A centre-unstable manifold of your dynamical system

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Generally, the lowest order, most important, terms are near the end of each expression.

off echo;

Specified dynamical system

$$\begin{split} \dot{x}_1 &= \varepsilon (-x_1y_1 + y_2) \\ \dot{x}_2 &= \varepsilon (-x_2y_1 - x_1y_2 + y_3) \\ \dot{x}_3 &= \sigma \varepsilon w_1 + \varepsilon (-x_3y_1 - 2x_2y_2 - x_1y_3) \\ \dot{y}_1 &= \varepsilon (x_2 - 1/2x_1^2 - 1/2y_1^2) - y_1 \\ \dot{y}_2 &= \varepsilon (x_3 - x_2x_1 - y_2y_1) - y_2 \\ \dot{y}_3 &= \sigma \varepsilon w_2 + \varepsilon (-x_3x_1 - x_2^2 - y_3y_1 - y_2^2) - y_3 \\ \text{off echo:} \end{split}$$

Time dependent centre-unstable manifold coordinates

$$y_1 = \varepsilon(X_2 - 1/2X_1^2)$$

$$y_2 = \varepsilon (X_3 - X_2 X_1)$$

 $y_3 = \sigma \varepsilon e^{-1t} \star w_2 + \varepsilon (-X_3 X_1 - X_2^2)$
 $x_1 = X_1$
 $x_2 = X_2$
 $x_3 = X_3$

Result centre-unstable manifold DEs

$$\begin{split} \dot{X}_1 &= \varepsilon^2 (X_3 - 2X_2X_1 + 1/2X_1^3) \\ \dot{X}_2 &= \sigma \varepsilon^2 w_2 + \varepsilon^2 (-2X_3X_1 - 2X_2^2 + 3/2X_2X_1^2) \\ \dot{X}_3 &= -\sigma \varepsilon^2 w_2 X_1 + \sigma \varepsilon w_1 + \varepsilon^2 (-3X_3X_2 + 3/2X_3X_1^2 + 3X_2^2X_1) \end{split}$$