing, nothing specific about how to come up with this number). So, I will fix the number of trees to 200 for the next step.

Step 2: Tune the interaction depth and minimum number of observations

Now, we will fix the number of trees at 200 (n.trees = 200) and learning rate at 0.1 (shrinkage=0.1). Then, we will do a grid search by assigning values for the interaction depth from 1 to 15 and values for the minimum number of observations at 5, 10, 20, 30, 40, and 50. We still keep bag fraction as 1.

```
grid <- expand.grid(shrinkage</pre>
                                        = 0.1,
                     n.trees
                                        = 200,
                     interaction.depth = 1:15,
                                        = c(5,10,20,30,40,50))
                     n.minobsinnode
gbm2 <- caret::train(blueprint_readability,</pre>
                      data
                                = read_tr,
                      method
                                = 'gbm',
                      trControl = cv,
                      tuneGrid = grid,
                      bag.fraction = 1,
                      verbose = FALSE)
gbm2$times
```

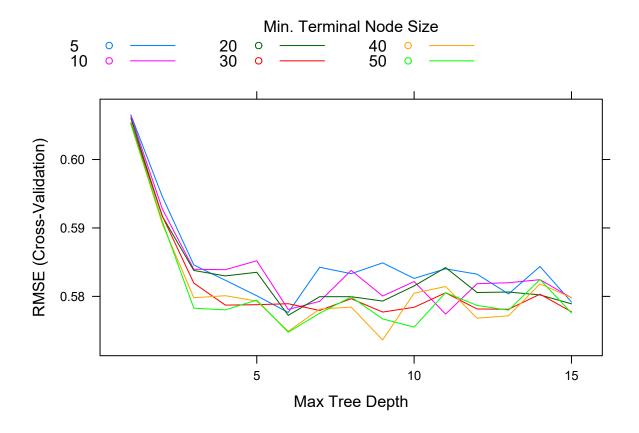
```
$everything
  user system elapsed
92.92 4.94 6202.95

$final
  user system elapsed
69.83 0.14 69.84

$prediction
[1] NA NA NA
```

This search took about 1 hour and 43 minutes. If we look at the cross-validates RMSE for all these 90 possible conditions, we see that the best result comes out when interaction depth is equal to 9 and minimum number of observations is equal to 40.

```
plot(gbm2,type='l')
```



```
gbm2$bestTune
   n.trees interaction.depth shrinkage n.minobsinnode
53
       200
                                    0.1
                                                     40
gbm3$results[which.min(gbm3$results$RMSE),]
     shrinkage interaction.depth n.minobsinnode n.trees
                                                            RMSE Rsquared
3377
          0.01
                                                     3377 0.5678
                                                                    0.701 0.4506
      RMSESD RsquaredSD
                          MAESD
3377 0.02724
                0.02495 0.02143
```

Step 3: Lower the learning rate and increase the number of trees

Now, we will fix the interaction depth at 9 (interaction.depth = 9) and minimum number of observations at 40 (n.minobsinnode = 40). We will lower the learning rate to 0.01 (shrinkage=0.01) and increase the number of trees to 5000 (n.trees = 1:5000) to explore if lower learning rate improves the performance.

\$everything

user system elapsed 839.83 6.74 2224.38

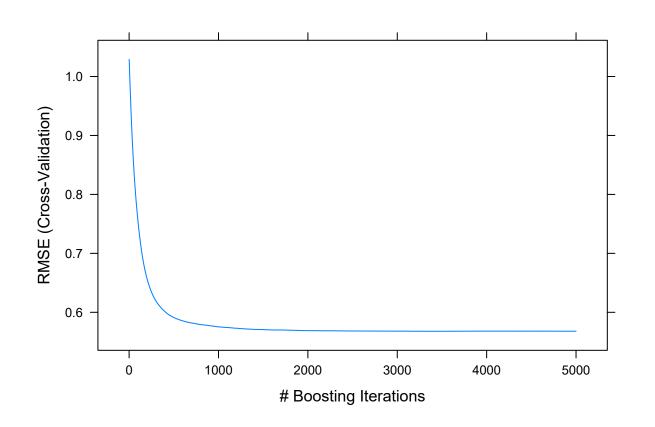
\$final

user system elapsed 818.95 0.85 819.30

${\tt \$prediction}$

[1] NA NA NA

plot(gbm3,type='1')



gbm3\$bestTune

```
n.trees interaction.depth shrinkage n.minobsinnode
3377 3377 9 0.01 40
gbm3$results[which.min(gbm3$results$RMSE),]
```

```
shrinkage interaction.depth n.minobsinnode n.trees RMSE Rsquared MAE 3377 0.01 9 40 3377 0.5678 0.701 0.4506 RMSESD RsquaredSD MAESD 3377 0.02724 0.02495 0.02143
```

This run took about another 37 minutes. The best performance was obtained with a model 3377 trees, and yielded an RMSE value of 0.5678. We can stop here, and decide that this is our final model. Or, we can play with bag.fraction and see we can squeeze a little bit more.

Step 4: Tune Bag Fraction

In order to play with the bag.fraction, we should write our own syntax as caret::train doesn allow it to be manipulated as a hyperparameter.

Notice that I fixed the values of shrinkage, n.trees,interaction.depth,n.minobsinnode at their optimal values. Then, I write a for loop to iterate over different values of bag.fraction from 0.1 to 1 with increments of 0.05. I save the model object from each iteration in a list object.

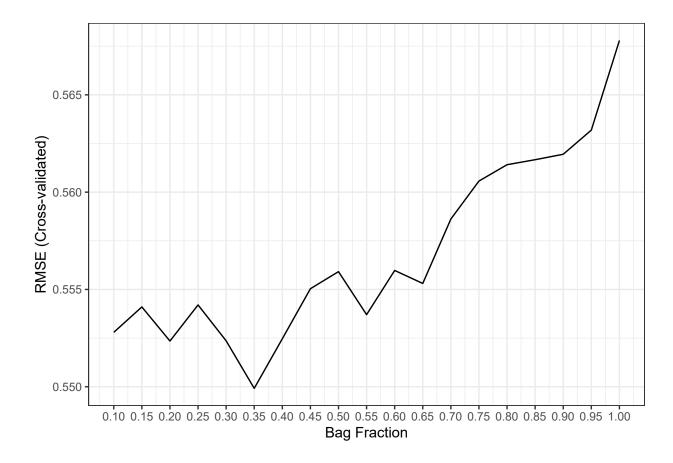
```
grid <- expand.grid(shrinkage</pre>
                                          = 0.01,
                                          = 3377.
                      interaction.depth = 9,
                      n.minobsinnode
                                         = 40)
bag.fr \leftarrow seq(0.1,1,.05)
my.models <- vector('list',length(bag.fr))</pre>
for(i in 1:length(bag.fr)){
  my.models[[i]] <- caret::train(blueprint_readability,</pre>
                                  data
                                            = read tr,
                                  method
                                             = 'gbm',
                                  trControl = cv,
                                  tuneGrid = grid,
                                  bag.fraction = bag.fr[i],
                                  verbose= FALSE)
}
```

This took about 8 hours to complete with 10 cores. Let's check if it improved the performance.

```
cv.rmse <- c()

for(i in 1:length(bag.fr)){
   cv.rmse[i] <- my.models[[i]]$results$RMSE
}</pre>
```

```
ggplot()+
  geom_line(aes(x=bag.fr,y=cv.rmse))+
  theme_bw()+
  xlab('Bag Fraction')+
  ylab('RMSE (Cross-validated)')+
  scale_x_continuous(breaks = bag.fr)
```



The best performance was obtained when bag.fr is equal to 0.35, so 35% of the observations randomly sampled at each iteration.

Finally, we can check the performance of the final model with these settings on the test dataset and compare it to other methods.

```
final.gbm <- my.models[[6]]

# Predictions from a Bagged tree model with 158 trees

predicted_te <- predict(final.gbm,read_te)

# MAE

mean(abs(read_te$target - predicted_te))</pre>
```

[1] 0.4332

```
# RMSE
sqrt(mean((read_te$target - predicted_te)^2))

[1] 0.538

# R-square
cor(read_te$target,predicted_te)^2
```

[1] 0.7244

	R-square	MAE	RMSE
Ridge Regression	0.727	0.435	0.536
Lasso Regression	0.725	0.434	0.538
Gradient Boosting	0.724	0.433	0.538
Random Forests	0.671	0.471	0.596
Bagged Trees	0.656	0.481	0.604
Linear Regression	0.644	0.522	0.644
KNN	0.623	0.500	0.629
Decision Tree	0.497	0.577	0.729

Predicting Recidivism Using Gradient Boosting Trees

The code below implements a similar strategy and demonstrates step by step how to fit a Gradient Boosting Tree model for the Recidivism dataset to predict recidivism in Year 2.

** Import the dataset, and and initial data preparation

```
# Import data
 recidivism <- read.csv('https://raw.githubusercontent.com/uo-datasci-specialization/c4-ml-fall-2021/m
# List of variable types in the dataset
  outcome <- c('Recidivism_Arrest_Year2')</pre>
  categorical <- c('Residence_PUMA',</pre>
                   'Prison_Offense',
                   'Age_at_Release',
                   'Supervision_Level_First',
                   'Education_Level',
                   'Prison_Years',
                   'Gender',
                   'Race',
                   'Gang_Affiliated',
                   'Prior_Arrest_Episodes_DVCharges',
                   'Prior_Arrest_Episodes_GunCharges',
                   'Prior_Conviction_Episodes_Viol',
                   'Prior_Conviction_Episodes_PPViolationCharges',
```

```
'Prior_Conviction_Episodes_DomesticViolenceCharges',
                   'Prior_Conviction_Episodes_GunCharges',
                   'Prior_Revocations_Parole',
                   'Prior_Revocations_Probation',
                   'Condition_MH_SA',
                   'Condition_Cog_Ed',
                   'Condition_Other',
                   'Violations_ElectronicMonitoring',
                   'Violations_Instruction',
                   'Violations FailToReport',
                   'Violations_MoveWithoutPermission',
                   'Employment Exempt')
            <- c('Supervision_Risk_Score_First',</pre>
 numeric
                 'Dependents',
                 'Prior_Arrest_Episodes_Felony',
                 'Prior_Arrest_Episodes_Misd',
                 'Prior_Arrest_Episodes_Violent',
                 'Prior_Arrest_Episodes_Property',
                 'Prior_Arrest_Episodes_Drug',
                 'Prior_Arrest_Episodes_PPViolationCharges',
                 'Prior_Conviction_Episodes_Felony',
                 'Prior_Conviction_Episodes_Misd',
                 'Prior_Conviction_Episodes_Prop',
                 'Prior_Conviction_Episodes_Drug',
                 'Delinquency_Reports',
                 'Program Attendances',
                 'Program_UnexcusedAbsences',
                 'Residence Changes',
                 'Avg_Days_per_DrugTest',
                 'Jobs_Per_Year')
             <- c('DrugTests_THC_Positive',</pre>
 props
                  'DrugTests_Cocaine_Positive',
                   'DrugTests_Meth_Positive',
                   'DrugTests_Other_Positive',
                   'Percent_Days_Employed')
# Convert all nominal, ordinal, and binary variables to factors
# Leave the rest as is
 for(i in categorical){
   recidivism[,i] <- as.factor(recidivism[,i])</pre>
 }
# For variables that represent proportions, add/substract a small number
# to Os/1s for logit transformation
 for(i in props){
   recidivism[,i] <- ifelse(recidivism[,i]==0,.0001,recidivism[,i])</pre>
   recidivism[,i] <- ifelse(recidivism[,i]==1,.9999,recidivism[,i])</pre>
```

```
}
# Blueprint for processing variables
 require(recipes)
 blueprint_recidivism <- recipe(x = recidivism,</pre>
                                 vars = c(categorical, numeric, props, outcome),
                                 roles = c(rep('predictor',48),'outcome')) %>%
   step_indicate_na(all_of(categorical),all_of(numeric),all_of(props)) %>%
   step zv(all numeric()) %>%
   step_impute_mean(all_of(numeric),all_of(props)) %>%
   step_impute_mode(all_of(categorical)) %>%
   step_logit(all_of(props)) %>%
   step_ns(all_of(numeric),all_of(props),deg_free=3) %>%
   step_normalize(paste0(numeric,'_ns_1'),
                   paste0(numeric,'_ns_2'),
                   pasteO(numeric, '_ns_3'),
                   paste0(props,'_ns_1'),
                   paste0(props,'_ns_2'),
                   paste0(props,'_ns_3')) %>%
   step_dummy(all_of(categorical),one_hot=TRUE) %>%
    step_num2factor(Recidivism_Arrest_Year2,
                    transform = function(x) x + 1,
                    levels=c('No','Yes'))
```

Train/Test Split, and Cross-validation Settings

```
# Train/Test Split
loc <- which(recidivism$Training_Sample==1)

recidivism_tr <- recidivism[loc, ]

recidivism_te <- recidivism[-loc, ]

# Cross validation settings

set.seed(10302021) # for reproducibility

recidivism_tr = recidivism_tr[sample(nrow(recidivism_tr)),]

# Create row indices for 10 folds with equal size

folds = cut(seq(1,nrow(recidivism_tr)),breaks=10,labels=FALSE)

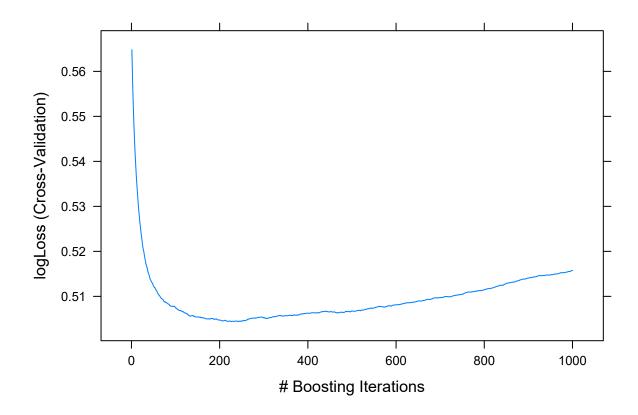
# Create the list object with each element representing
# the row indices for each fold

my.indices <- vector('list',10)
for(i in 1:10){
    my.indices[[i]] <- which(folds!=i)
}</pre>
```

Initial model fit to tune the number of trees

We fix the learning rate at 0.1 (shrinkage=0.1), interaction depth at 5 (interaction.depth=5), and minimum number of observations at 10 (n.minobsinnode = 10). We do a grid search for optimal number of trees from 1 to 1000 (n.trees = 1:1000).

```
grid <- expand.grid(shrinkage</pre>
                                    = 0.1,
                                    = 1:1000,
                   interaction.depth = 5,
                   n.minobsinnode = 10)
gbm1 <- caret::train(blueprint_recidivism,</pre>
                            = recidivism_tr,
                    data
                               = 'gbm',
                    method
                    trControl = cv,
                    tuneGrid = grid,
                    bag.fraction = 1,
                    metric = 'logLoss')
plot(gbm1,type='l')
gbm1$bestTune
```



```
n.trees interaction.depth shrinkage n.minobsinnode 242 242 5 0.1 10
```

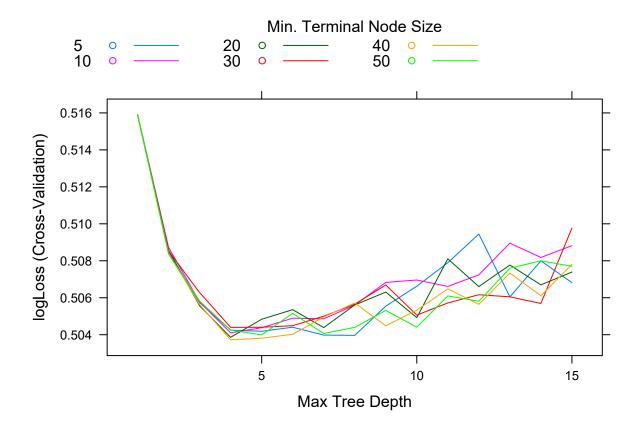
This indicates that 242 trees is the optimal at the initial search.

Tune the interaction depth and minimum number of observations

We fix the number of trees at 242 (n.trees = 242) and learning rate at 0.1 (shrinkage=0.1). Then, we do a grid search by assigning values for the interaction depth from 1 to 15 and values for the minimum number of observations at 5, 10, 20, 30, 40, and 50.

```
grid <- expand.grid(shrinkage</pre>
                                         = 0.1,
                                         = 242,
                     interaction.depth = 1:15,
                                         = c(5,10,20,30,40,50))
                     n.minobsinnode
gbm2 <- caret::train(blueprint_recidivism,</pre>
                       data
                                     = recidivism_tr,
                      method
                                     = 'gbm',
                       trControl
                                     = cv,
                       tuneGrid
                                     = grid,
                      bag.fraction = 1,
                                     = 'logLoss')
                      metric
```

```
plot(gbm2)
gbm2$bestTune
```



```
n.trees interaction.depth shrinkage n.minobsinnode 23 \quad 242 \quad 4 \quad 0.1 \quad 40
```

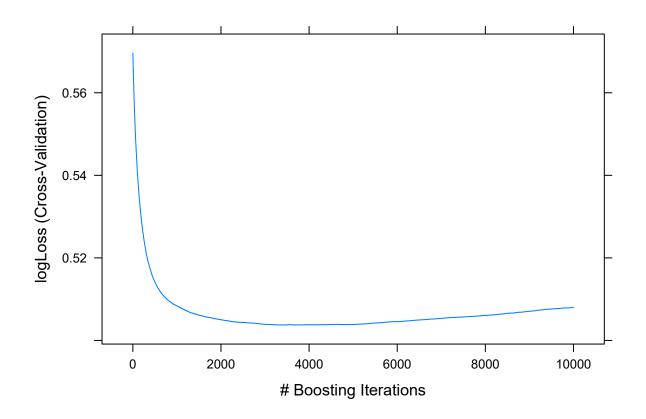
The search indicates that the best performance is obtained when the interaction depth is equal to 4 and minimum number of observations is equal to 40.

Lower the learning rate and increase the number of trees

We fix the interaction depth at 4 (interaction.depth = 4) and minimum number of observations at 40 (n.minobsinnode = 40). We will lower the learning rate to 0.01 (shrinkage=0.01) and increase the number of trees to 10000 (n.trees = 1:10000) to explore if lower learning rate improves the performance.

```
trControl = cv,
tuneGrid = grid,
bag.fraction = 1,
metric = 'logLoss')

plot(gbm3,type='l')
gbm3$bestTune
```



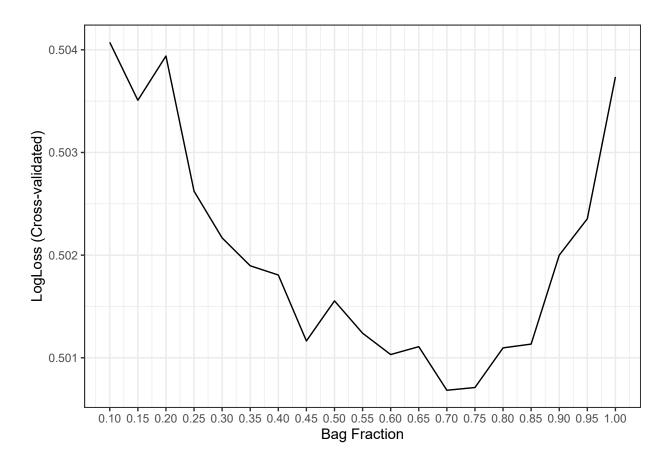
```
n.trees interaction.depth shrinkage n.minobsinnode 3397 \qquad 3397 \qquad 4 \qquad 0.01 \qquad 40
```

Tune the bag fraction

```
cv.LogL <- c()

for(i in 1:length(bag.fr)){
   cv.LogL[i] <- my.models[[i]]$results$logLoss
}

ggplot()+
   geom_line(aes(x=bag.fr,y=cv.LogL))+
   theme_bw()+
   xlab('Bag Fraction')+
   ylab('LogLoss (Cross-validated)')+
   scale_x_continuous(breaks = bag.fr)</pre>
```



The best result is obtained when the bag fraction is 0.7. So, we will proceed with that as our final model.

Final Predictions

```
final.gbm <- my.models[[13]]</pre>
# Predict the probabilities for the observations in the test dataset
predicted_te <- predict(final.gbm, recidivism_te, type='prob')</pre>
head(predicted_te)
      No
1 0.9321 0.06793
2 0.5283 0.47173
3 0.7162 0.28380
4 0.5000 0.50001
5 0.7985 0.20145
6 0.8021 0.19785
# Compute the AUC
require(cutpointr)
cut.obj <- cutpointr(x = predicted_te$Yes,</pre>
                     class = recidivism_te$Recidivism_Arrest_Year2)
auc(cut.obj)
[1] 0.7364
# Confusion matrix assuming the threshold is 0.5
pred_class <- ifelse(predicted_te$Yes>.5,1,0)
confusion <- table(recidivism_te$Recidivism_Arrest_Year2,pred_class)</pre>
confusion
  pred_class
  0 3946 200
  1 1098 216
# True Negative Rate
confusion[1,1]/(confusion[1,1]+confusion[1,2])
[1] 0.9518
# False Positive Rate
confusion[1,2]/(confusion[1,1]+confusion[1,2])
[1] 0.04824
```

True Positive Rate

confusion[2,2]/(confusion[2,1]+confusion[2,2])

[1] 0.1644

Precision

confusion[2,2]/(confusion[1,2]+confusion[2,2])

[1] 0.5192

Comparison of Results

	-LL	AUC	ACC	TPR	TNR	FPR	PRE
Gradient Boosted Trees	0.5007	0.7364	0.762	0.164	0.952	0.048	0.519
Random Forests	0.5097	0.7242	0.762	0.126	0.963	0.037	0.519
Bagged Trees	0.5088	0.7225	0.758	0.130	0.957	0.043	0.489
Logistic Regression with Lasso Penalty	0.5090	0.7200	0.754	0.127	0.952	0.048	0.458
Logistic Regression with Elastic Net	0.5091	0.7200	0.753	0.127	0.952	0.048	0.456
Logistic Regression	0.5096	0.7192	0.755	0.142	0.949	0.051	0.471
Logistic Regression with Ridge Penalty	0.5111	0.7181	0.754	0.123	0.954	0.046	0.461
Decision Tree	0.5522	0.6521	0.752	0.089	0.962	0.038	0.427