# Slow manifold of your dynamical system

# A. J. Roberts, University of Adelaide http://www.maths.adelaide.edu.au/anthony.roberts

## The specified dynamical system

$$\dot{x}_1 = \sigma w_1 - 4x_1^5 \varepsilon^2 - 2x_1^3 \varepsilon + 4x_1 y_1^2 \varepsilon^2 + 2x_1 y_1 \varepsilon$$
$$\dot{y}_1 = \sigma w_2 + 4x_1^4 \varepsilon^2 - 4x_1^2 y_1 \varepsilon^2 + x_1^2 \varepsilon - y_1$$

#### The stochastic slow manifold

$$y_{1} = \sigma \left( -8e^{-1t} \star e^{-1t} \star w_{2} X_{1}^{2} - 4e^{-1t} \star e^{-1t} \star w_{1} X_{1}^{3} - 4e^{-1t} \star w_{2} X_{1}^{2} + e^{-1t} \star w_{2} - 32e^{-1t} \star w_{1} X_{1}^{3} - 2e^{-1t} \star w_{1} X_{1} \right) + 8 X_{1}^{4} + X_{1}^{2}$$

$$x_{1} = \sigma \left( -8e^{-1t} \star w_{2} X_{1}^{3} - 2e^{-1t} \star w_{2} X_{1} + 4e^{-1t} \star w_{1} X_{1}^{2} \right) + X_{1}$$

### Slow manifold SDEs

$$\dot{X}_{1} = \sigma^{2} \Big( -16e^{-1t} \star e^{-1t} \star w_{2} \ w_{1} X_{1}^{2} - \underbrace{8e^{-1t} \star e^{-1t} \star w_{1} \ w_{1} X_{1}^{3}}_{1} + \underbrace{4e^{-1t} \star w_{2} \ w_{2} X_{1}}_{24e^{-1t} \star w_{2} \ w_{1} X_{1}^{2}} + \underbrace{4e^{-1t} \star w_{2} \ w_{2} X_{1}}_{24e^{-1t} \star w_{2} \ w_{1} X_{1}^{2}} + \underbrace{4e^{-1t} \star w_{2} \ w_{1} X_{1}^{2}}_{1} - \underbrace{8e^{-1t} \star w_{1} \ w_{2} X_{1}^{2}}_{1} - \underbrace{4e^{-1t} \star w_{2} \ w_{1} X_{1}^{2}}_{1} - \underbrace{8e^{-1t} \star w_{1} \ w_{2} X_{1}^{2}}_{1} - \underbrace{8e^{-1t} \star w_{1} \ w_{2} X_{1}^{2}}_{1} - \underbrace{8e^{-1t} \star w_{2} \ w_{1} X_{1}^{2}}_{1} - \underbrace{8e^{-1t} \star$$

$$112e^{-1t} \cdot w_1 \cdot w_1 X_1 - 4e^{-1t} \star w_1 \cdot w_1 X_1 + \sigma \left( \frac{32w_2 X_1^5}{4} - 8w_2 X_1^3 + 2w_2 X_1 - \frac{88w_1 X_1^4}{4} - 4w_1 X_1^2 + w_1 \right) + 12X_1^5$$