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$$V_{DC} = I_{DC}R \quad \text{OR} \quad v_{(t)} = i_{(t)}R$$

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$$p_{(t)} = v_{(t)} i_{(t)}$$

$$p(t) = v(t) \cdot i(t)$$

$$v_{L(t)} = V_{L(pk)} \cos(1000\pi t) \quad \text{and} \quad i_{L(t)} = V_{L(pk)} \cos(1000\pi t)/R$$

$$v_L(t) = V_{L(pk)} \cos(1000\pi t) \quad \text{and} \quad i_L(t) = \frac{V_{L(pk)} \cos(1000\pi t)}{R}$$

$$p_{L(t)} = \frac{V_{L(pk)}^2}{R} \cos^2(1000\pi t) = \frac{V_{L(pk)}^2}{2R} [\cos(2000\pi t) + 1]$$

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$$P = \frac{1}{T_L} \int_0^{T_L} p_{L(t)} dt = \frac{1}{T_L} \int_0^{T_L} v_{(t)} i_{(t)} dt = V_{L(pk)}^2 / 2R$$

$$P = \frac{1}{T_L} \int_0^{T_L} p_L(t) dt = \frac{1}{T_L} \int_0^{T_L} v(t) \cdot i(t) dt = \frac{V_{L(pk)}^2}{2R}$$

$$\begin{aligned}
P &= \frac{1}{T_L} \int_0^{T_L} p_{L(t)} dt = \frac{1}{T_L} \int_0^{T_L} v_{(t)} i_{(t)} dt = \frac{1}{RT_L} \int_0^{T_L} v_{(t)}^2 dt \stackrel{\text{OR}}{=} \frac{R}{T_L} \int_0^{T_L} i_{(t)}^2 dt \\
P &= \frac{1}{T_L} \int_0^{T_L} p_L(t) dt = \frac{1}{T_L} \int_0^{T_L} v(t) \cdot i(t) dt = \frac{1}{RT_L} \int_0^{T_L} v^2(t) dt \stackrel{\text{OR}}{=} \frac{R}{T_L} \int_0^{T_L} i^2(t) dt
\end{aligned}$$

$$\begin{aligned}
V_{RMS}^2 &= \frac{1}{T_L} \int_0^{T_L} v_{(t)}^2 dt \quad \text{and} \quad I_{RMS}^2 = \frac{1}{T_L} \int_0^{T_L} i_{(t)}^2 dt \\
V_{\text{RMS}}^2 &= \frac{1}{T_L} \int_0^{T_L} v^2(t) dt \quad \text{and} \quad I_{\text{RMS}}^2 = \frac{1}{T_L} \int_0^{T_L} i^2(t) dt
\end{aligned}$$

$$\begin{aligned}
V_{RMS} &= \sqrt{\frac{1}{T_L} \int_0^{T_L} V_{L(pk)}^2 \cos^2(\omega_L t) dt} = \sqrt{\frac{1}{T_L} \int_0^{T_L} \frac{V_{L(pk)}^2}{2} [\cos(2\omega_L t) + 1] dt} = \frac{V_{L(pk)}}{\sqrt{2}} \\
V_{\text{RMS}} &= \sqrt{\frac{1}{T_L} \int_0^{T_L} V_{L(\text{pk})}^2 \cos^2(\omega_L t) dt} = \sqrt{\frac{1}{T_L} \int_0^{T_L} \frac{V_{L(\text{pk})}^2}{2} [\cos(2\omega_L t) + 1] dt} = \frac{V_{L(\text{pk})}}{\sqrt{2}}
\end{aligned}$$

$$\begin{aligned}
|S| &= V_{RMS} I_{RMS} \\
|S| &= V_{\text{RMS}} \cdot I_{\text{RMS}}
\end{aligned}$$

$$\begin{aligned}
p.f. &= \frac{P}{|S|} \\
p.f. &= \frac{P}{|S|}
\end{aligned}$$

$$\begin{aligned}
Q &= \sqrt{|S|^2 - P^2} \\
Q &= \sqrt{|S|^2 - P^2}
\end{aligned}$$

$$\begin{aligned} S &= P + jQ \\ S &= P + jQ \end{aligned}$$

$$v_{L(t)} = V_{L(pk)} \cos(1000\pi t) \quad \text{and} \quad i_{L(t)} = V_{L(pk)} \cos(1000\pi t - \pi/2)/\omega_L L$$

$$v_L(t) = V_{L(\text{pk})} \cos(1000\pi t) \quad \text{and} \quad i_L(t) = \frac{V_{L(\text{pk})} \cos(1000\pi t - \frac{\pi}{2})}{\omega_L L}$$

$$\begin{aligned} p_{L(t)} &= \frac{V_{L(pk)}^2}{\omega_L L} \cos(1000\pi t) \cos(1000\pi t - \pi/2) = \frac{V_{L(pk)}^2}{2\omega_L L} \sin(2000\pi t) \\ p_L(t) &= \frac{V_{L(\text{pk})}^2}{\omega_L L} \cos(1000\pi t) \cos(1000\pi t - \frac{\pi}{2}) = \frac{V_{L(\text{pk})}^2}{2\omega_L L} \sin(2000\pi t) \end{aligned}$$

$$\begin{aligned} P &= \frac{1}{T_L} \int_0^{T_L} p_{L(t)} dt = 0 \quad \text{and} \quad Q = \frac{V_{L(pk)}^2}{2\omega_L L} = \frac{V_{L(\text{RMS})}^2}{\omega_L L} \\ P &= \frac{1}{T_L} \int_0^{T_L} p_L(t) dt = 0 \quad \text{and} \quad Q = \frac{V_{L(\text{pk})}^2}{2\omega_L L} = \frac{V_{L(\text{RMS})}^2}{\omega_L L} \end{aligned}$$

$$\begin{aligned} V_{pk} &= \sqrt{2}V_{RMS} \quad \text{and} \quad I_{pk} = \sqrt{2}I_{RMS} \\ V_{\text{pk}} &= \sqrt{2}V_{\text{RMS}} \quad \text{and} \quad I_{\text{pk}} = \sqrt{2}I_{\text{RMS}} \end{aligned}$$

$$\begin{aligned} P &= V_{RMS} I_{RMS} = I_{RMS}^2 R = V_{RMS}^2 / R \\ P &= V_{\text{RMS}} I_{\text{RMS}} = I_{\text{RMS}}^2 R = \frac{V_{\text{RMS}}^2}{R} \end{aligned}$$

$$v_{vs(t)} = v_{L(t)} R_b / (R_a + R_b)$$

$$v_{vs} = v_L(t) \frac{R_b}{R_a + R_b}$$

$$V_{vs(pk-pk)} = V_{L(pk-pk)} R_b / (R_a + R_b) \Rightarrow 1 \geq 15.4 \times 2\sqrt{2} R_b / (R_a + R_b) \Rightarrow R_a \geq 41.4 R_b$$

$$V_{vs(pk-pk)} = V_{L(pk-pk)} \frac{R_b}{R_a + R_b} \Rightarrow 1 \geq 15.4 \times 2\sqrt{2} \frac{R_b}{R_a + R_b} \Rightarrow R_a \geq 41.4 R_b$$

$$P_{vs-loss} = V_{L(RMS)}^2 / (R_a + R_b)$$

$$P_{vs-loss} = \frac{V_{L(RMS)}^2}{R_a + R_b}$$

$$v_{is(t)} = i_{L(t)} R_s$$

$$v_{is} = i_L(t) \cdot R_s$$

$$P_{is-loss} = I_{L(RMS)}^2 R_s \Rightarrow 0.05 \geq 0.55^2 R_s \Rightarrow R_s \leq 165 m\Omega$$

$$P_{is-loss} = I_{L(RMS)}^2 \cdot R_s \Rightarrow 0.05 \geq 0.55^2 R_s \Rightarrow R_s \leq 165 m\Omega$$

$$V_{is(pk-pk)-highest} = 0.55 \times 2\sqrt{2} \times 0.16 \approx 250 mV$$

$$V_{is(pk-pk)-highest} = 0.55 \times 2\sqrt{2} \times 0.16 \approx 250 mV$$

$$V_{is(pk-pk)-lowest} = 0.16 \times 2\sqrt{2} \times 0.16 \approx 72mV$$

$$V_{is(pk-pk)-lowest} = 0.16 \times 2\sqrt{2} \times 0.16 \approx 72 \text{ mV}$$

$$R_{dc} = \frac{\rho l}{A}$$

$$R_{dc} = \frac{\rho \cdot l}{A}$$

$$C = \frac{\epsilon_r \epsilon_0 A}{d}$$

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$$\text{Time per Bit} = \frac{1}{\text{Baud Rate}}$$

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$$\text{Data Rate} = \frac{\text{Data Bits per Frame}}{\text{Total Bits per Frame}} \times \text{Baud Rate}$$

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$$\text{Transmission Time} = \frac{\text{Data Bits to Transmit}}{\text{Data Rate}}$$

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$$\text{Baud Rate} = \frac{f_{osc}}{16 \times (UBRR0 + 1)} \quad \text{or} \quad UBRR0 = \frac{f_{osc}}{(\text{Baud Rate}) \times 16} - 1$$

$$\text{Baud Rate} = \frac{f_{osc}}{16 \times (\text{UBRR0} + 1)} \quad \text{or} \quad \text{UBRR0} = \frac{f_{osc}}{(\text{Baud Rate}) \times 16} - 1$$

$$t_{sample} = \frac{1}{f_{sample}}$$

$$t_{\text{sample}} = \frac{1}{f_{\text{sample}}}$$

$$f_{sample(max)} = \frac{1}{t_{acquisition(min)} + t_{conversion(min)}}$$

$$f_{\text{sample(max)}} = \frac{1}{t_{\text{acquisition(min)}} + t_{\text{conversion(min)}}}$$

$$V_{step} = \frac{V_{ref}}{2^{resolution}}$$

$$V_{\text{step}} = \frac{V_{\text{ref}}}{2^{\text{resolution}}}$$

$$\tau = (R_{signal} + R_{sample})C_{sample}$$

$$\tau = (R_{\text{signal}} + R_{\text{sample}})C_{\text{sample}}$$

$$V_{\text{Absolute Error}} = V_{\text{step}} \times LSB_{\text{Absolute Error}}$$

$$V_{\text{Absolute Error}} = V_{\text{step}} \times \text{LSB}_{\text{Absolute Error}}$$

$$V_{\text{ADC}} - V_{\text{Absolute Error}} \leq V_{\text{Actual}} \leq V_{\text{ADC}} + V_{\text{Absolute Error}}$$

$$V_{\text{ADC}} - V_{\text{Absolute Error}} \leq V_{\text{Actual}} \leq V_{\text{ADC}} + V_{\text{Absolute Error}}$$

$$V_{vf} = G_{vs}G_{vo}V_{AC} + V_{off}$$

$$V_{vf} = G_{vs}G_{vo}V_{AC} + V_{off}$$

$$V_{if} = G_{is}G_{io}I_L + V_{off}$$

$$V_{if} = G_{is}G_{io}I_L + V_{off}$$

$$V_{AC}[i] = (ADC0Value[i] \times 5/1024 - V_{off}) / (G_{vs}G_{vo})$$

$$V_{AC}[i] = \frac{\text{ADC0Value}[i] \times \frac{5}{1024} - V_{off}}{G_{vs}G_{vo}}$$

$$I_L[i] = (ADC1Value[i] \times 5/1024 - V_{off}) / (G_{is}G_{io})$$

$$I_L[i] = \frac{\text{ADC1Value}[i] \times \frac{5}{1024} - V_{off}}{G_{is}G_{io}}$$

$$RMS = \frac{Peak}{\sqrt{2}}$$

$$\text{RMS} = \frac{\text{Peak}}{\sqrt{2}}$$

$$V_{AC_{rms}} = \sqrt{\frac{1}{T_p} \int_0^{T_p} V_{AC}^2 dt} \quad \text{OR} \quad I_{L_{rms}} = \sqrt{\frac{1}{T_p} \int_0^{T_p} I_L^2 dt}$$

$$V_{AC(RMS)} = \sqrt{\frac{1}{T_p} \int_0^{T_p} V_{AC}^2 dt} \quad \text{or} \quad I_{L(RMS)} = \sqrt{\frac{1}{T_p} \int_0^{T_p} I_L^2 dt}$$

$$V_{AC_{rms}}^2 = \frac{1}{N\Delta t_{sample}} \sum_{i=0}^{N-1} V_{AC}^2[i] \Delta t_{sample} \quad \text{OR} \quad I_{L_{rms}}^2 = \frac{1}{N\Delta t_{sample}} \sum_{i=0}^{N-1} I_L^2[i] \Delta t_{sample}$$

$$V_{AC(RMS)}^2 = \frac{1}{N\Delta t_{sample}} \sum_{i=0}^{N-1} V_{AC}^2[i] \cdot \Delta t_{sample} \quad \text{or} \quad I_{L(RMS)}^2 = \frac{1}{N\Delta t_{sample}} \sum_{i=0}^{N-1} I_L^2[i] \cdot \Delta t_{sample}$$

$$P = V_{AC_{rms}} I_{L_{rms}} \cos(\theta)$$

$$P = V_{AC(RMS)} I_{L(RMS)} \cos(\theta)$$

$$P = \frac{1}{T_p} \int_0^{T_p} V_{AC} I_L dt$$

$$P = \frac{1}{T_p} \int_0^{T_p} V_{AC} I_L dt$$

$$P = \frac{1}{N\Delta t_{sample}} \sum_{i=0}^{N-1} V_{AC}[i] I_L[i] \Delta t_{sample} = \frac{1}{N} \sum_{i=0}^{N-1} V_{AC}[i] I_L[i]$$

$$P = \frac{1}{N\Delta t_{sample}} \sum_{i=0}^{N-1} (V_{AC}[i] \cdot I_L[i] \cdot \Delta t_{sample}) = \frac{1}{N} \sum_{i=0}^{N-1} (V_{AC}[i] \cdot I_L[i])$$

$$\bar{V}_{AC}[i] = (V_{AC}[i] + V_{AC}[i+1]) / 2$$

$$\bar{V}_{AC}[i] = \frac{V_{AC}[i] + V_{AC}[i+1]}{2}$$

$$\begin{aligned}\bar{I}_L[i] &= \left(I_L[i-1] + I_L[i] \right) / 2 \\ \bar{I}_{\text{L}}[i] &= \frac{I_{\text{L}}[i-1] + I_{\text{L}}[i]}{2}\end{aligned}$$

$$\begin{aligned}P &= \frac{1}{2N} \sum_{i=0}^{N-1} \left[V_{AC}[i] \bar{I}_L[i] + \bar{V}_{AC}[i] I_L[i] \right] \\ P &= \frac{1}{2N} \sum_{i=0}^{N-1} \left[V_{\text{AC}}[i] \cdot \bar{I}_{\text{L}}[i] + \bar{V}_{\text{AC}}[i] \cdot I_{\text{L}}[i] \right]\end{aligned}$$

$$\begin{aligned}T_{\text{system_clk}} &= \frac{1}{f_{\text{system_clk}}} \\ T_{\text{system_clk}} &= \frac{1}{f_{\text{system_clk}}}\end{aligned}$$

$$\begin{aligned}T_{\text{cpu_clk}} &= \frac{1}{f_{\text{cpu_clk}}} \\ T_{\text{cpu_clk}} &= \frac{1}{f_{\text{cpu_clk}}}\end{aligned}$$

$$\begin{aligned}f_{\text{timer_clk}} &= \frac{f_{\text{system_clk}}}{\text{Prescaler}} \\ f_{\text{timer_clk}} &= \frac{f_{\text{system_clk}}}{\text{Prescaler}}\end{aligned}$$

$$\begin{aligned}0 \leqslant \text{count} &< 2^{\text{bits}} \\ 0 \leqslant \text{count} &< 2^{\text{bits}}\end{aligned}$$

$$\text{Resolution} = \frac{1}{f_{\text{timer_clk}}}$$

$$\text{Resolution} = \frac{1}{f_{\text{timer_clk}}}$$

$$\text{Range} = \text{Resolution} \times (2^{\text{bits}} - 1)$$

$$\text{Range} = \text{Resolution} \times (2^{\text{bits}} - 1)$$

$$\text{Period} = \text{Resolution} \times (\text{Top} + 1)$$

$$\text{Period} = \text{Resolution} \times (\text{Top} + 1)$$

$$T_p = T_{on} + T_{off}$$

$$T_p = T_{on} + T_{off}$$

$$V_{DC} = V_{\text{supply}} \times T_{on}/T_p = DV_{\text{supply}}$$

$$V_{DC} = V_{\text{supply}} \times \frac{T_{on}}{T_p} = D \cdot V_{\text{supply}}$$

$$T_p = \text{Resolution} \times (\text{Top} + 1) = (\text{Top} + 1) / f_{\text{timer_clk}}$$

$$T_p = \text{Resolution} \times (\text{Top} + 1) = \frac{\text{Top} + 1}{f_{\text{timer_clk}}}$$

$$T_{on} = \text{Resolution} \times (\text{Compare} + 1) = (\text{Compare} + 1) / f_{\text{timer_clk}}$$

$$T_{on} = \text{Resolution} \times (\text{Compare} + 1) = \frac{\text{Compare} + 1}{f_{\text{timer_clk}}}$$

$$\begin{aligned} V_{DC} &= I_{DC}R \\ V_{\text{DC}} &= I_{\text{DC}}R \end{aligned}$$

$$\begin{aligned} v_{(t)} &= i_{(t)}R \\ v(t) &= i(t)R \end{aligned}$$

$$\begin{aligned} \bar{V} &= \bar{I}R \\ \bar{V} &= \bar{I}R \end{aligned}$$

$$\begin{aligned} v_{(t)} &= i_{(t)}R \\ v(t) &= i(t)R \end{aligned}$$

$$\begin{aligned} V_{(s)} &= I_{(s)}R \\ V(s) &= I(s)R \end{aligned}$$

$$\begin{aligned} v_{(t)} &= L \frac{di_{(t)}}{dt} \\ v(t) &= L \frac{di(t)}{dt} \end{aligned}$$

$$\begin{aligned} \bar{V} &= jX_L\bar{I} = j\omega L\bar{I} \\ \bar{V} &= jX_L\bar{I} = j\omega L\bar{I} \end{aligned}$$

$$\begin{aligned} v_{(t)} &= L \frac{di_{(t)}}{dt} \\ v(t) &= L \frac{di(t)}{dt} \end{aligned}$$

$$\begin{aligned} V_{(s)} &= sLI_{(s)} \\ V(s) &= sLI(s) \end{aligned}$$

$$\begin{aligned} i_{(t)} &= C \frac{dv_{(t)}}{dt} \\ i(t) &= C \frac{dv(t)}{dt} \end{aligned}$$

$$\begin{aligned} \bar{V} &= jX_C\bar{I} = \bar{I}/j\omega C \\ \bar{V} &= jX_C\bar{I} = \frac{\bar{I}}{j\omega C} \end{aligned}$$

$$\begin{aligned} i_{(t)} &= C \frac{dv_{(t)}}{dt} \\ i(t) &= C \frac{dv(t)}{dt} \end{aligned}$$

$$\begin{aligned} V_{(s)} &= I_{(s)} / sC \\ V(s) &= \frac{I(s)}{sC} \end{aligned}$$

$$\begin{aligned} I_{in} - I_1 - I_2 &= 0 \\ I_{in} - I_1 - I_2 &= 0 \end{aligned}$$

$$\begin{aligned} V_{in} - V_1 - V_3 &= 0 \Rightarrow V_{in} = I_1 R_1 + (I_1 + I_2) R_3 \\ V_{in} - V_1 - V_3 &= 0 \Rightarrow V_{in} = I_1 R_1 + (I_1 + I_2) R_3 \end{aligned}$$

$$\begin{aligned} V_1 - V_2 &= 0 \Rightarrow I_1 R_1 = I_2 R_2 \\ V_1 - V_2 &= 0 \Rightarrow I_1 R_1 = I_2 R_2 \end{aligned}$$

$$\begin{aligned} I_1 &= I_2 = 0.5A \quad \& \quad I_{in} = 1A \\ I_1 &= I_2 = 0.5 \text{ A} \quad \& \quad I_{in} = 1 \text{ A} \end{aligned}$$

R_1 , ensures the voltage at PB7 is pulled to 5V (i.e. VCC supplied to the MCU) when the push-button is released. The filter capacitor, ' C_1 ', is used for debouncing. When the push-button is pressed it creates 0V at PB7, when released PB7 will be 5V. LED is connected to PB5 through a current limiting resistor, ' R_2 '. Generating 5V at PB5 will create a current to flow turning-on the LED (i.e. ' $I_{LED} = (5 - V_f) / R_2$ ' where ' $V_f \approx 2V$

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$$\begin{aligned} T_{system_clk} \\ T_{\text{system_clk}} \end{aligned}$$