

Algorithmics	Student information	Date	Number of session
	UO: 295180	26/02/24	3
	Surname: Orviz Viesca		
	Name: Mario		

Activity 1. Direct exchange or Bubble algorithm

Using **Vector.java** class, we can create an ordered vector, a vector in reverse order, and a randomize vector. The **Bubble.java** class implements the bubble sort algorithm needed for sort this vector. Finally with the **BubbleTimes.java** we can increase the size of the problem and the times that it's executed.

N	t ordered	t reverse	t random
10000	627 ms	1942 ms	1422 ms
20000	2544 ms	7986 ms	5827 ms
40000	9827 ms	31729 ms	23609 ms
80000	41002 ms	Oot	Oot
160000	Oot	Oot	Oot

The times obtained matches with what was expected because the Bubble sort algorithm has a time complexity of $O(n^2)$

Activity 2. Selection algorithm

N	t ordered	t reverse	t random
10000	475 ms	538 ms	663 ms
20000	1994 ms	3146 ms	2102 ms
40000	8403 ms	9302 ms	9675 ms
80000	35484 ms	38448 ms	36442 ms
160000	Oot	Oot	Oot

It can be seen that, although the complexity is the same as in the Bubble algorithm, the Selection algorithm works better for unordered vectors than the bubble one

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Activity 3. Insertion algorithm

N	t ordered	t reverse	t random
10000	LoR	1167 ms	382 ms
20000	LoR	3862 ms	1584 ms
40000	LoR	13083 ms	6008 ms
80000	LoR	54204 ms	25926 ms
160000	LoR	Oot	Oot
320000	LoR	Oot	Oot
640000	LoR	Oot	Oot
1280000	LoR	Oot	Oot
2560000	80 ms	Oot	Oot
5120000	120 ms	Oot	Oot
10240000	236 ms	Oot	Oot
20480000	468 ms	Oot	Oot
40960000	936 ms	Oot	Oot
81920000	1883 ms	Oot	Oot

As it can be seen, the performance of the Insertion algorithm is really fast when the array is already sorted. It has a time complexity of $O(n)$ for sorted arrays because it only needs to iterate the array once, without swapping any value and inserting all the values into the sorted array in order.

Activity 4. Quicksort algorithm

N	t ordered	t reverse	t random
250000	71 ms	75 ms	145 ms
500000	150 ms	148 ms	294 ms

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1000000	301 ms	314 ms	636 ms
2000000	622 ms	637 ms	1399 ms
4000000	1185 ms	1276 ms	3194 ms
8000000	2365 ms	2680 ms	7729 ms
16000000	5103 ms	5383 ms	20487 ms

As it can be seen, the quicksort algorithm is really fast, also for big size arrays. The fact that we can obtain better performance on the ordered and reverse algorithm is because our quicksort algorithm uses the median of three approach to obtain the pivot, so it always takes the best one.

If we introduce a random vector of that size in the bubble, selection and insertion algorithm, we will need to wait so more time:

$O(n) \rightarrow 20487 \text{ ms}$

$O(n^2) \rightarrow t_2$

Therefore, t_2 in milliseconds will be $t_2 = (20487 * 16,000,000^2) / 16,000,000 = 327.792.000.000$. Therefore, those algorithms will take over 3793 days to end the execution

Activity 5. Quicksort + Insertion algorithm

N	t random
Quicksort	20164 ms
Quicksort+Insertion (k = 5)	21991 ms
Quicksort+Insertion (k = 10)	21813 ms
Quicksort+Insertion (k = 20)	20616 ms
Quicksort+Insertion (k = 30)	21183 ms
Quicksort+Insertion (k = 40)	20956 ms
Quicksort+Insertion (k = 50)	20407 ms

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Quicksort+Insertion (k = 100)	18811 ms
Quicksort+Insertion (k = 200)	15703 ms
Quicksort+Insertion (k = 500)	26015 ms
Quicksort+Insertion (k = 1000)	55302 ms

As it can be seen, I'm obtaining the best performance when $k = 200$. In this case, we're taking advantage of the Insertion method, that has the best performance with ordered arrays, and iterating less on the quicksort, so we gain time.