COMS30035, Machine learning: Combining Models 1, Model Selection and Averaging

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Agenda

- Model Selection
- Model Averaging
- ► Ensembles: Bagging and Boosting
- ▶ Tree-based Models
- Conditional Mixture Models
- Ensembles of Humans

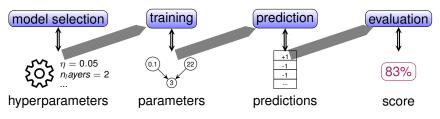
Textbook

We will follow Chapter 14 of the Bishop book: Bishop, C. M., Pattern recognition and machine learning (2006). Available for free here.

The Model Selection Problem

- Select a model h from a set of possible models in a set H,
- The models in H can differ in various ways, such as:
 - ▶ The structure of the model, e.g., differences in graphical models;
 - ▶ The choice of prior distribution $p(\theta)$ over model parameters;
 - The learning algorithm used, e.g., EM, MCMC, backpropagation, etc.; algorithm;
 - The features of the data used as inputs to the model.
 - The examples in the dataset the model is trained on.
 - Random initialisation, e.g., of parameters for EM or gradient descent for neural networks

Hyperparameters



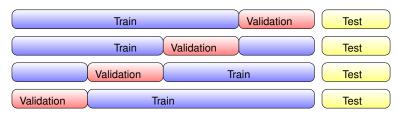
- It's useful to characterise modelling decisions as choosing the values of a set of parameters called hyperparameters
- All parameters that are fixed before training are hyperparameters.
- Typical hyperparameters include:
 - Parameters of the prior distribution
 - Parameters of the learning algorithm, e.g., the learning rate for a neural network
 - Parameters of feature extractors.

Model Selection on a Validation Set

Dataset: Train Validation / Development Test

- Train the model with different combinations of features, hyperparameter values and random initialisations
- Choose the model h that maximises performance on a validation set.
 - As seen in week 1.
 - Validation set is obtained by setting aside some part of the labelled set.
 - Can't tune on the training set as it would lead to overfitting
- Advantage: optimises a performance metric we really care about.
- Disadvantage: we didn't use all the data in training;
- Disadvantage: if the validation set is small, we might choose the wrong model!

Cross-validation



- Split the training data into k random, equally-sized subsets;
- For each of the *k* folds: leave out the *k*th subset from training, train on the rest and test on the *k*th subset;
- Compute the average performance across all k folds;
- Avoids overfitting by tuning on training set performance...
- And avoids tuning on a single small validation set.

A Probabilistic View of Model Selection

- Suppose we have the following machine learning task:
 - Latent variables to predict (e.g., class labels in the test set): **z**;
 - ► Training data: **X**;
 - ▶ Model: h.
- \blacktriangleright We obtain the prediction of z from a chosen model h as follows:

$$p(\boldsymbol{z}|\boldsymbol{X}) \approx p(\boldsymbol{z}|\boldsymbol{X},h) \tag{1}$$

Bayesian Model Selection

- \blacktriangleright How can we choose h in p(z|X,h)?
- Choose $h = h^*$ to *maximise* the marginal likelihood of the data:

$$h^* = \underset{h}{\operatorname{argmax}} p(\mathbf{X}|h) = \underset{h}{\operatorname{argmax}} \int p(\mathbf{X}|\theta, h) p(\theta|h) d\theta$$
 (2)

- Similar to maximum likelihood estimation, which we used before to optimise parameters θ .
 - \triangleright Here, we use a Bayesian approach and integrate out (marginalise) θ .
 - Relies on finding a single, good model given our training set.

Bayesian Model Averaging (BMA)

- Even after computing marginal likelihood, we may be uncertain about which model h is correct
- We can express this by assigning a probability to each model given the training data, $p(h|\mathbf{X})$.

Bayesian Model Averaging (BMA)

- ▶ Rather than choosing a single model, we can now take an expectation.
- Our predictions now come from a *weighted sum* over models, where $p(h|\mathbf{X})$ are weights:

$$p(\boldsymbol{z}|\boldsymbol{X}) = \sum_{h=1}^{H} p(\boldsymbol{z}|\boldsymbol{X}, h)p(h|\boldsymbol{X})$$
 (3)

Bayesian Model Averaging (BMA)

Apply Bayes' rule to estimate the weights:

$$p(h|\mathbf{X}) = \frac{p(\mathbf{X}|h)p(h)}{\sum_{h'=1}^{H} p(\mathbf{X}|h)p(h')}$$
(4)

- ▶ What happens as we increase the amount of data in X? p(h|X) becomes more focussed on one model.
- So BMA is soft model selection, it does not combine models to make a more powerful model.

Now do the quiz!

Please do the quiz for this lecture on Blackboard.