Normal form of your dynamical system

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6:16am, September 8, 2014

Specified dynamical system

$$\dot{x}_1 = \varepsilon^2 (-x_1^3 + x_1) + \varepsilon y_1 a$$
$$\dot{y}_1 = \varepsilon (-\frac{d y_1}{d t} y_1^2 + w_1 y_1^2 \sigma) + w_1 \sigma - y_1$$

Time dependent coordinate transform

$$\begin{split} y_1 &= \varepsilon^2 (7/8e^{3t} \star w_1 \, Y_1^4 \sigma + 9/4e^t \star w_1 \, Y_1^4 \sigma + 25/8e^{-1t} \star w_1 \, Y_1^4 \sigma + 5/8Y_1^5) \, + \\ \varepsilon (-3/2e^t \star w_1 \, Y_1^2 \sigma - 3/2e^{-1t} \star w_1 \, Y_1^2 \sigma - 1/2Y_1^3) + e^{-1t} \star w_1 \, \sigma + Y_1 \\ x_1 &= \varepsilon^2 (-e^{2t} \star w_1 \, Y_1^2 a \sigma + 3/2e^t \star w_1 \, Y_1^2 a \sigma + 1/2e^{-1t} \star w_1 \, Y_1^2 a \sigma + \\ 1/6Y_1^3 a) + \varepsilon (-e^{-1t} \star w_1 \, a \sigma - Y_1 a) + X_1 \end{split}$$

Result normal form DEs

$$\dot{Y}_1 = 3\varepsilon e^{-1t} \star w_1 \, w_1 Y_1 \sigma^2 - Y_1$$
$$\dot{X}_1 = \varepsilon^3 (3w_1 X_1^2 a\sigma - w_1 a\sigma) + \varepsilon^2 (-X_1^3 + X_1) + \varepsilon w_1 a\sigma$$