Normal form of your dynamical system

A. J. Roberts, University of Adelaide http://orcid.org/0000-0001-8930-1552

8:17am, April 18, 2021

Throughout and generally: the lowest order, most important, terms are near the end of each expression.

off echo;

Specified dynamical system

$$\dot{x}_1 = -\varepsilon x_1 y_1$$

$$\dot{y}_1 = \sigma w_1 + \varepsilon (x_1^2 - 2y_1^2) - y_1$$
off echo;

Time dependent coordinate transform

$$y_1 = 4\sigma\varepsilon e^{-1t} \star w_1 Y_1 + \sigma e^{-1t} \star w_1 + \varepsilon (X_1^2 + 2Y_1^2) + Y_1$$

 $x_1 = \sigma\varepsilon e^{-1t} \star w_1 X_1 + \varepsilon X_1 Y_1 + X_1$

Result normal form DEs

$$\dot{Y}_1 = 8\sigma^2 \varepsilon^2 e^{-1t} \star w_1 w_1 Y_1 - 4\sigma \varepsilon w_1 Y_1 - 2\varepsilon^2 X_1^2 Y_1 - Y_1$$
$$\dot{X}_1 = 2\sigma^2 \varepsilon^2 e^{-1t} \star w_1 w_1 X_1 - \sigma \varepsilon w_1 X_1 - \varepsilon^2 X_1^3$$